

Non-Deterministic Planning

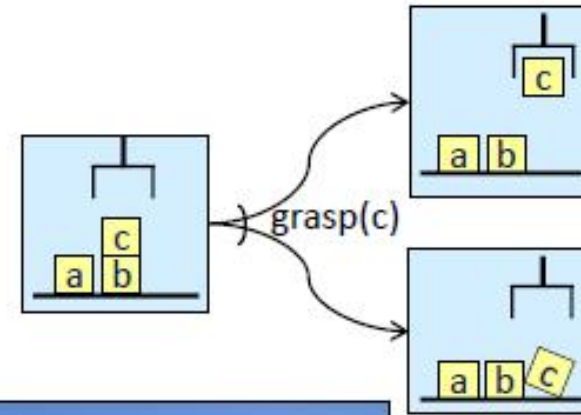
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Motivation

- We've assumed action a in state s has just one possible outcome
 - $\gamma(s, a)$
- Often more than one possible outcome
 - Unintended outcomes
 - Exogenous events
 - Inherent uncertainty



Nondeterministic Planning Domains

- 3-tuple (S, A, γ)
 - S and A – finite sets of states and actions
 - $\gamma: S \times A \rightarrow 2^S$
- $\gamma(s, a) = \{\text{all possible “next states” after applying action } a \text{ in state } s\}$
 - a is applicable in state s iff $\gamma(s, a) \neq \emptyset$
- $\text{Applicable}(s) = \{\text{all actions applicable in } s\} = \{a \in A \mid \gamma(s, a) \neq \emptyset\}$
- One action representation: n mutually exclusive “effects” lists

$a(z_1, \dots, z_k)$

pre: p_1, \dots, p_m

eff₁: e_{11}, e_{12}, \dots

eff₂: e_{21}, e_{22}, \dots

...

eff_n: e_{n1}, e_{n2}, \dots

- Problem: n may be combinatorially large

- Suppose a can cause any possible combination of effects e_1, e_2, \dots, e_k
- Need $\text{eff}_1, \text{eff}_2, \dots, \text{eff}_{2^k}$
 - One for each combination

- For now, ignore most of that

- states, actions \Leftrightarrow nodes, edges in a graph

Nondeterministic Planning Domains

- For deterministic planning problems, search space was a graph
- Now it's an AND/OR graph

➤ *OR branch:*

- several applicable actions, which one to choose?

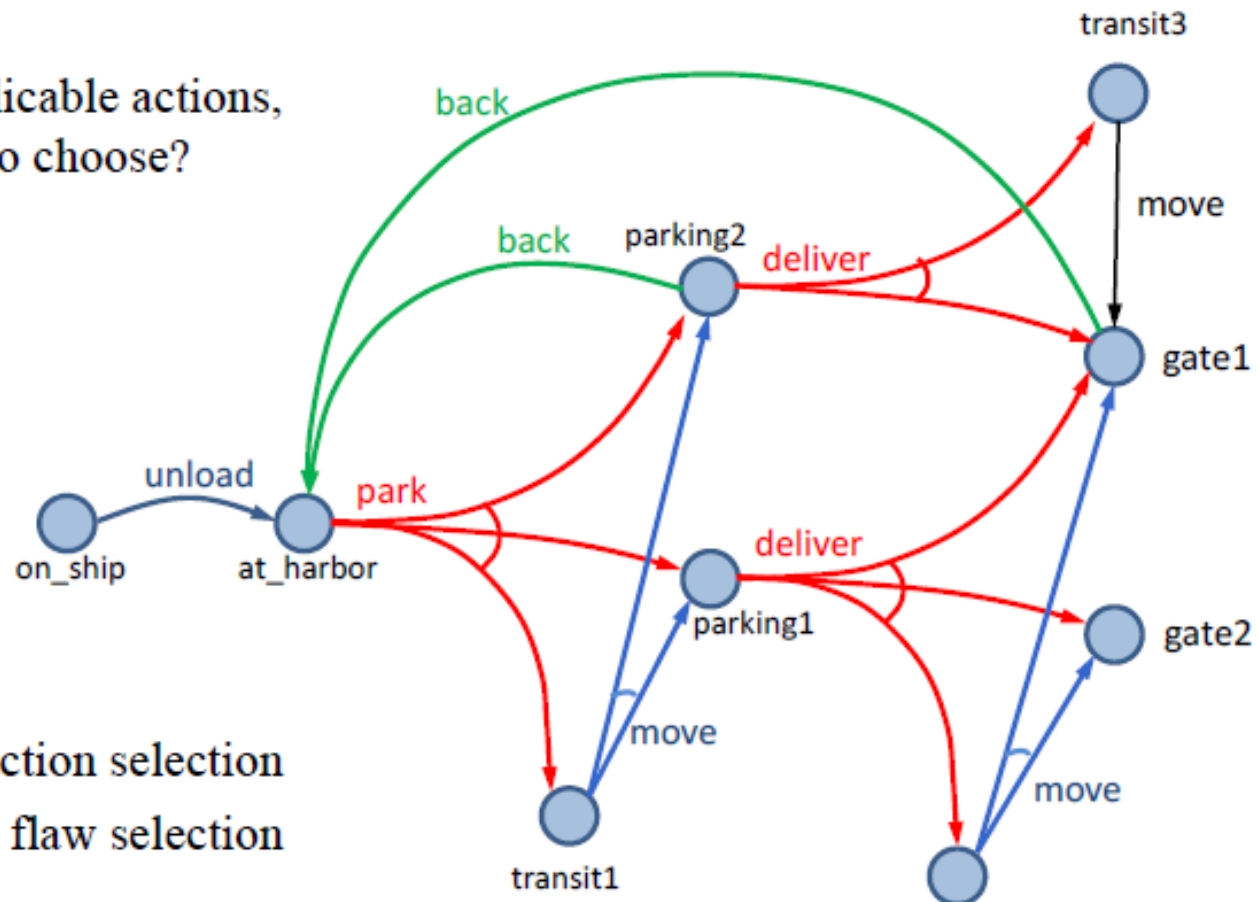
➤ *AND branch:*

- multiple possible outcomes
- must handle all of them

- Analogy to PSP

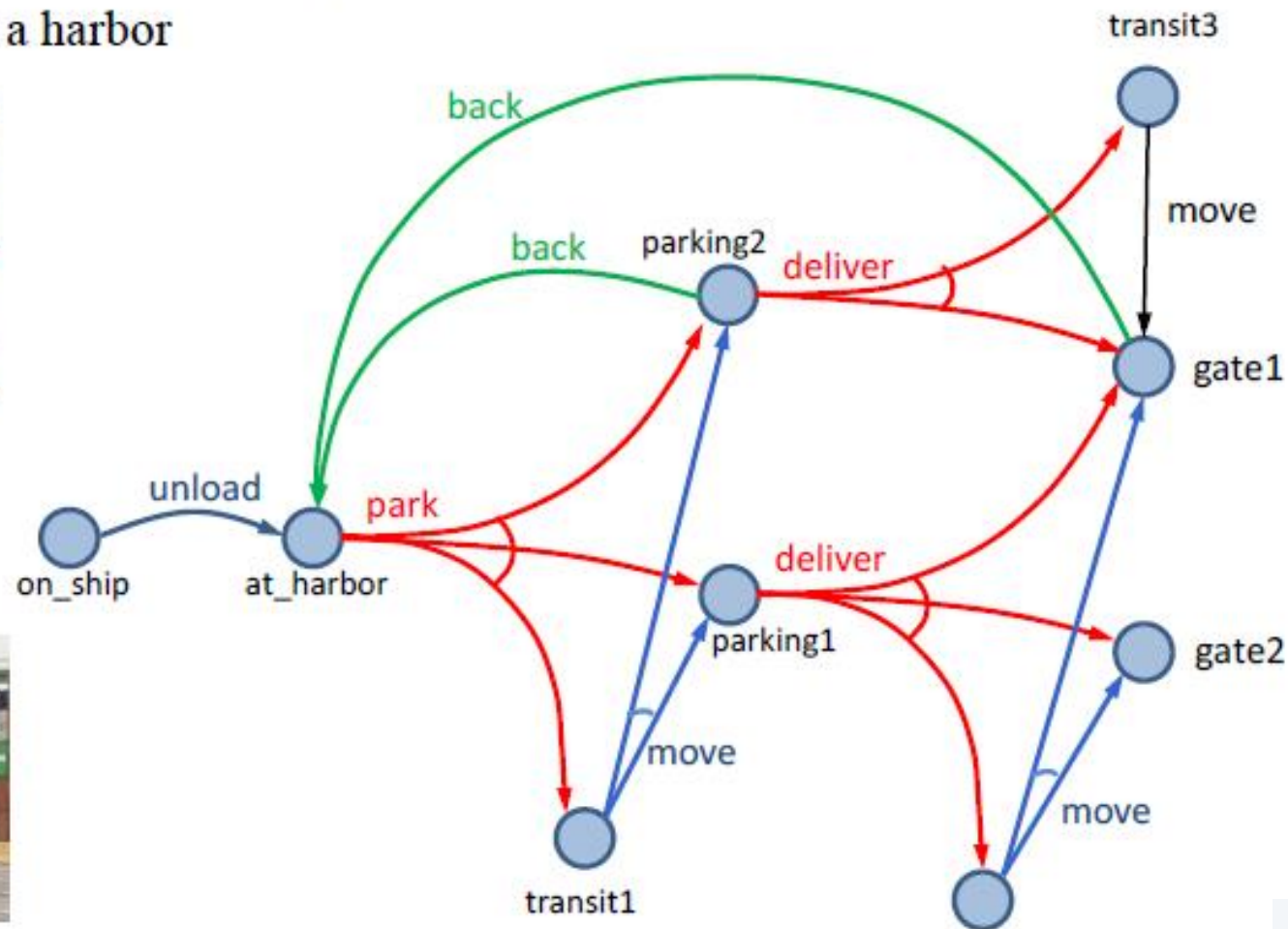
➤ *OR branch* \Leftrightarrow action selection

➤ *AND branch* \Leftrightarrow flaw selection



Example

- Very simple harbor management domain
 - Unload a single item from a ship
 - Move it around a harbor

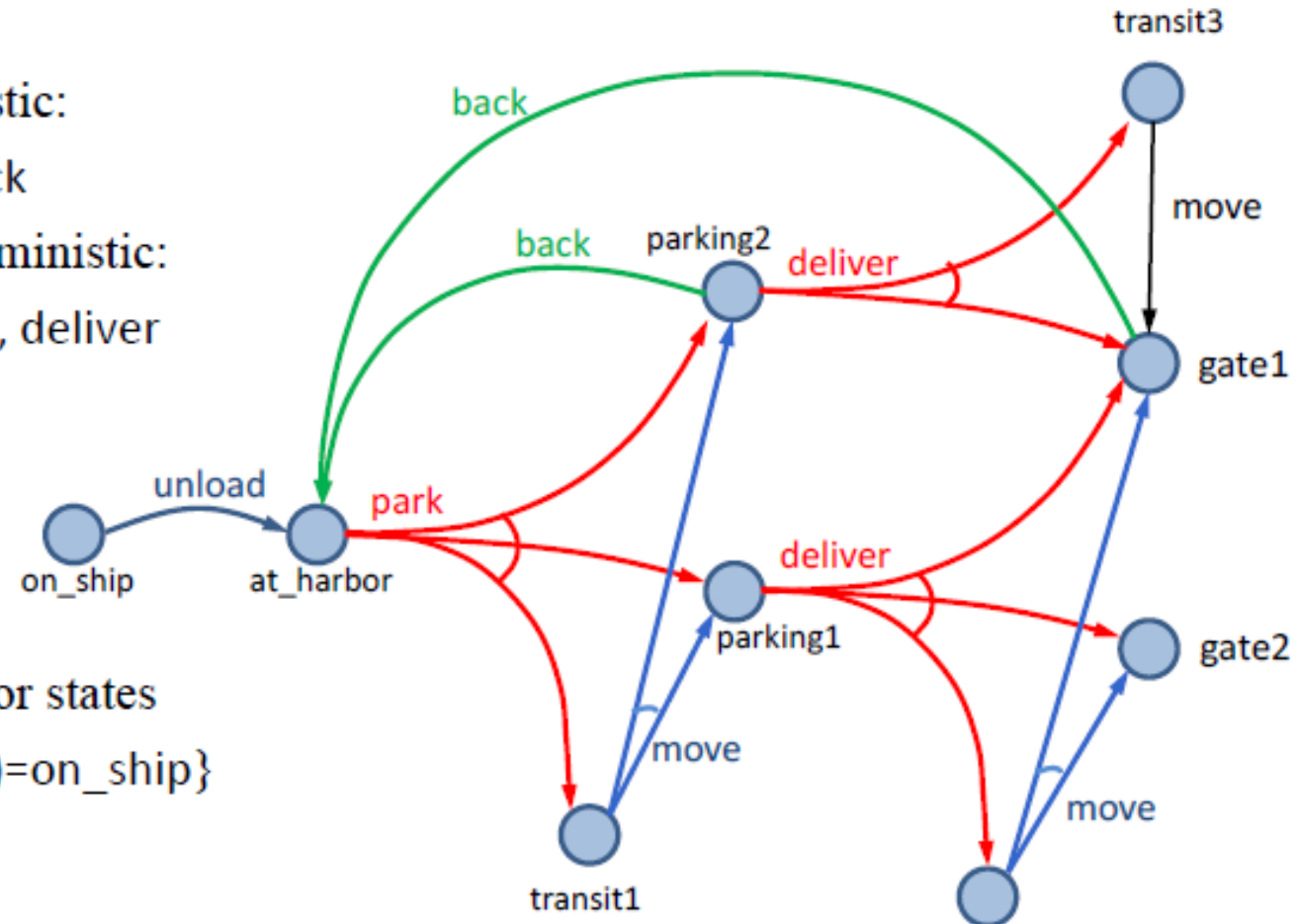


Example

- One state variable: $\text{pos}(\text{item})$

- Five actions

- Two deterministic:
 - unload, back
- Three nondeterministic:
 - park, move, deliver



- Simplified names for states

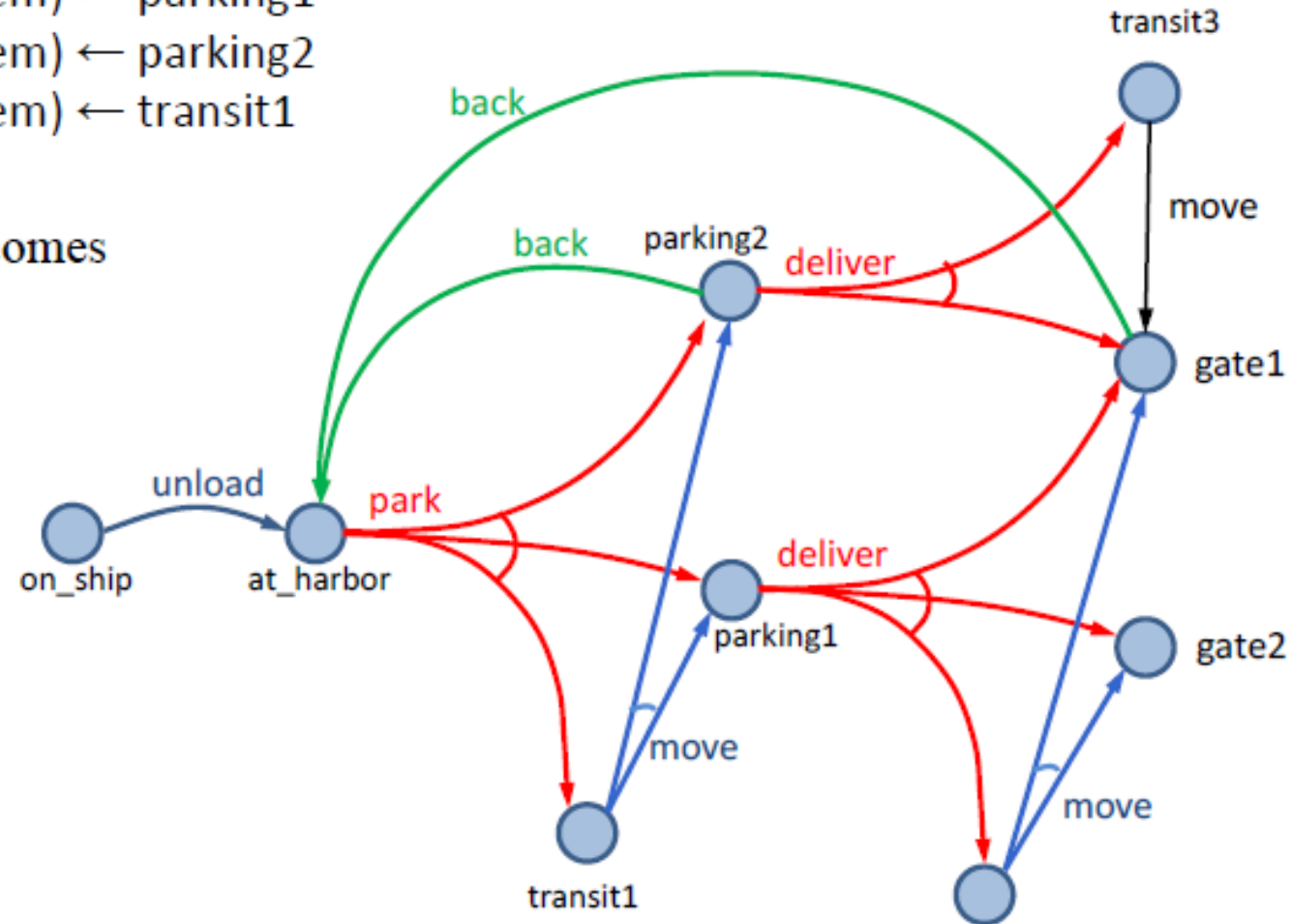
- For $\{\text{pos}(\text{item})=\text{on_ship}\}$ write on_ship

Actions

- park
 - pre: $\text{pos}(\text{item}) = \text{at_harbor}$
 - eff₁: $\text{pos}(\text{item}) \leftarrow \text{parking1}$
 - eff₂: $\text{pos}(\text{item}) \leftarrow \text{parking2}$
 - eff₃: $\text{pos}(\text{item}) \leftarrow \text{transit1}$

- Three possible outcomes

- put item in parking1 or parking2 if one of them has space
- or in transit1 if there's no parking space



Plans Policies

- Need something more general than a sequence of actions
 - After park, what do we do next?

- *Policy*: a partial function $\pi : S \mapsto A$

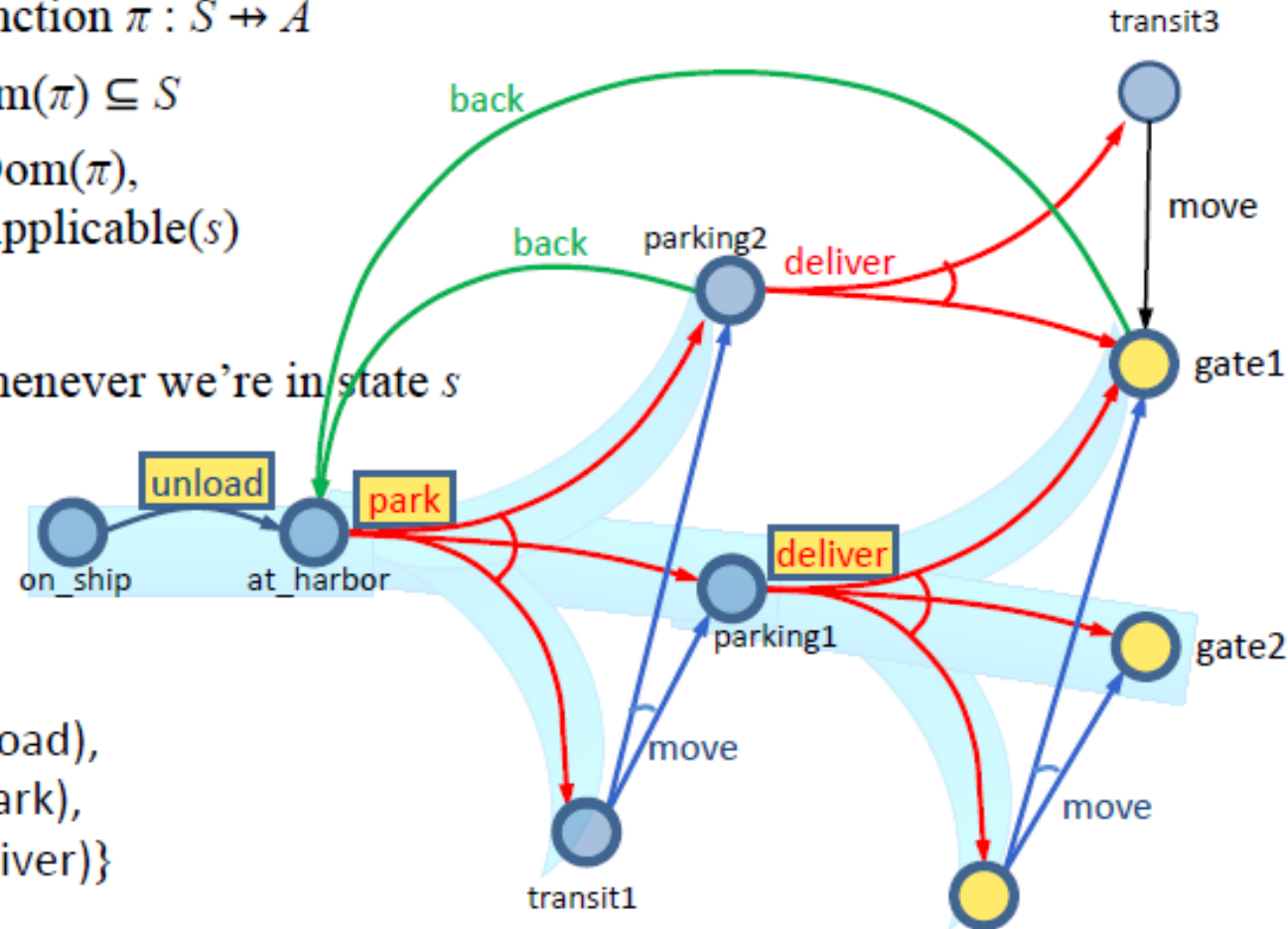
- ▶ i.e., $\text{Dom}(\pi) \subseteq S$

- ▶ For every $s \in \text{Dom}(\pi)$,
require $\pi(s) \in \text{Applicable}(s)$

- Meaning:

- ▶ perform $\pi(s)$ whenever we're in state s

- $\pi_1 = \{(on_ship, unload),$
 $(at_harbor, park),$
 $(parking1, deliver)\}$



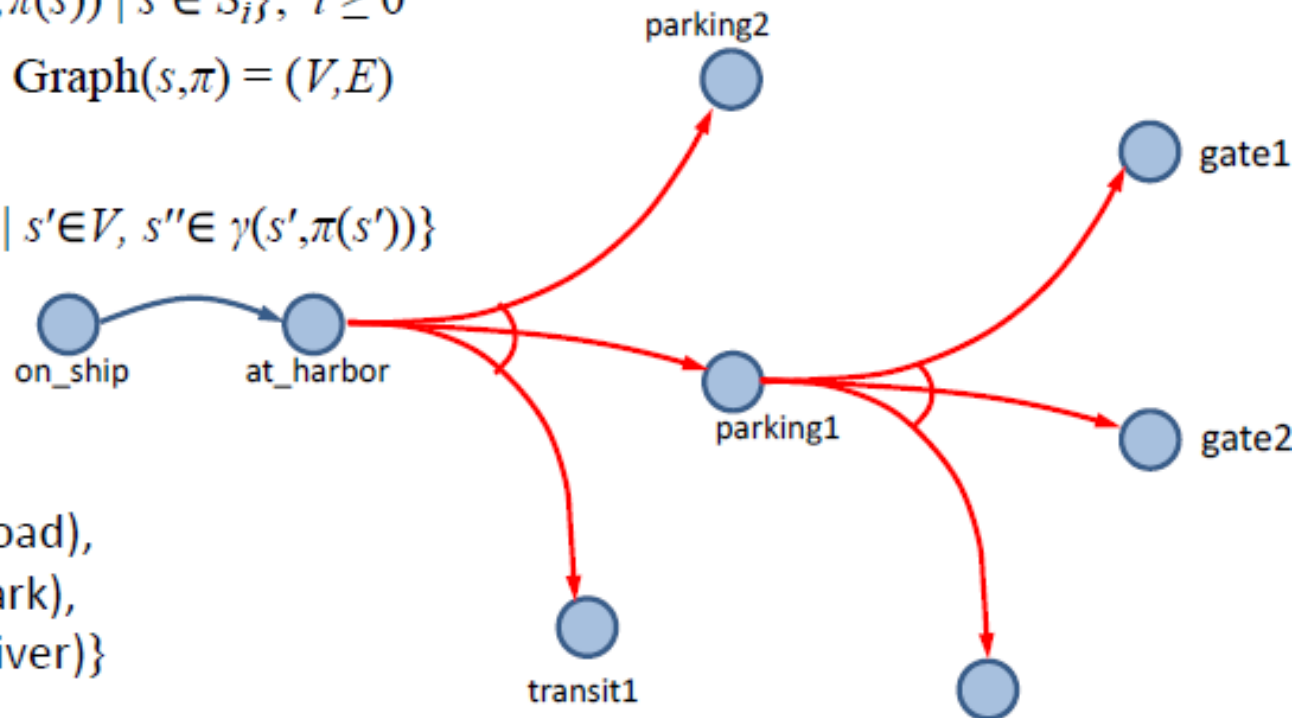
Definitions Over Policies

- *Transitive closure*:
{all states reachable from s using π }
- $leaves(s, \pi) = \hat{\gamma}(s, \pi) \setminus \text{Dom}(\pi)$
 - may be empty

➤ $\hat{\gamma}(s, \pi) = S_0 \cup S_1 \cup S_2 \cup \dots$

- $S_0 = \{s\}$
- $S_{i+1} = \cup \{\gamma(s, \pi(s)) \mid s \in S_i\}, i \geq 0$

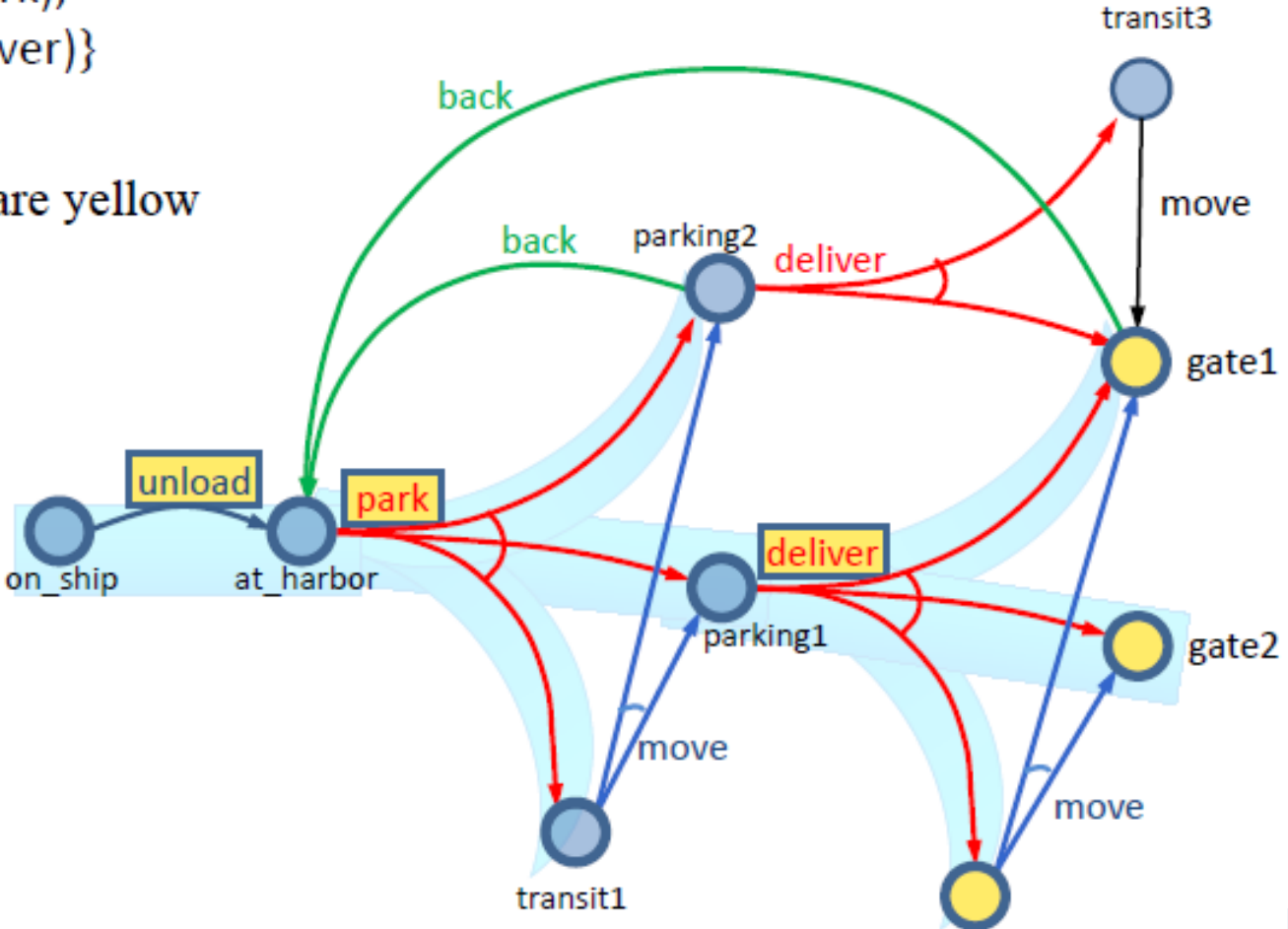
- *Reachability graph*: $\text{Graph}(s, \pi) = (V, E)$
 - $V = \hat{\gamma}(s, \pi)$
 - $E = \{(s', s'') \mid s' \in V, s'' \in \gamma(s', \pi(s'))\}$



- $\pi_1 = \{(on_ship, unload),$
 $(at_harbor, park),$
 $(parking1, deliver)\}$

Definitions Over Policies

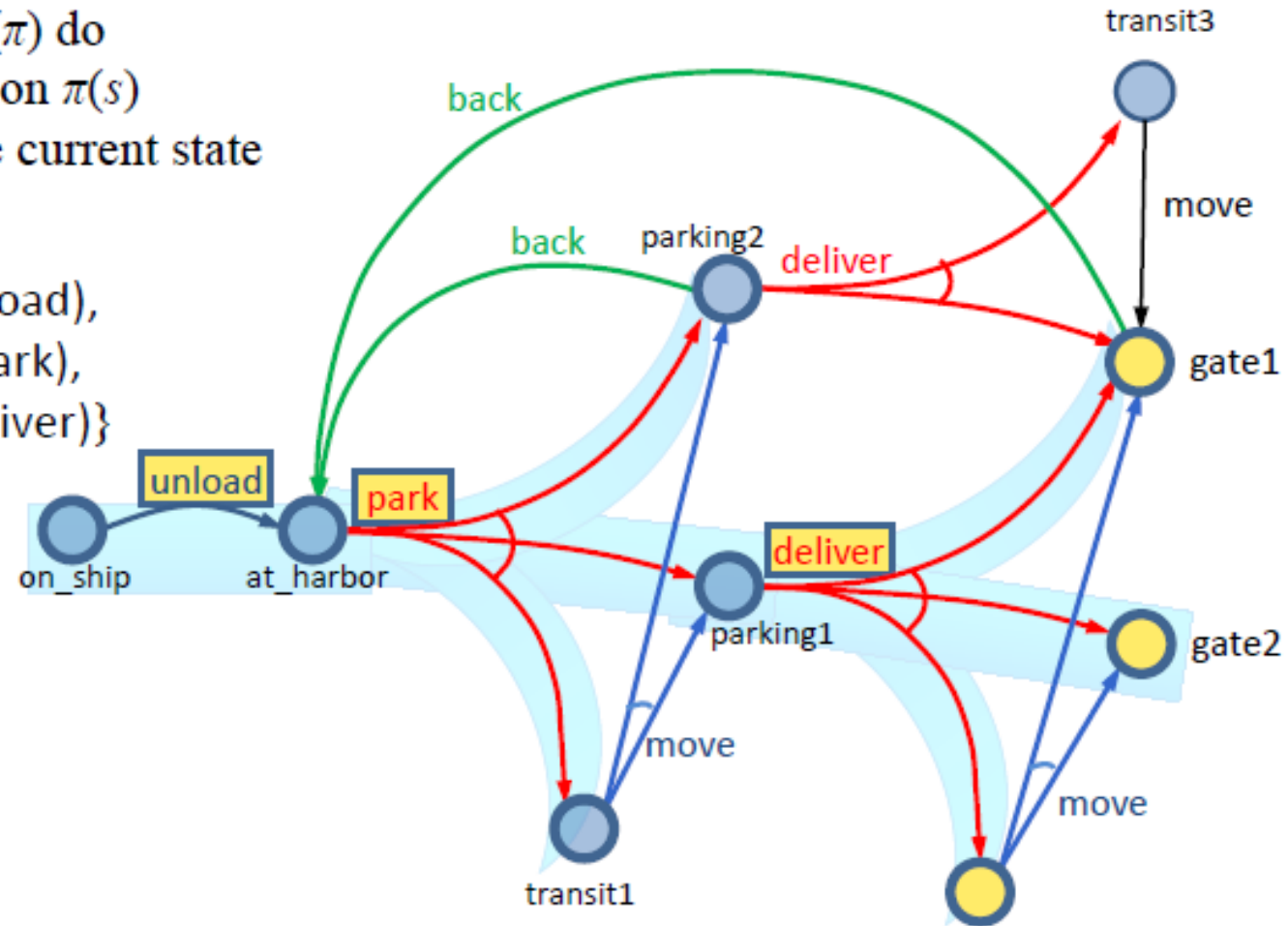
- $\pi_1 = \{(on_ship, unload), (at_harbor, park), (parking1, deliver)\}$
- $leaves(on_ship, \pi_1)$ are yellow
- $leaves(s, \pi) = \hat{\gamma}(s, \pi) \setminus \text{Dom}(\pi)$
 - may be empty



Performing a Policy

- $\text{PerformPolicy}(\pi)$
 - $s \leftarrow \text{observe current state}$
 - while $s \in \text{Dom}(\pi)$ do
 - perform action $\pi(s)$
 - $s \leftarrow \text{observe current state}$

- $\pi_1 = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver})\}$



Planning Problems and Solutions

- Planning problem $P = (\Sigma, s_0, S_g)$
 - planning domain $\Sigma = (S, A, \gamma)$, initial state $s_0 \in S$, set of goal states $S_g \subseteq S$ (shown in green)

$\pi_1 = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver})\}$

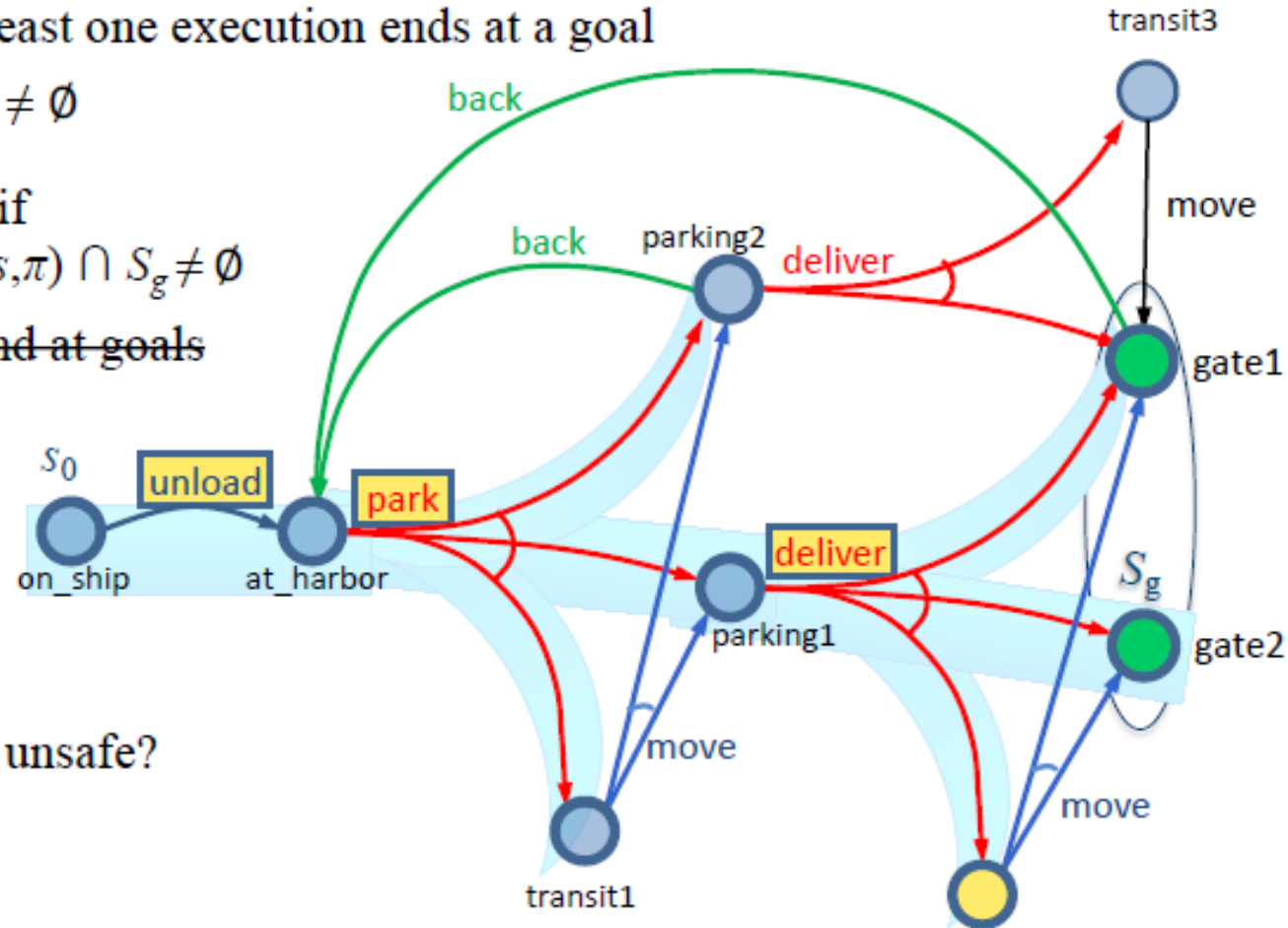
- π is a *solution* if at least one execution ends at a goal
 - $\text{leaves}(s, \pi) \cap S_g \neq \emptyset$

- A solution π is *safe* if
 - $\forall s \in \hat{\gamma}(s_0, \pi), \text{leaves}(s, \pi) \cap S_g \neq \emptyset$

➤ ~~all executions end at goals~~

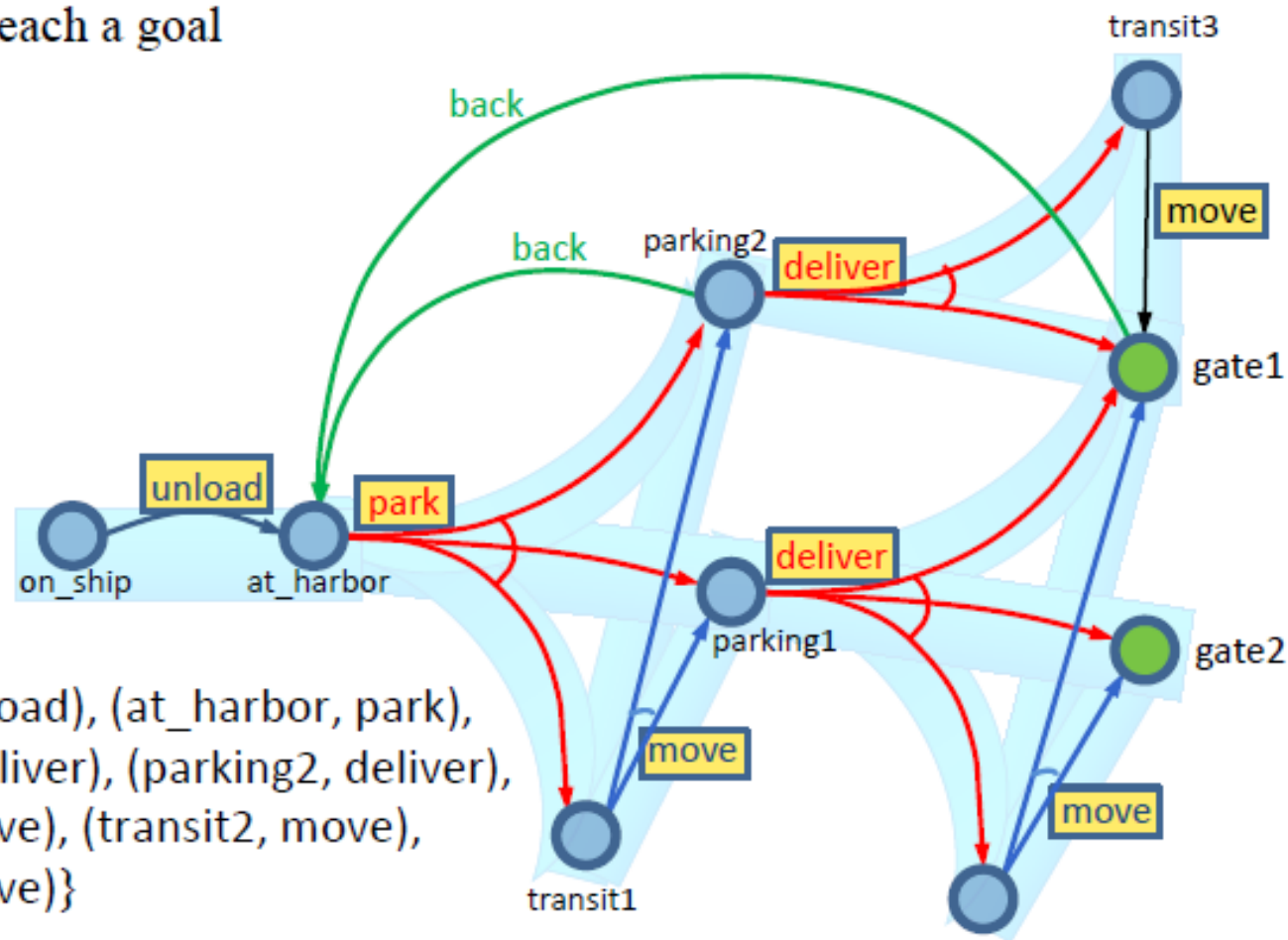
➤ at every node of $\text{Graph}(s_0, \pi)$, the goal is reachable

- Otherwise, *unsafe*
 - Is π_1 safe or unsafe?



Safe Solutions

- *Acyclic safe solution*
 - $\text{Graph}(s_0, \pi)$ is acyclic, and $\text{leaves}(s, \pi) \subseteq S_g$
 - Guaranteed to reach a goal



- $\pi_2 = \{(\text{on_ship}, \text{unload}), (\text{at_harbor}, \text{park}), (\text{parking1}, \text{deliver}), (\text{parking2}, \text{deliver}), (\text{transit1}, \text{move}), (\text{transit2}, \text{move}), (\text{transit3}, \text{move})\}$

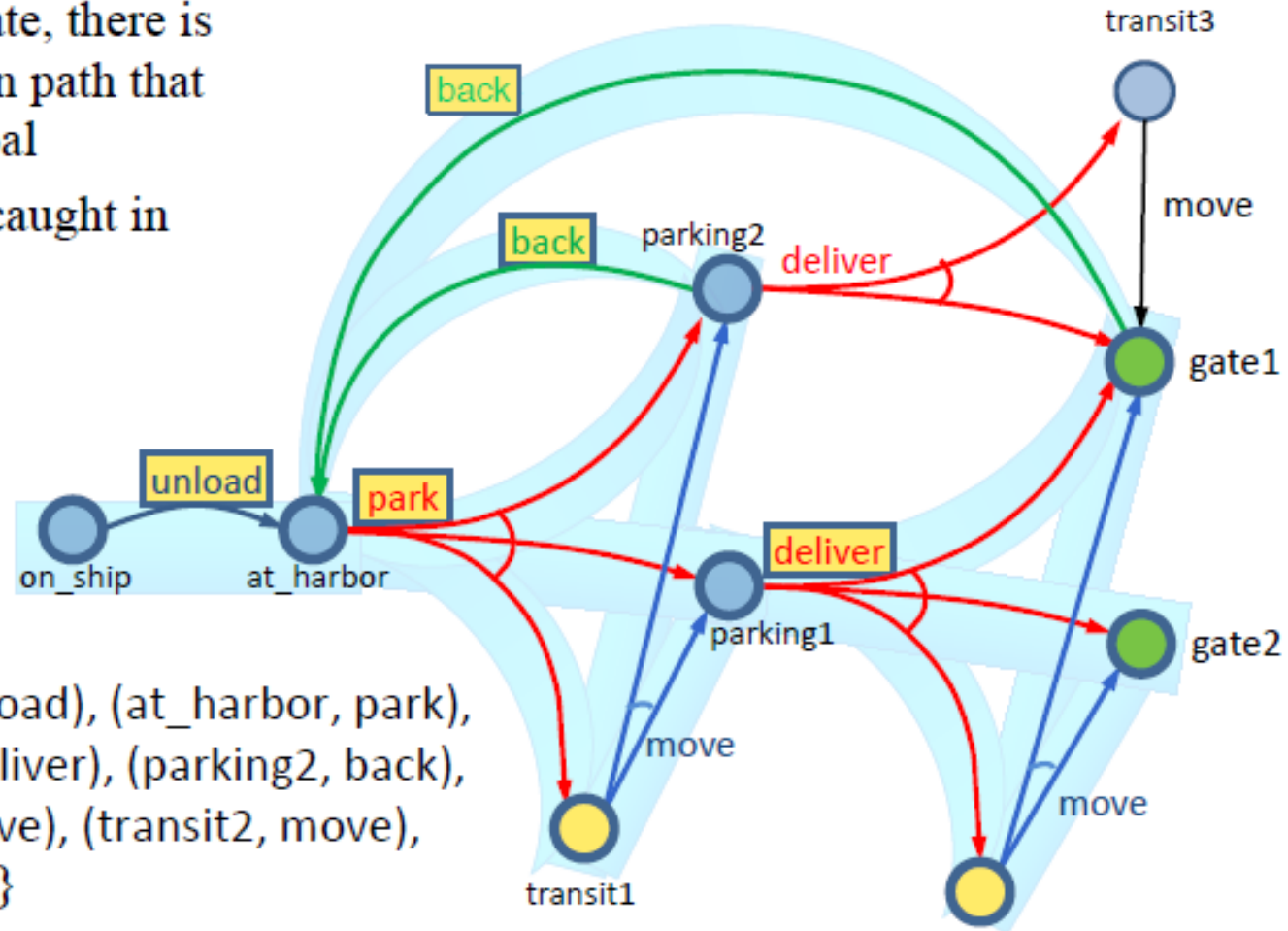
Safe Solutions

- *Cyclic safe solution*

- $\text{Graph}(s_0, \pi)$ is cyclic, $\text{leaves}(s, \pi) \subseteq S_g$, $\forall s \in \hat{\gamma}(s_0, \pi)$, $\text{leaves}(s, \pi) \cap S_g \neq \emptyset$

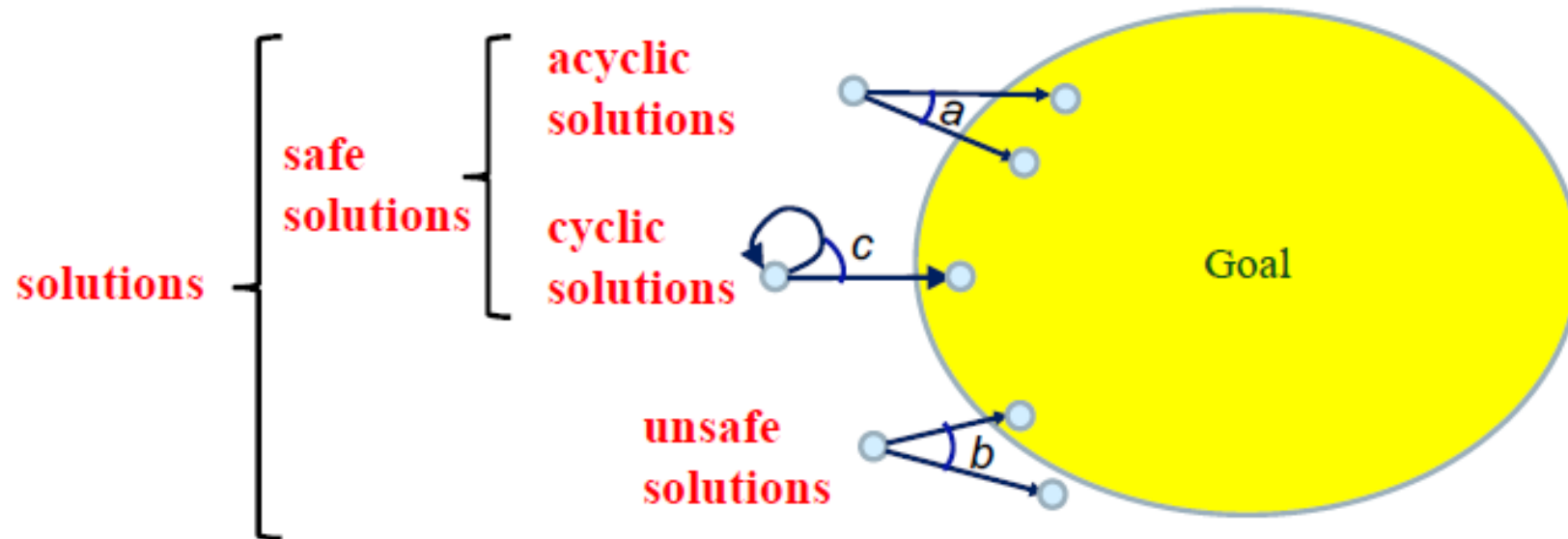
- At every state, there is an execution path that ends at a goal

- Will never get caught in a dead end



- $\pi_3 = \{(\text{on_ship}, \text{unload}), (\text{at_harbor}, \text{park}), (\text{parking1}, \text{deliver}), (\text{parking2}, \text{back}), (\text{transit1}, \text{move}), (\text{transit2}, \text{move}), (\text{gate1}, \text{back})\}$

Kinds of Solutions



Finding (Unsafe) Solutions

For comparison:

Forward-search (Σ, s_0, g)

$s \leftarrow s_0; \pi \leftarrow \langle \rangle$

loop

if s satisfies g then return π

$A' \leftarrow \{a \in A \mid a \text{ is applicable in } s\}$

if $A' = \emptyset$ then return failure

nondeterministically choose $a \in A'$

$s \leftarrow \gamma(s, a); \pi \leftarrow \pi.a$

Find-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset; s \leftarrow s_0; Visited \leftarrow \{s_0\}$

loop

if $s \in S_g$ then return π

$A' \leftarrow \text{Applicable}(s)$

if $A' = \emptyset$ then return failure

nondeterministically choose $a \in A'$

(*) nondeterministically choose $s' \in \gamma(s, a)$

if $s' \in Visited$ then return failure

$\pi(s) \leftarrow a; Visited \leftarrow Visited \cup \{s'\}; s \leftarrow s'$

Decide which state to plan for

Cycle-checking

Poll: which should (*) be?

1. nondeterministically choose
2. arbitrarily choose

Find-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$; $s \leftarrow s_0$; $Visited \leftarrow \{s_0\}$

loop

if $s \in S_g$ then return π

$A' \leftarrow \text{Applicable}(s)$

if $A' = \emptyset$ then return failure

nondeterministically choose $a \in A'$

nondeterministically choose $s' \in \gamma(s, a)$

if $s' \in Visited$ then return failure

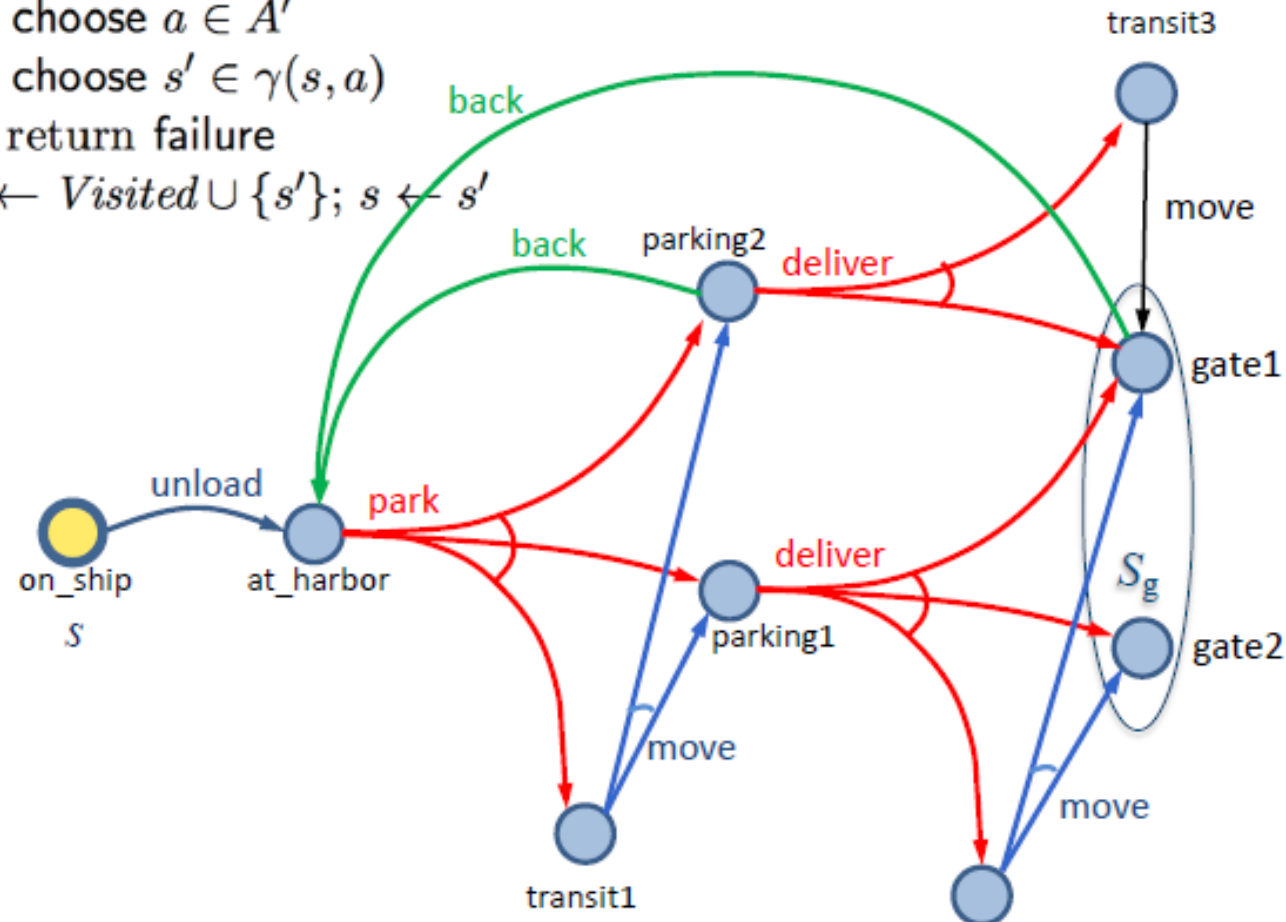
$\pi(s) \leftarrow a$; $Visited \leftarrow Visited \cup \{s'\}$; $s \leftarrow s'$

$s = \text{on_ship}$

$\pi = \{\}$

$Visited = \{\text{on_ship}\}$

Example



Find-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$; $s \leftarrow s_0$; $Visited \leftarrow \{s_0\}$

loop

if $s \in S_g$ then return π

$A' \leftarrow \text{Applicable}(s)$

if $A' = \emptyset$ then return failure

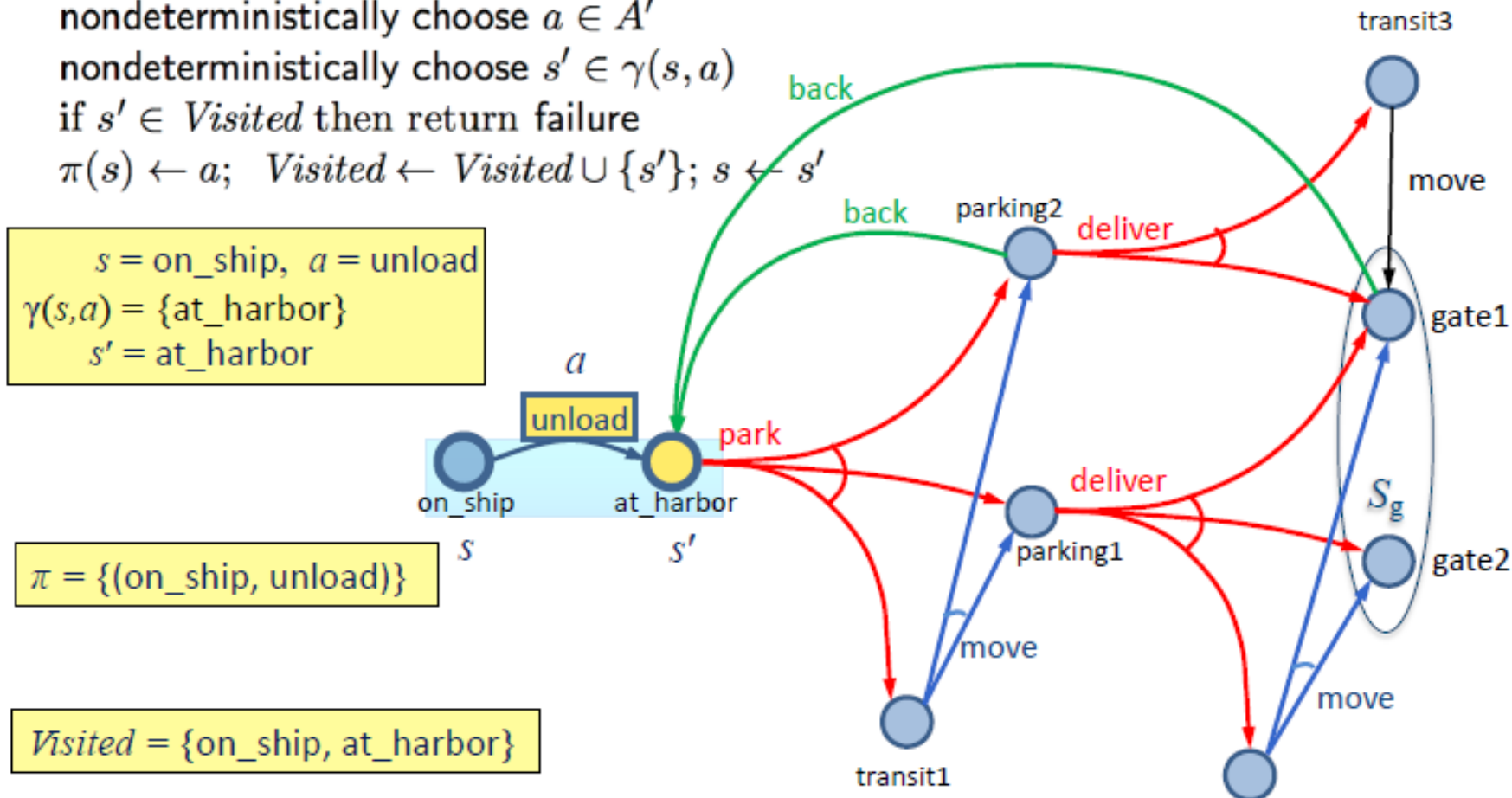
nondeterministically choose $a \in A'$

nondeterministically choose $s' \in \gamma(s, a)$

if $s' \in Visited$ then return failure

$\pi(s) \leftarrow a$; $Visited \leftarrow Visited \cup \{s'\}$; $s \leftarrow s'$

Example



Find-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$; $s \leftarrow s_0$; $Visited \leftarrow \{s_0\}$

loop

if $s \in S_g$ then return π

$A' \leftarrow \text{Applicable}(s)$

if $A' = \emptyset$ then return failure

nondeterministically choose $a \in A'$

nondeterministically choose $s' \in \gamma(s, a)$

if $s' \in Visited$ then return failure

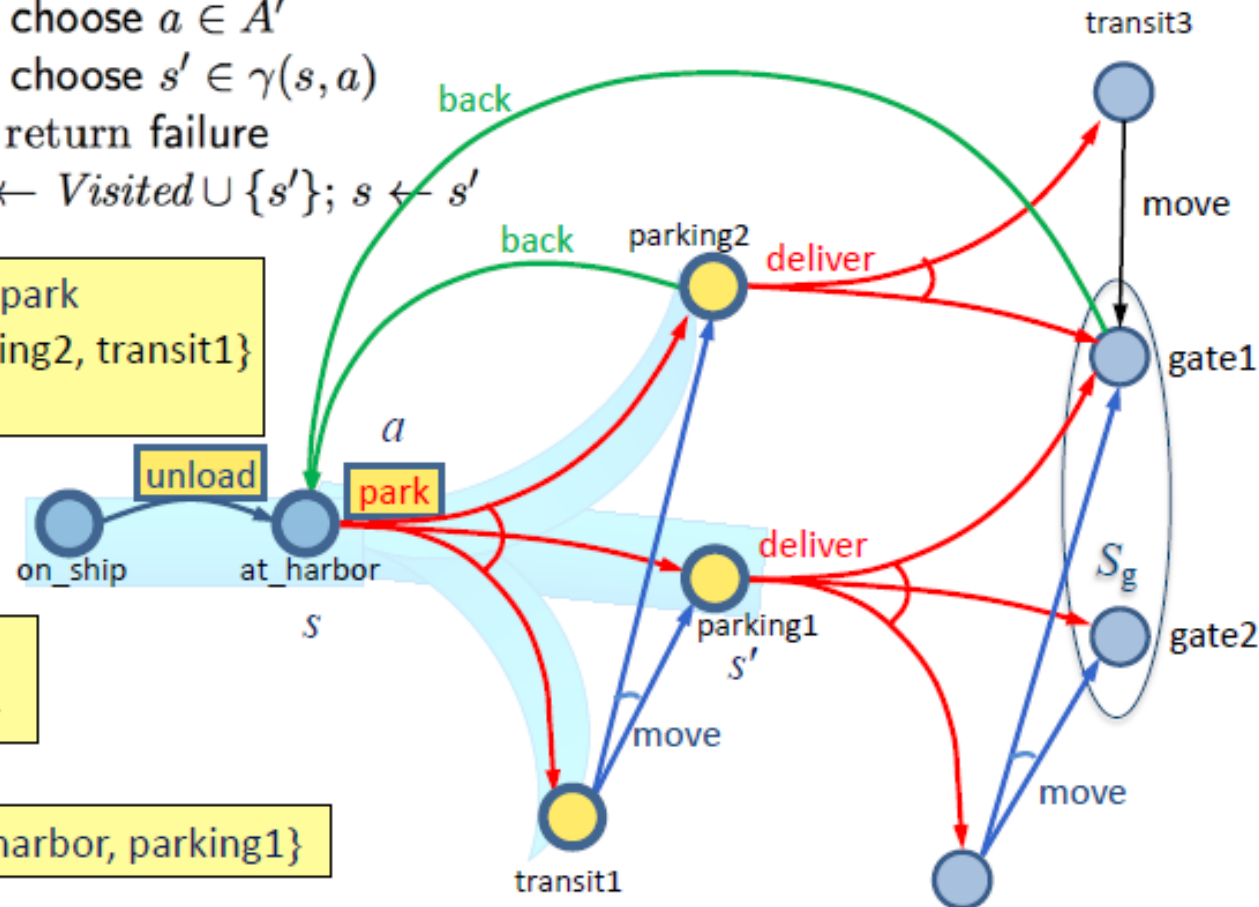
$\pi(s) \leftarrow a$; $Visited \leftarrow Visited \cup \{s'\}$; $s \leftarrow s'$

$s = \text{at_harbor}$, $a = \text{park}$
 $\gamma(s, a) = \{\text{parking1}, \text{parking2}, \text{transit1}\}$
 $s' = \text{parking1}$

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park})\}$

$Visited = \{\text{on_ship}, \text{at_harbor}, \text{parking1}\}$

Example



Find-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset; s \leftarrow s_0; Visited \leftarrow \{s_0\}$

loop

if $s \in S_g$ then return π

$A' \leftarrow \text{Applicable}(s)$

if $A' = \emptyset$ then return failure

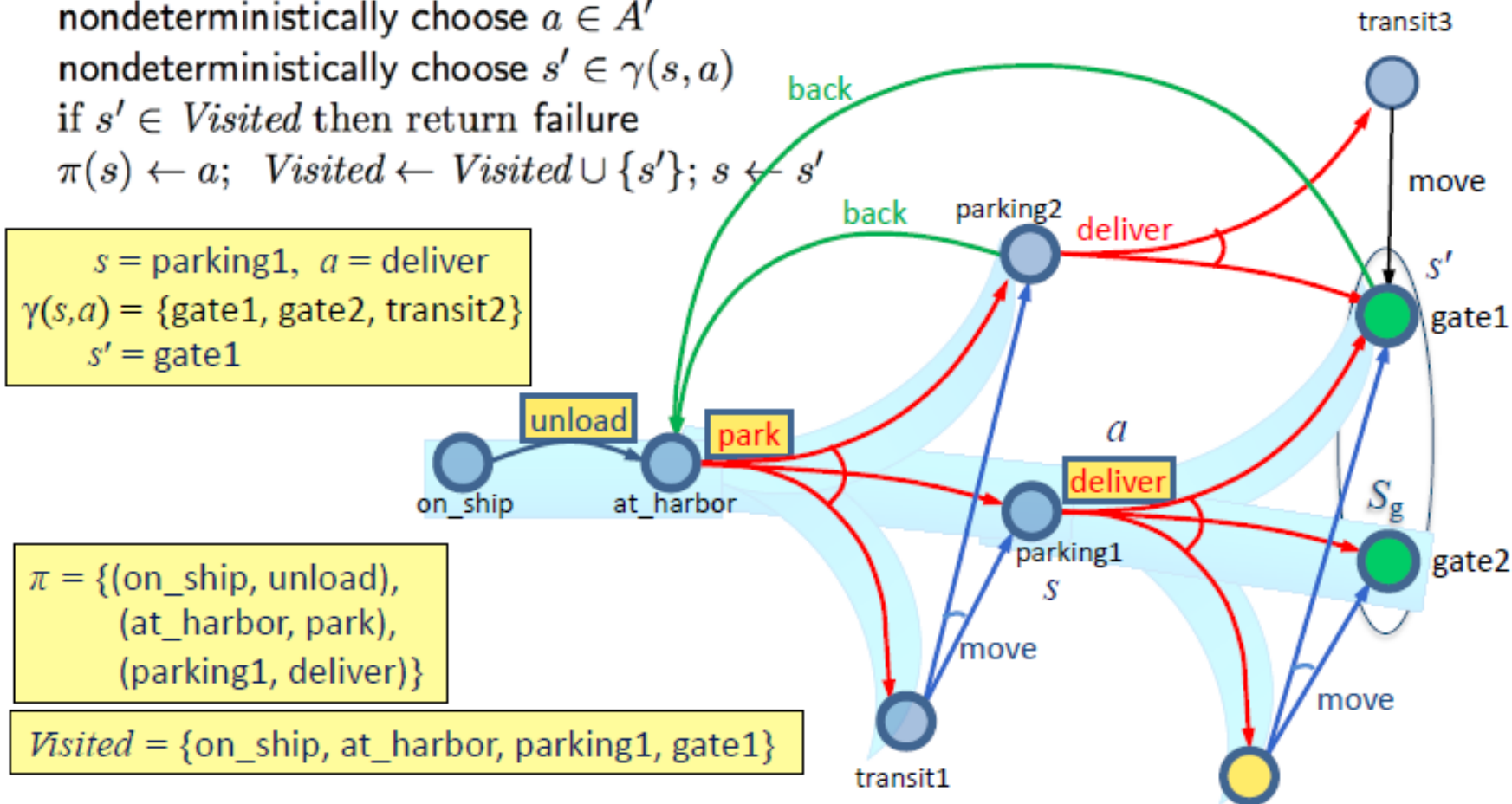
nondeterministically choose $a \in A'$

nondeterministically choose $s' \in \gamma(s, a)$

if $s' \in Visited$ then return failure

$\pi(s) \leftarrow a; Visited \leftarrow Visited \cup \{s'\}; s \leftarrow s'$

Example



Find-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$; $s \leftarrow s_0$; $Visited \leftarrow \{s_0\}$

loop

if $s \in S_g$ then return π

$A' \leftarrow \text{Applicable}(s)$

if $A' = \emptyset$ then return failure

nondeterministically choose $a \in A'$

nondeterministically choose $s' \in \gamma(s, a)$

if $s' \in Visited$ then return failure

$\pi(s) \leftarrow a$; $Visited \leftarrow Visited \cup \{s'\}$; $s \leftarrow s'$

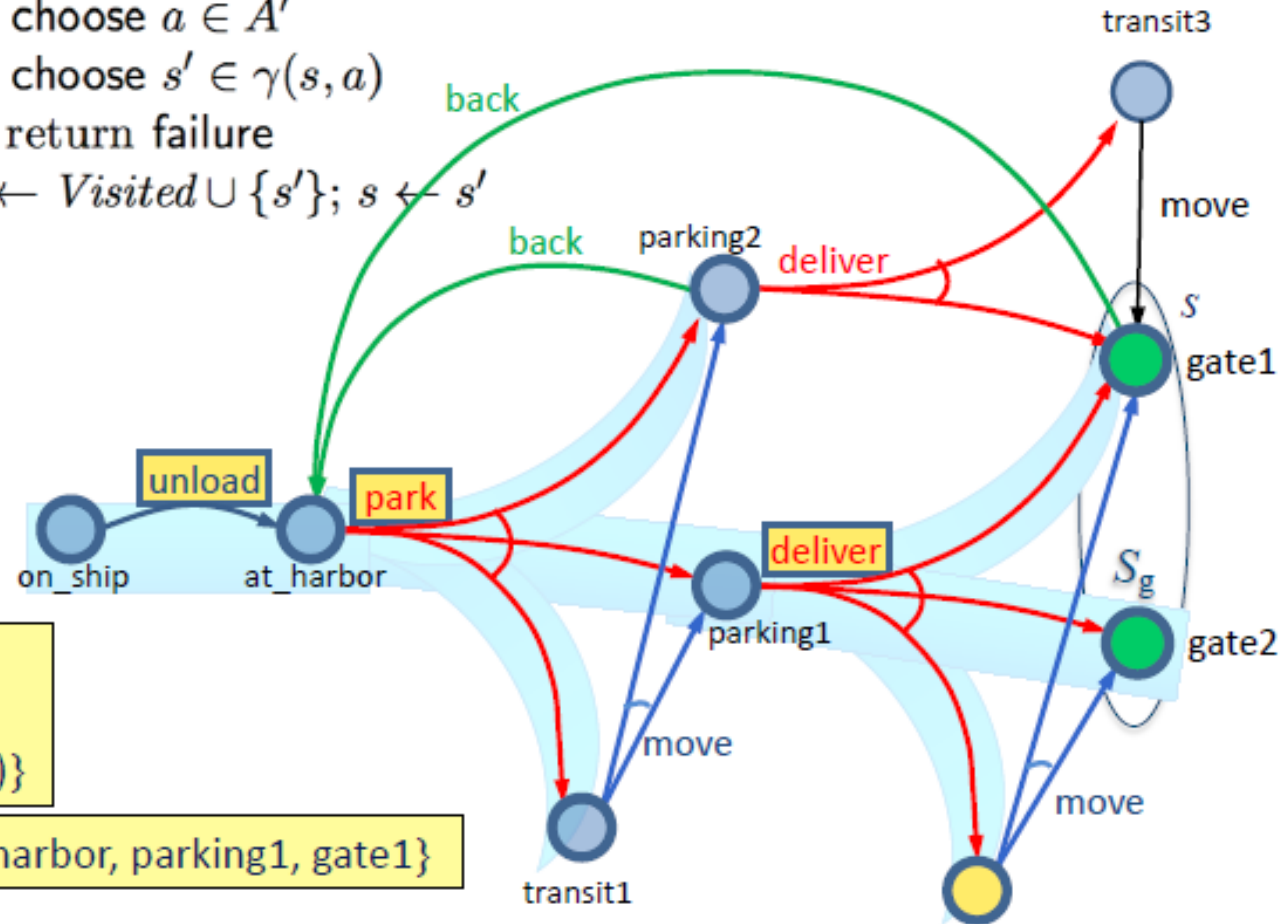
$s = \text{gate1}$

gate1 is a goal,
so return π

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver})\}$

$Visited = \{\text{on_ship}, \text{at_harbor}, \text{parking1}, \text{gate1}\}$

Example



Finding Acyclic Safe Solutions

Find-Acyclic-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

 if $Applicable(s) = \emptyset$ then return failure

 nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

 if $has-loops(\pi, a, Frontier)$ then return failure

return π

Check for cycles:

For each $s' \in \gamma(s, a) \cap Dom(\pi)$, is $s \in \hat{\gamma}(s', \pi)$?

Find-Acyclic-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

 if $Applicable(s) = \emptyset$ then return failure

 nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

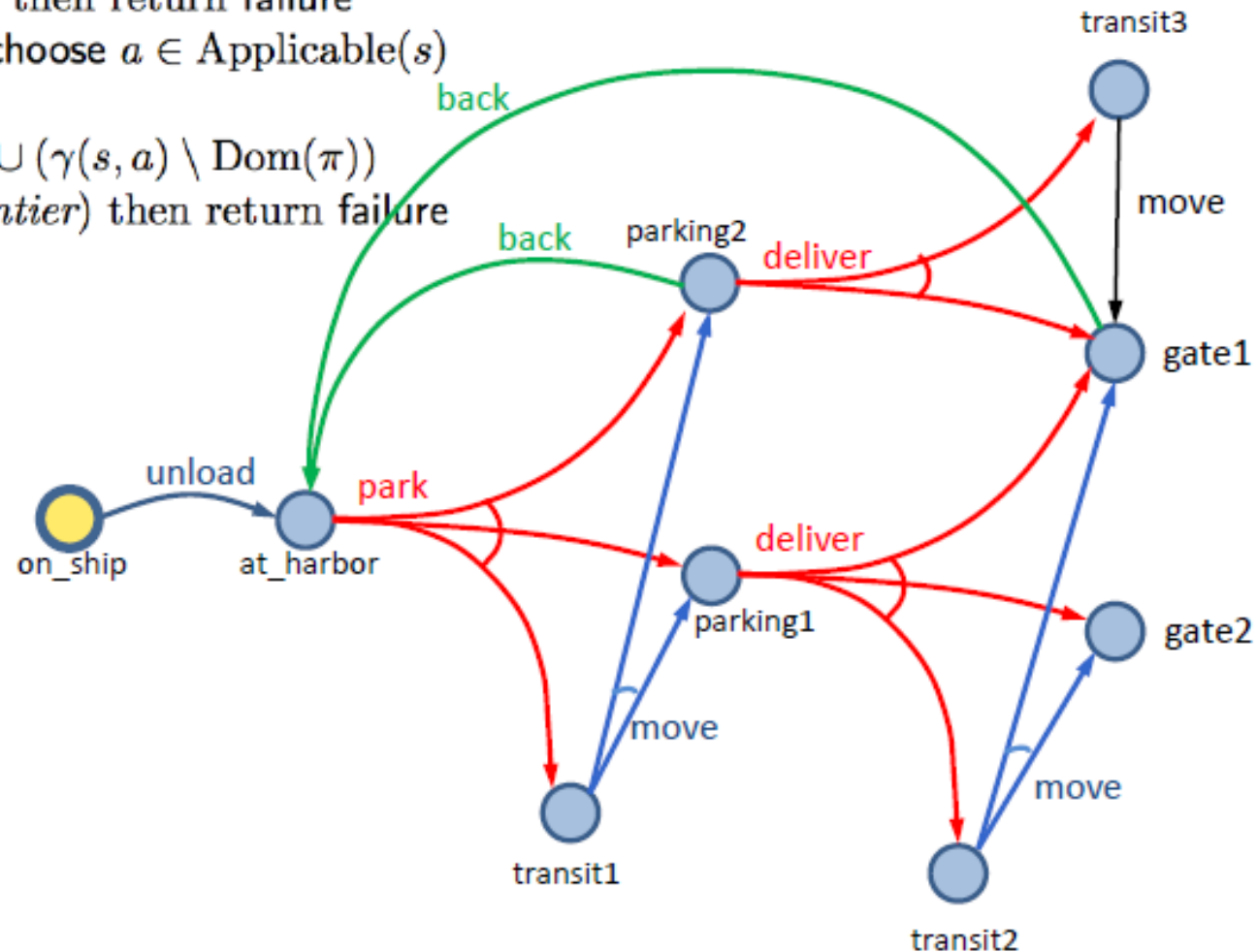
 if $has-loops(\pi, a, Frontier)$ then return failure

return π

$Frontier \setminus S_g = \{on_ship\}$

$\pi = \{\}$

Example



Example

Find-Acyclic-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

 if $Applicable(s) = \emptyset$ then return failure

 nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

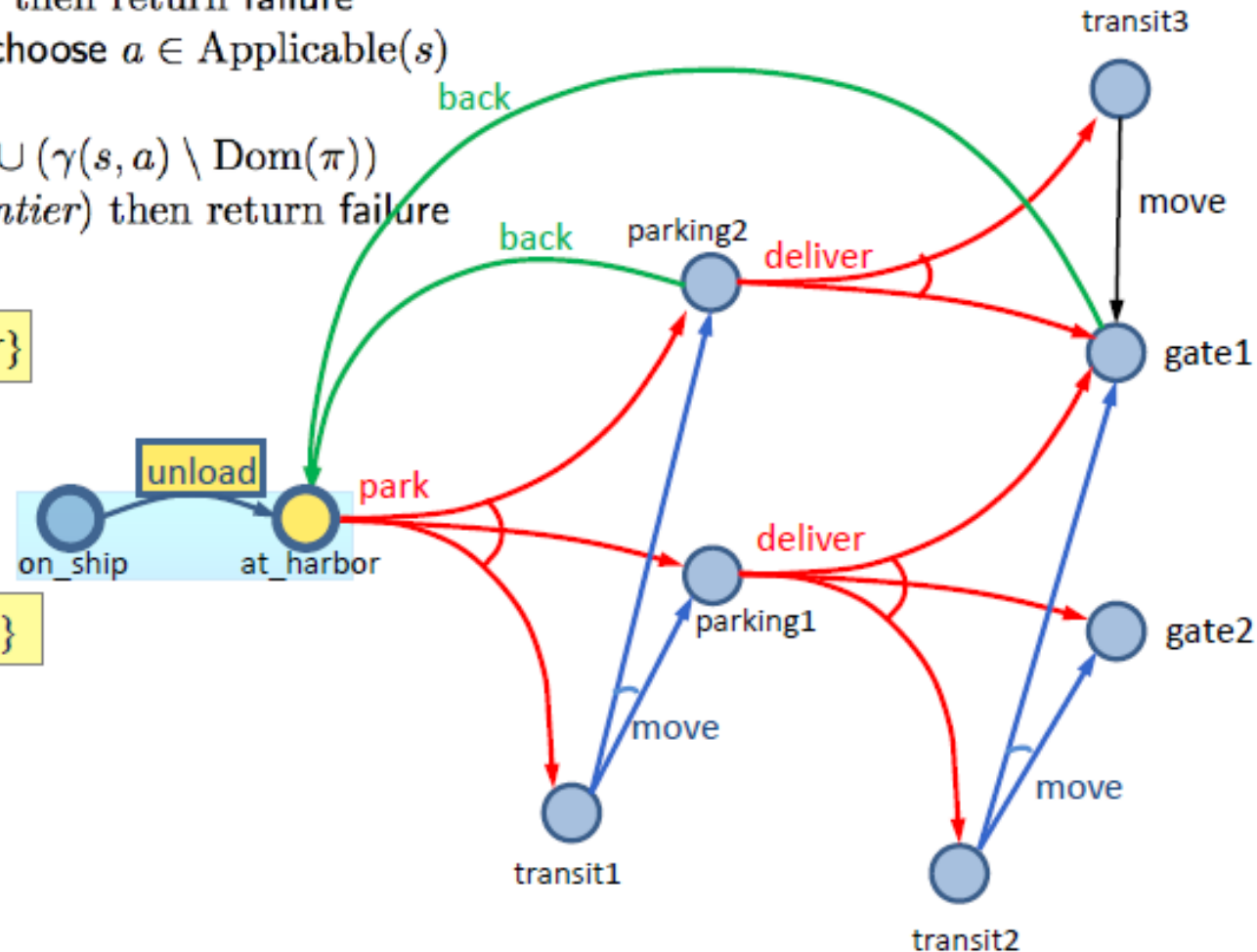
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

 if $has-loops(\pi, a, Frontier)$ then return failure

return π

$Frontier \setminus S_g = \{at_harbor\}$

$\pi = \{(on_ship, unload)\}$



Example

Find-Acyclic-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

if $Applicable(s) = \emptyset$ then return failure

nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

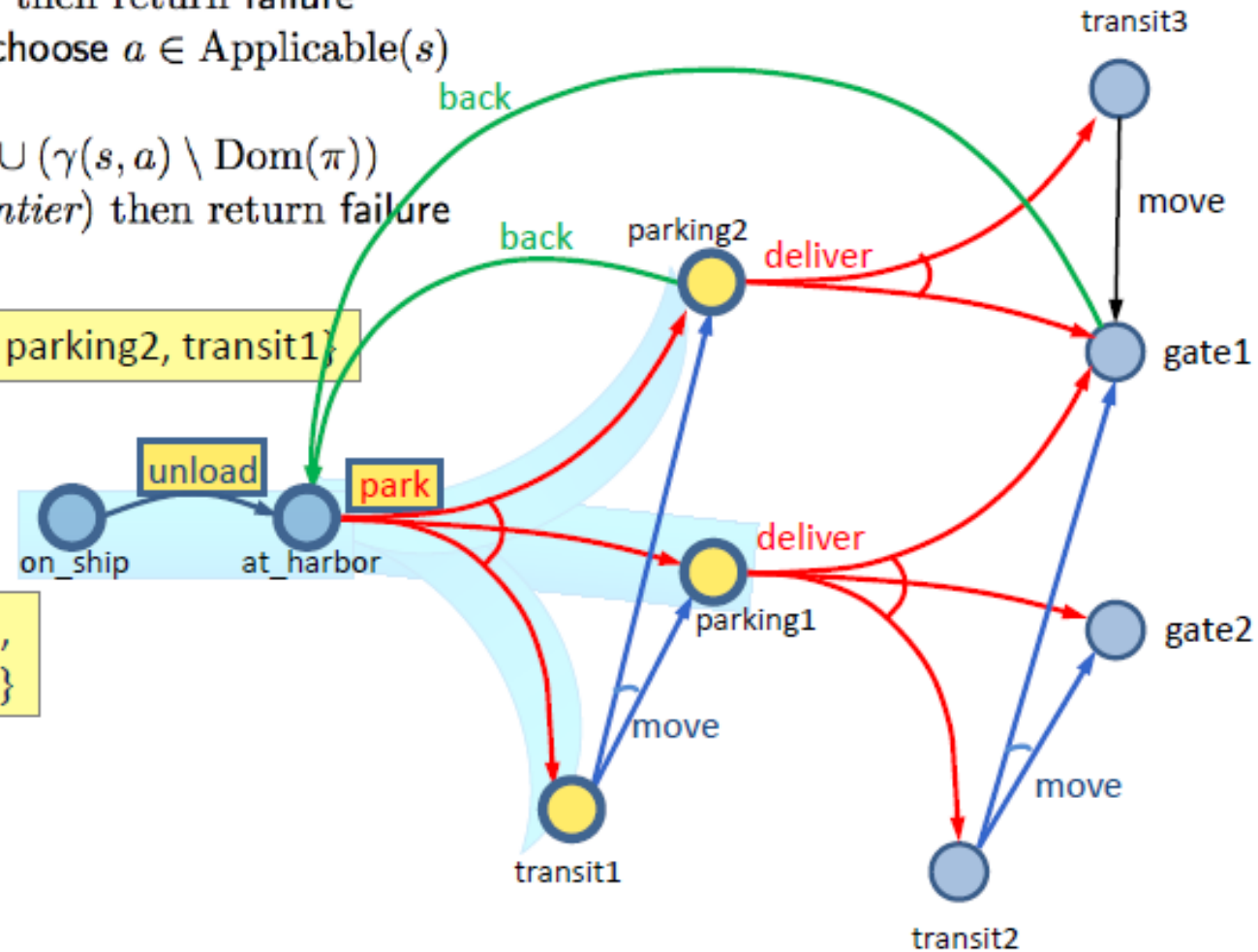
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if $has-loops(\pi, a, Frontier)$ then return failure

return π

$Frontier \setminus S_g = \{parking1, parking2, transit1\}$

$\pi = \{(on_ship, unload), (at_harbor, park)\}$



Example

Find-Acyclic-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

 if $Applicable(s) = \emptyset$ then return failure

 nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

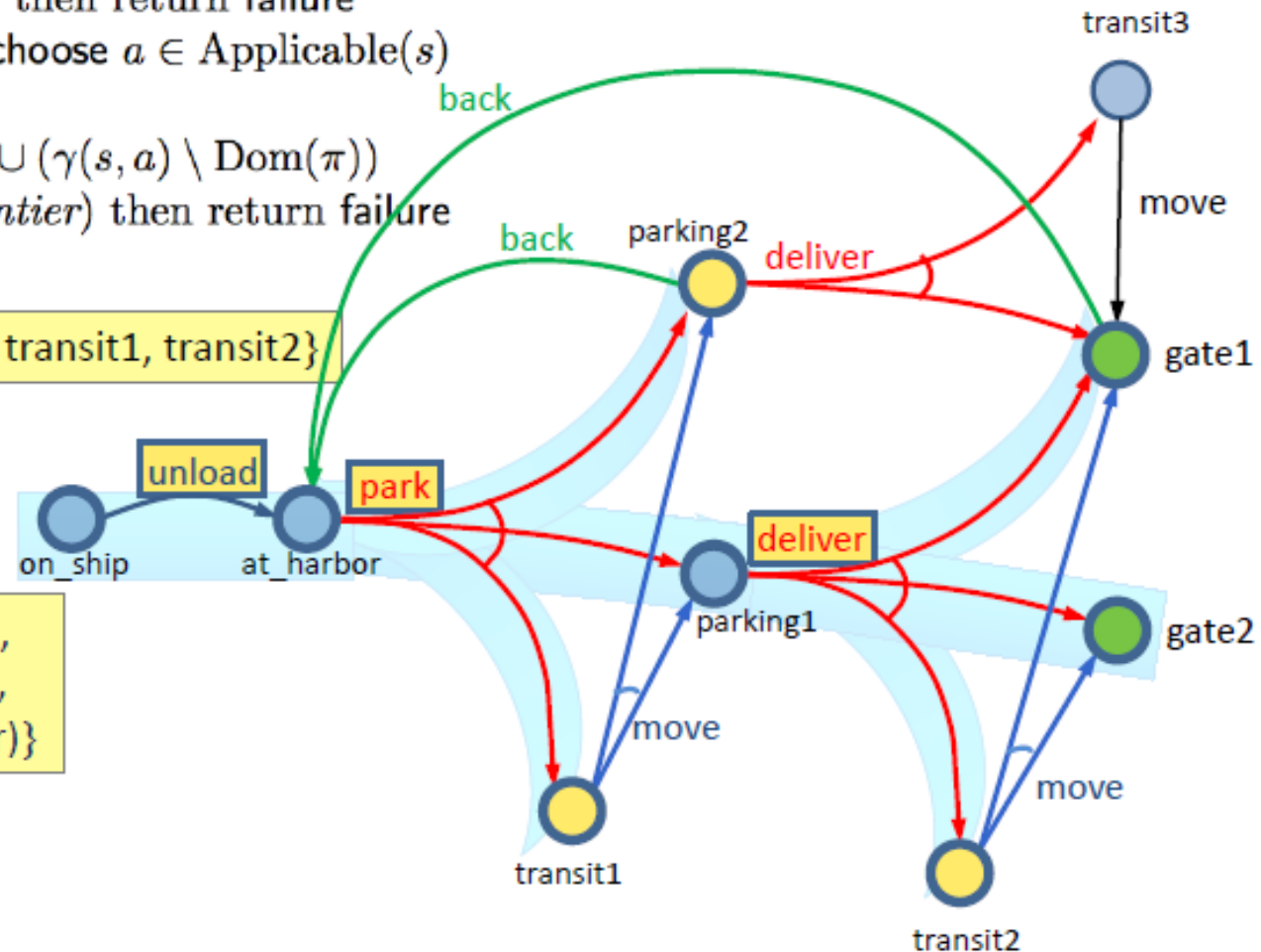
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

 if $has-loops(\pi, a, Frontier)$ then return failure

return π

$Frontier \setminus S_g = \{\text{parking2}, \text{transit1}, \text{transit2}\}$

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver})\}$



Find-Acyclic-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

 if $Applicable(s) = \emptyset$ then return failure

 nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

 if $has-loops(\pi, a, Frontier)$ then return failure

return π

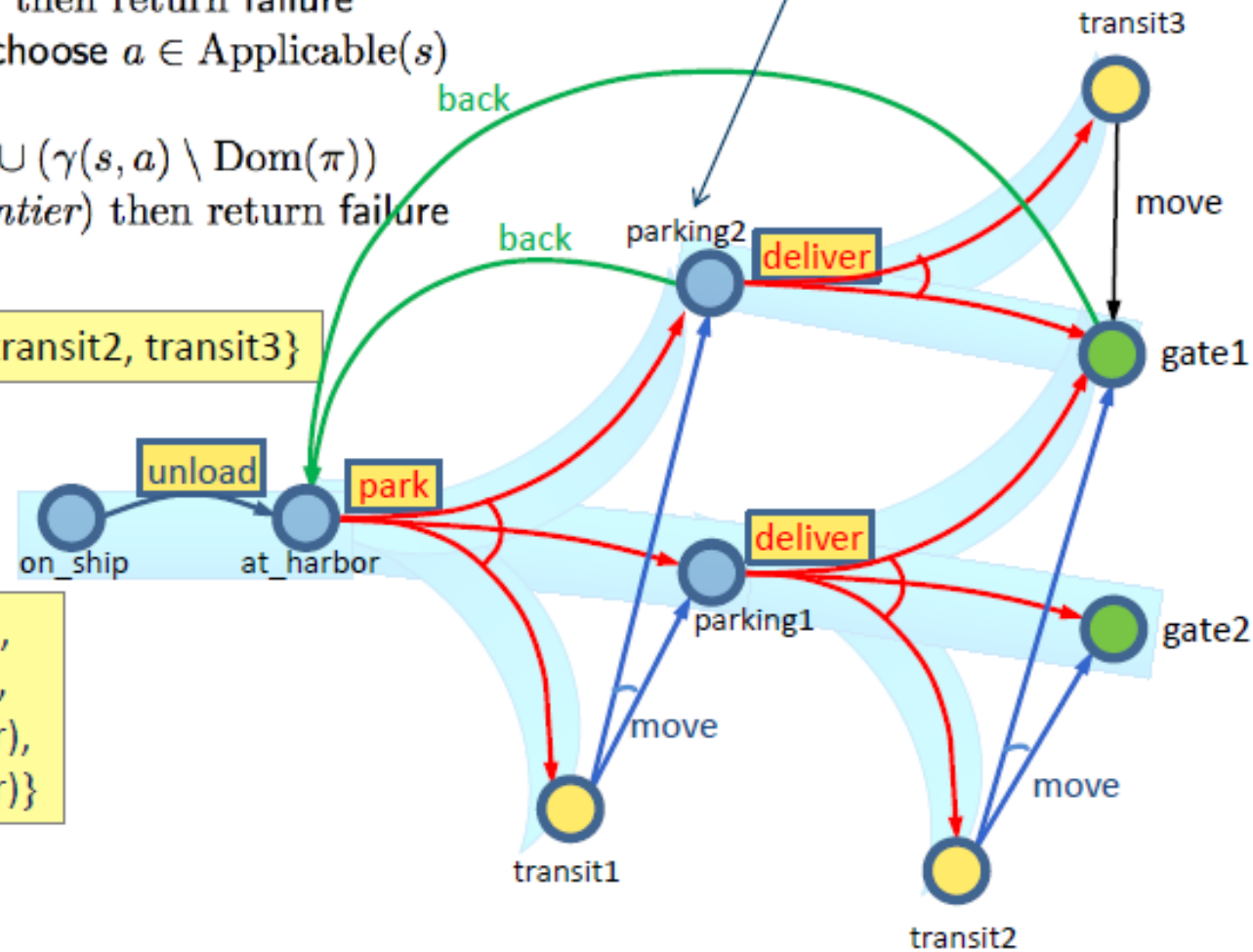
$Frontier \setminus S_g = \{transit1, transit2, transit3\}$

$\pi = \{(on_ship, unload),$
 $(at_harbor, park),$
 $(parking1, deliver),$
 $(parking2, deliver)\}$

Example

nondeterministically choose back or deliver

- back \Rightarrow cycle, so return failure
- deliver \Rightarrow no cycle, so continue



Example

Find-Acyclic-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

 if $Applicable(s) = \emptyset$ then return failure

 nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

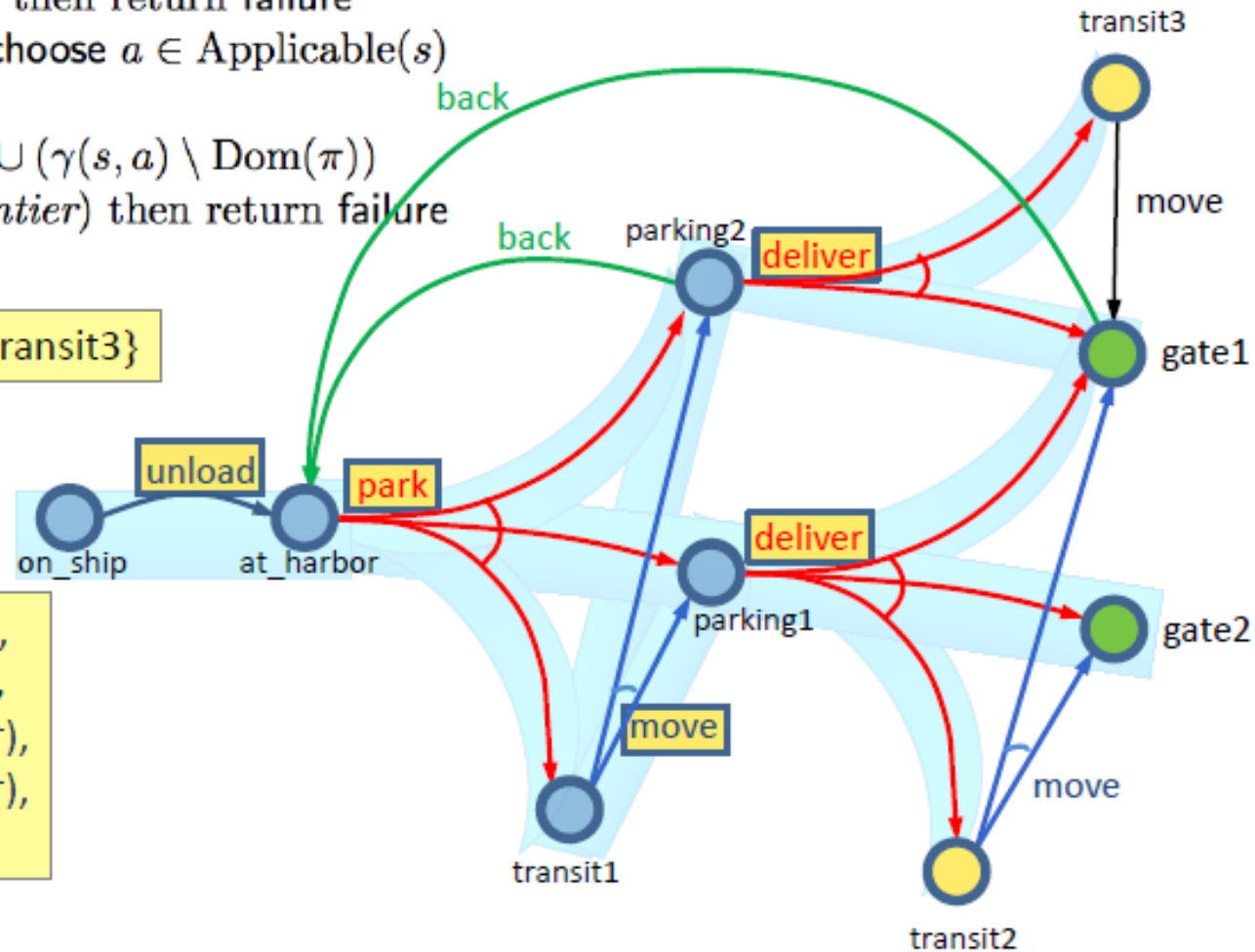
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

 if $has-loops(\pi, a, Frontier)$ then return failure

return π

$Frontier \setminus S_g = \{transit2, transit3\}$

$\pi = \{(on_ship, unload),$
 $(at_harbor, park),$
 $(parking1, deliver),$
 $(parking2, deliver),$
 $(transit1, move)\}$



Example

Find-Acyclic-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

 if $Applicable(s) = \emptyset$ then return failure

 nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

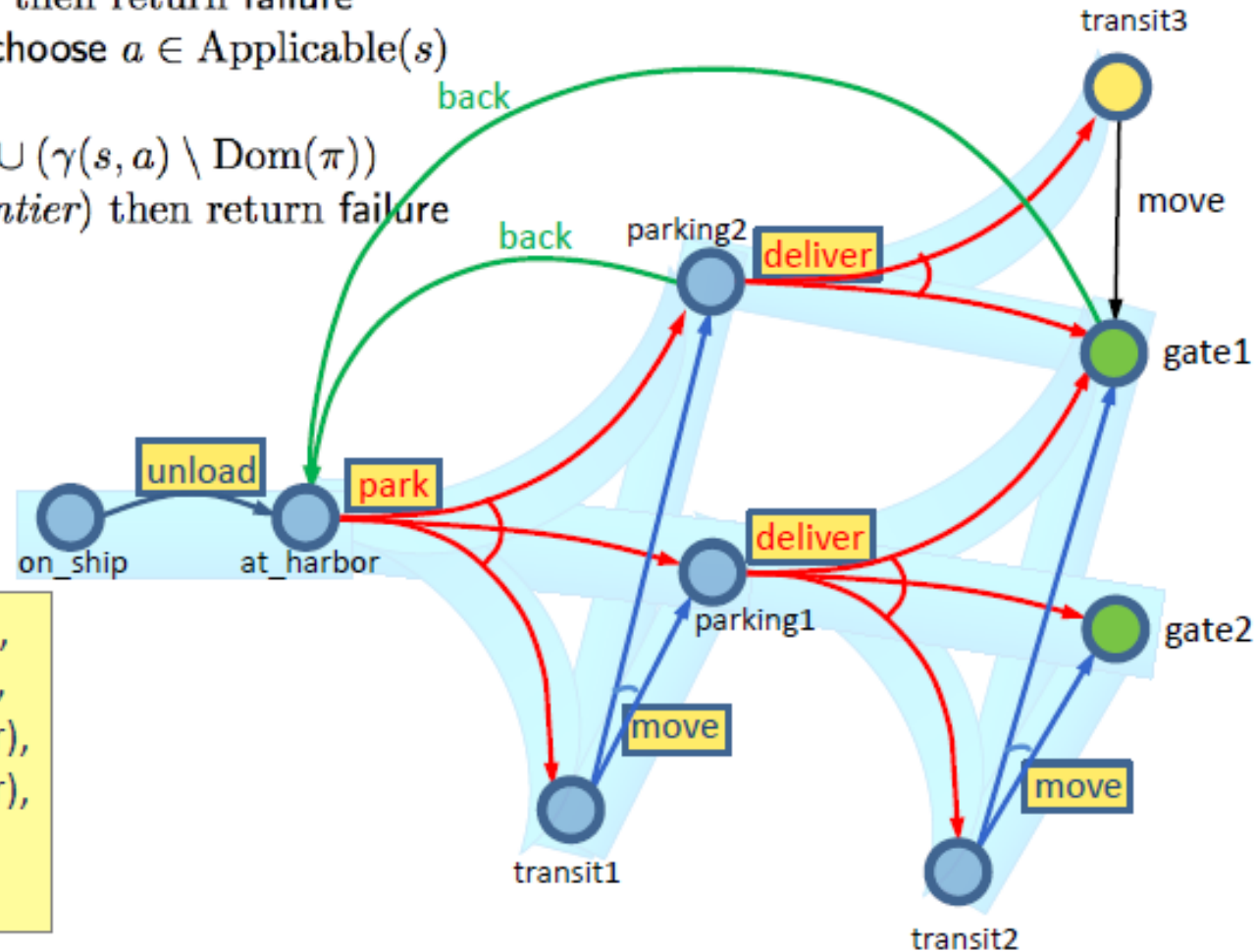
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

 if $has-loops(\pi, a, Frontier)$ then return failure

return π

$Frontier \setminus S_g = \{transit3\}$

$\pi = \{(on_ship, unload),$
 $(at_harbor, park),$
 $(parking1, deliver),$
 $(parking2, deliver),$
 $(transit1, move),$
 $(transit2, move)\}$



Find-Acyclic-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

 if $Applicable(s) = \emptyset$ then return failure

 nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

 if $has-loops(\pi, a, Frontier)$ then return failure

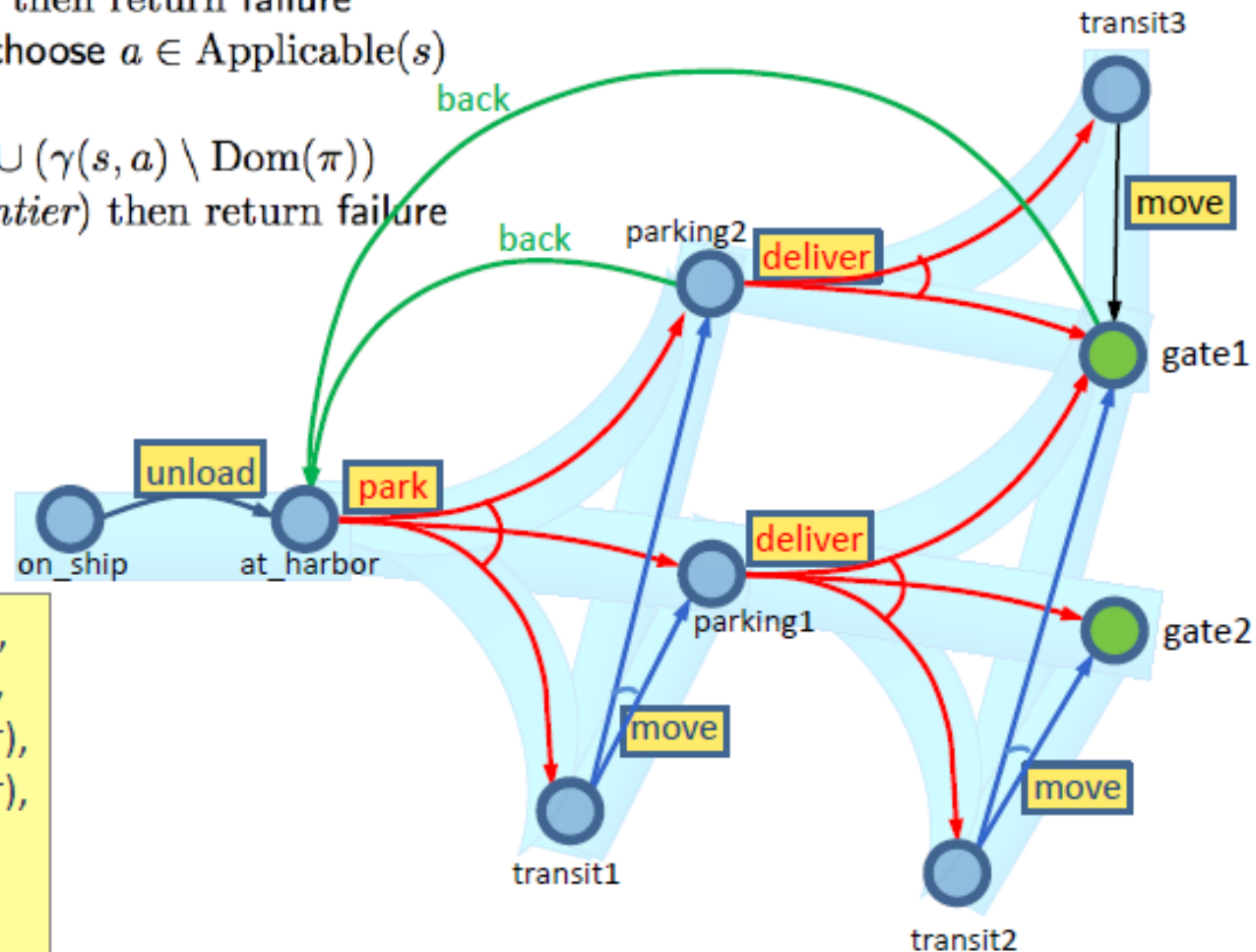
return π

$Frontier \setminus S_g = \emptyset$

Found a solution

$\pi = \{(on_ship, unload),$
 $(at_harbor, park),$
 $(parking1, deliver),$
 $(parking2, deliver),$
 $(transit1, move),$
 $(transit2, move),$
 $(transit3, move)\}$

Example



Find-Safe-Solution

Find-Safe-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

*Keep track of unexpanded states, like A^**

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

if $Applicable(s) = \emptyset$ then return failure

nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

*Add all outcomes that
 π doesn't already handle*

if $has_unsafe_loops(\pi, a, Frontier)$ then return failure

return π

- Same as Find-Acyclic-Solution except for one difference:
- has_unsafe_loops instead of has_loops
 - Check whether π contains any cycles that can't be escaped:
 - For each $s' \in \gamma(s, a) \cap Dom(\pi)$, is $\hat{\gamma}(s', \pi) \cap Frontier = \emptyset$?

Find-Safe-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

 if $Applicable(s) = \emptyset$ then return failure

 nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

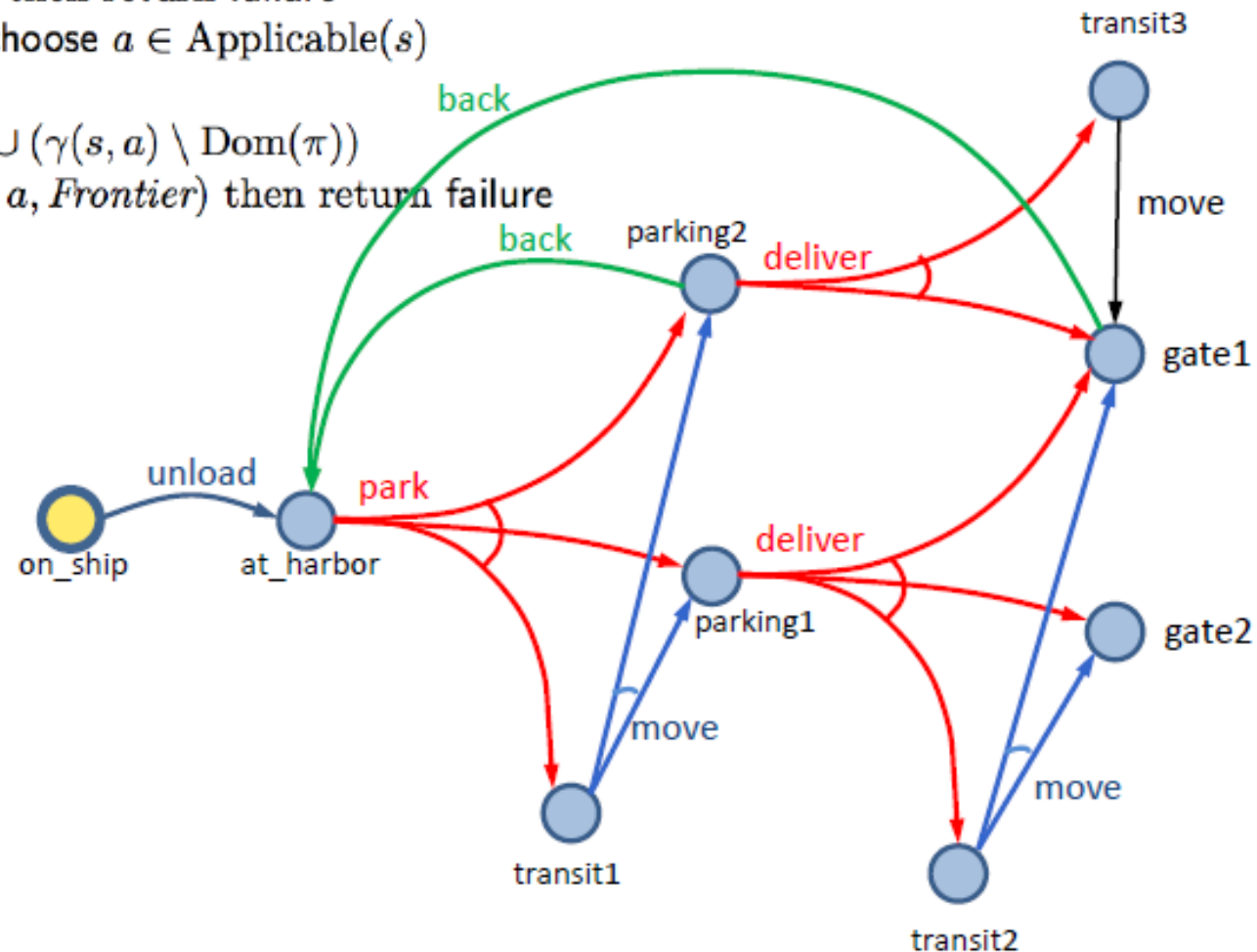
 if $has_unsafe_loops(\pi, a, Frontier)$ then return failure

return π

$Frontier \setminus S_g = \{on_ship\}$

$\pi = \{\}$

Example



Find-Safe-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

 if $Applicable(s) = \emptyset$ then return failure

 nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

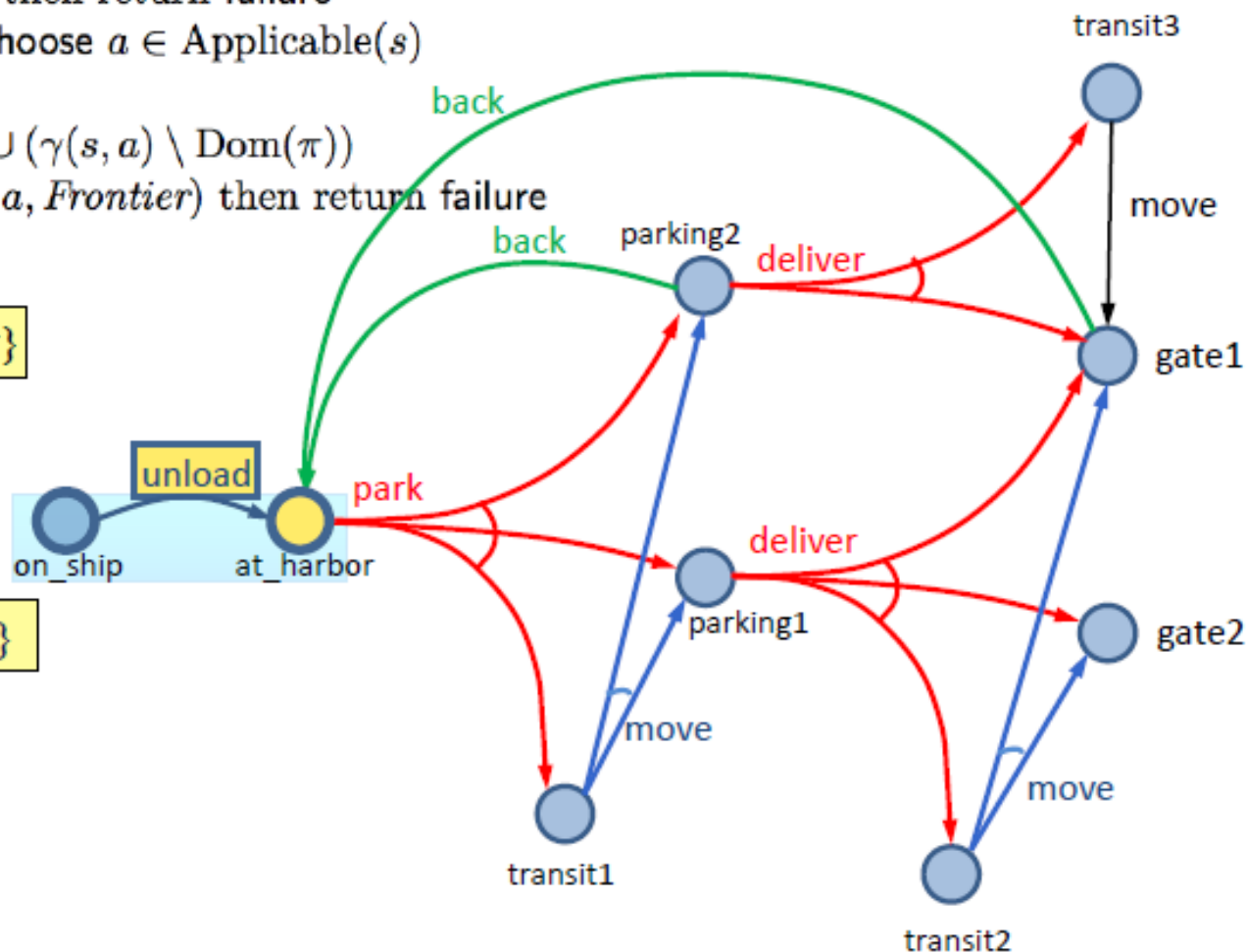
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

 if $has_unsafe_loops(\pi, a, Frontier)$ then return failure

return π

$Frontier \setminus S_g = \{at_harbor\}$

$\pi = \{(on_ship, unload)\}$



Example

Example

Find-Safe-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

 if $Applicable(s) = \emptyset$ then return failure

 nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

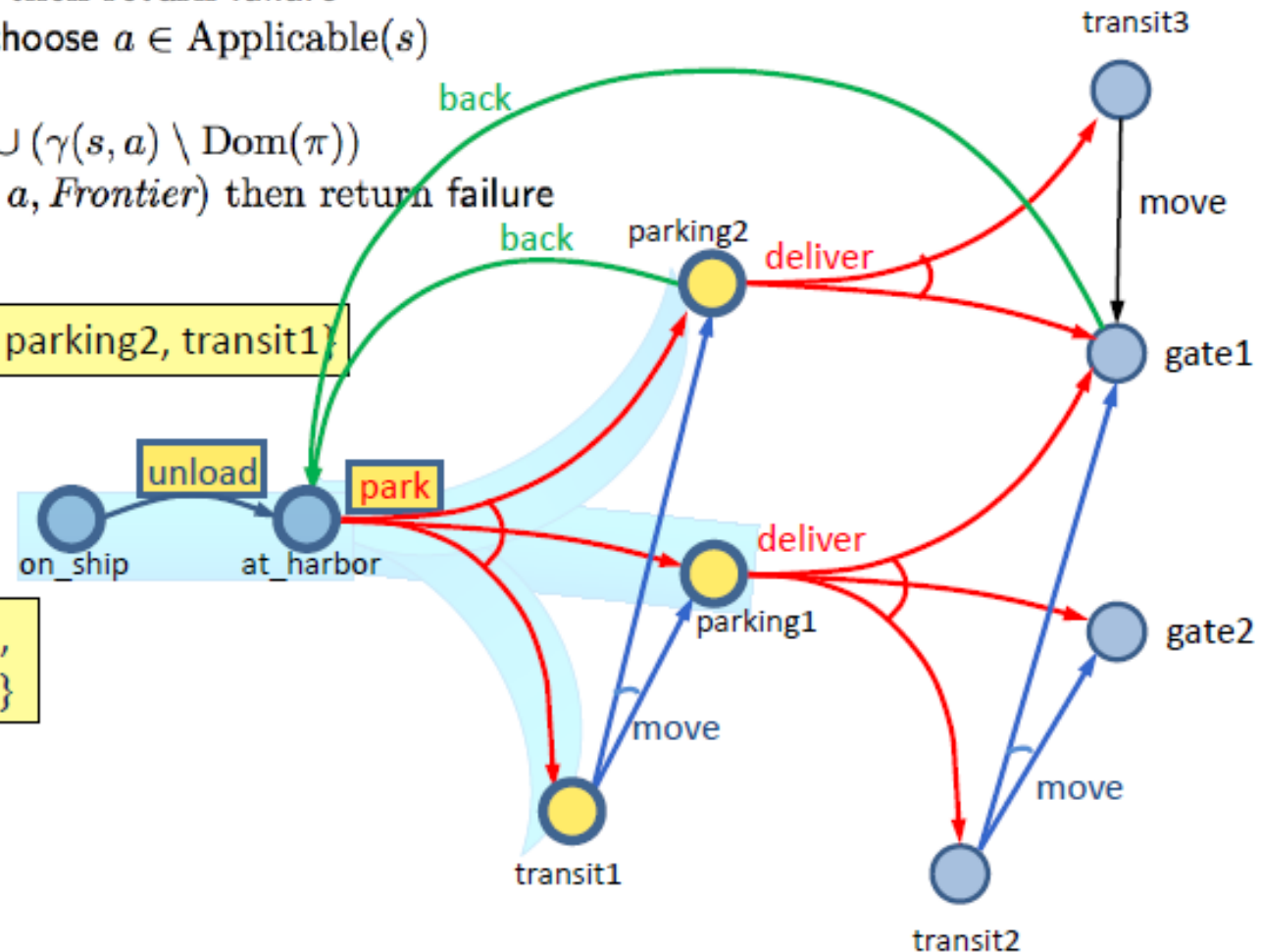
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

 if $has_unsafe_loops(\pi, a, Frontier)$ then return failure

return π

$Frontier \setminus S_g = \{parking1, parking2, transit1\}$

$\pi = \{(on_ship, unload), (at_harbor, park)\}$



Example

Find-Safe-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

 if $Applicable(s) = \emptyset$ then return failure

 nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

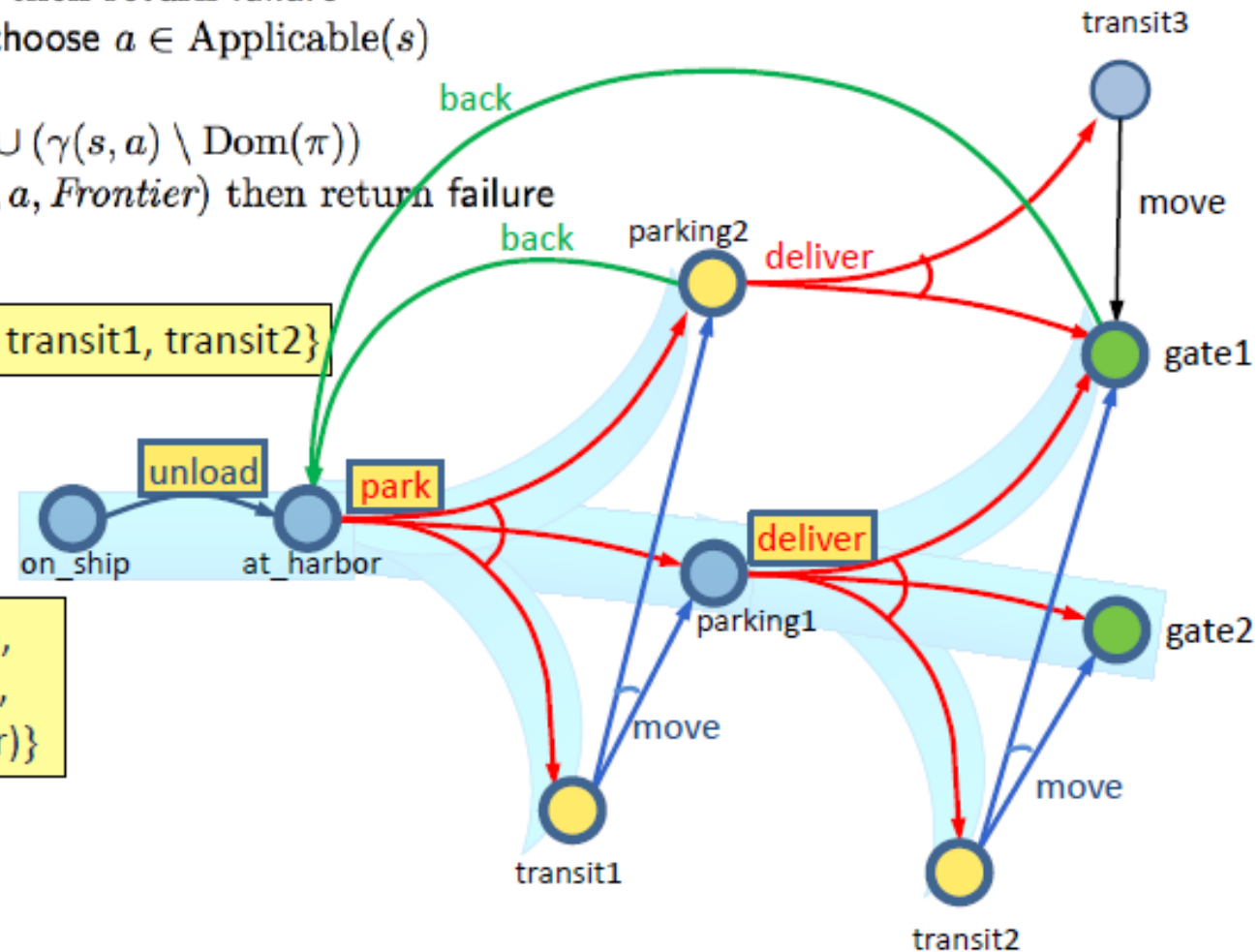
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

 if $has_unsafe_loops(\pi, a, Frontier)$ then return failure

return π

$Frontier \setminus S_g = \{parking2, transit1, transit2\}$

$\pi = \{(on_ship, unload),$
 $(at_harbor, park),$
 $(parking1, deliver)\}$



Find-Safe-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

if $Applicable(s) = \emptyset$ then return failure

nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if $has_unsafe_loops(\pi, a, Frontier)$ then return failure

return π

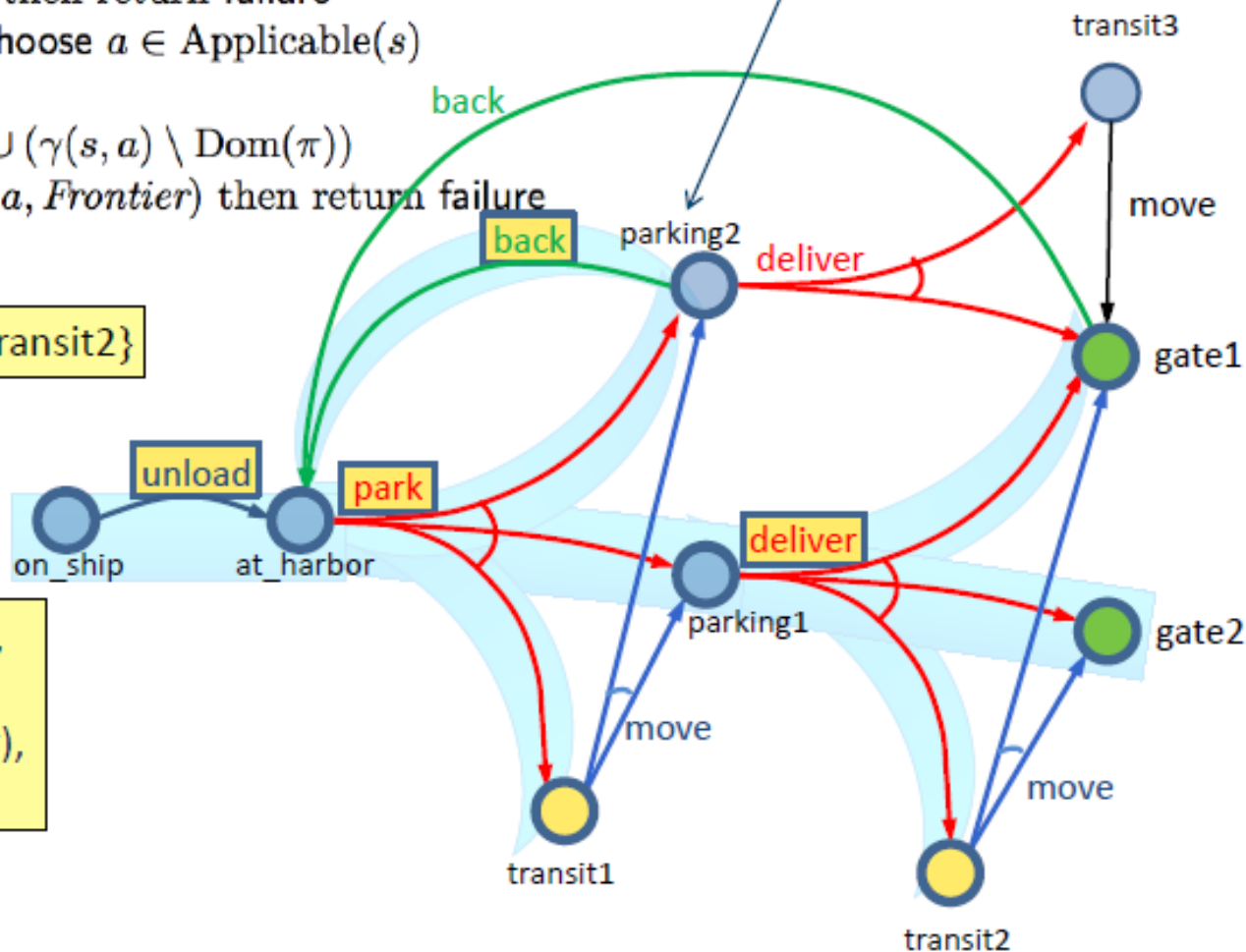
$Frontier \setminus S_g = \{transit1, transit2\}$

$\pi = \{(on_ship, unload),$
 $(at_harbor, park),$
 $(parking1, deliver),$
 $(parking2, back)\}$

Example

Nondeterministically choose back or deliver

- back is OK: escapable cycle



Example

Find-Safe-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

if $Applicable(s) = \emptyset$ then return failure

nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

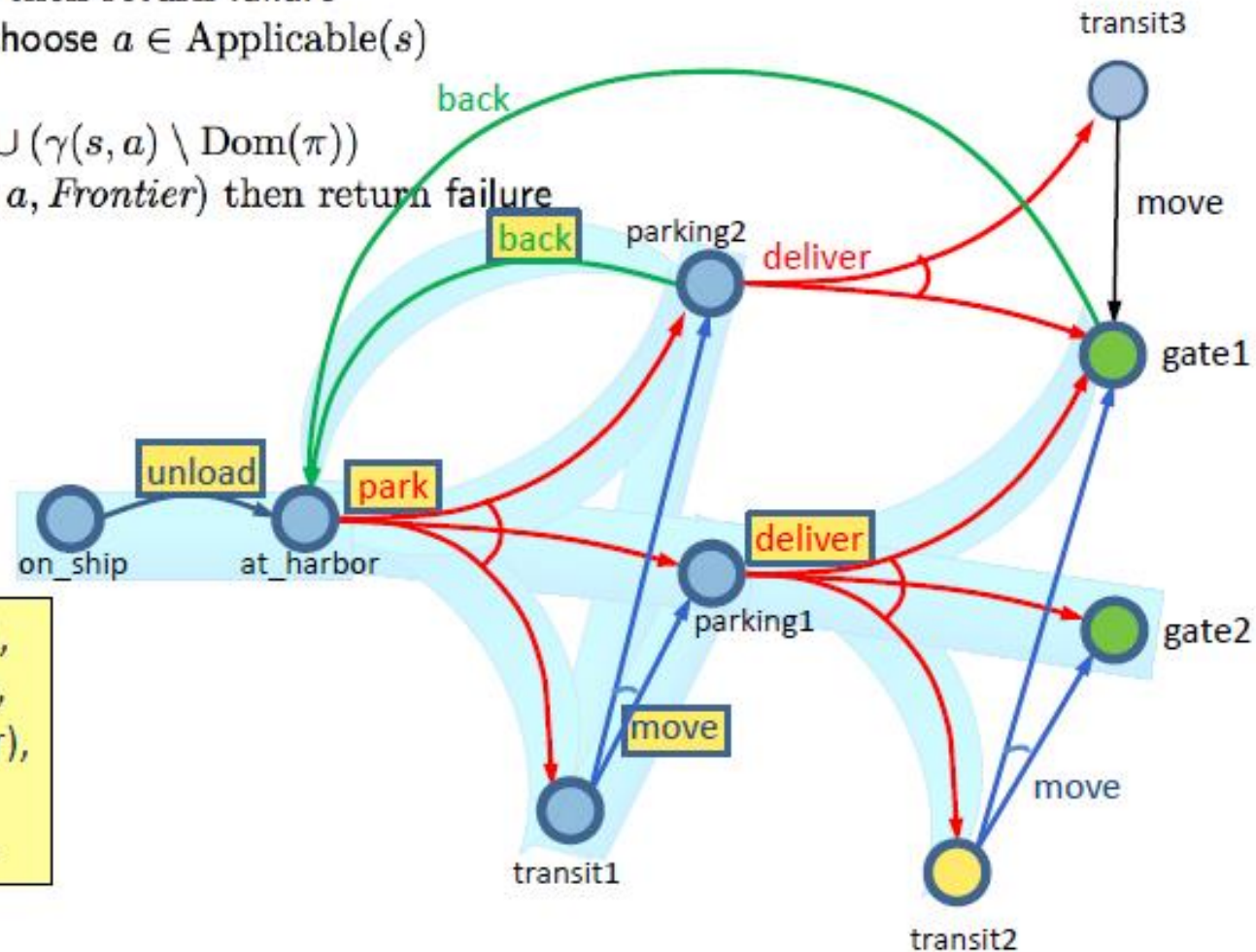
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if $has_unsafe_loops(\pi, a, Frontier)$ then return failure

return π

$Frontier \setminus S_g = \{transit2\}$

$\pi = \{(on_ship, unload),$
 $(at_harbor, park),$
 $(parking1, deliver),$
 $(parking2, back),$
 $(transit1, move)\}$



Example

Find-Safe-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

 if $Applicable(s) = \emptyset$ then return failure

 nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

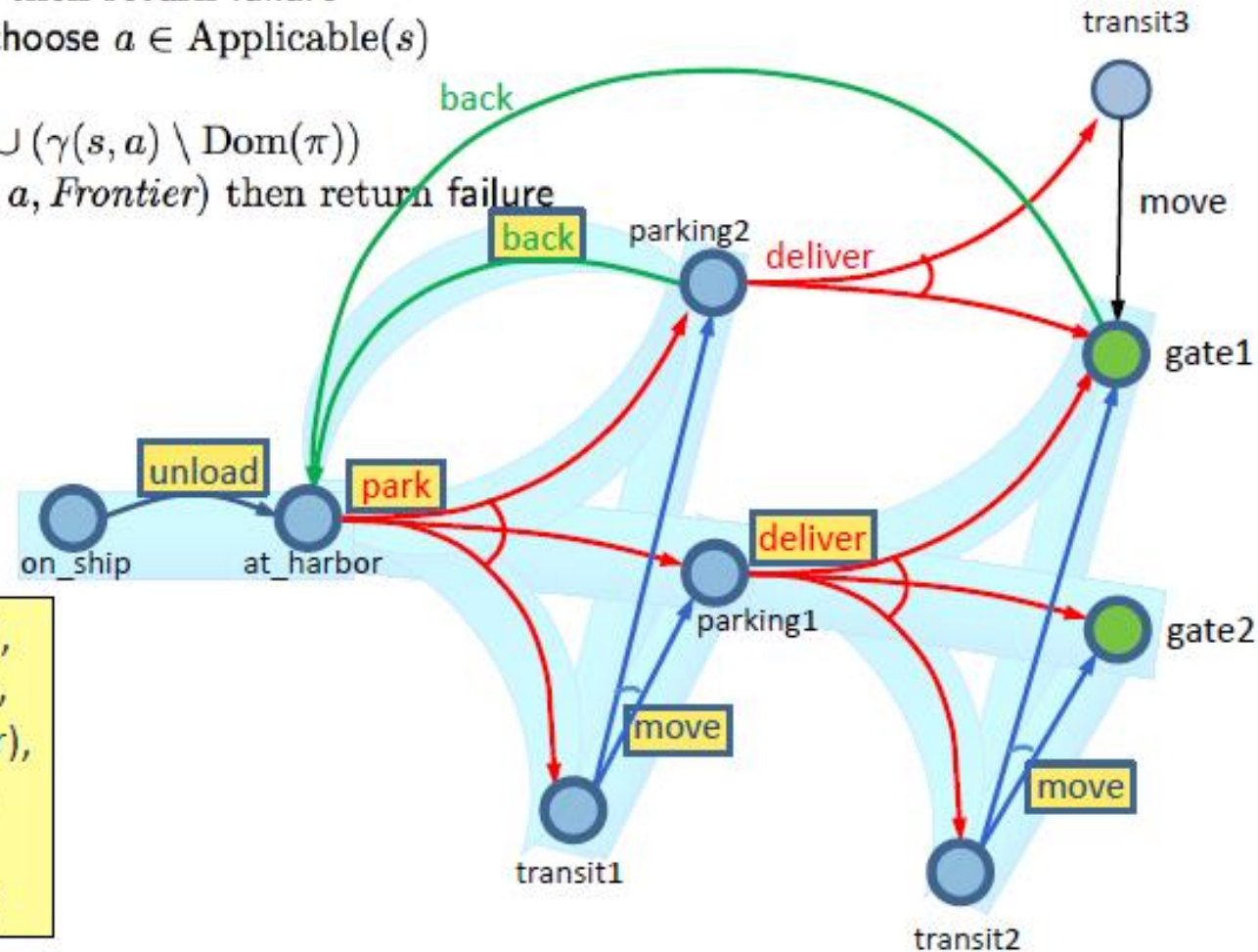
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

 if $has_unsafe_loops(\pi, a, Frontier)$ then return failure

return π

$Frontier \setminus S_g = \emptyset$

$\pi = \{(on_ship, unload),$
 $(at_harbor, park),$
 $(parking1, deliver),$
 $(parking2, back),$
 $(transit1, move),$
 $(transit2, move)\}$



Guided-Find-Safe-Solution

- Motivation:
 - Much easier to find solutions if they don't have to be safe
 - Find-Safe-Solution needs plans for all possible outcomes of actions
 - Find-Solution only needs a plan for one of them
- Idea:
 - loop
 - Find a solution π
 - Look at each leaf node of π
 - ▶ If the leaf node isn't a goal, find a solution and incorporate it into π

Guided-Find-Safe-Solution

Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)

if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return(π)

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ then do

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ then return failure *(not in book)*

else for every s' and a such that $s \in \gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

π is a solution. Return the part that's reachable from s_0 .

Choose any leaf s that isn't a goal. Find a solution π' for s .

For each (s, a) in π' , add to π unless π already has an action at s

s is unsolvable. For each (s', a) that can produce s , modify π and Σ so we'll never use a at s'

Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)

if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return(π)

select arbitrarily $s \in Q$

$\pi' \leftarrow Find\text{-}Solution(\Sigma, s, S_g)$

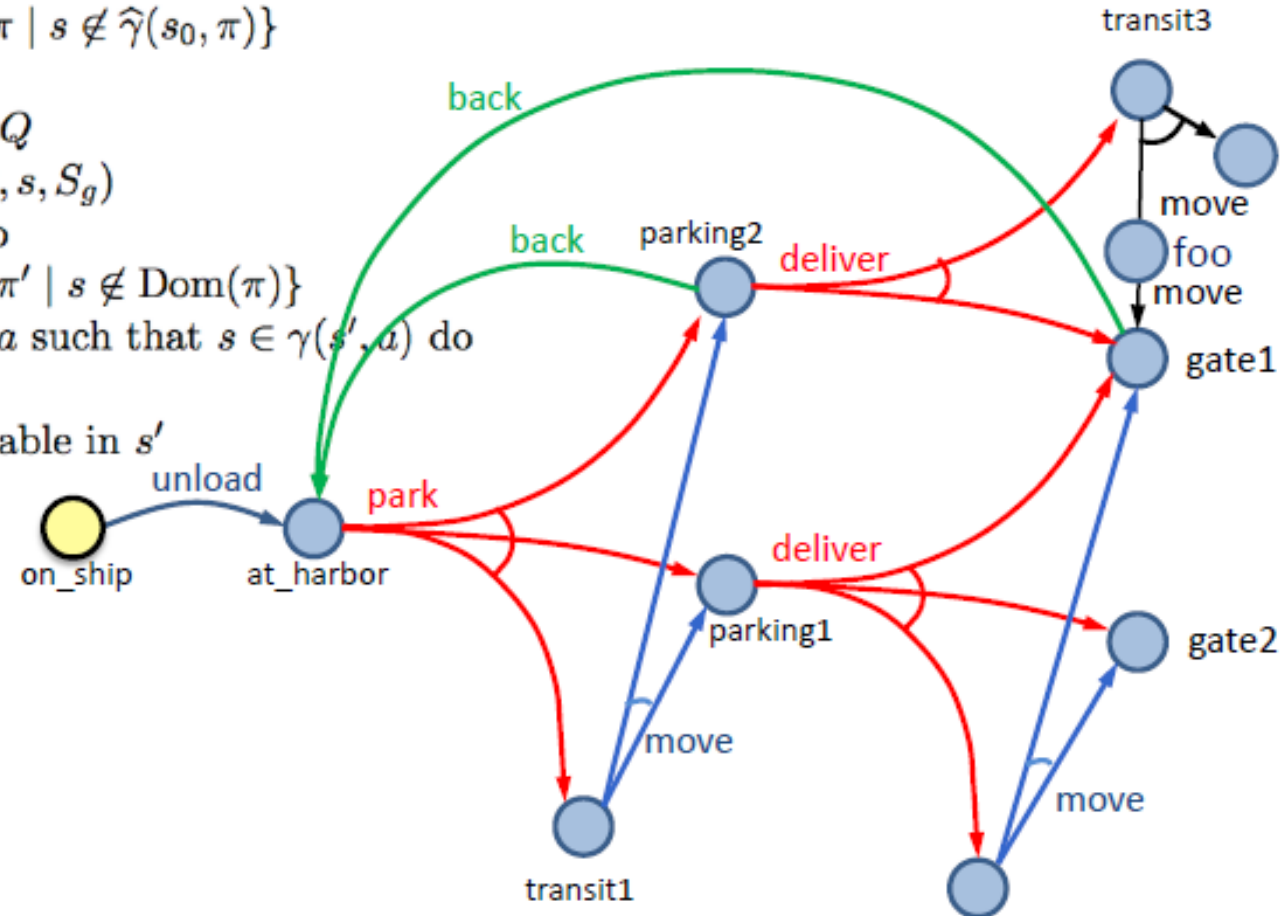
if $\pi' \neq failure$ then do

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every s' and a such that $s \in \gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'



Example

Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)

if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return(π)

select arbitrarily $s \in Q$

$\pi' \leftarrow Find\text{-}Solution(\Sigma, s, S_g)$

if $\pi' \neq failure$ then do

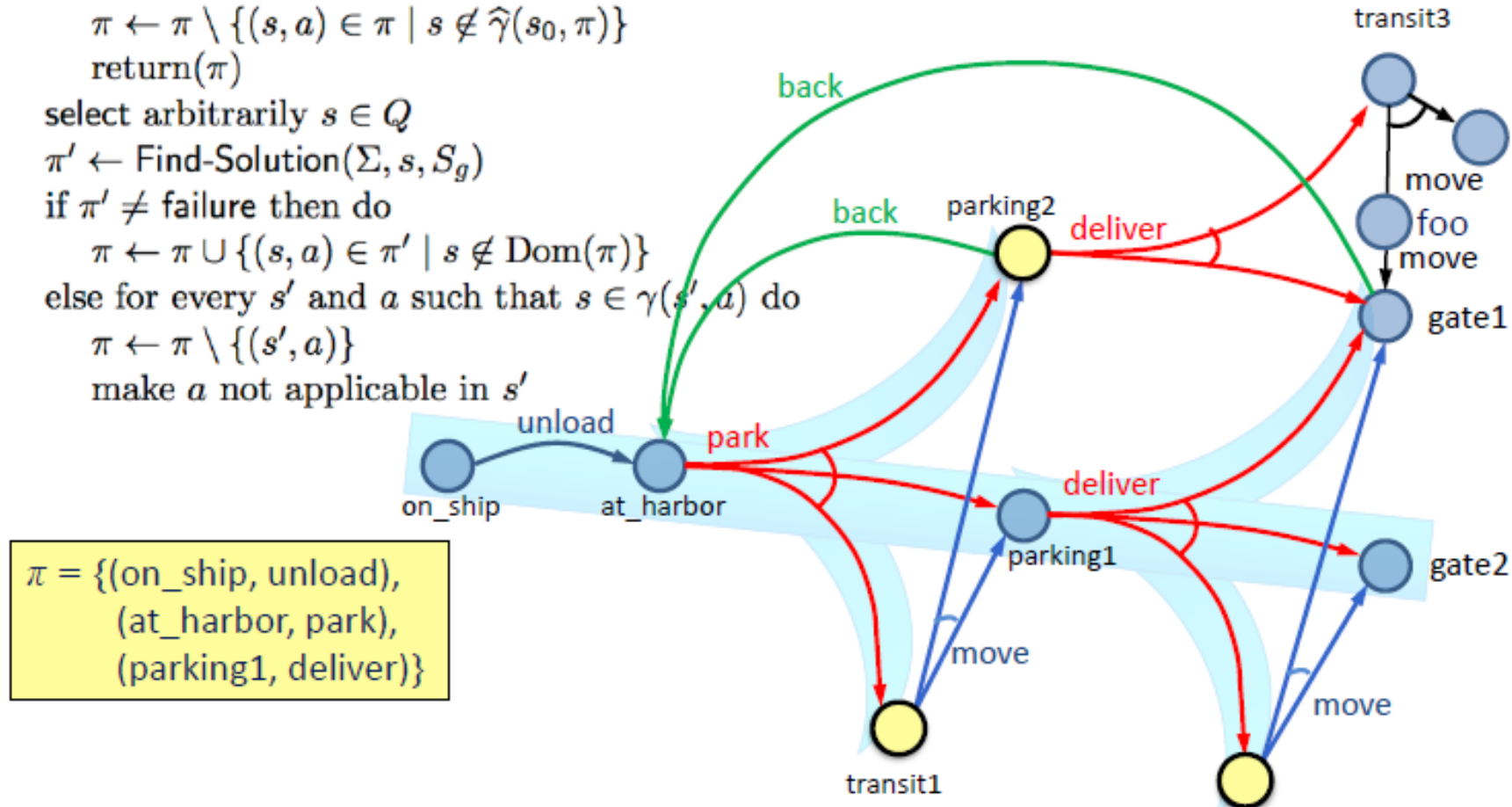
$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every s' and a such that $s \in \gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)
if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return(π)

select arbitrarily $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

if $\pi' \neq failure$ then do

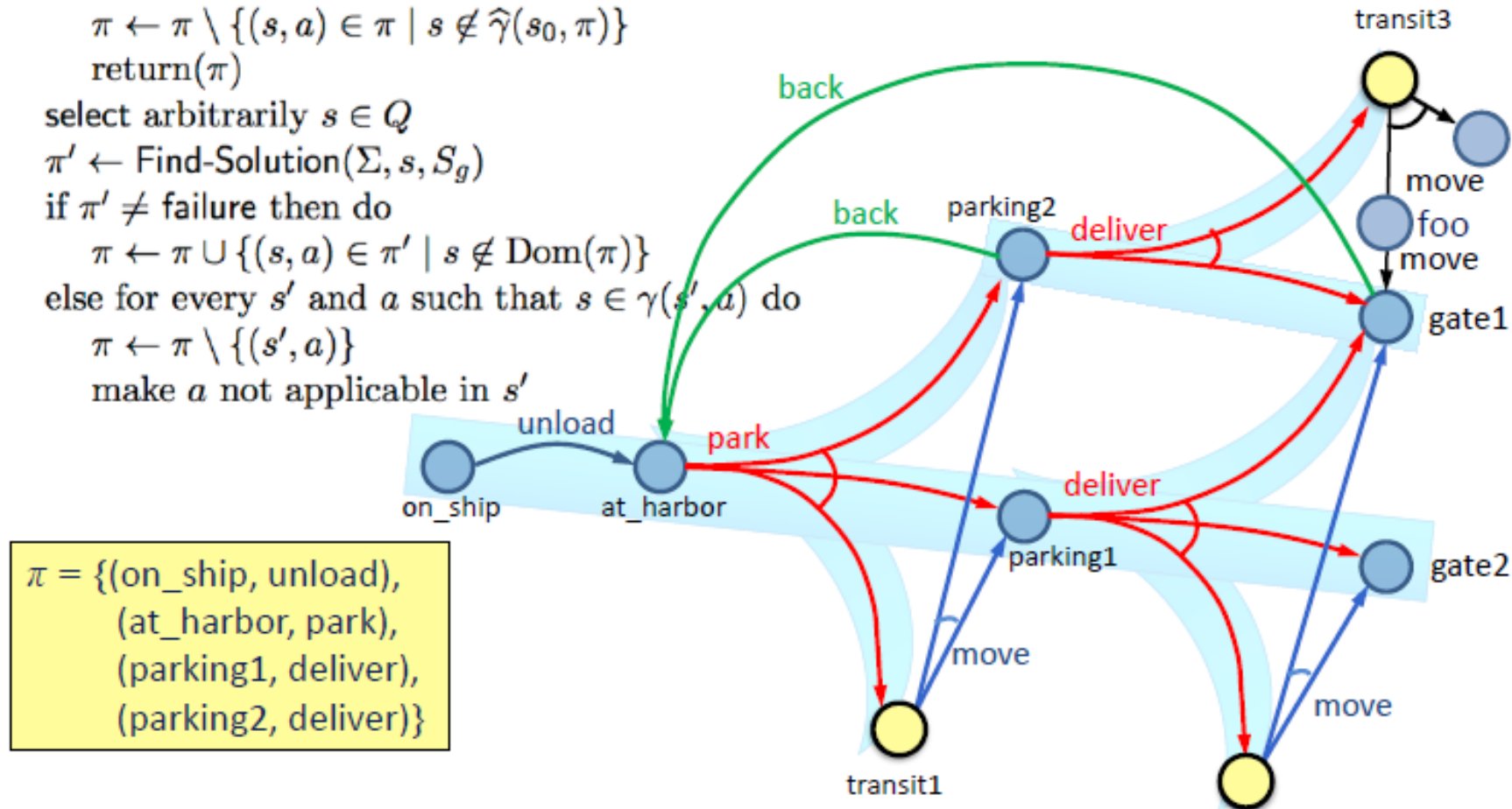
$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every s' and a such that $s \in \gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)

if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return(π)

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

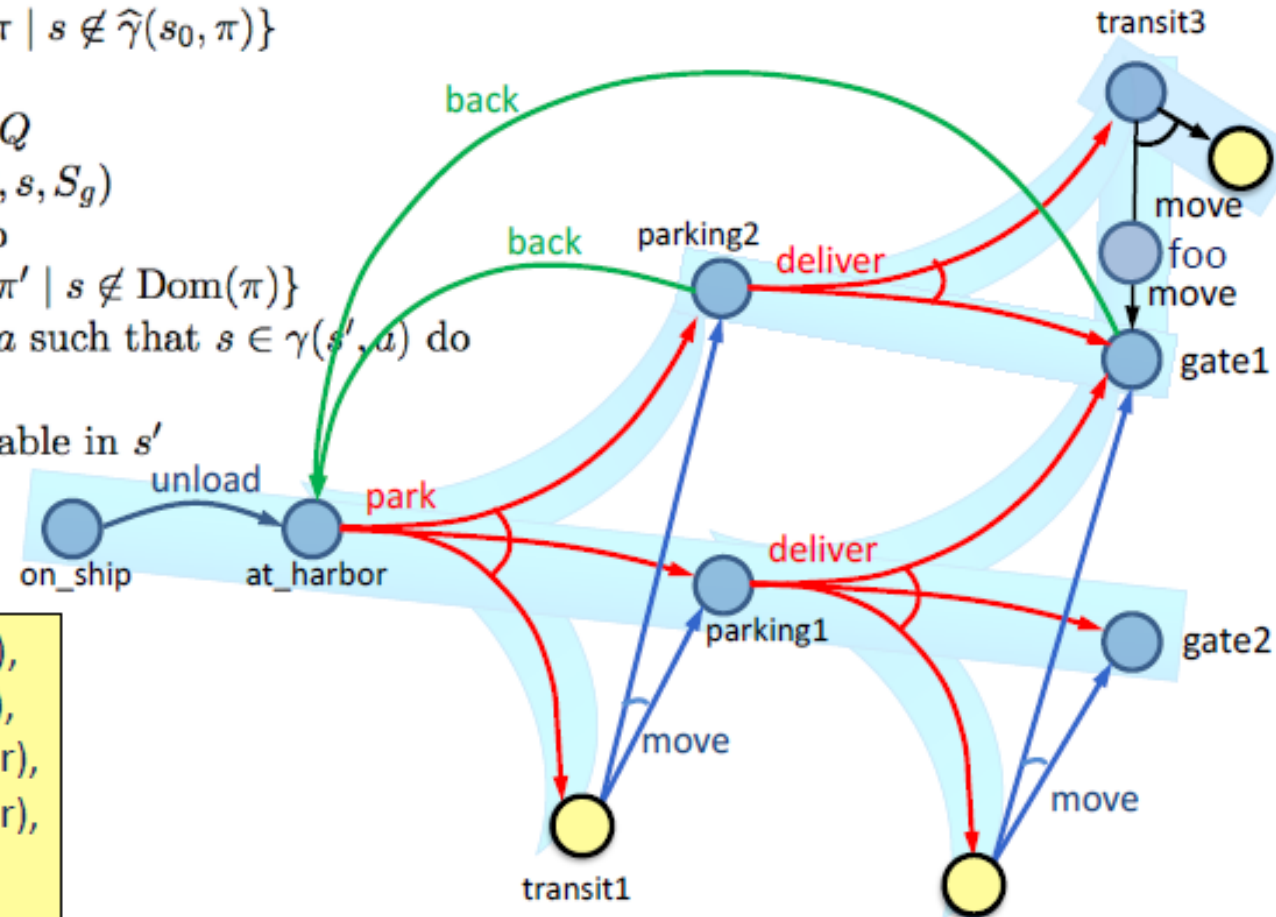
if $\pi' \neq \text{failure}$ then do

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else for every s' and a such that $s \in \gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'



$\pi = \{(on_ship, unload),$
 $(at_harbor, park),$
 $(parking1, deliver),$
 $(parking2, deliver),$
 $(transit3, move),$
 $(foo, move)\}$

Example

Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)

if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return(π)

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ then do

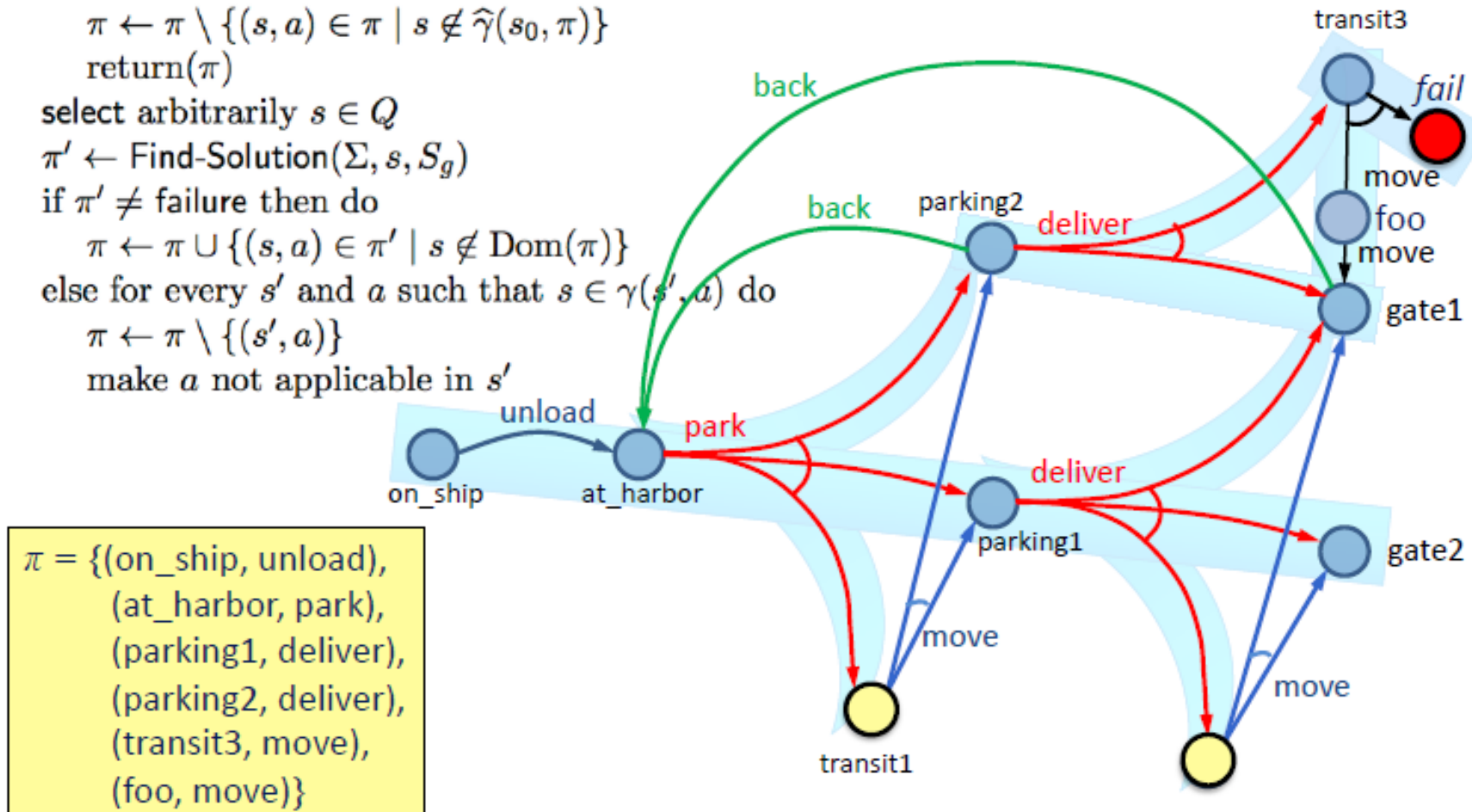
$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else for every s' and a such that $s \in \gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)

if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return(π)

select arbitrarily $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

if $\pi' \neq failure$ then do

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

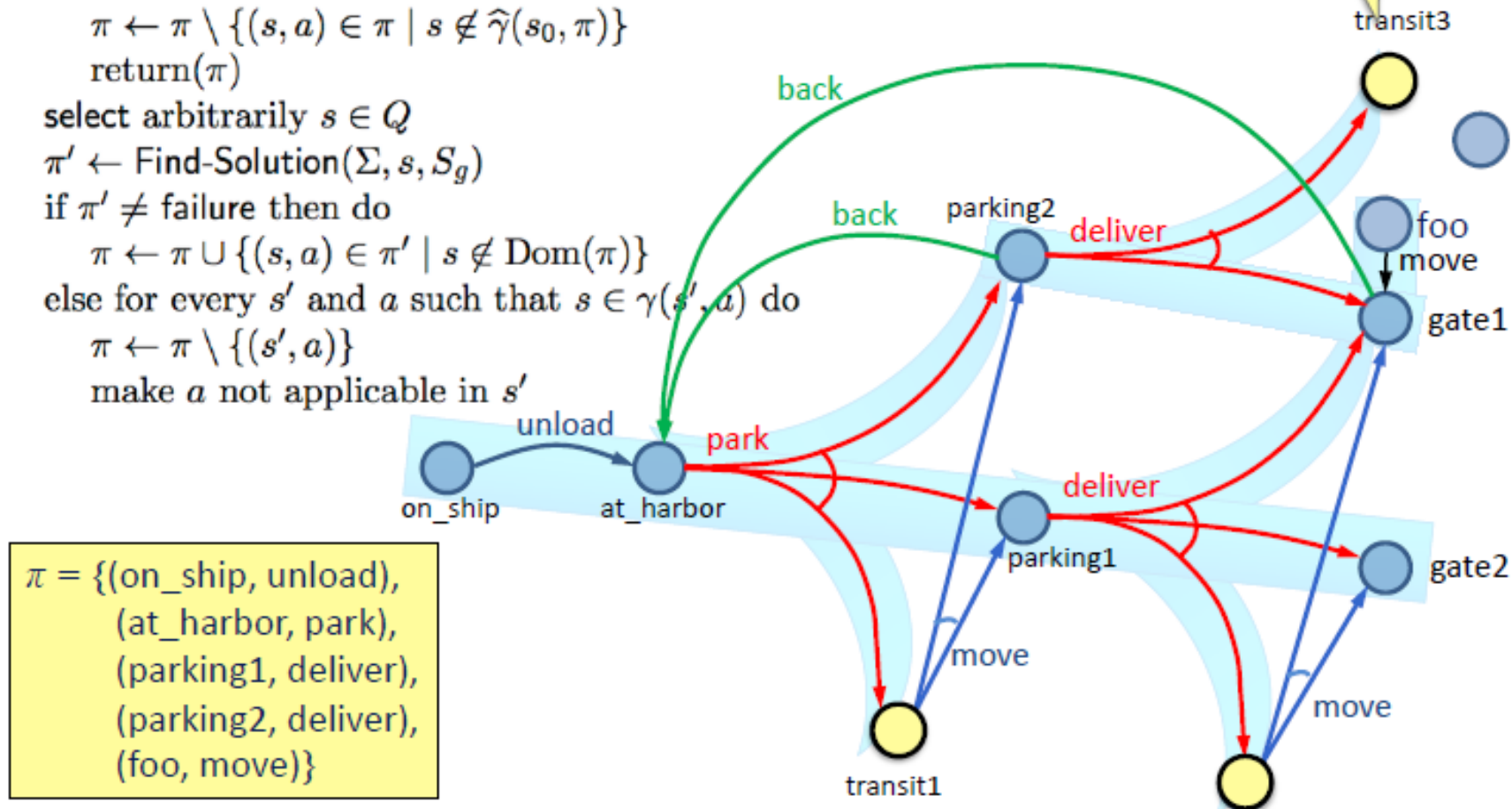
else for every s' and a such that $s \in \gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example

Modify Σ_d to make move inapplicable



Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)

if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return(π)

select arbitrarily $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

if $\pi' \neq failure$ then do

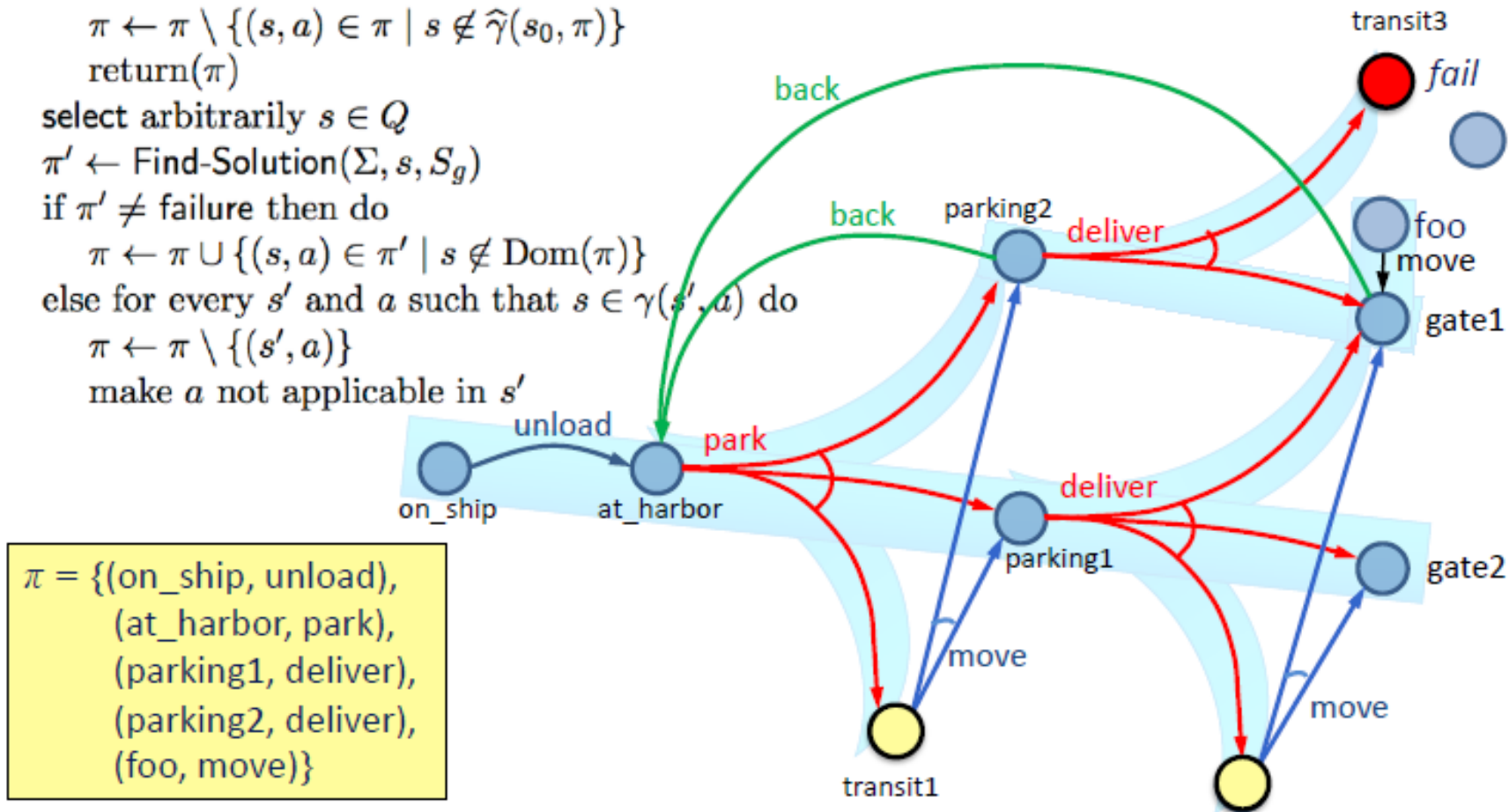
$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every s' and a such that $s \in \gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)
if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return(π)

select arbitrarily $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

if $\pi' \neq failure$ then do

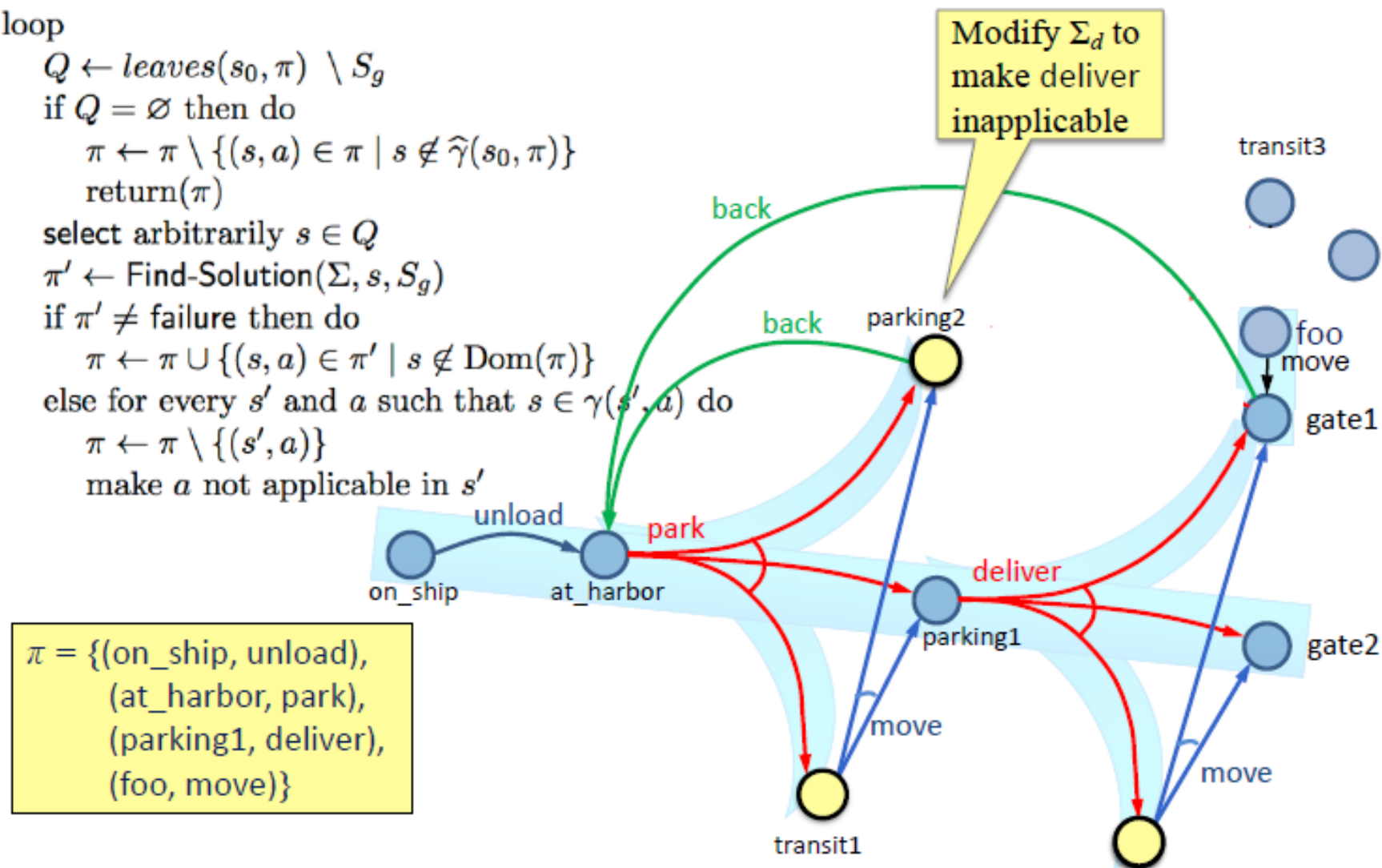
$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every s' and a such that $s \in \gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

```
if  $s_0 \in S_g$  then return( $\emptyset$ )  
if  $Applicable(s_0) = \emptyset$  then return(failure)  
 $\pi \leftarrow \emptyset$   
loop
```

```
   $Q \leftarrow leaves(s_0, \pi) \setminus S_g$ 
```

```
  if  $Q = \emptyset$  then do
```

```
     $\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$ 
```

```
    return( $\pi$ )
```

```
  select arbitrarily  $s \in Q$ 
```

```
   $\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$ 
```

```
  if  $\pi' \neq failure$  then do
```

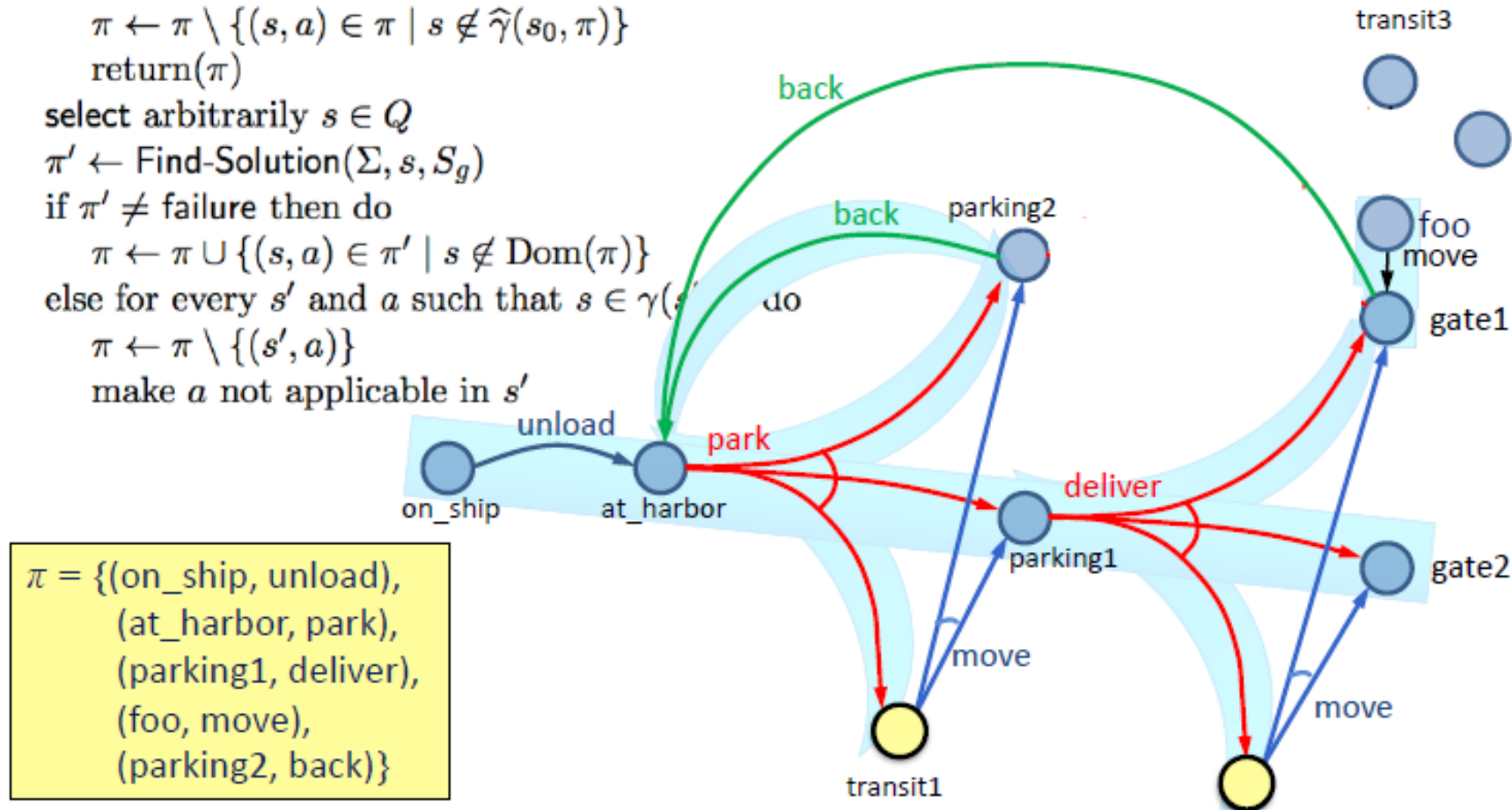
```
     $\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$ 
```

```
  else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do
```

```
     $\pi \leftarrow \pi \setminus \{(s', a)\}$ 
```

```
    make  $a$  not applicable in  $s'$ 
```

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)
if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return(π)

select arbitrarily $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

if $\pi' \neq failure$ then do

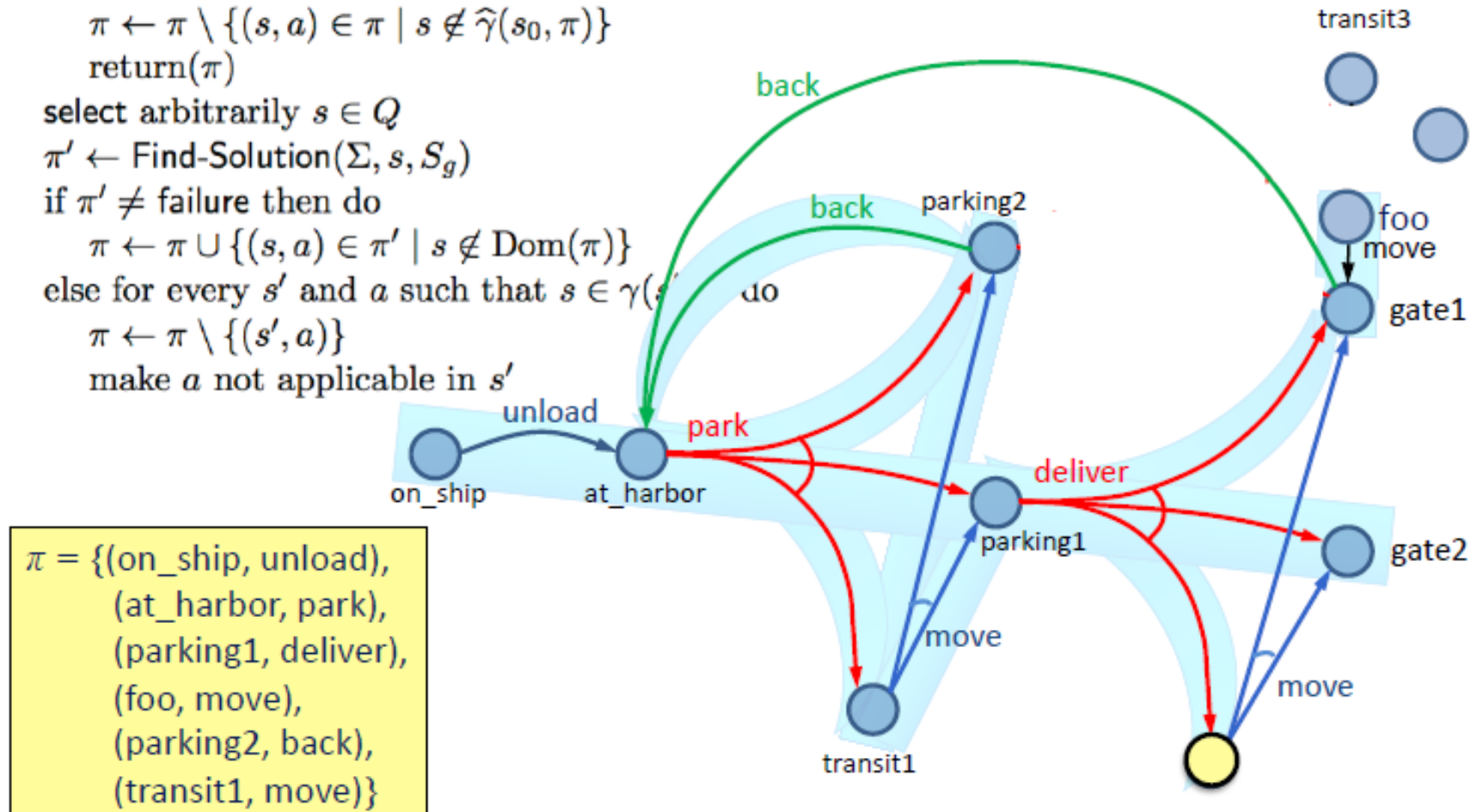
$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every s' and a such that $s \in \gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)
if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return(π)

select arbitrarily $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

if $\pi' \neq failure$ then do

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every s' and a such that $s \in \gamma(s', a)$ do

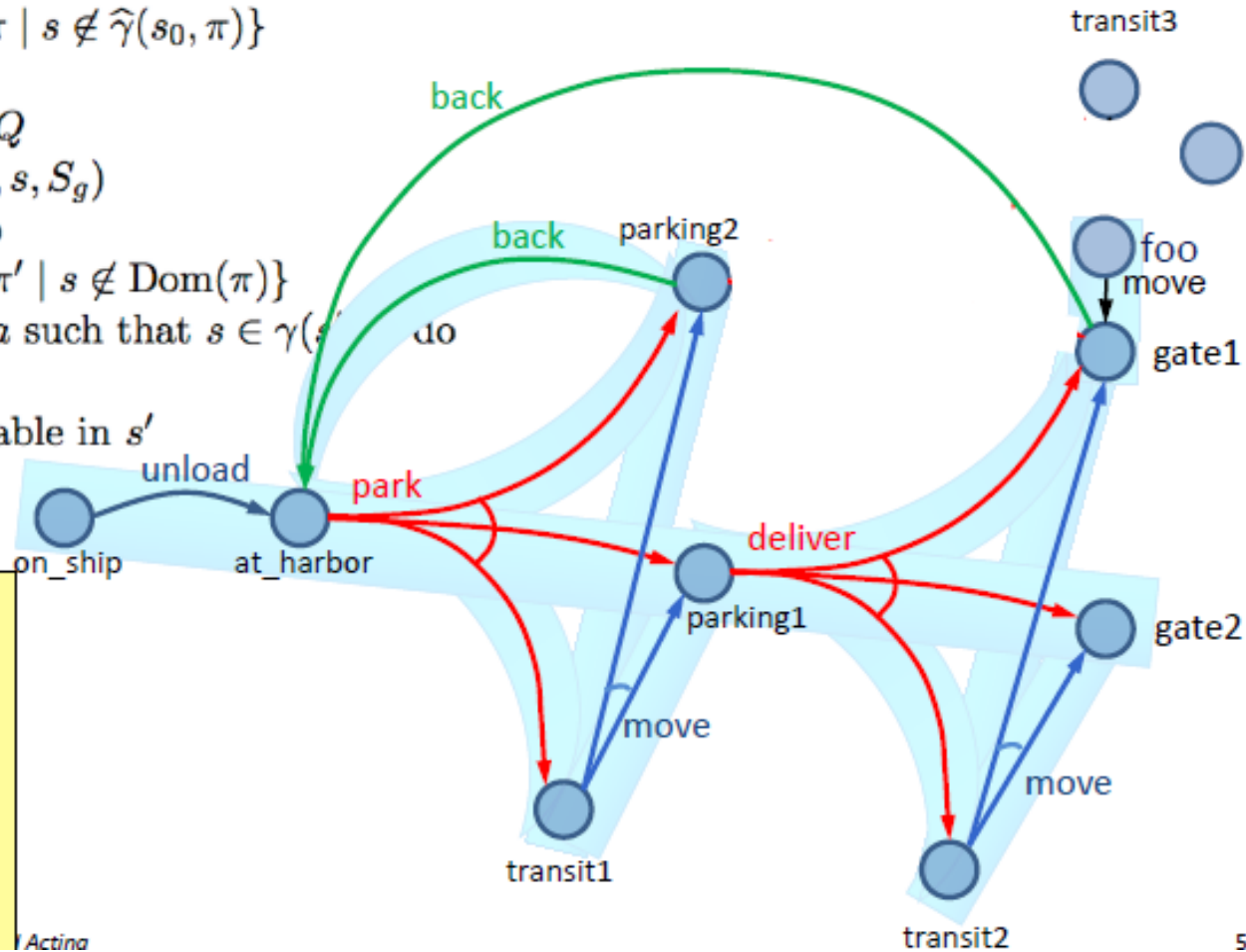
$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

$\pi = \{(on_ship, unload),$
 $(at_harbor, park),$
 $(parking1, deliver),$
 $(foo, move),$
 $(parking2, back),$
 $(transit1, move),$
 $(transit2, move)\}$

Actina

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)

if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return(π)

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ then do

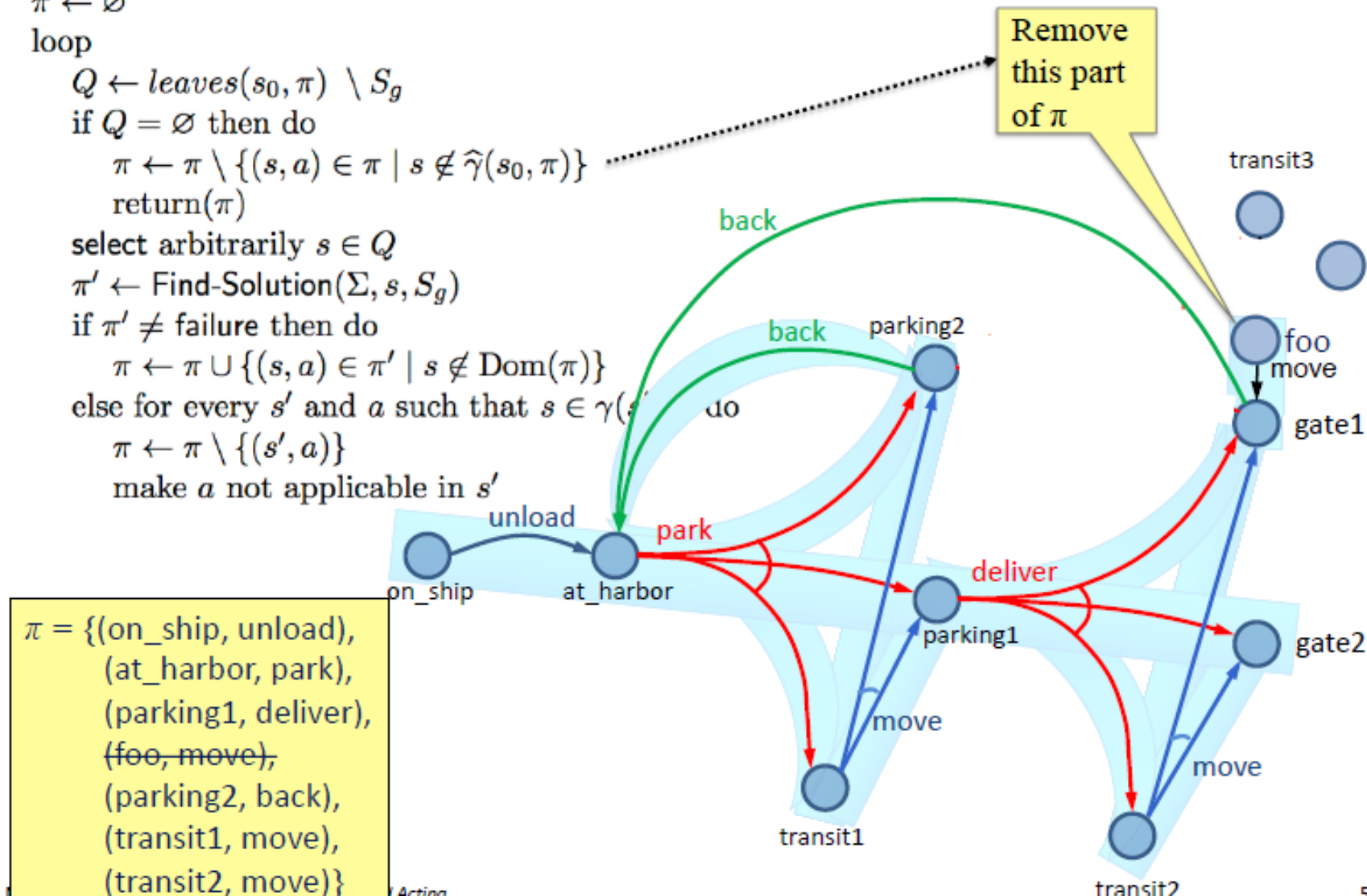
$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else for every s' and a such that $s \in \gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)

if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return(π)

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ then do

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else for every s' and a such that $s \in \gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

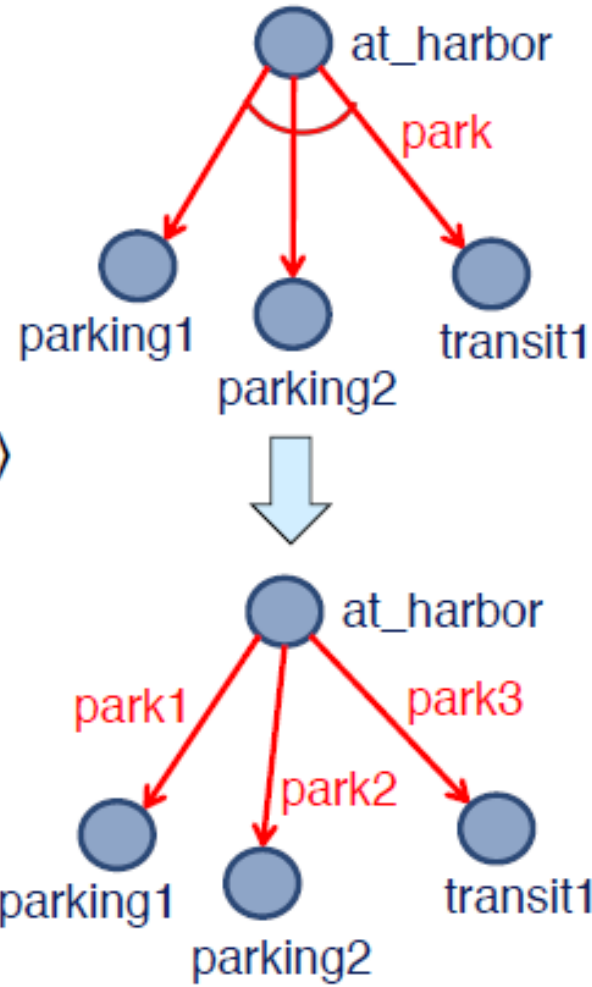
make a not applicable in s'

Determinization

- How to implement it?
 - Need implementation of Find-Solution
 - Need it to be very efficient
 - We'll call it many times
- Idea: instead of Find-Solution, use a classical planner

Determinization

- Convert the nondeterministic actions into something the classical planner can use
- *Determinize*
 - Suppose a_i has n possible outcomes
 - n deterministic actions, one for each outcome
- Classical planner returns a plan $p = \langle a_1, a_2, \dots, a_n \rangle$
- If p is acyclic, can convert it to a policy
 - (unsafe) solution for P
 - $\{(s_0, a_1), (s_1, a_2), \dots, (s_{n-1}, a_n)\}$where
 - each a_i is the nondeterministic action whose determinization includes a_i
 - $s_i \in \gamma(s_{i-1}, a_i)$



Determinization

- Nondeterministic planning problem $P = (\Sigma, s_0, S_g)$
- Determinization $P_d = (\Sigma_d, s_0, S_g)$
- Classical planner returns a solution for P
 - a plan $p = \langle a_1, a_2, \dots, a_n \rangle$
- If p is acyclic, can convert it to an (unsafe) solution for P
 - $\{(s_0, a_1), (s_1, a_2), \dots, (s_{n-1}, a_n)\}$
where each a_i is the nondeterministic action whose determinization includes a_i
 - each $s_i \in \gamma(s_{i-1}, a_i)$

```
Plan2policy( $p = \langle a_1, \dots, a_n \rangle, s$ )  
   $\pi \leftarrow \emptyset$   
  loop for  $i$  from 1 to  $n$  do  
     $\pi \leftarrow \pi \cup (s, \text{det2nondet}(a_i))$   
     $s \leftarrow \gamma_d(s, a_i)$   
  return  $\pi$ 
```

Determinization

Find-Safe-Solution-by-Determinization (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)

if $Applicable(s_0) = \emptyset$ then return(failure)

$\pi \leftarrow \emptyset$

$\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

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make the actions in the determinization of a
not applicable in s'

Same as
Guided-Find-Safe-Solution

Any classical planner that
doesn't return cyclic plans

Convert p' to a policy. Add each (s, a)
to π unless π already has an action at s

s is unsolvable. For each (s', a)
that can produce s , modify π
and Σ_d so we'll never use a at s'

Example

Find-Safe-Solution-by-Determinization (Σ, s_0, S_g)

if $s_0 \in S_g$ then return(\emptyset)

if $Applicable(s_0) = \emptyset$ then return(failure)

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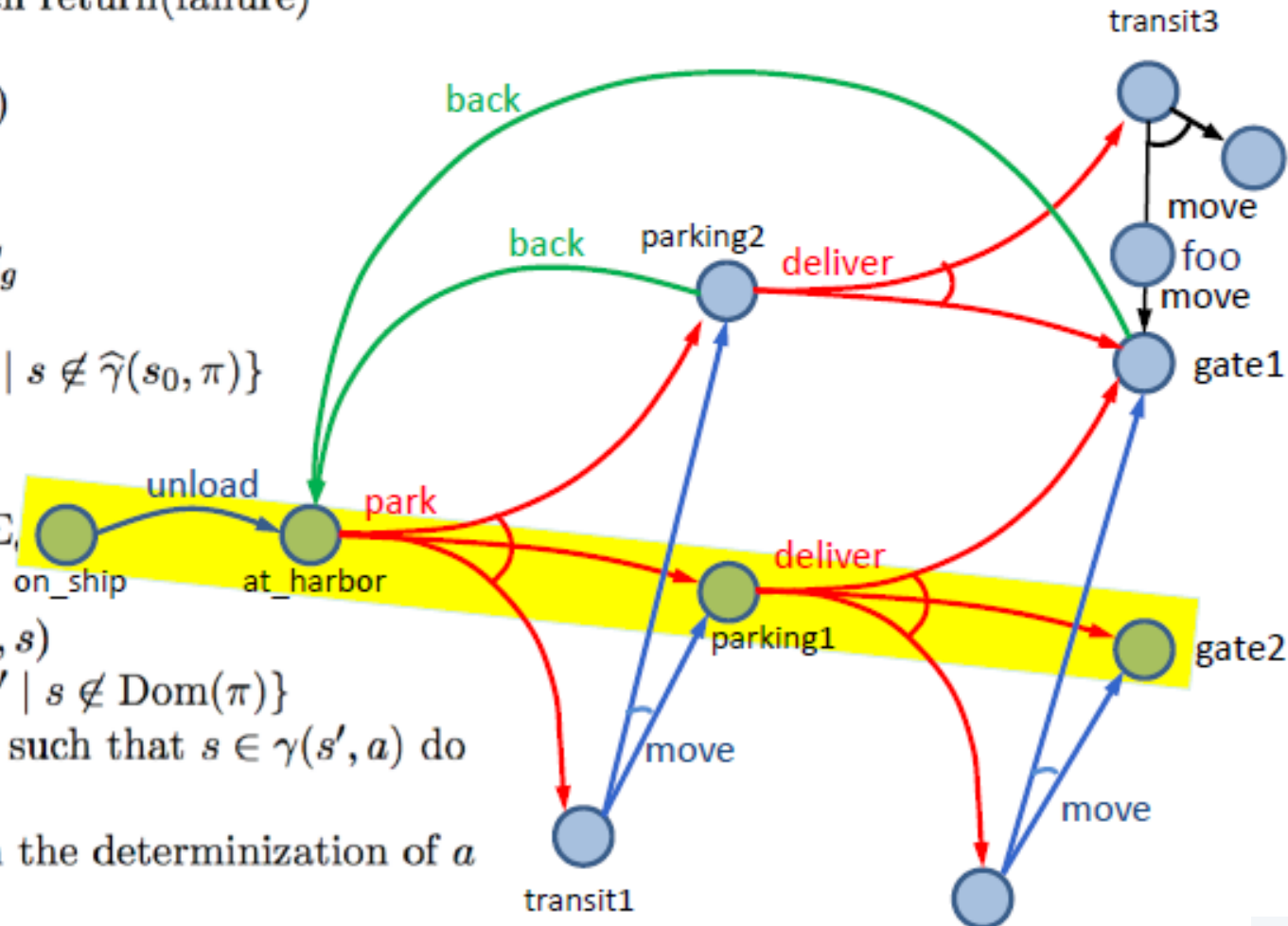
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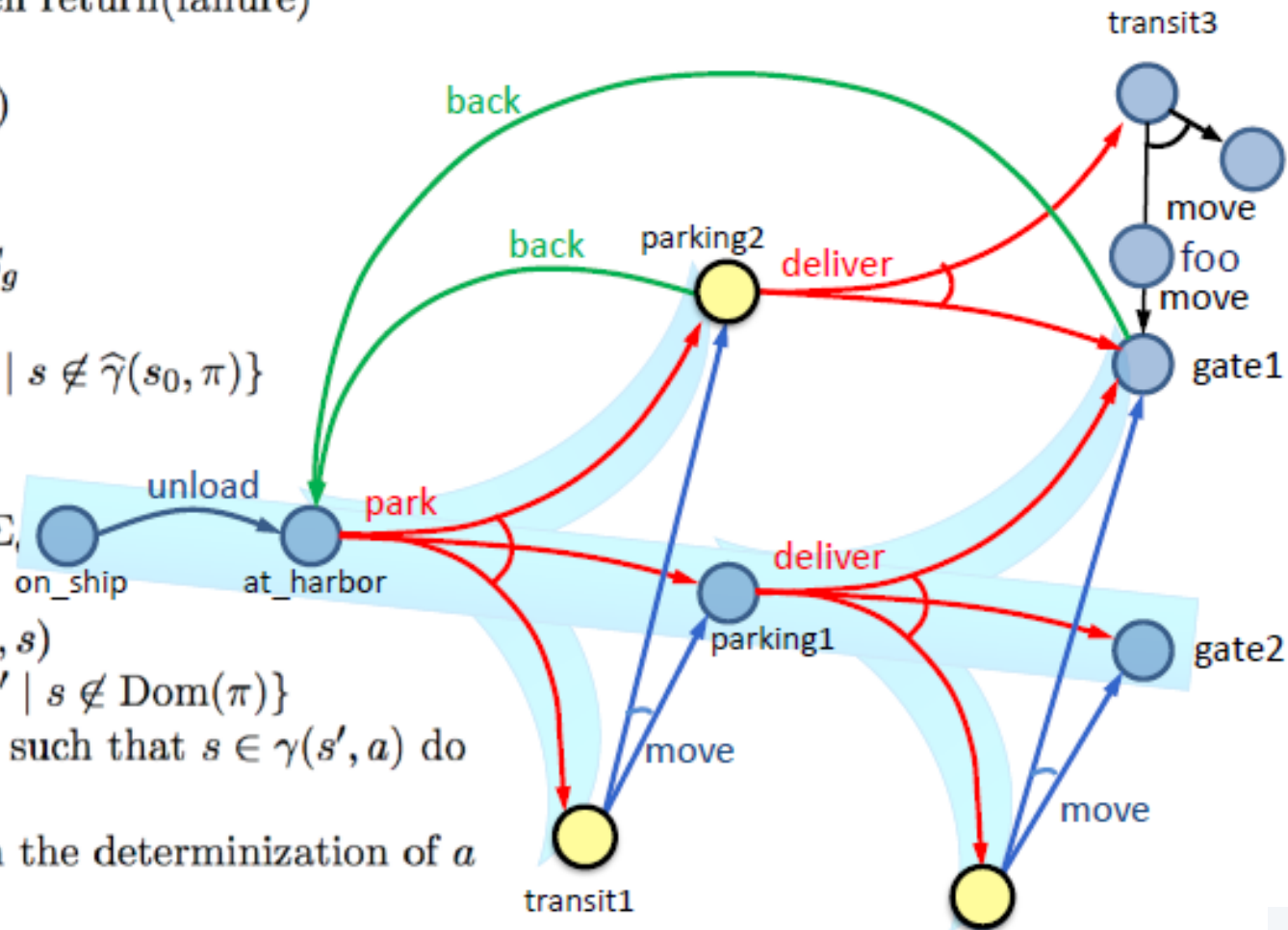
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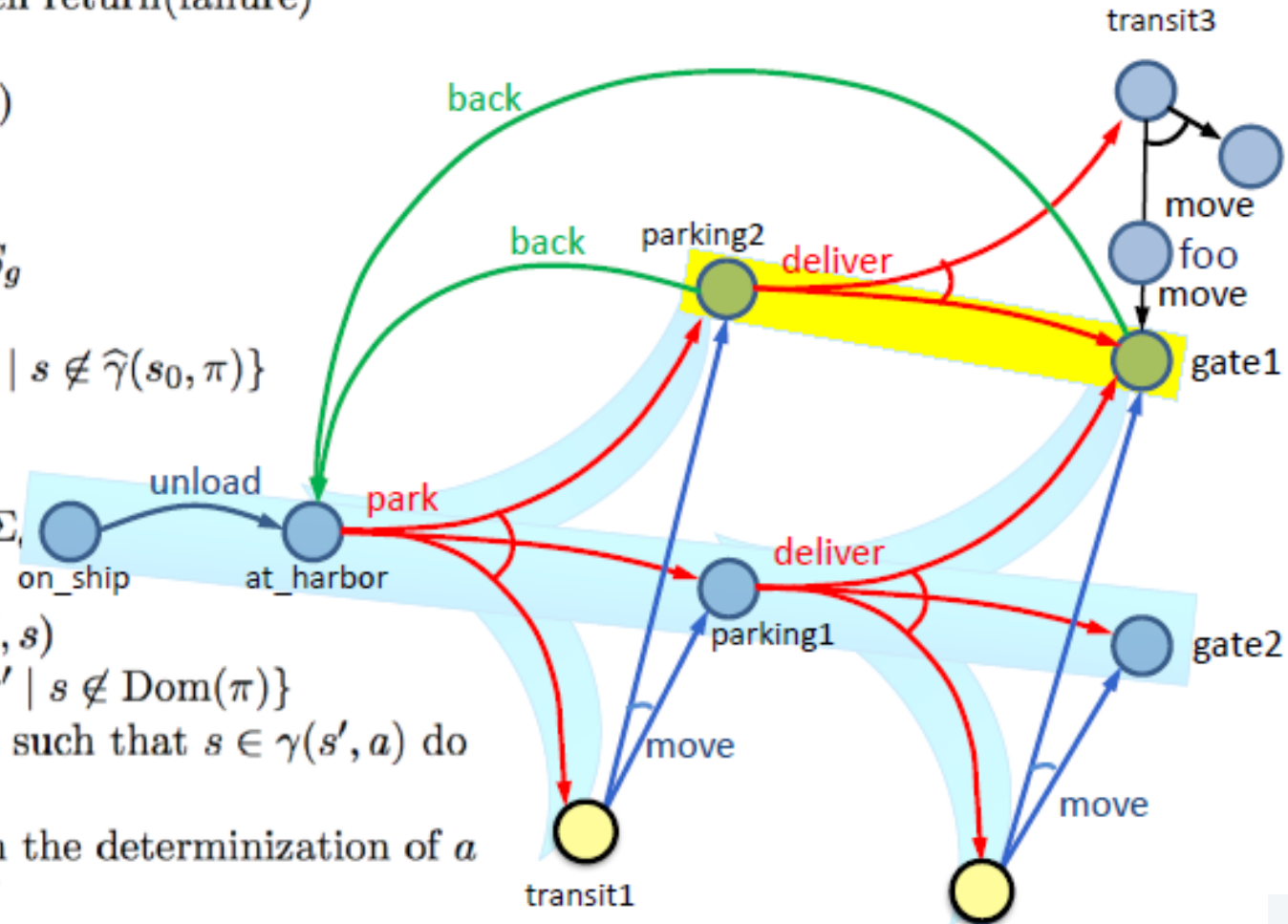
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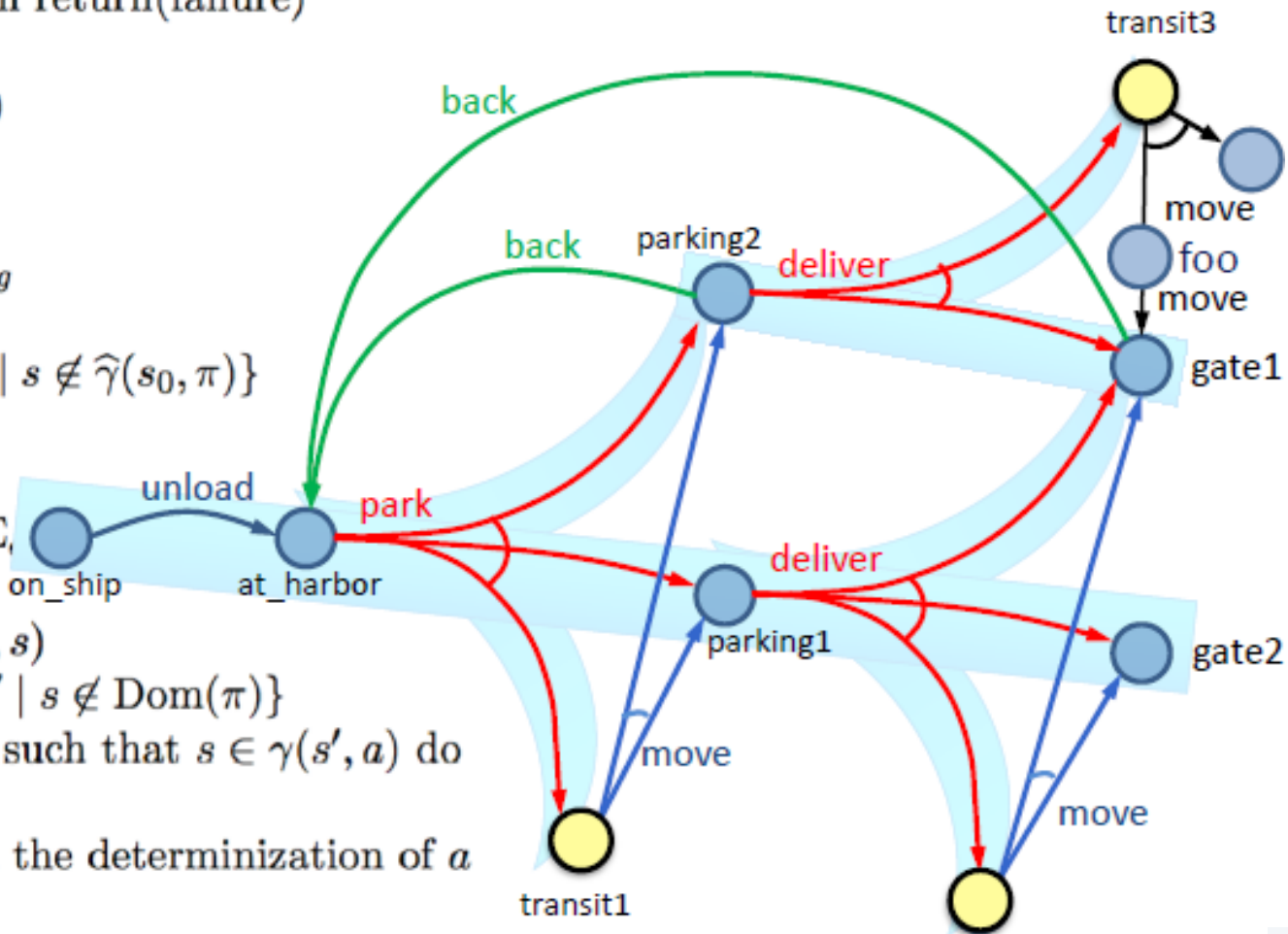
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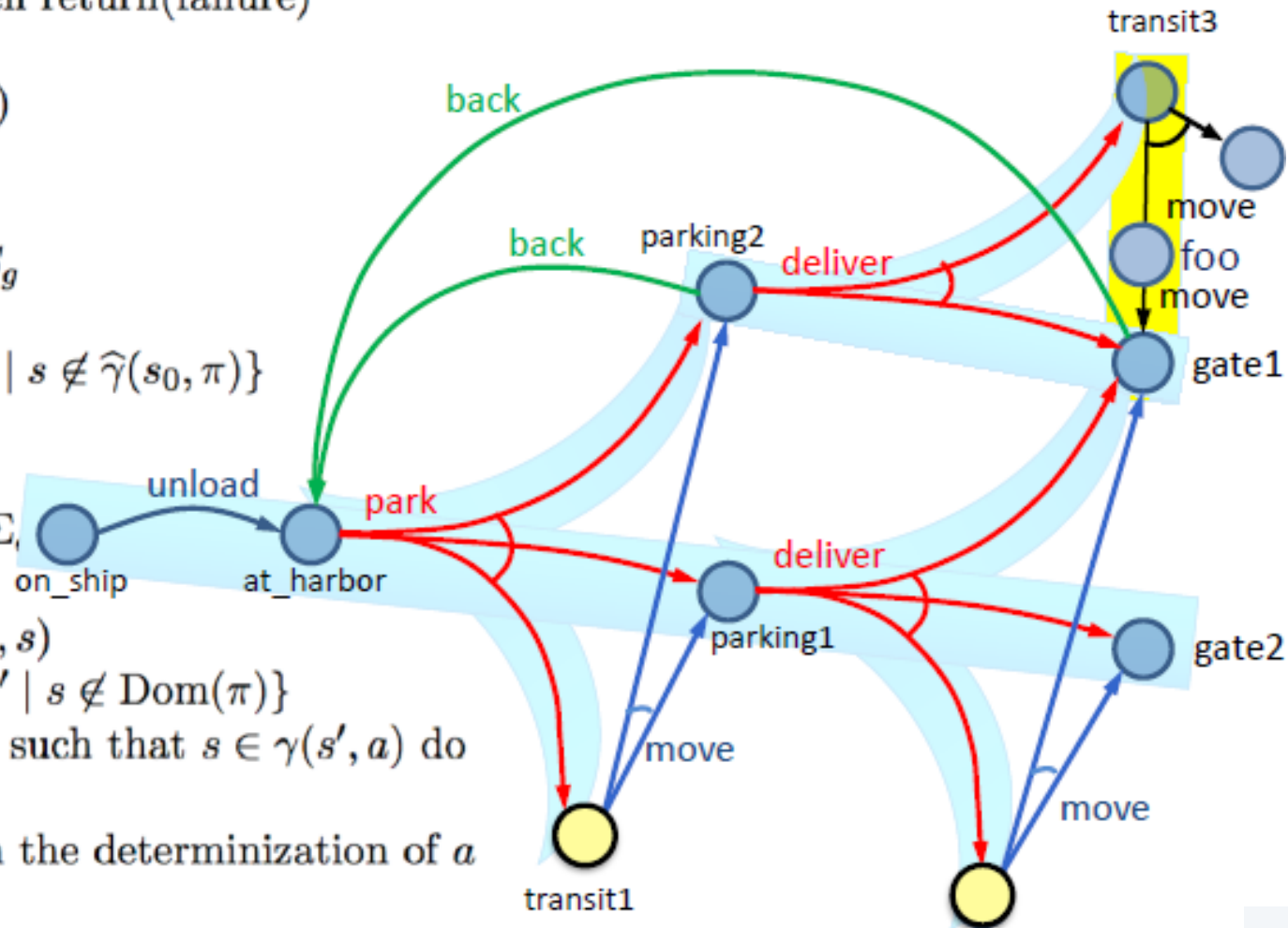
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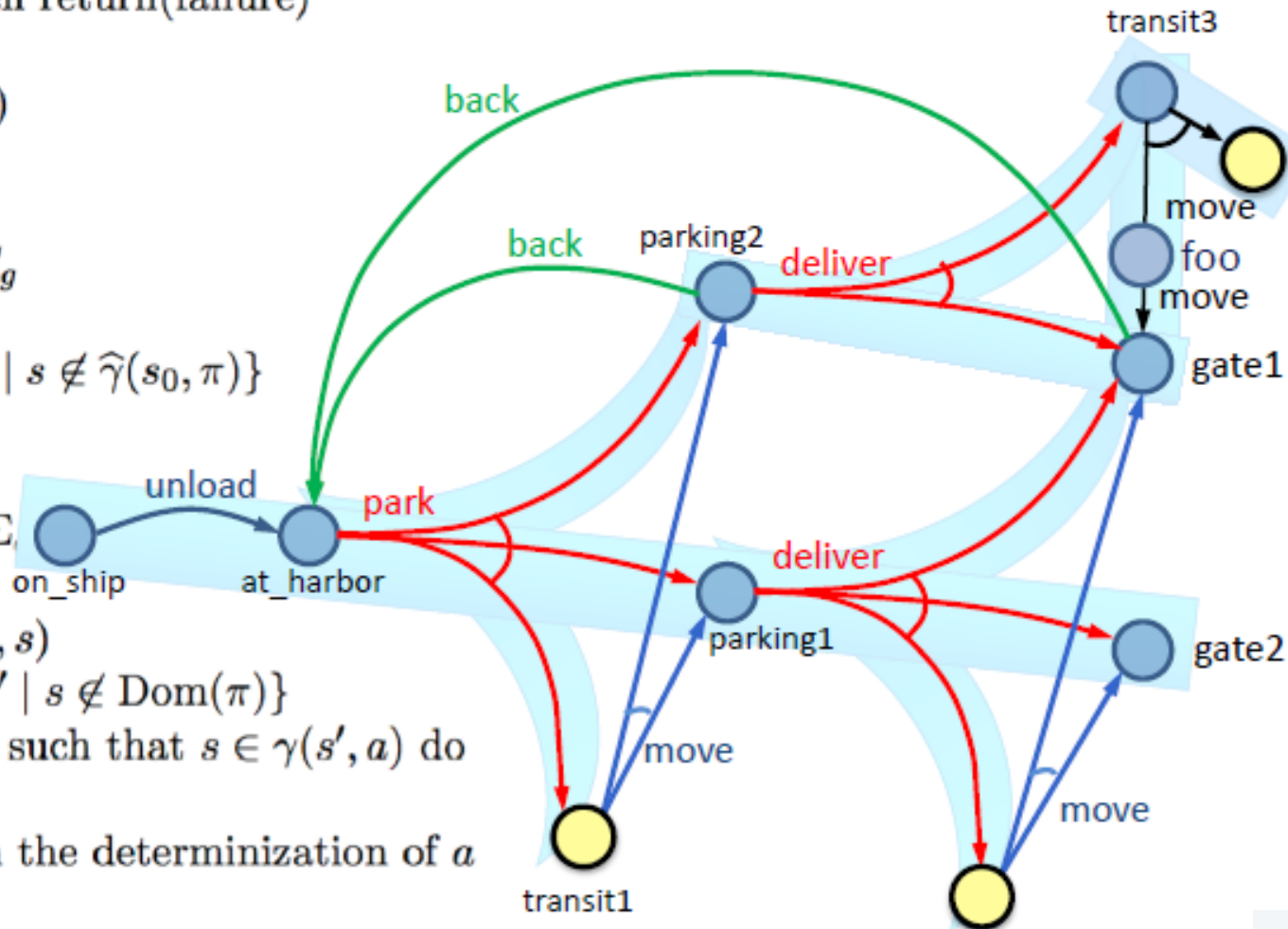
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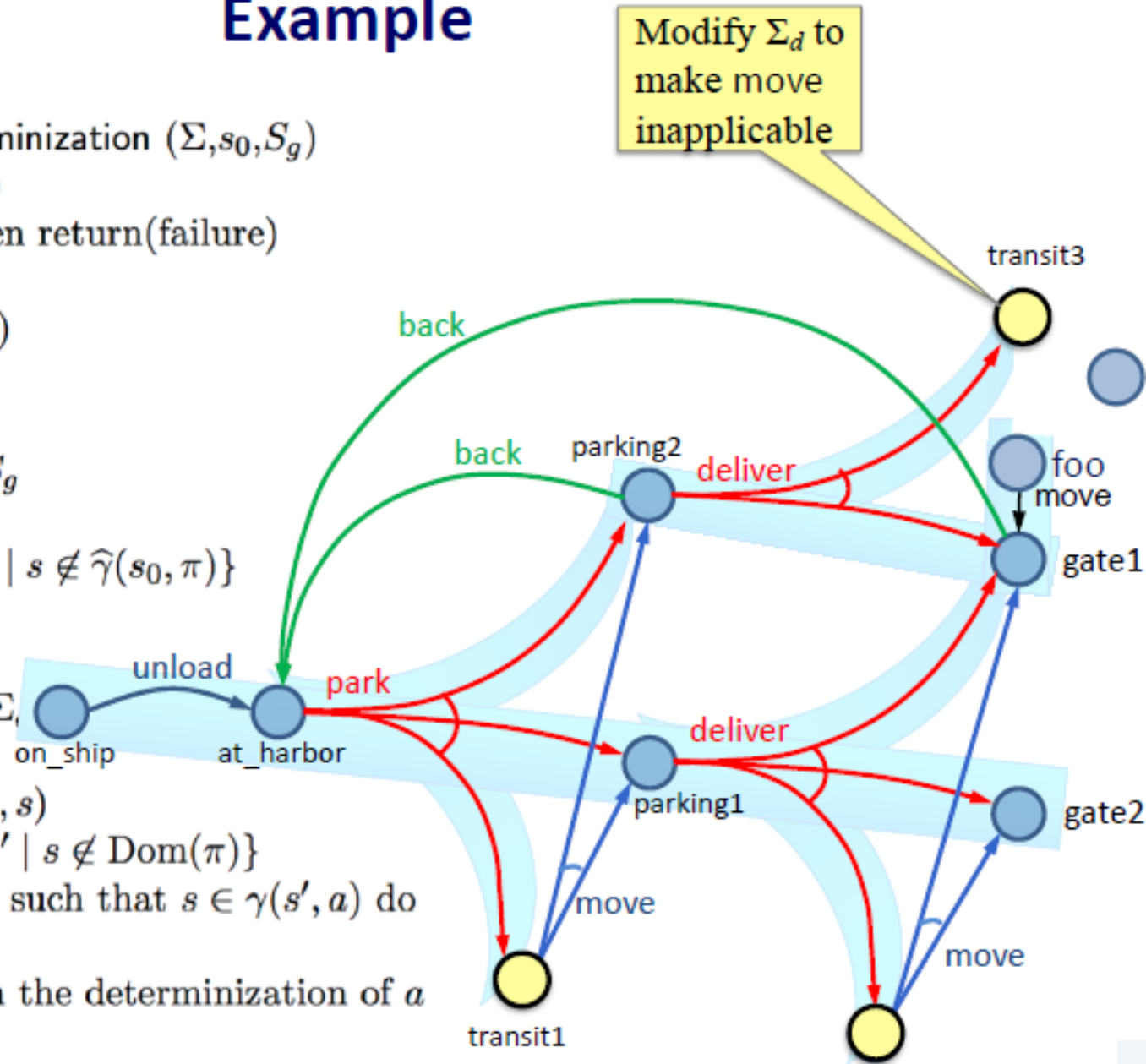
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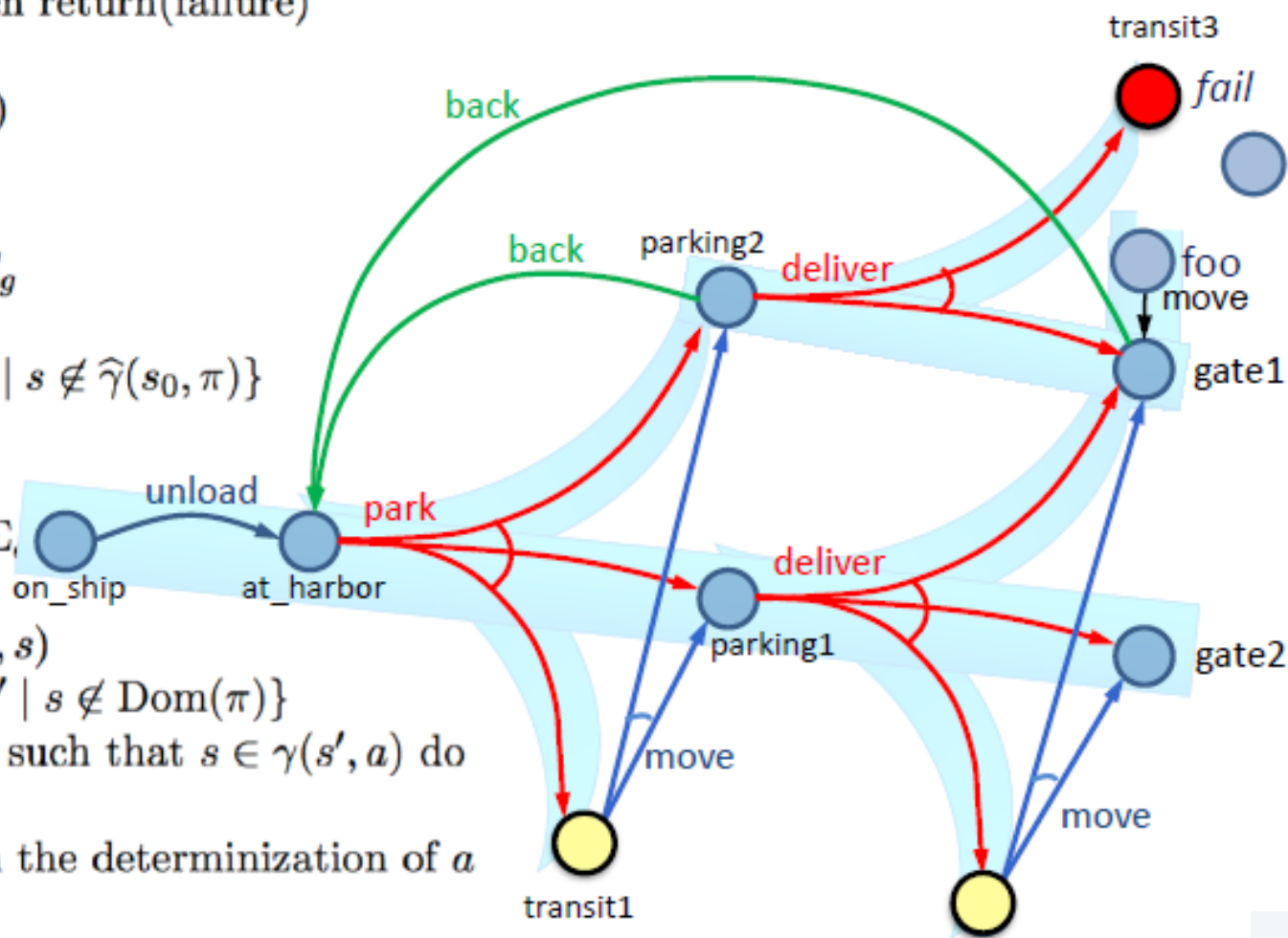
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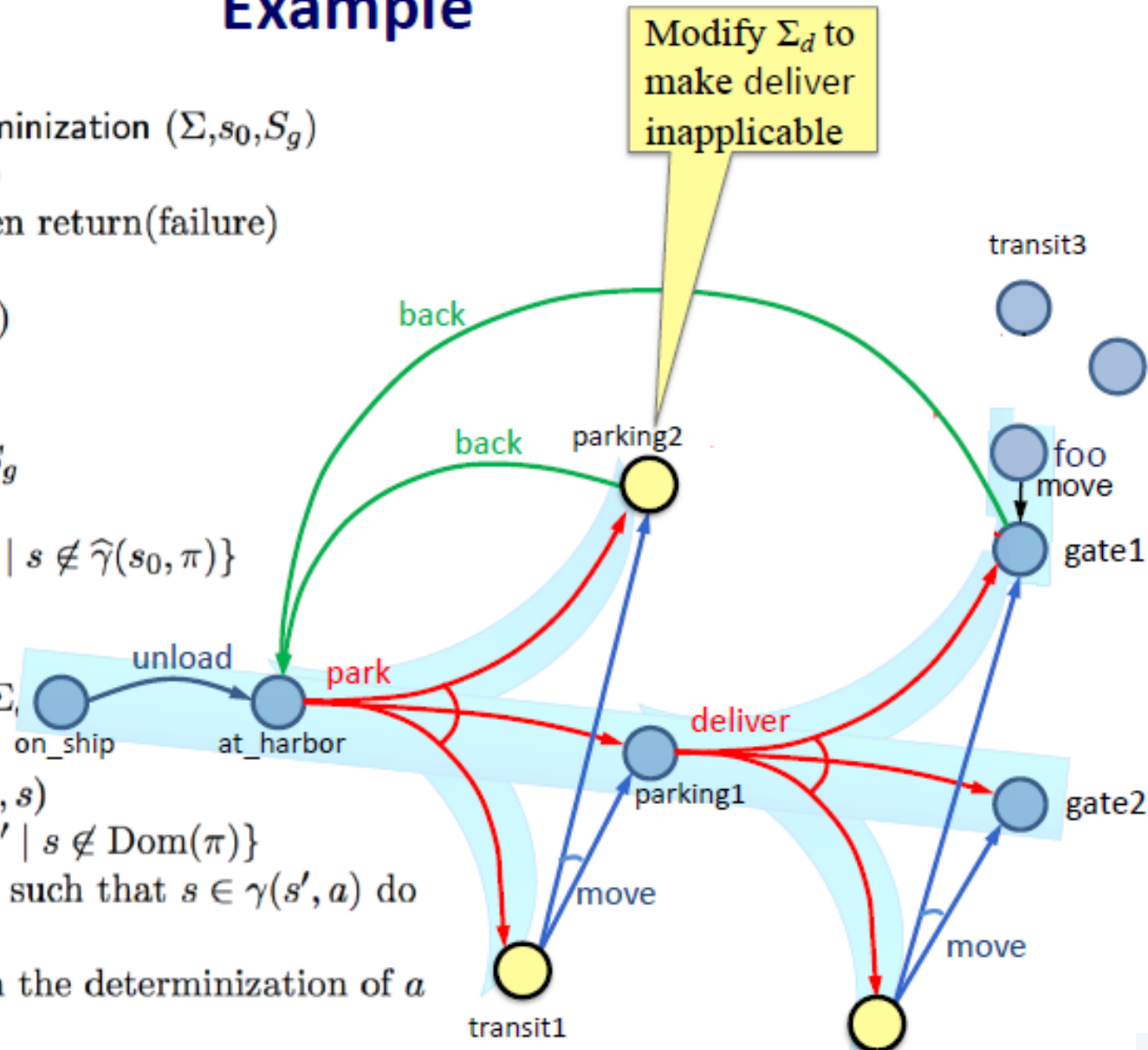
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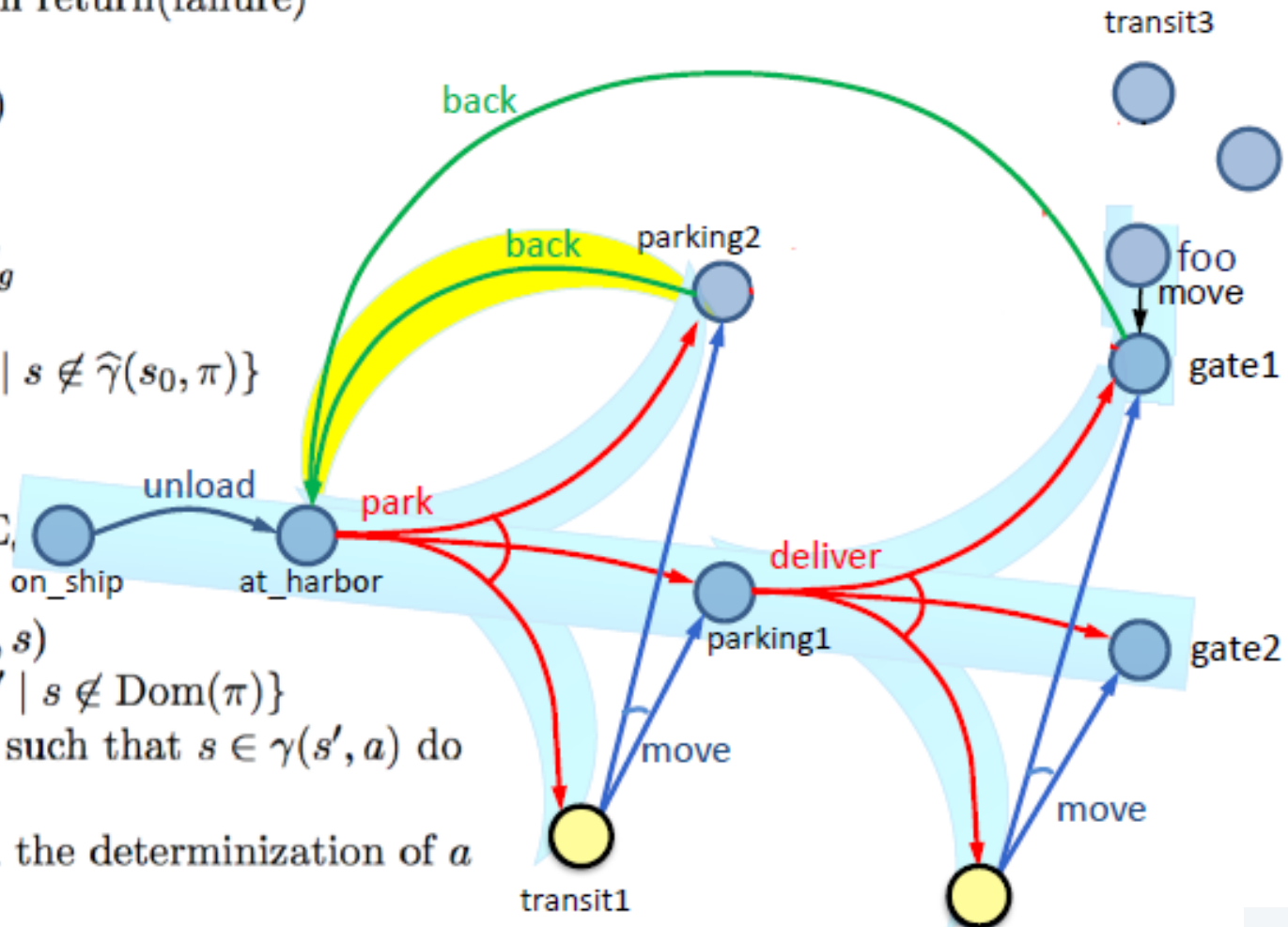
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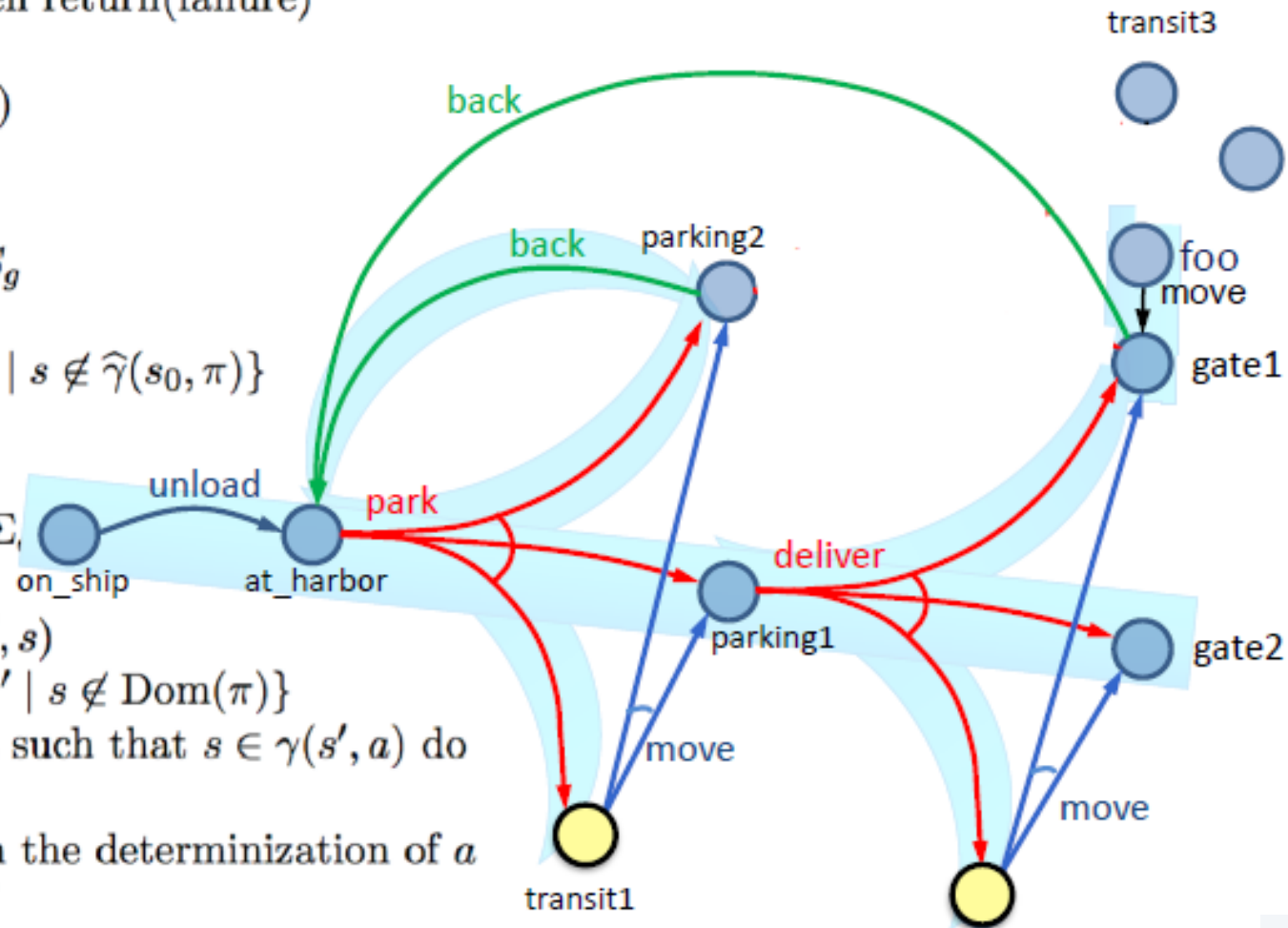
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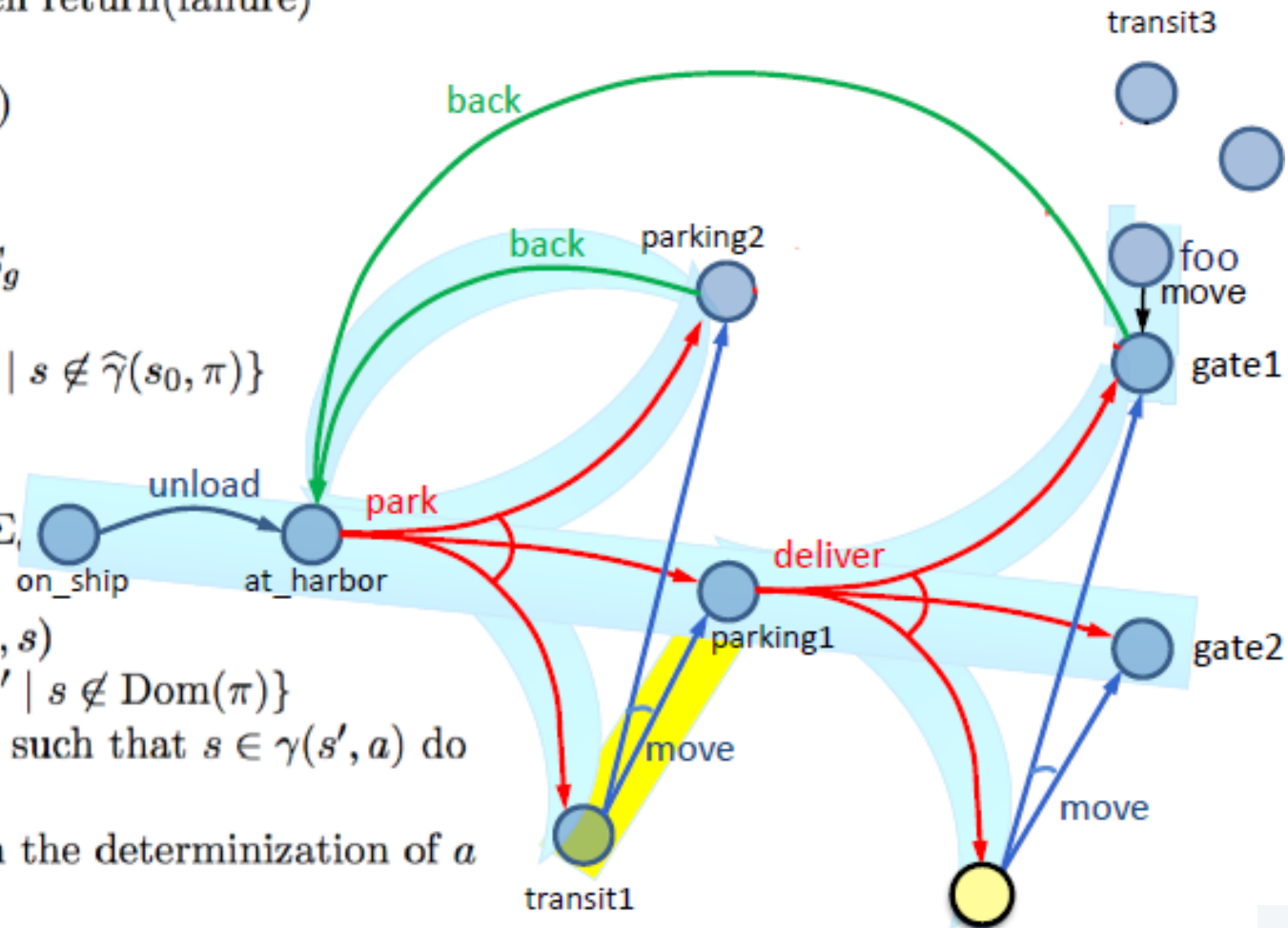
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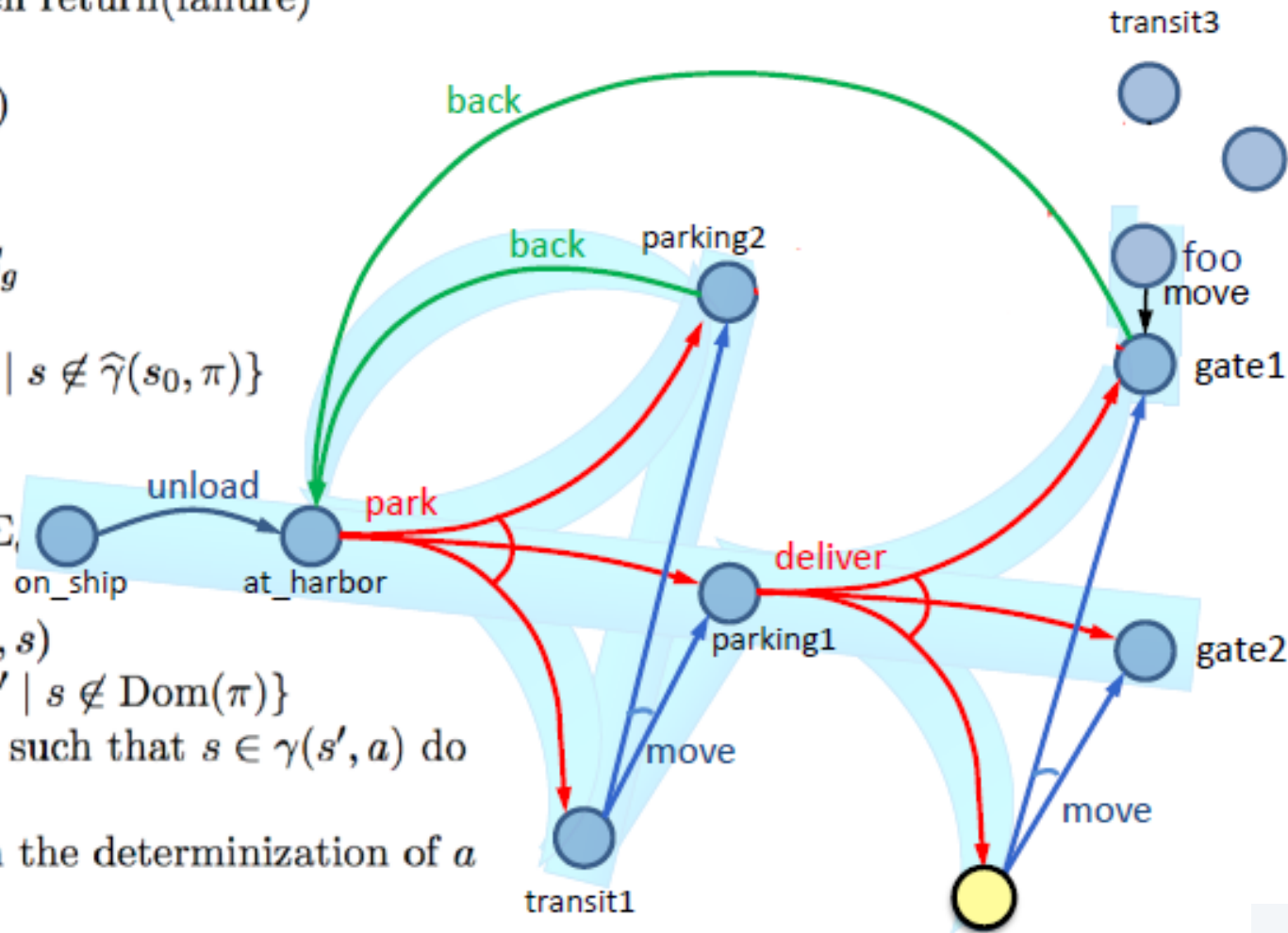
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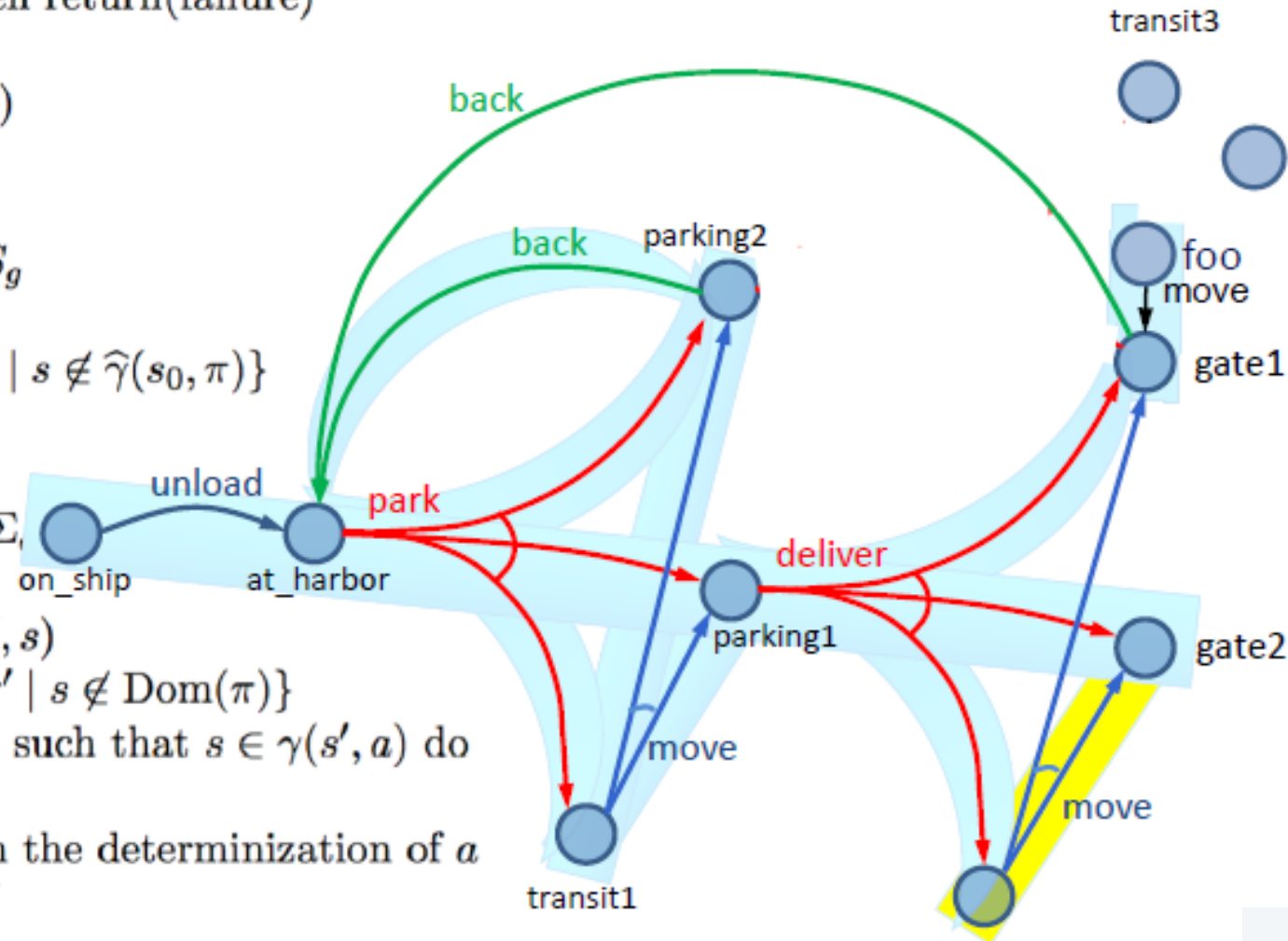
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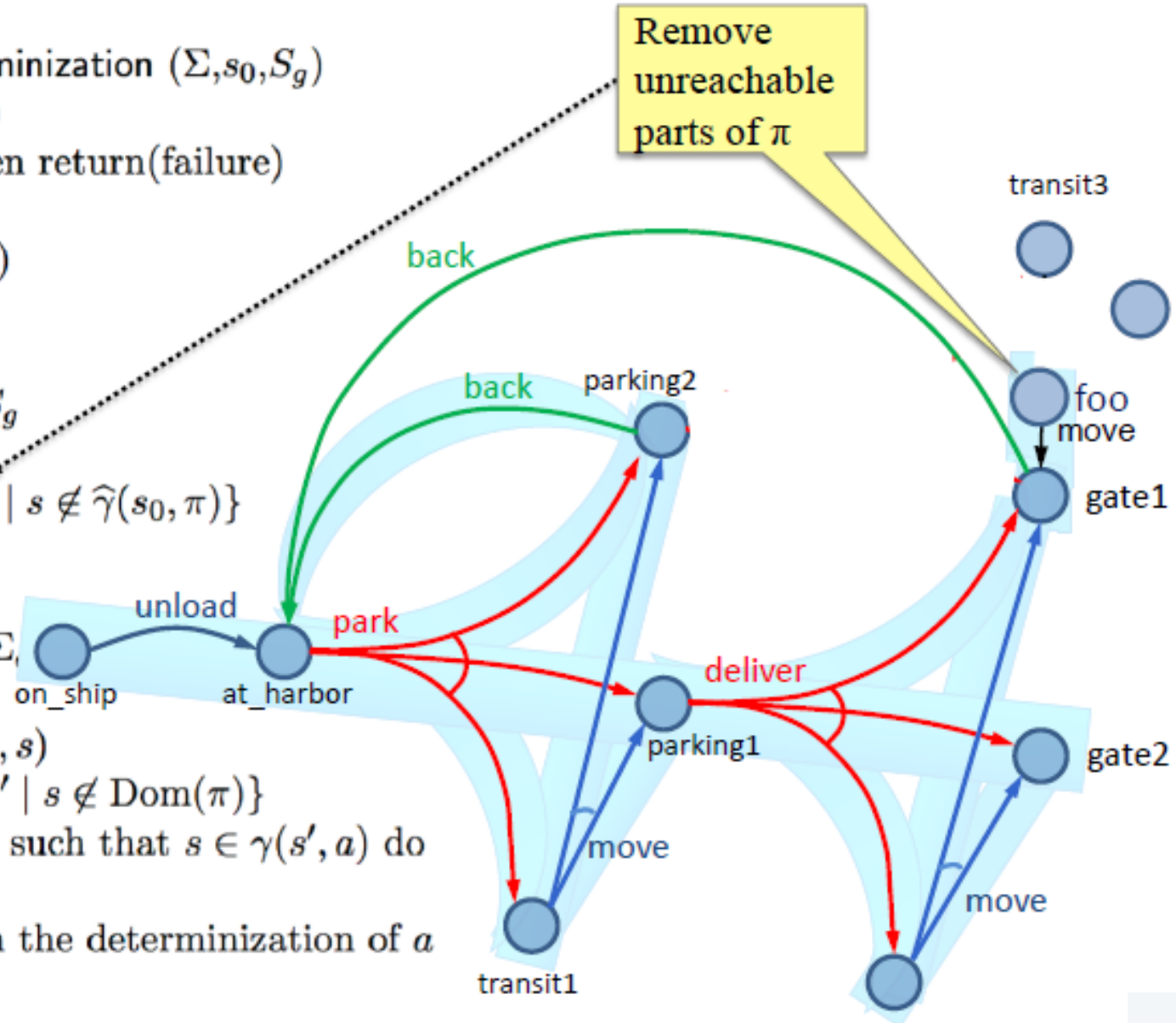
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Making Actions Inapplicable

Find-Safe-Solution-by-Determinization (Σ, s_0, S_g)

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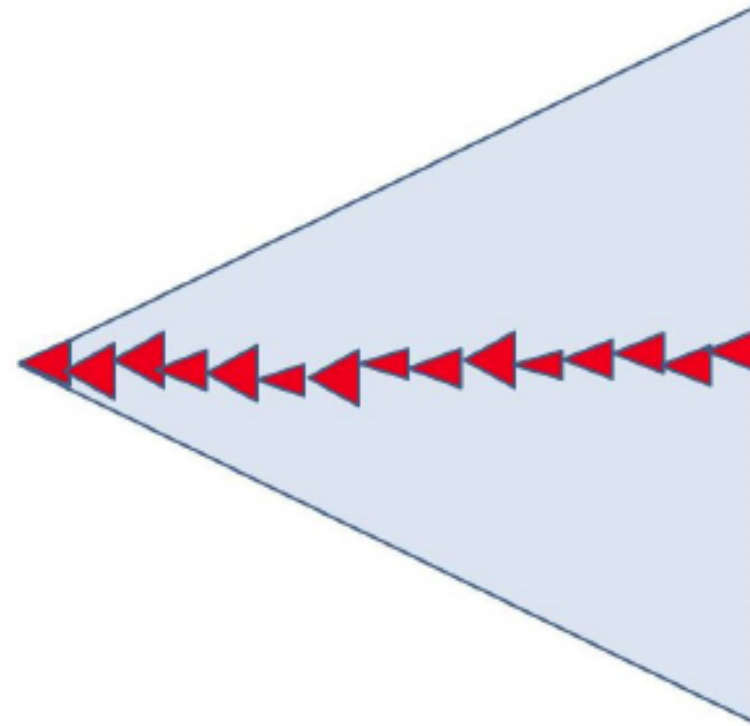
- Modify Σ_d to make actions inapplicable
 - worst-case exponential time
- Better: table of bad state-action pairs
 - For every (s', a) such that $s \in \gamma(s', a)$,
 $Bad[s'] \leftarrow Bad[s'] \cup \text{determinization}(a)$
 - Modify classical planner to take the table as an argument
 - if s is current state, only choose actions in $Applicable(s) \setminus Bad(s)$

Skip Ahead

- Several topics I'll skip for now
 - will come back later if there's time
 - Other kinds of search algorithms
 - min-max search
 - Symbolic model checking techniques
 - Backward search
 - BDD representation
 - ▶ Reduce search-space size by planning over sets of states

5.6 Online Approaches

- Motivation
 - Planning models are approximate – execution seldom works out as planned
 - Large problems may require too much planning time
- 2nd motivation even more stronger in nondeterministic domains
 - Nondeterminism makes planning exponentially harder
 - Exponentially more time, exponentially larger policies



Offline vs Runtime
Search Spaces

Online Approaches

- Need to identify *good* actions without exploring entire search space
 - Can be done using heuristic estimates
- Some domains are *safely explorable*
 - Safe to create partial plans, because goal states are reachable from all situations
- Other domains contain dead-ends, partial planning won't guarantee success
 - Can get trapped in dead ends that we would have detected if we had planned fully
 - No applicable actions
 - ▶ robot goes down a steep incline and can't come back up
 - Applicable actions, but caught in a loop
 - ▶ robot goes into a collection of rooms from which there's no exit
 - However, partial planning can still make success more likely

Lookahead-Partial-Plan

- Adaptation of Run-Lazy-Lookahead (Chapter 2)
- Lookahead is any planning algorithm that returns a policy π
 - π may be partial solution, or unsafe solution
 - Lookahead-Partial-Plan executes π as far as it will go, then calls Lookahead again

```
Lookahead-Partial-Plan( $\Sigma, s_0, S_g$ )  
   $s \leftarrow s_0$   
  while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do  
     $\pi \leftarrow \text{Lookahead}(s, \theta)$   
    if  $\pi = \emptyset$  then return failure  
    else do  
      perform partial plan  $\pi$   
       $s \leftarrow$  observe current state
```

FS-Replan

- Adaptation of Run-Lookahead
- Calls Forward-Search on determinized domain, converts to a policy
 - Unsafe solution

FS-Replan (Σ, s, S_g)

```
 $\pi_d \leftarrow \emptyset$   
while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do  
  if  $\pi_d$  undefined for  $s$  then do  
     $\pi_d \leftarrow \text{Plan2policy}(\text{Forward-search}(\Sigma_d, s, S_g), s)$   
    if  $\pi_d = \text{failure}$  then return failure  
  perform action  $\pi_d(s)$   
   $s \leftarrow$  observe resulting state
```

- Generalization:
 - Lookahead can be any planning algorithm that returns a policy π

FS-Replan (Σ, s, S_g) (*generalize*)

```
 $\pi_d \leftarrow \emptyset$   
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  if  $\pi_d$  undefined for  $s$  then do  
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   $s \leftarrow$  observe resulting state
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Possibilities for Lookahead

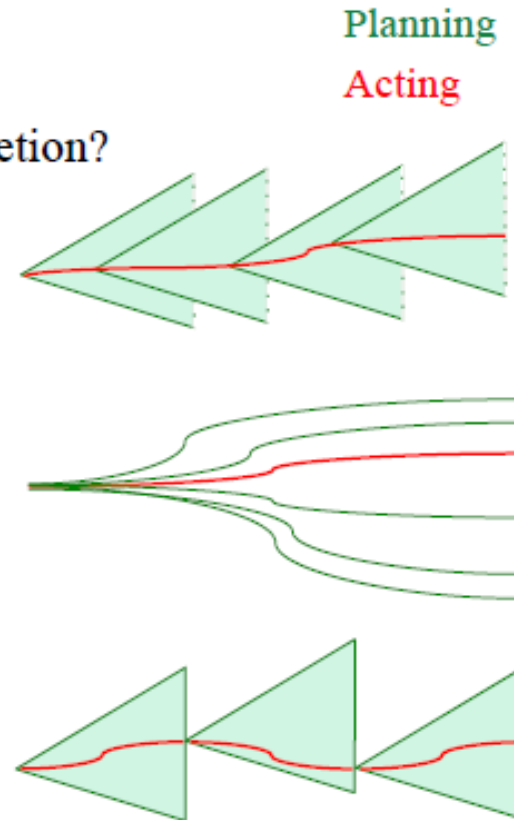
- Lookahead could be one of the algorithms we discussed earlier

- Find-Safe-Solution
- Find-Acyclic-Solution
- Guided-Find-Safe-Solution
- Find-Safe-Solution-by-Determinization

- What if it doesn't have time to run to completion?

- Can use the same techniques we discussed in Chapter 3

- Receding horizon
- Sampling
- Subgoaling
- Iterative deepening



Possibilities for Lookahead

- *Full horizon, limited breadth:*
 - look for solution that works for *some* of the outcomes
 - E.g., modify Find-Acyclic-Solution to examine i outcomes of every action
- *Iterative broadening:*
 - for $i = 1$ by 1 until time runs out
 - look for a solution that handles i outcomes per action

Find-Acyclic-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every $s \in Frontier \setminus S_g$ do

$Frontier \leftarrow Frontier \setminus \{s\}$

if $Applicable(s) = \emptyset$ then return failure

nondeterministically choose $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if $has-loops(\pi, a, Frontier)$ then return failure

return π

$T \leftarrow i$ elements of $\gamma(s, a) \setminus Dom(\pi)$

$Frontier \leftarrow Frontier \cup T$

Safely Explorable Domains

- *Safely explorable* domain
 - for every state s , at least one goal state is reachable from s
- Suppose
 - We use Lookahead-Partial-Plan or FS-Replan in a safely explorable domain
 - Lookahead never returns failure
 - No “unfair” executions
- Then we will eventually reach a goal
- What would happen if we just chose a random action each time?

Summary

- Actions, plans, policies, planning problems
- types of solutions: unsafe, cyclic safe, acyclic safe
 - algorithms for each
- Guided-find-safe-solution
 - call find-solution to get an unsafe solution
 - call find-solution additional times on the leaves
- find-safe-solution-by-determinization
 - use determinized actions
 - call classical planner rather than find-solution
 - if dead-ends are encountered, modify actions that lead to them

- continued on next page

Summary

- Online approaches
 - Lookahead-partial-plan
 - adaptation of Run-Lazy-Lookahead
 - FS-replan
 - adaptation of Run-Lookahead
- ways to do the lookahead
 - full breadth with limited depth,
 - iterative deepening
 - full depth with limited breadth
 - iterative broadening
 - convergence in safely explorable domains
- min-max-LRTA*

Can also adapt
Run-Concurrent-Lookahead

Can put bounds on both
depth and breadth