# Combinatorial Algorithms: HW1 – Knights Placement

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https://industrialinformatics.fel.cvut.cz/

## 1 Homework assignment

Your task is to place as many Knights as possible on  $8 \times 8$  chessboard such that no two Knights attack each other. Furthermore, there might be some Rooks already placed in some fixed positions on the chessboard – in that case, you have to place the Knights such that they are not attacked by the Rooks.

We remind you that Knight moves in an 'L-shape' as illustrated in Figure 1.

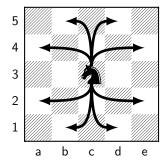


Figure 1: Knight moves illustration.

In case of the presence of a Rook on the chessboard, it threatens the whole row and column of the chessboard, as shown in Figure 2. We remind you that you do not come up with the positions for the Rooks; these are given to you as input. They just restrict some of the squares for your Knights.

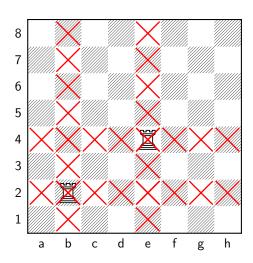


Figure 2: Red crosses represent the area threatened by the Rooks.

**Homework assignment:** Your task is to develop an Integer Linear Programming (ILP) formulation of the abovementioned problem. Therefore, you will develop a computer program that takes the input, builds the ILP model, solves it using the Gurobi solver, and outputs the solution according to the specifications given below. Upload your source code to BRUTE, where it will be automatically evaluated.

**Hint:** Look for inspiration with the maximum independent set problem we did during the last lab.

## 2 Assignment evaluation

Upload your code to BRUTE. If your program is able to pass all the tests, you will obtain 5 points for the assignment. Supported programming languages are C++ and Python (see https://cw.fel.cvut.cz/b232/courses/rm35koa/upload\_system for more details).

Your program will be executed with two arguments: the first one is the absolute path to the input file, and the second one is the absolute path to the output file (the output file has to be created by your program).

#### 2.1 Input File

The input file has the following form:

R  $r_1$   $r_2$   $\vdots$   $r_R$ 

Integer number R represents the number of Rooks present on the board (can be 0). Then R lines follow, containing strings  $r_1, r_2, \ldots, r_R$  representing the positions of the rooks. Each string  $r_i$  contains two characters (letter and number) representing the column and the row, respectively. E.g., if  $r_i = a3$ , then a Rook is placed on column 'a' and row '3' (or in chess terms, "a-file" and "the third rank").

#### 2.2 Output File

The output file has the following form:

 $\begin{array}{c}
N \\
n_1 \\
n_2 \\
\vdots \\
n_N
\end{array}$ 

The first line of the output file contains the value of the objective function N, i.e., the number of the Knights placed on the chessboard, formated as an integer. The remaining N lines contain strings  $n_1, n_2, \ldots, n_N$  representing the positions of the Knights (again, each  $n_i$  contains exactly two symbols - one character and one number representing the column and the row, respectively).

In the case when no Knight can be placed on the board, the output file should consist of value 0 only.

# 3 Examples

# 3.1 Example 1

Input:

0

This input represents the scenario without the Rooks.

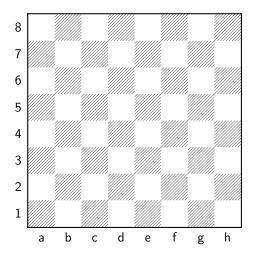


Figure 3: Input of Example 1.

#### Output:

32

b1 d1

f1

h1

a2 c2

e2

g2 b3

d3 f3

h3 a4

c4 e4

g4 b5

d5 f5

h5 a6

c6 e6

g6 b7

d7 f7

f7 h7

a8 c8

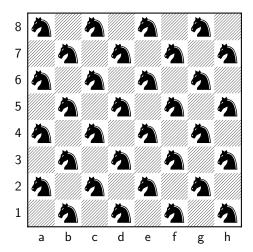


Figure 4: Solution of Example 1.

# 3.2 Example 2

The input represents the scenario with 2 Rooks shown in Figure 2.

Input:

2

b2 d5

Output:

20

a1

c1

e1 f1

g1

h1

a3

a4

e4 f4

g4

h4

a6

с6

h7

a8 c8

e8

g8 h8

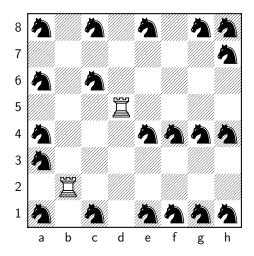


Figure 5: Solution of Example 2.

# 3.3 Example 3

The input represents a scenario where no Knight can be placed.

#### Input:

8

a1

b2 c3

d4

e5

f6

g7 h2

#### Output:

0

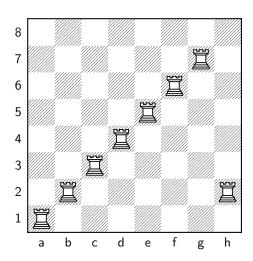


Figure 6: Solution of Example 3.