

# Planning Problem Representation

Problem representations + Assignment #1-2

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PUI Tutorial  
Week 3

# Lecture check

- Any questions regarding the lecture?

Teacher: any questions

Me: \*asks question\*

Teacher:



## **Thank you for your feedback!**

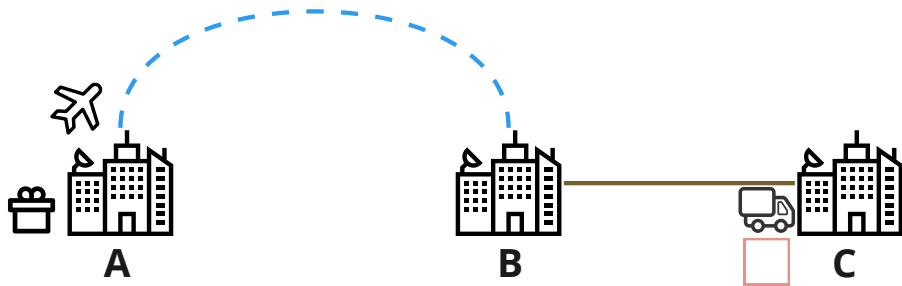
- 5 responses
- Suggestions
  - Slow down the tutorials a bit
  - Everyone keeps up with the lecture with no problems

- **STRIPS**
- **FDR**
- **Specify** the model
- Representations used in planners with the search algorithms
- PDDL → Grounding → STRIPS/FDR

- Process that creates **grounded** problem representation ready to be transformed into STRIPS, FDR, ...
- Many works on effective grounding, partial grounding, ...
- Can speed up a planner significantly

# Grounding

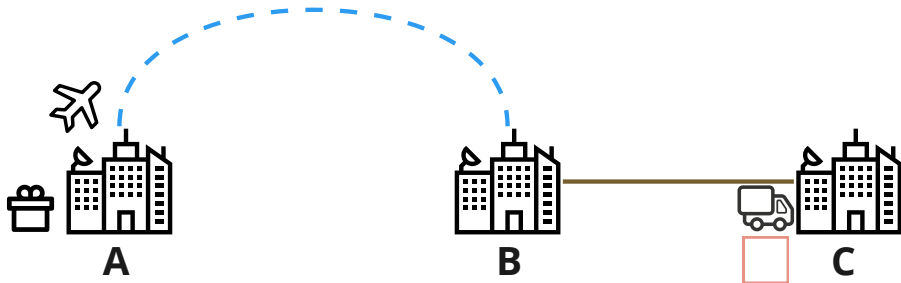
Let's create grounding for the example from the last time.



# Grounding

```
(:types  
  package vehicle - object  
  location  
  airplane truck - vehicle  
)
```

```
(:objects  
  A B C - location  
  t - truck  
  a - airplane  
  p - package  
)
```



## Ground all predicates

- Naive grounding → create all instances of predicates with existing objects

(:predicates

(at ?o - object ?l - location)

(in ?p - package ?v - vehicle)

(road ?l1 - location ?l2 - location)

(corridor ?l1 - location ?l2 - location)

(empty ?v - vehicle)

)



## Full naive grounding of predicates

(at a A)	(road A B)	(corridor A B)
(at a B)	(road B A)	(corridor B A)
(at a C)	(road A A)	(corridor A A)
(at t A)	(road B B)	(corridor B B)
(at t B)	(road A C)	(corridor A C)
(at t C)	(road C A)	(corridor C A)
(at p A)	(road A A)	(corridor A A)
(at p B)	(road C C)	(corridor C C)
(at p C)	(road B C)	(corridor B C)
(empty a)	(road C B)	(corridor C B)
(empty t)	(road B B)	(corridor B B)
(in p a)	(road C C)	(corridor C C)
(in p t)		

## Ground all actions

- Naive grounding → create all instances of actions with existing objects

(load ?p - package ?l - location ?v - vehicle)

(unload ?p - package ?l - location ?v - vehicle)

(drive ?t - truck ?l1 - location ?l2 - location)

(fly ?a - airplane ?l1 - location ?l2 - location)

**Full naive grounding of actions** (*all preconditions and effects have to be grounded as well*)

(load p A t)	(unload p A t)	(drive t A A)	(fly a A A)
(load p B t)	(unload p B t)	(drive t A B)	(fly a A B)
(load p C t)	(unload p C t)	(drive t A B)	(fly a A B)
(load p A a)	(unload p A a)	(drive t B A)	(fly a B A)
(load p B a)	(unload p B a)	(drive t B B)	(fly a B B)
(load p C a)	(unload p C a)	(drive t B C)	(fly a B C)
		(drive t C A)	(fly a C A)
		(drive t C B)	(fly a C B)
		(drive t C C)	(fly a C C)

**Full naive grounding of actions** (*all preconditions and effects have to be grounded as well*)

		(drive t A A)	(fly a A A)
(load p A t)	(unload p A t)	(drive t A B)	(fly a A B)
(load p B t)	(unload p B t)	(drive t A B)	(fly a A B)
(load p C t)	(unload p C t)	(drive t B A)	(fly a B A)
(load p A a)	(unload p A a)	(drive t B B)	(fly a B B)
(load p B a)	(unload p B a)	(drive t B C)	(fly a B C)
(load p C a)	(unload p C a)	(drive t C A)	(fly a C A)
		(drive t C B)	(fly a C B)
		(drive t C C)	(fly a C C)

Now we have **full naive grounding** so we can start creating problem representations for planners!

STRIPS problem  $\Pi = \langle F, O, s_{init}, s_{goal}, c \rangle$

- $F = \{f_1, f_2, \dots, f_n\}$  (facts)
- $O = \{o_1, o_2, \dots, o_m\}$  (operators)
- $s_{init} \subseteq F$  (initial state)
- $s_{goal} \subseteq F$  (goal state specification)
- $c(o_i) \in \mathbb{R}^+$  (cost function)

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STRIPS operator  $o = \langle pre(o), add(o), del(o) \rangle$

- $pre(o) \subseteq F$  (set of preconditions)
- $add(o) \subseteq F$  (set of add effects)
- $del(o) \subseteq F$  (set of delete effects)

STRIPS problem  $\Pi = \langle F, O, s_{init}, s_{goal}, c \rangle$

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STRIPS operator  $o = \langle pre(o), add(o), del(o) \rangle$

- $pre(o) \subseteq F$  (set of preconditions)
- $add(o) \subseteq F$  (set of add effects)
- $del(o) \subseteq F$  (set of delete effects)
- operators are **well-formed**
  - $add(o) \cap del(o) = \emptyset$
  - $pre(o) \cap add(o) = \emptyset$

## Applicable operator

Operator  $o$  is applicable in state  $s$  if  $pre(o) \subseteq s$ .

**Resulting state**  $res(o, s) = (s \setminus del(o)) \cup add(o)$ .

State  $s$  is a **goal state** iff  $s_{goal} \subseteq s$ .



## Applicable operator

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## Sequence of applicable operators

**Sequence of operators**  $\pi = \langle o_1, o_2, \dots, o_n \rangle$  is applicable in state  $s_0$  if there are states  $s_1, s_2, \dots, s_n$  such that  $o_i$  is applicable in  $s_{i-1}$  and  $s_i = res(o_i, s_{i-1})$  for  $1 \leq i \leq n$ .

- $res(\pi, s_0) = s_n$  (result of the applied operator sequence  $\pi$ )
- $c(\pi) = \sum_{o \in \pi} c(o)$  (cost of applying the operator sequence  $\pi$ )

## Applicable operator

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- $c(\pi) = \sum_{o \in \pi} c(o)$  (cost of applying the operator sequence  $\pi$ )

Sequence  $\pi$  is called a **plan** if  $s_{goal} \subseteq res(\pi, s_{init})$ .

- $\pi$  is an **optimal plan** if  $c(\pi)$  is the minimal cost over all plans

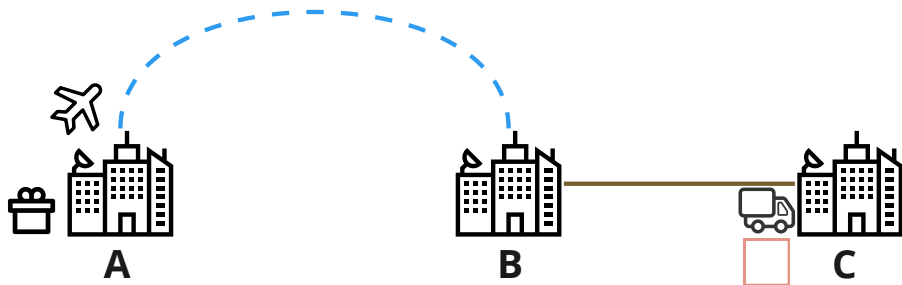
## Reachable state

State  $s$  is **reachable** if there exists an applicable sequence of operators  $\pi$  such that  $res(\pi, s_{init} = s)$ .

Set of all reachable states is denoted  $\mathcal{R}_\Pi$ .

# STRIPS Example

Let's formulate STRIPS representation for the logistics problem.



$$\Pi = \langle F, O, s_{init}, s_{goal}, c \rangle$$

## Full naive grounding of predicates corresponds to STRIPS facts

(at a A)  $\rightarrow$  a-A  
(at a B)  $\rightarrow$  a-B  
(at a C)  $\rightarrow$  a-C  
(at t A)  $\rightarrow$  t-A  
(at t B)  $\rightarrow$  t-B  
(at t C)  $\rightarrow$  t-C  
(at p A)  $\rightarrow$  p-A  
(at p B)  $\rightarrow$  p-B  
(at p C)  $\rightarrow$  p-C  
(empty a)  $\rightarrow$  emp-a  
(empty t)  $\rightarrow$  emp-t  
(in p a)  $\rightarrow$  p-a  
(in p t)  $\rightarrow$  p-t

(road A B)  $\rightarrow$  r-A-B  
(road B A) ...  
(road A A) ...  
(road B B)  $\rightarrow$  r-B-B  
(road A C) ...  
(road C A) ...  
(road A A) ...  
(road C C) ...  
(road B C)  $\rightarrow$  r-B-C  
(road C B) ...  
(road B B) ...  
(road C C) ...

(corridor A B)  $\rightarrow$  c-A-B  
(corridor B A) ...  
(corridor A A) ...  
(corridor B B) ...  
(corridor A C) ...  
(corridor C A)  $\rightarrow$  c-C-A  
(corridor A A) ...  
(corridor C C) ...  
(corridor B C) ...  
(corridor C B) ...  
(corridor B B)  $\rightarrow$  c-B-B  
(corridor C C) ...

## Full naive grounding of actions can be transformed into STRIPS operators

(load p A t)

(load p B t)

(load p C t)

(load p A a)

(load p B a)

(load p C a)

(unload p A t)

(unload p B t)

(unload p C t)

(unload p A a)

(unload p B a)

(unload p C a)

(drive t A A)

(drive t A B)

(drive t A B)

(drive t B A)

(drive t B B)

(drive t B C)

(drive t C A)

(drive t C B)

(drive t C C)

(fly a A A)

(fly a A B)

(fly a A B)

(fly a B A)

(fly a B B)

(fly a B C)

(fly a C A)

(fly a C B)

(fly a C C)

# STRIPS Example

## Lifted action

```
(:action load
  :parameters (
    ?p - package
    ?l - location
    ?v - vehicle)
  :precondition (and
    (at ?p ?l)
    (at ?v ?l)
    (empty ?v)
  )
  :effect (and
    (not (at ?p ?l))
    (in ?p ?v)
    (not (empty ?v))
  )
)
```

# STRIPS Example

## Lifted action

```
(:action load
  :parameters (
    ?p - package
    ?l - location
    ?v - vehicle)
  :precondition (and
    (at ?p ?l)
    (at ?v ?l)
    (empty ?v)
  )
  :effect (and
    (not (at ?p ?l))
    (in ?p ?v)
    (not (empty ?v))
  )
)
```

## Grounded action

```
(:action load
  :parameters (
    p - package
    A - location
    t - vehicle)
  :precondition (and
    (at p A)
    (at t A)
    (empty t)
  )
  :effect (and
    (not (at p A))
    (in p t)
    (not (empty t))
  )
)
```



# STRIPS Example

## Grounded action

```
(:action load
  :parameters (
    p - package
    A - location
    t - vehicle)
  :precondition (and
    (at p A)
    (at t A)
    (empty t)
  )
  :effect (and
    (not (at p A))
    (in p t)
    (not (empty t))
  )
)
```

# STRIPS Example

## Grounded action

```
(:action load
  :parameters (
    p - package
    A - location
    t - vehicle)
  :precondition (and
    (at p A)
    (at t A)
    (empty t)
  )
  :effect (and
    (not (at p A))
    (in p t)
    (not (empty t))
  )
)
```

## STRIPS operator load-p-A-t

```
pre(load-p-A-t) = {}
add(load-p-A-t) = {}
del(load-p-A-t) = {}
```

# STRIPS Example

## Grounded action

```
(:action load
  :parameters (
    p - package
    A - location
    t - vehicle)
  :precondition (and
    (at p A)
    (at t A)
    (empty t)
  )
  :effect (and
    (not (at p A))
    (in p t)
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```

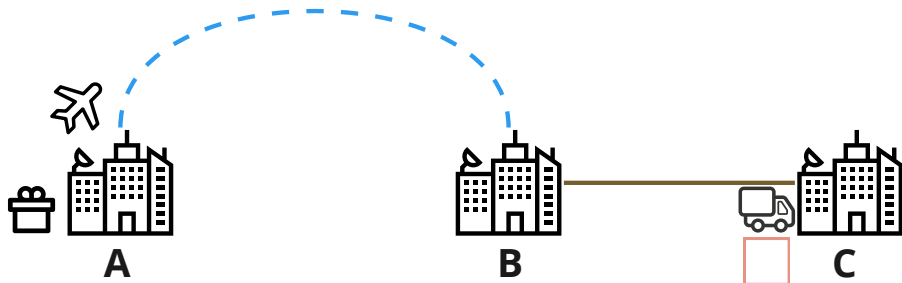
## STRIPS operator load-p-A-t

$\text{pre}(\text{load-p-A-t}) = \{\text{p-A}, \text{t-A}, \text{emp-t}\}$

$\text{add}(\text{load-p-A-t}) = \{\text{p-t}\}$

$\text{del}(\text{load-p-A-t}) = \{\text{p-A}, \text{emp-t}\}$

# STRIPS Example



$$\Pi = \langle F, O, s_{init}, s_{goal}, C \rangle$$

$F = \{a-A, a-B, \dots, t-A, \dots, p-A, \dots, emp-a, emp-t, r-A-A, \dots, c-A-A, \dots\}$

$O = \{load-p-A-t, \dots, unload-p-A-t, \dots, drive-t-A-A, \dots, fly-a-A-A, \dots\}$

$s_{init} = \{p-A, a-A, t-C, c-A-B, c-B-A, r-B-C, r-C-B\}$

$s_{goal} = \{p-C\}$

**BUT WAIT**



**THERE'S MORE**

FDR problem  $P = \langle \mathcal{V}, \mathcal{O}, s_{init}, s_{goal}, c \rangle$

- $\mathcal{V} = \{V_1, V_2, \dots, V_n\}$  (*finite set of variables*)
- $\mathcal{O} = \{o_1, o_2, \dots, o_m\}$  (*set of operators*)
- $s_{init}$  (*initial state*)
- $s_{goal}$  (*goal state*)
- $c(o_i) \in \mathbb{R}^+$

FDR problem  $P = \langle \mathcal{V}, \mathcal{O}, s_{init}, s_{goal}, c \rangle$

- $\mathcal{V}$  (*finite set of variables*)
  - $V \in \mathcal{V}$  (*variable*)
  - $D_V$  (*finite domain of variable  $V$* )
- $s$  (*state*) is partial variable assignment over  $\mathcal{V}$ 
  - $\text{vars}(s) = V \in \mathcal{V}$  assigned in  $s$
  - $s[V]$  = value of  $V$  in  $s$
  - $s$  is **consistent** with  $s'$  if  $s[V] = s'[V]$  for all  $V \in \text{vars}(s')$
  - atom  $V = v$  is true in  $s$  if  $s[V] = v$

FDR operator  $o = \langle pre(o), eff(o) \rangle$

- $\mathcal{O}$  (set of operators)
  - $pre(o)$  = partial assignment over  $\mathcal{V}$  (preconditions)
  - $eff(o)$  = partial assignment over  $\mathcal{V}$  (effects)
  - $V = v$  cannot be in both  $pre(o)$  and  $eff(o)$



## Applicable operator

Operator  $o$  is applicable in state  $s$  if  $pre(o)$  is **consistent** with  $s$ .

**Resulting state**  $res(o, s) = \begin{cases} eff(o)[V], & \text{if } V \in vars(eff(o)) \\ s[V], & \text{otherwise} \end{cases}$

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## Sequence of applicable operators

**Sequence of operators**  $\pi = \langle o_1, o_2, \dots, o_n \rangle$  is applicable in state  $s_0$  if there are state  $s_1, s_2, \dots, s_n$  such that  $o_i$  is applicable in  $s_{i-1}$  and  $s_i = res(o_i, s_{i-1})$  for  $1 \leq i \leq n$ .

- $res(\pi, s_0) = s_n$  (*result of the applied operator sequence  $\pi$* )
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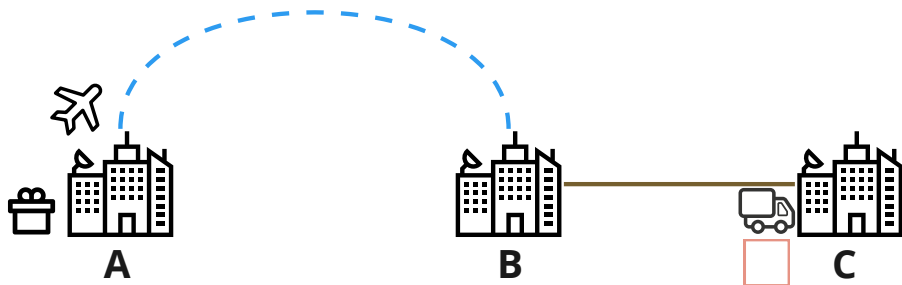
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Sequence  $\pi$  is called a **plan** if  $res(\pi, s_{init})$  is consistent with  $s_{goal}$ .

- $\pi$  is an **optimal plan** if  $c(\pi)$  is the minimal cost over all plans

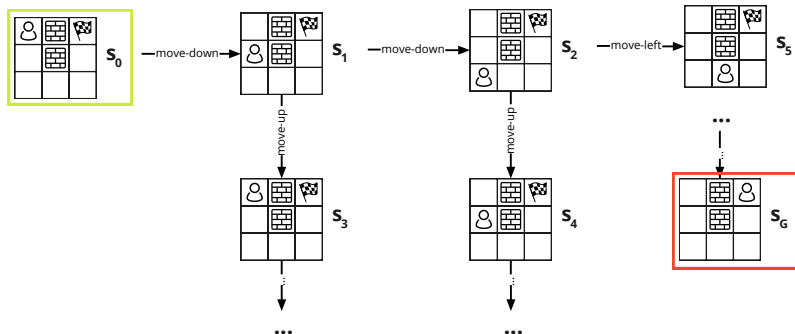
# FDR Example

Let's model the logistics example using FDR.



# Transition system

- Both STRIP and FDR have a notion of **state** and **operator**
  - $s_0$  is the initial state which gets expanded by using  $o \in O$  creating new state  $s' \rightarrow$  **transition system**



# Assignment #1-2 - Grounding

- Second part of the Assignment #1
- **Task:** implement a grounder for parsed PDDL files that will be base for the STRIPS representation in your planner
- **Points:** maximum 10
- **Deadlines**
  - 20.3.2023 - 23:59 (Monday)
  - 22.3.2023 - 23:59 (Wednesday)

All information is available on Courseware

- You know how to create naive grounding
- You know how to construct STRIPS and FDR representations
- You should be able to implement Assignment 1-2 - Grounding



Feedback form

