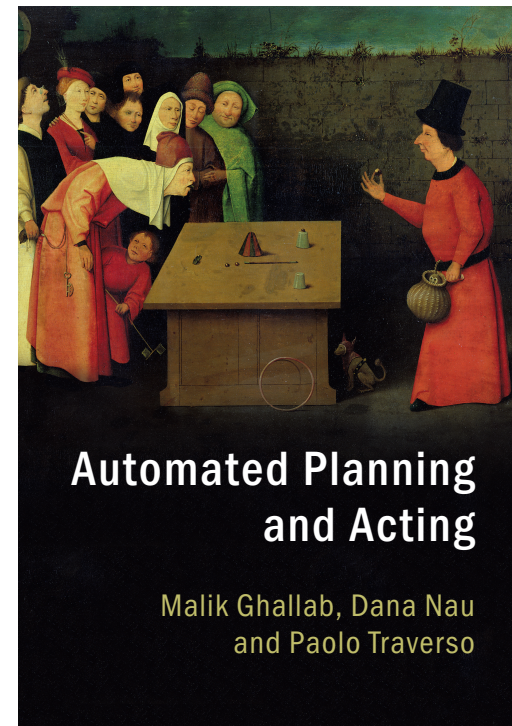


## Chapter 5

# Deliberation with Nondeterministic Domain Models

Dana S. Nau

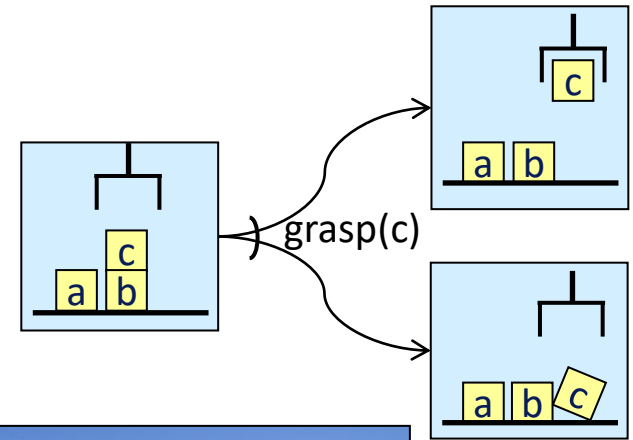
University of Maryland



<http://www.laas.fr/planning>

# Motivation

- We've assumed action  $a$  in state  $s$  has just one possible outcome
  - $\gamma(s, a)$
- Often more than one possible outcome
  - Unintended outcomes
  - Exogenous events
  - Inherent uncertainty



# Nondeterministic Planning Domains

- 3-tuple  $(S, A, \gamma)$ 
  - $S$  and  $A$  – finite sets of states and actions
  - $\gamma: S \times A \rightarrow 2^S$
- $\gamma(s, a) = \{\text{all possible “next states” after applying action } a \text{ in state } s\}$ 
  - $a$  is applicable in state  $s$  iff  $\gamma(s, a) \neq \emptyset$
- $\text{Applicable}(s) = \{\text{all actions applicable in } s\} = \{a \in A \mid \gamma(s, a) \neq \emptyset\}$
- One action representation:  $n$  mutually exclusive “effects” lists

$a(z_1, \dots, z_k)$

pre:  $p_1, \dots, p_m$

eff<sub>1</sub>:  $e_{11}, e_{12}, \dots$

eff<sub>2</sub>:  $e_{21}, e_{22}, \dots$

...

eff <sub>$n$</sub> :  $e_{n1}, e_{n2}, \dots$

- Problem:  $n$  may be combinatorially large
  - Suppose  $a$  can cause any possible combination of effects  $e_1, e_2, \dots, e_k$
  - Need  $\text{eff}_1, \text{eff}_2, \dots, \text{eff}_{2^k}$ 
    - ▶ One for each combination
  - Section 5.4: a way to alleviate this
- For now, ignore most of that
  - states, actions  $\Leftrightarrow$  nodes, edges in a graph

# Nondeterministic Planning Domains

- For deterministic planning problems, search space was a graph
- Now it's an AND/OR graph

➤ *OR branch:*

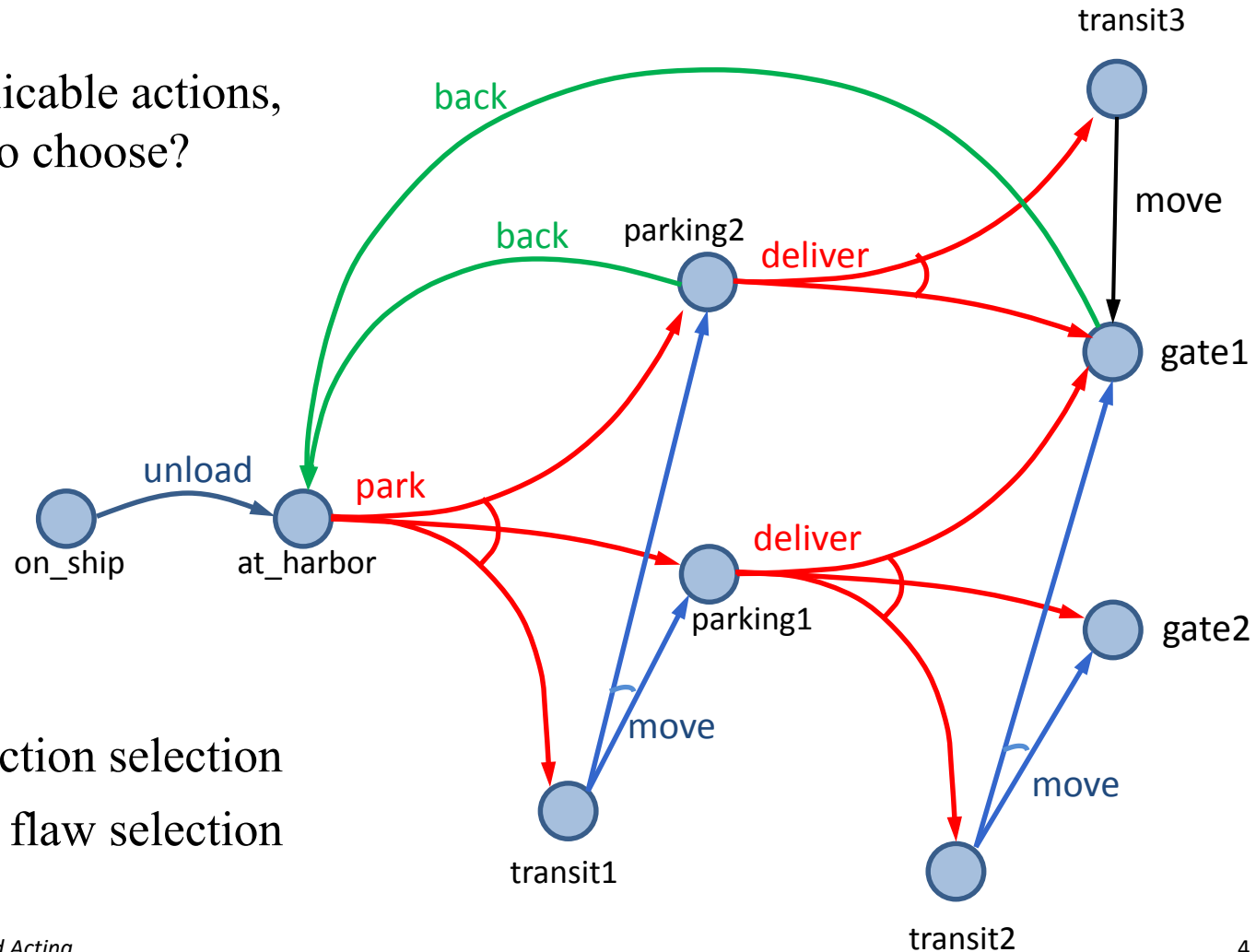
- several applicable actions, which one to choose?

➤ *AND branch:*

- multiple possible outcomes
- must handle all of them

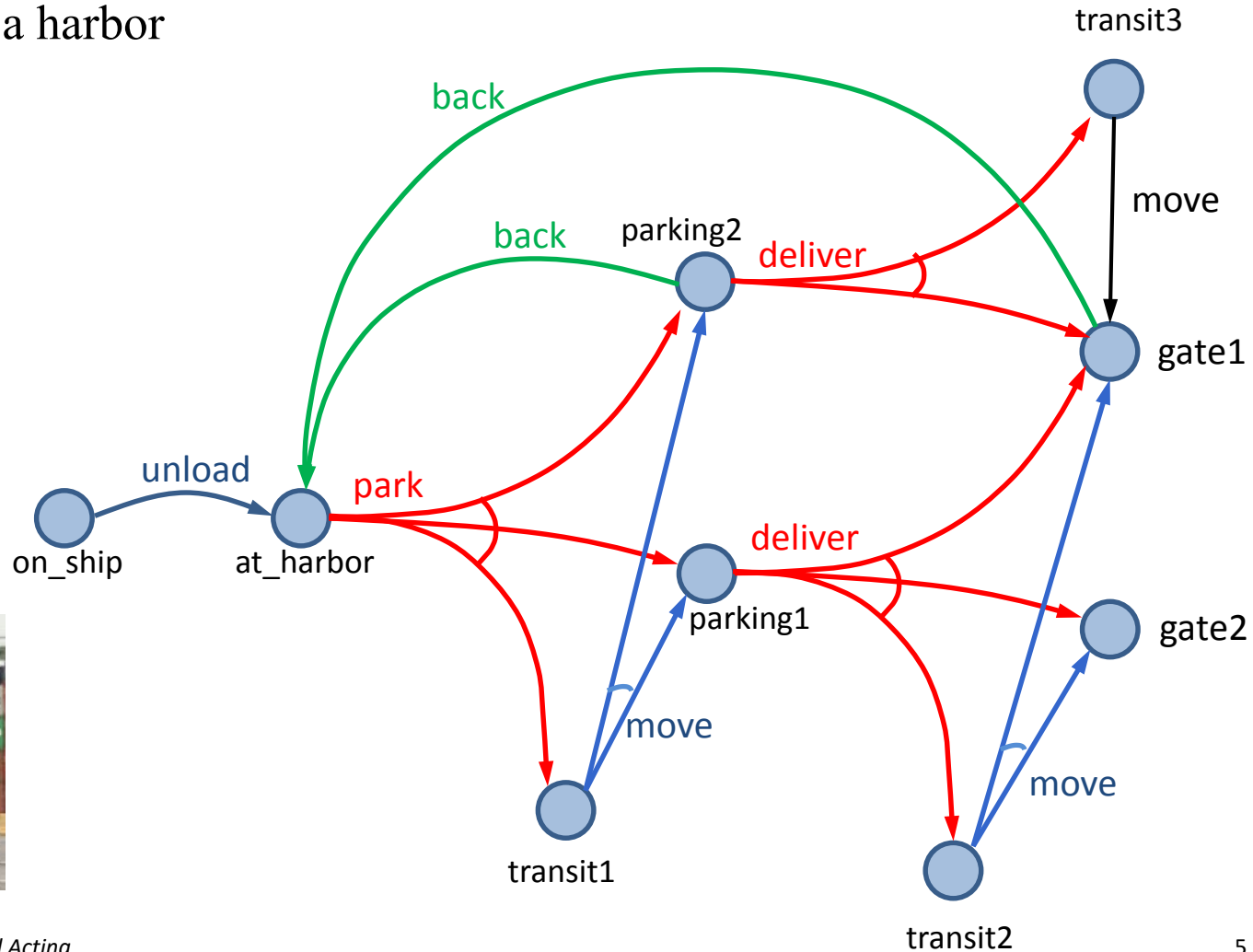
- Analogy to PSP

- *OR branch*  $\Leftrightarrow$  action selection
- *AND branch*  $\Leftrightarrow$  flaw selection



# Example

- Very simple harbor management domain
  - Unload a single item from a ship
  - Move it around a harbor

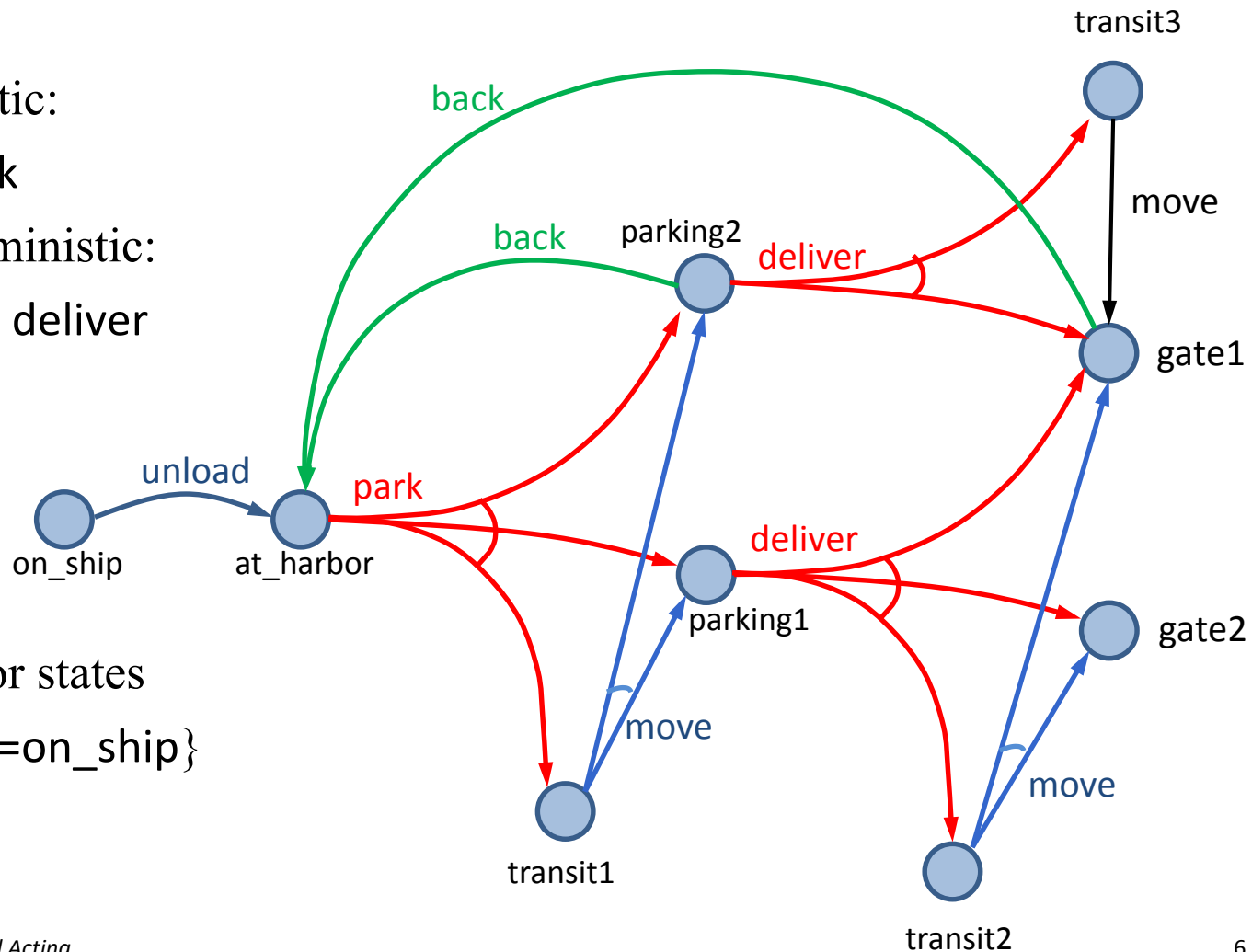


# Example

- One state variable:  $\text{pos}(\text{item})$

- Five actions

- Two deterministic:
  - unload, back
- Three nondeterministic:
  - park, move, deliver



- Simplified names for states

- For  $\{\text{pos}(\text{item})=\text{on\_ship}\}$  write  $\text{on\_ship}$

# Actions

- park

pre:  $\text{pos}(\text{item}) = \text{at\_harbor}$

eff<sub>1</sub>:  $\text{pos}(\text{item}) \leftarrow \text{parking1}$

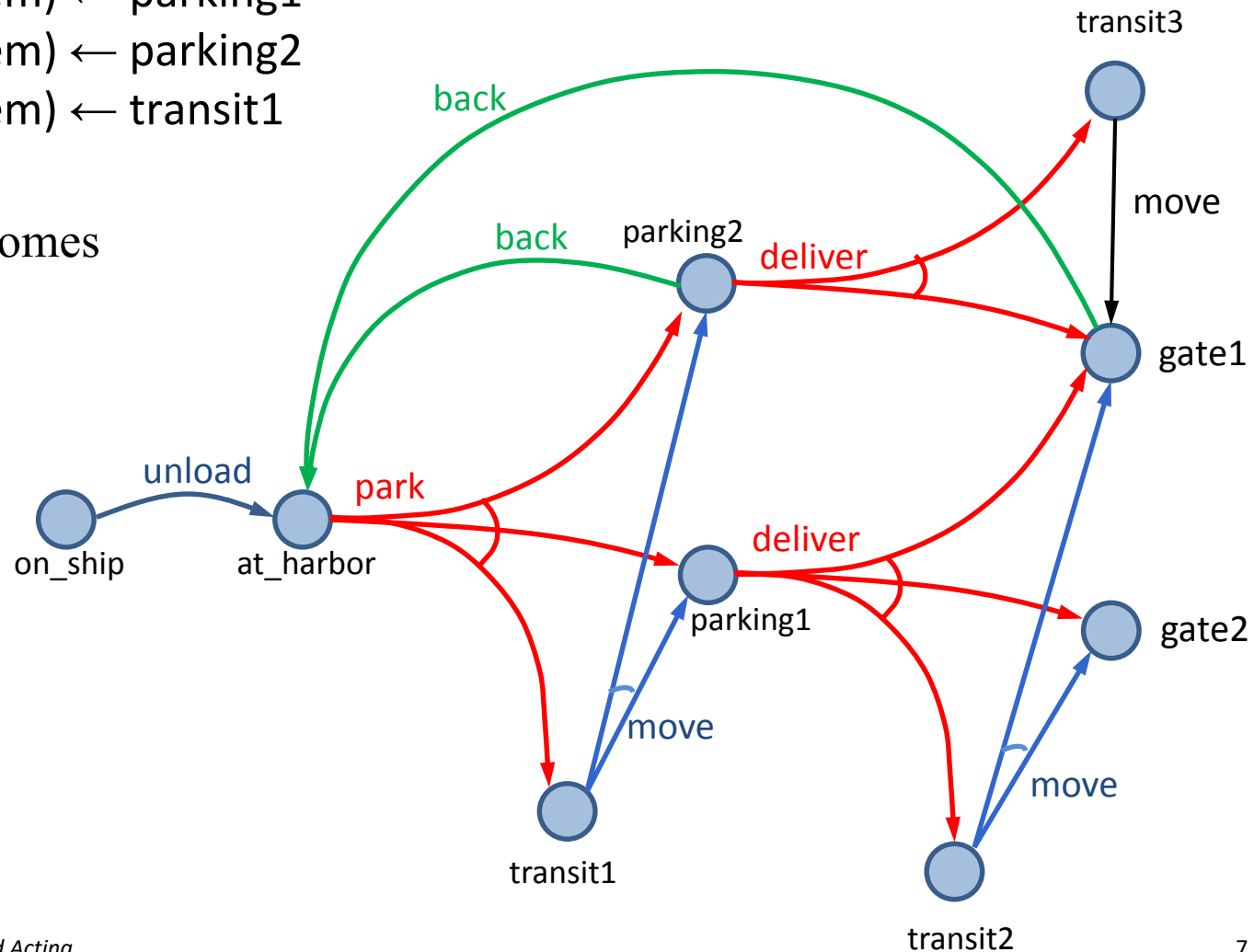
eff<sub>2</sub>:  $\text{pos}(\text{item}) \leftarrow \text{parking2}$

eff<sub>3</sub>:  $\text{pos}(\text{item}) \leftarrow \text{transit1}$

- Three possible outcomes

- put item in parking1 or parking2 if one of them has space

- or in transit1 if there's no parking space



# Plans Policies

- Need something more general than a sequence of actions
  - After park, what do we do next?

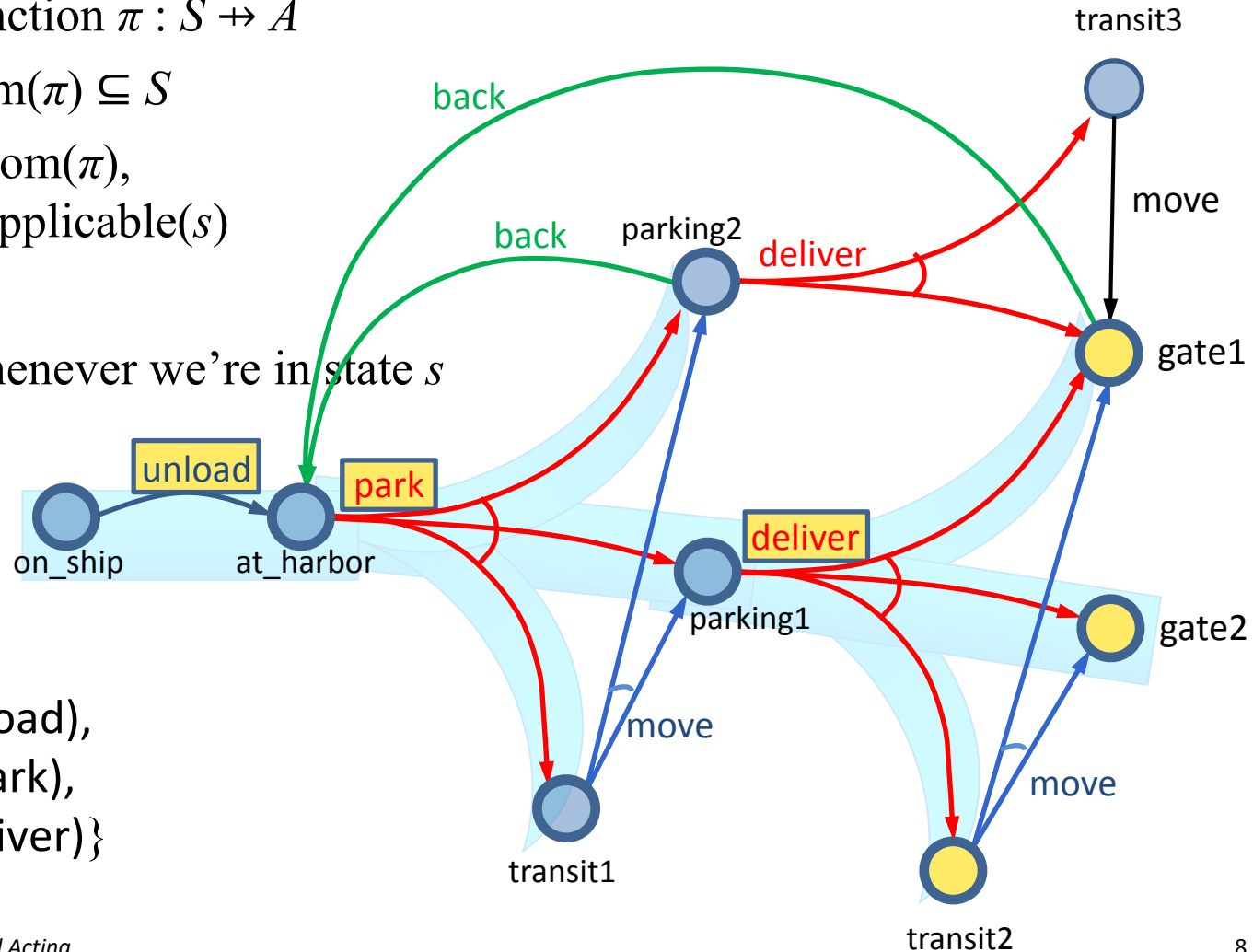
- *Policy*: a *partial* function  $\pi : S \mapsto A$

- ▶ i.e.,  $\text{Dom}(\pi) \subseteq S$

- ▶ For every  $s \in \text{Dom}(\pi)$ , require  $\pi(s) \in \text{Applicable}(s)$

- Meaning:

- ▶ perform  $\pi(s)$  whenever we're in state  $s$



- $\pi_1 = \{(\text{on\_ship}, \text{unload}), (\text{at\_harbor}, \text{park}), (\text{parking1}, \text{deliver})\}$



# Definitions Over Policies

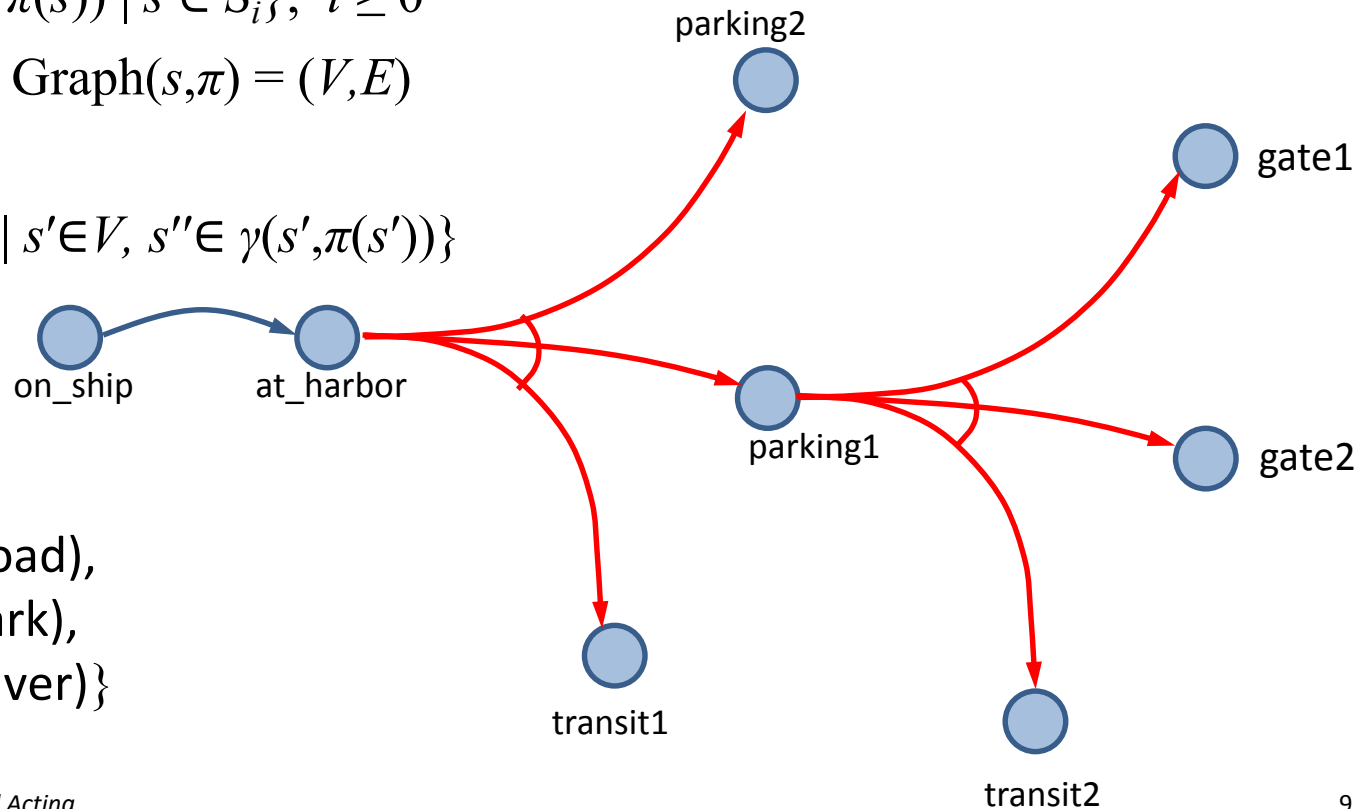
- *Transitive closure*:  
 {all states reachable from  $s$  using  $\pi$ }
  - $leaves(s,\pi) = \hat{\gamma}(s, \pi) \setminus \text{Dom}(\pi)$ 
    - may be empty

➤  $\hat{\gamma}(s,\pi) = S_0 \cup S_1 \cup S_2 \cup \dots$

- $S_0 = \{s\}$
- $S_{i+1} = \cup \{\gamma(s,\pi(s)) \mid s \in S_i\}, i \geq 0$

- *Reachability graph*:  $\text{Graph}(s,\pi) = (V,E)$

- $V = \hat{\gamma}(s,\pi)$
- $E = \{(s',s'') \mid s' \in V, s'' \in \gamma(s',\pi(s'))\}$



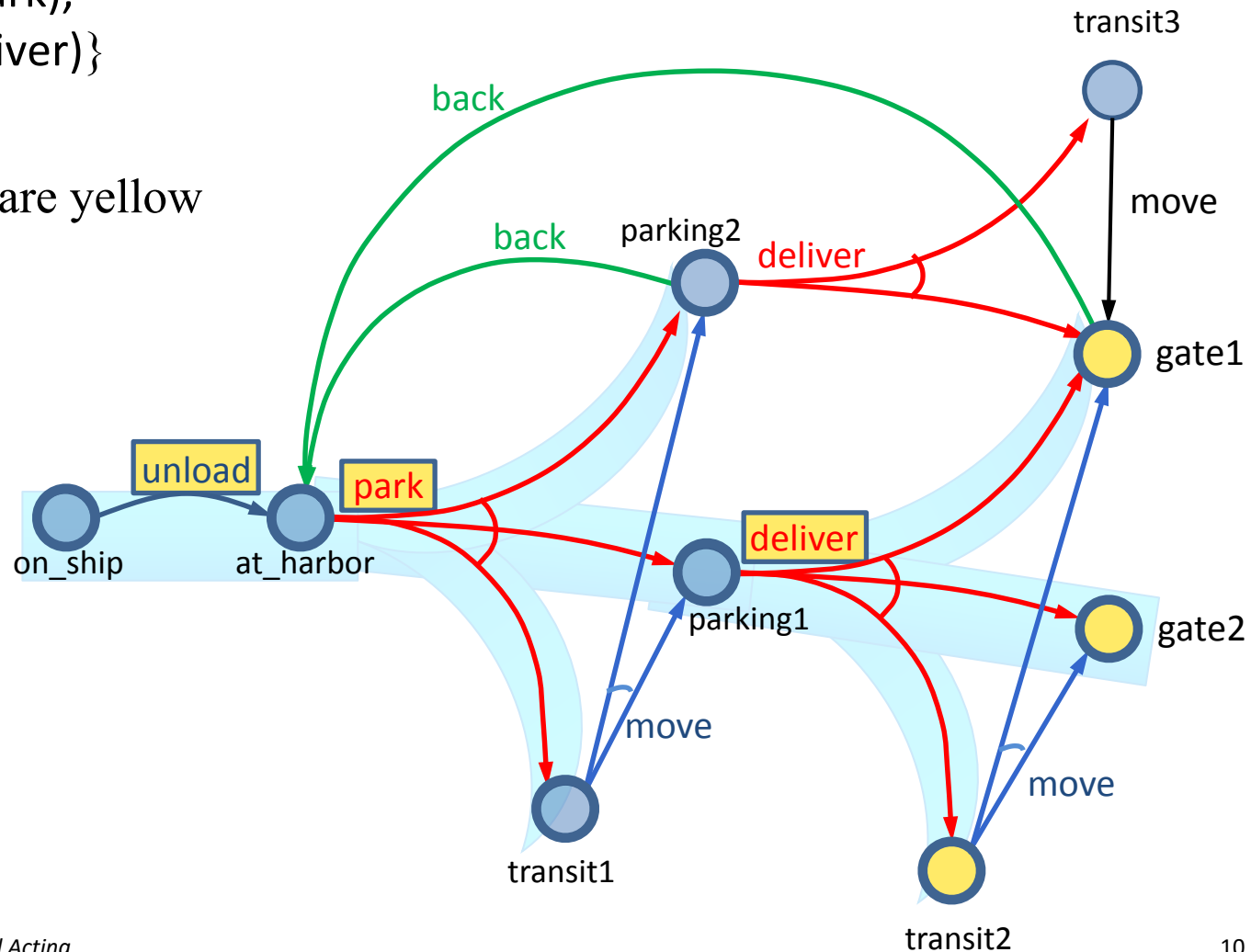
- $\pi_1 = \{(on\_ship, unload),$   
 $(at\_harbor, park),$   
 $(parking1, deliver)\}$

# Definitions Over Policies

- $\pi_1 = \{(on\_ship, unload), (at\_harbor, park), (parking1, deliver)\}$

- $leaves(on\_ship, \pi_1)$  are yellow

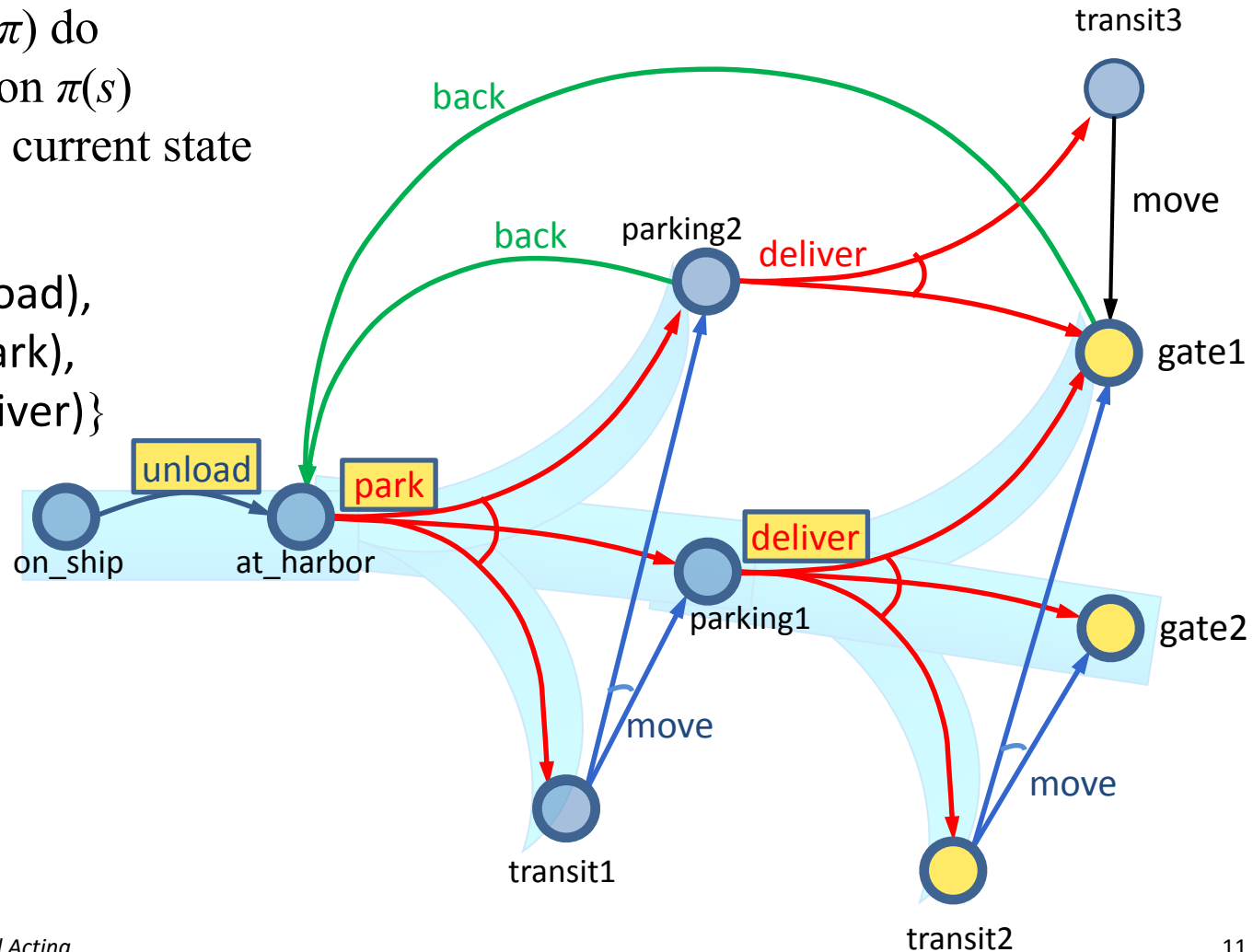
- $leaves(s, \pi) = \hat{\gamma}(s, \pi) \setminus \text{Dom}(\pi)$ 
  - may be empty



# Performing a Policy

- PerformPolicy( $\pi$ )
  - $s \leftarrow$  observe current state
  - while  $s \in \text{Dom}(\pi)$  do
  - perform action  $\pi(s)$
  - $s \leftarrow$  observe current state

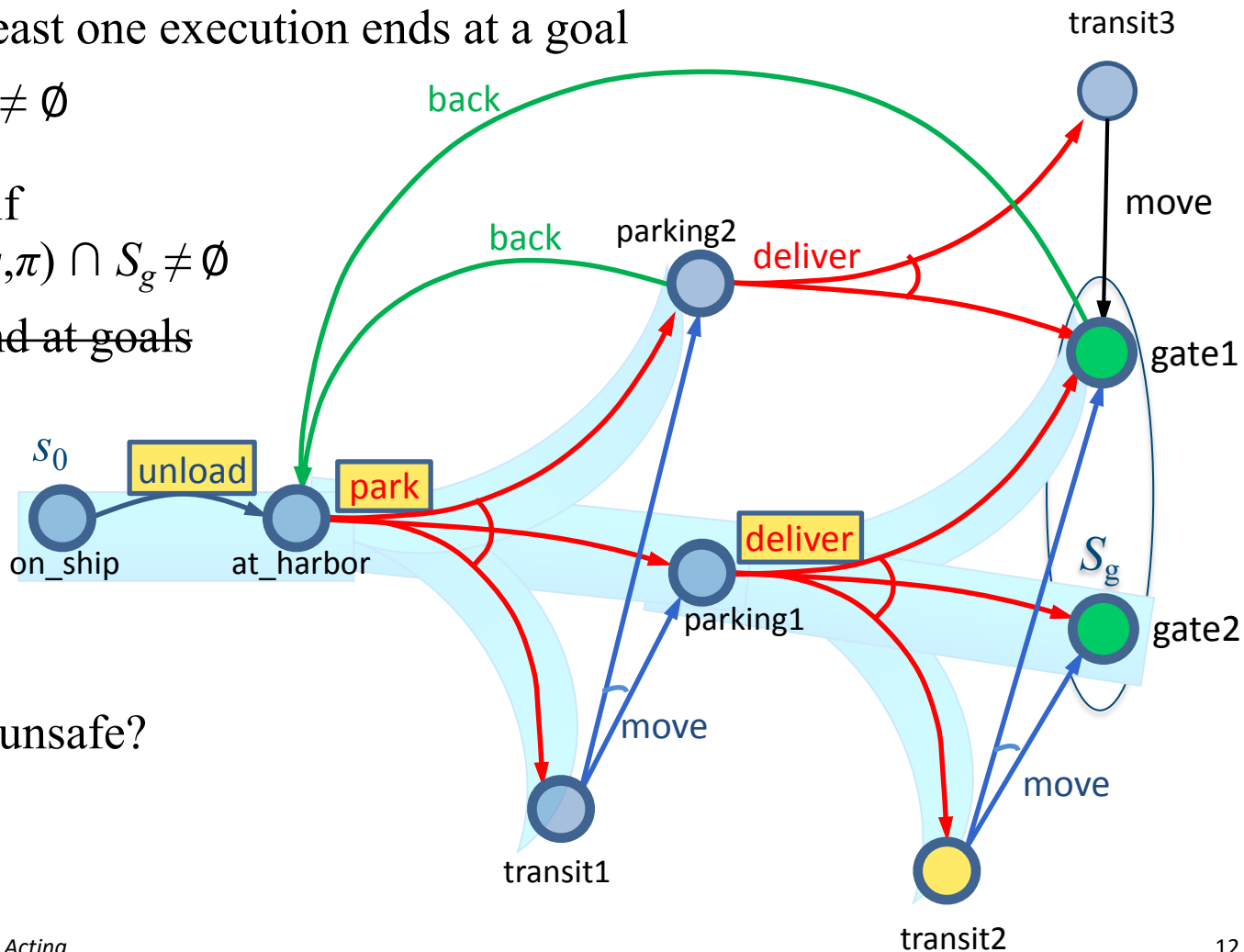
- $\pi_1 = \{(\text{on\_ship}, \text{unload}),$   
 $(\text{at\_harbor}, \text{park}),$   
 $(\text{parking1}, \text{deliver})\}$



# Planning Problems and Solutions

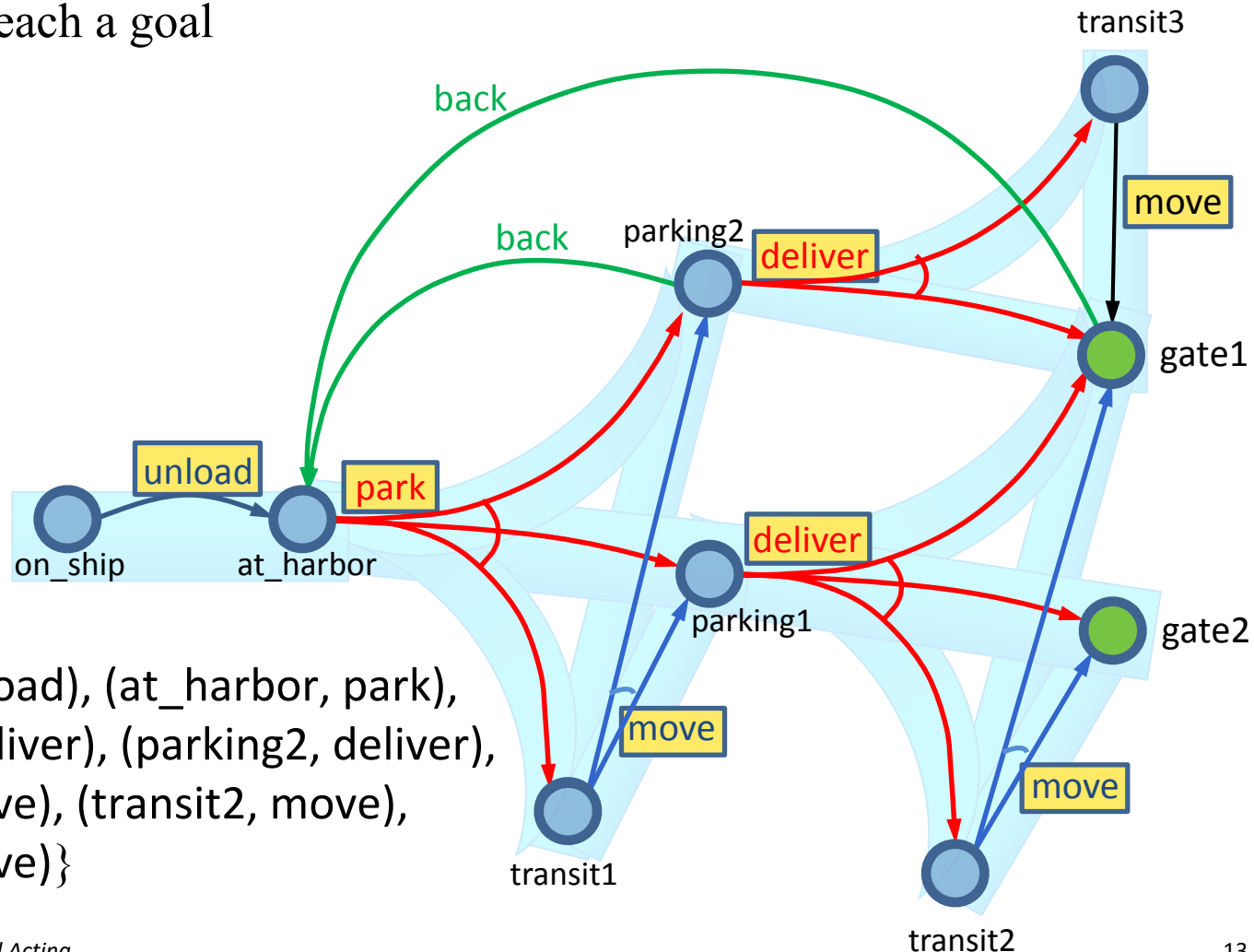
- Planning problem  $P = (\Sigma, s_0, S_g)$ 
  - planning domain  $\Sigma = (S, A, \gamma)$ , initial state  $s_0 \in S$ , set of goal states  $S_g \subseteq S$  (shown in green)
- $\pi$  is a *solution* if at least one execution ends at a goal
  - $leaves(s, \pi) \cap S_g \neq \emptyset$
- A solution  $\pi$  is *safe* if
  - $\forall s \in \hat{\gamma}(s_0, \pi), leaves(s, \pi) \cap S_g \neq \emptyset$
  - ~~all executions end at goals~~
  - at every node of  $Graph(s_0, \pi)$ , the goal is reachable
- Otherwise, *unsafe*
  - Is  $\pi_1$  safe or unsafe?

$\pi_1 = \{(on\_ship, unload), (at\_harbor, park), (parking1, deliver)\}$



# Safe Solutions

- *Acyclic* safe solution
  - $\text{Graph}(s_0, \pi)$  is acyclic, and  $\text{leaves}(s, \pi) \subseteq S_g$
  - Guaranteed to reach a goal



- $\pi_2 = \{(\text{on\_ship}, \text{unload}), (\text{at\_harbor}, \text{park}), (\text{parking1}, \text{deliver}), (\text{parking2}, \text{deliver}), (\text{transit1}, \text{move}), (\text{transit2}, \text{move}), (\text{transit3}, \text{move})\}$

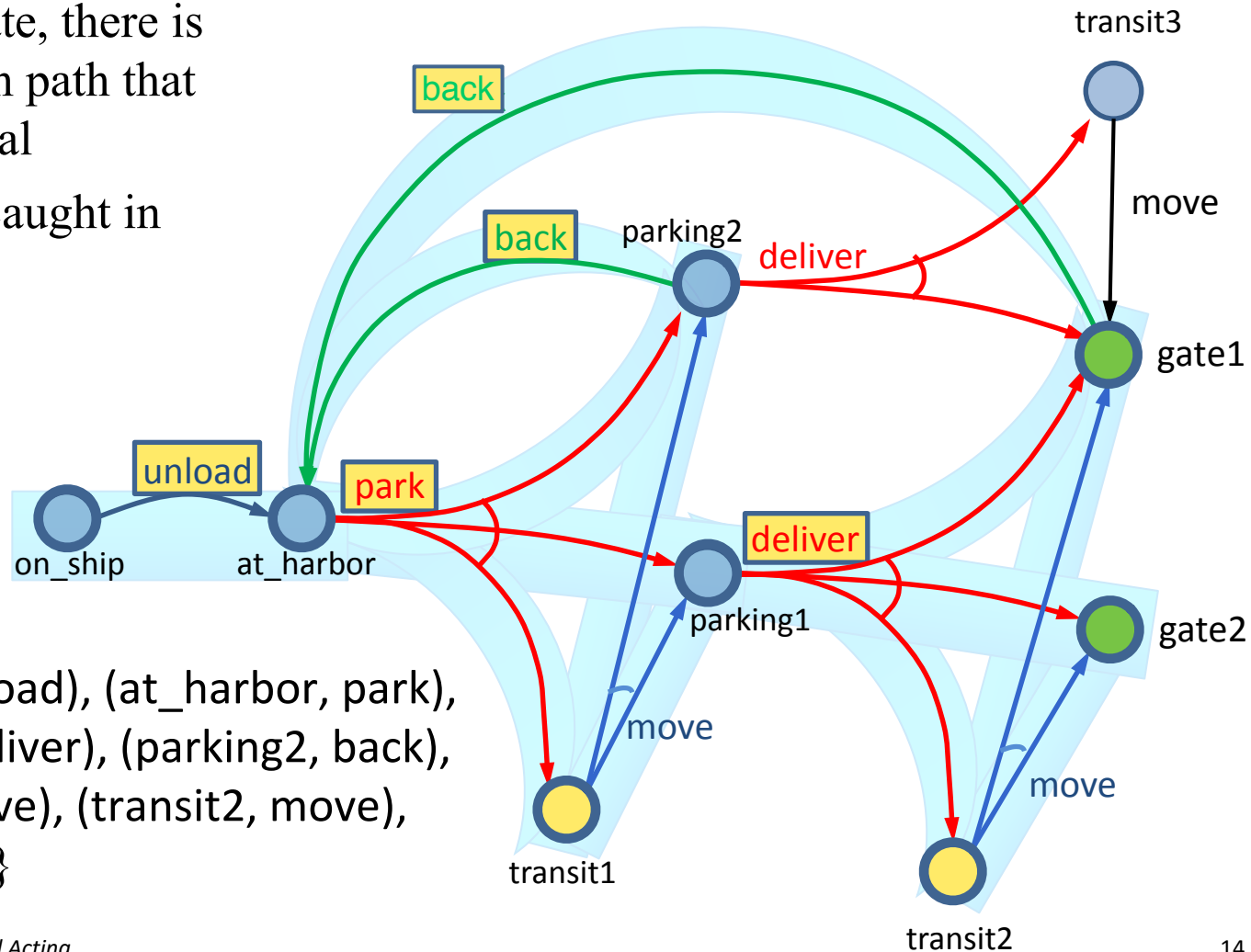
# Safe Solutions

- *Cyclic* safe solution

- $\text{Graph}(s_0, \pi)$  is cyclic,  $\text{leaves}(s, \pi) \subseteq S_g$ ,  $\forall s \in \hat{\gamma}(s_0, \pi)$ ,  $\text{leaves}(s, \pi) \cap S_g \neq \emptyset$

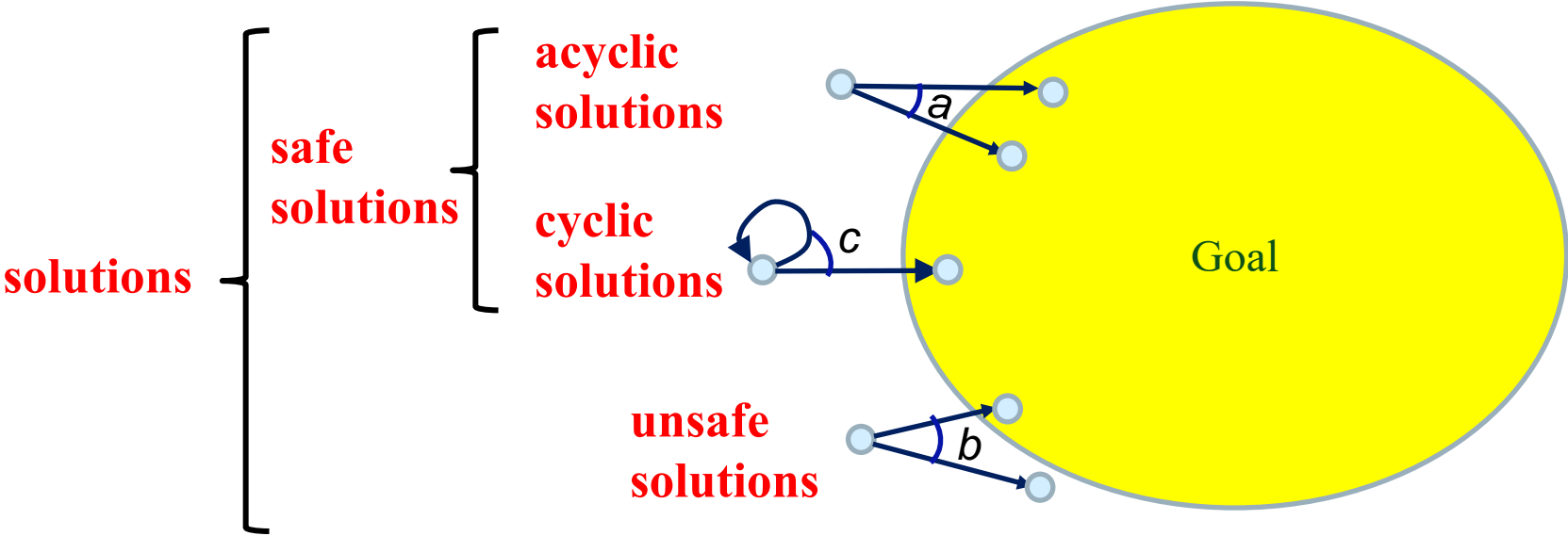
- At every state, there is an execution path that ends at a goal

- Will never get caught in a dead end



- $\pi_3 = \{(\text{on\_ship}, \text{unload}), (\text{at\_harbor}, \text{park}), (\text{parking1}, \text{deliver}), (\text{parking2}, \text{back}), (\text{transit1}, \text{move}), (\text{transit2}, \text{move}), (\text{gate1}, \text{back})\}$

# Kinds of Solutions



# Finding (Unsafe) Solutions

For comparison:

Forward-search  $(\Sigma, s_0, g)$

$s \leftarrow s_0; \pi \leftarrow \langle \rangle$

loop

if  $s$  satisfies  $g$  then return  $\pi$

$A' \leftarrow \{a \in A \mid a \text{ is applicable in } s\}$

if  $A' = \emptyset$  then return failure

nondeterministically choose  $a \in A'$

$s \leftarrow \gamma(s, a); \pi \leftarrow \pi.a$

Find-Solution  $(\Sigma, s_0, S_g)$

$\pi \leftarrow \emptyset; s \leftarrow s_0; Visited \leftarrow \{s_0\}$

loop

if  $s \in S_g$  then return  $\pi$

$A' \leftarrow \text{Applicable}(s)$

if  $A' = \emptyset$  then return failure

nondeterministically choose  $a \in A'$

(\*) nondeterministically choose  $s' \in \gamma(s, a)$  ← Decide which state to plan for

if  $s' \in Visited$  then return failure ← Cycle-checking

$\pi(s) \leftarrow a; Visited \leftarrow Visited \cup \{s'\}; s \leftarrow s'$

**Poll:** which should (\*) be?

1. nondeterministically choose
2. arbitrarily choose



Find-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset; s \leftarrow s_0; Visited \leftarrow \{s_0\}$

loop

if  $s \in S_g$  then return  $\pi$

$A' \leftarrow \text{Applicable}(s)$

if  $A' = \emptyset$  then return failure

nondeterministically choose  $a \in A'$

nondeterministically choose  $s' \in \gamma(s, a)$

if  $s' \in Visited$  then return failure

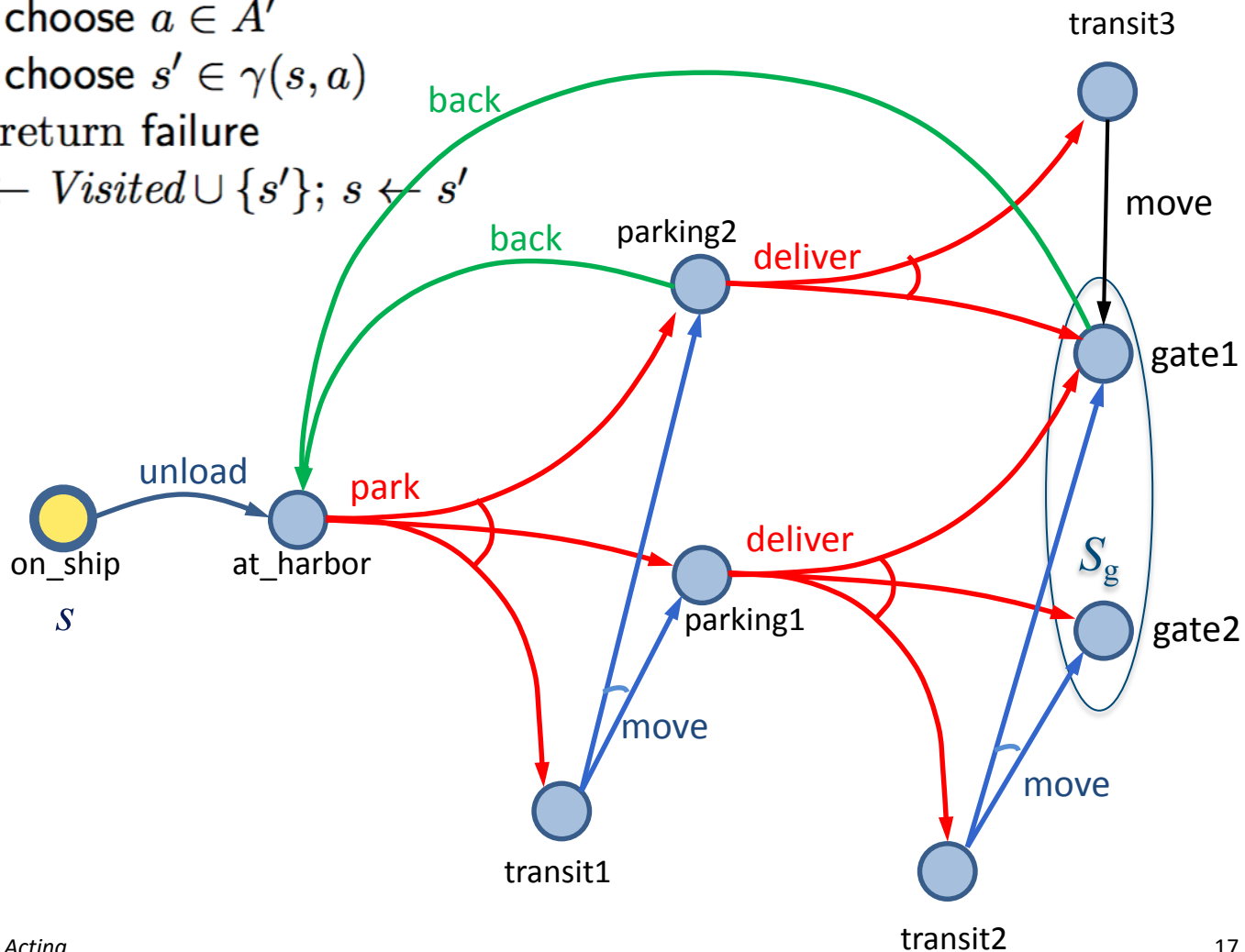
$\pi(s) \leftarrow a; Visited \leftarrow Visited \cup \{s'\}; s \leftarrow s'$

$s = \text{on\_ship}$

$\pi = \{\}$

$Visited = \{\text{on\_ship}\}$

# Example



# Find-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$ ;  $s \leftarrow s_0$ ;  $Visited \leftarrow \{s_0\}$

loop

if  $s \in S_g$  then return  $\pi$

$A' \leftarrow \text{Applicable}(s)$

if  $A' = \emptyset$  then return failure

nondeterministically choose  $a \in A'$

nondeterministically choose  $s' \in \gamma(s, a)$

if  $s' \in Visited$  then return failure

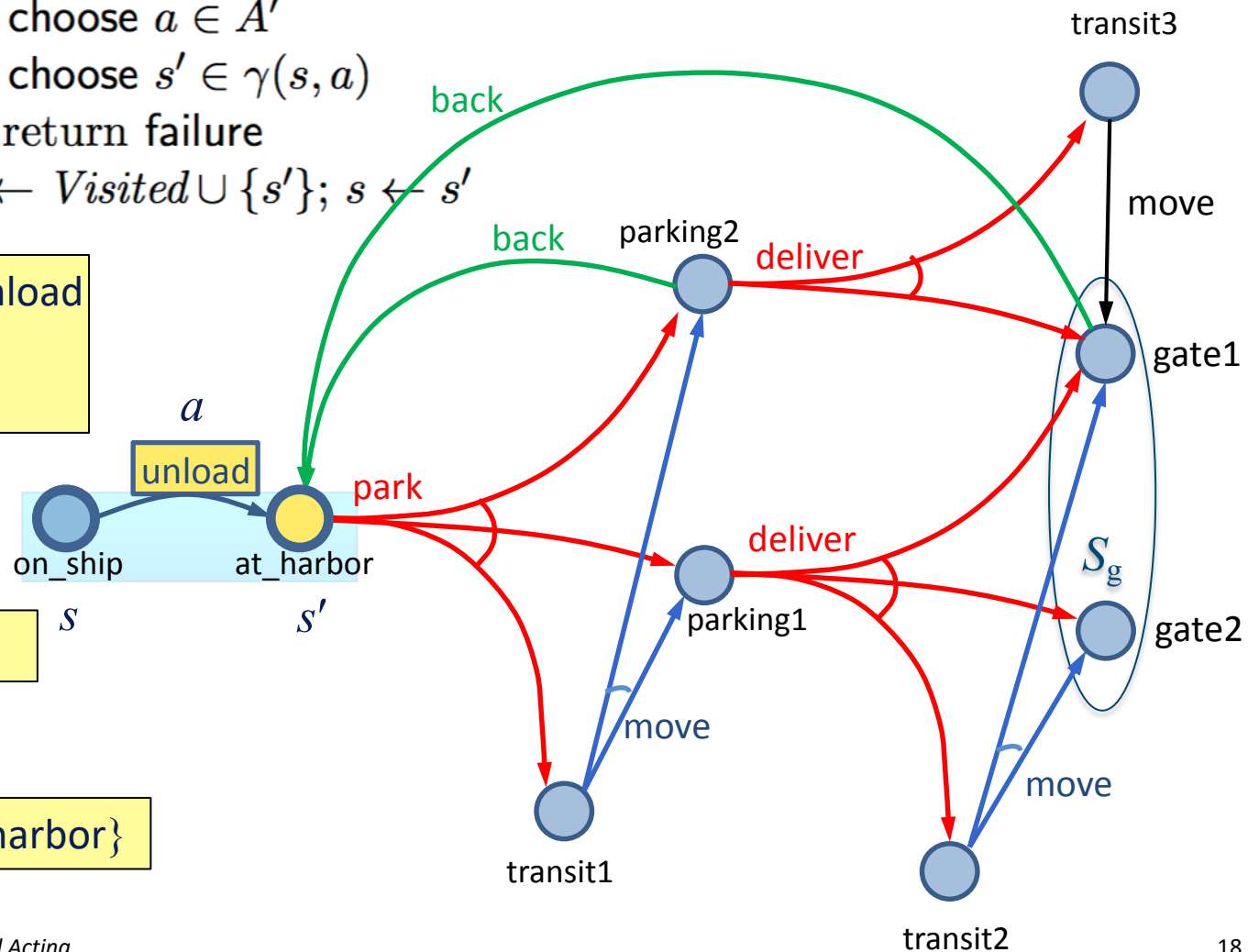
$\pi(s) \leftarrow a$ ;  $Visited \leftarrow Visited \cup \{s'\}$ ;  $s \leftarrow s'$

$s = \text{on\_ship}$ ,  $a = \text{unload}$   
 $\gamma(s, a) = \{\text{at\_harbor}\}$   
 $s' = \text{at\_harbor}$

$\pi = \{(\text{on\_ship}, \text{unload})\}$

$Visited = \{\text{on\_ship}, \text{at\_harbor}\}$

## Example



# Find-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset; s \leftarrow s_0; Visited \leftarrow \{s_0\}$

loop

if  $s \in S_g$  then return  $\pi$

$A' \leftarrow \text{Applicable}(s)$

if  $A' = \emptyset$  then return failure

nondeterministically choose  $a \in A'$

nondeterministically choose  $s' \in \gamma(s, a)$

if  $s' \in Visited$  then return failure

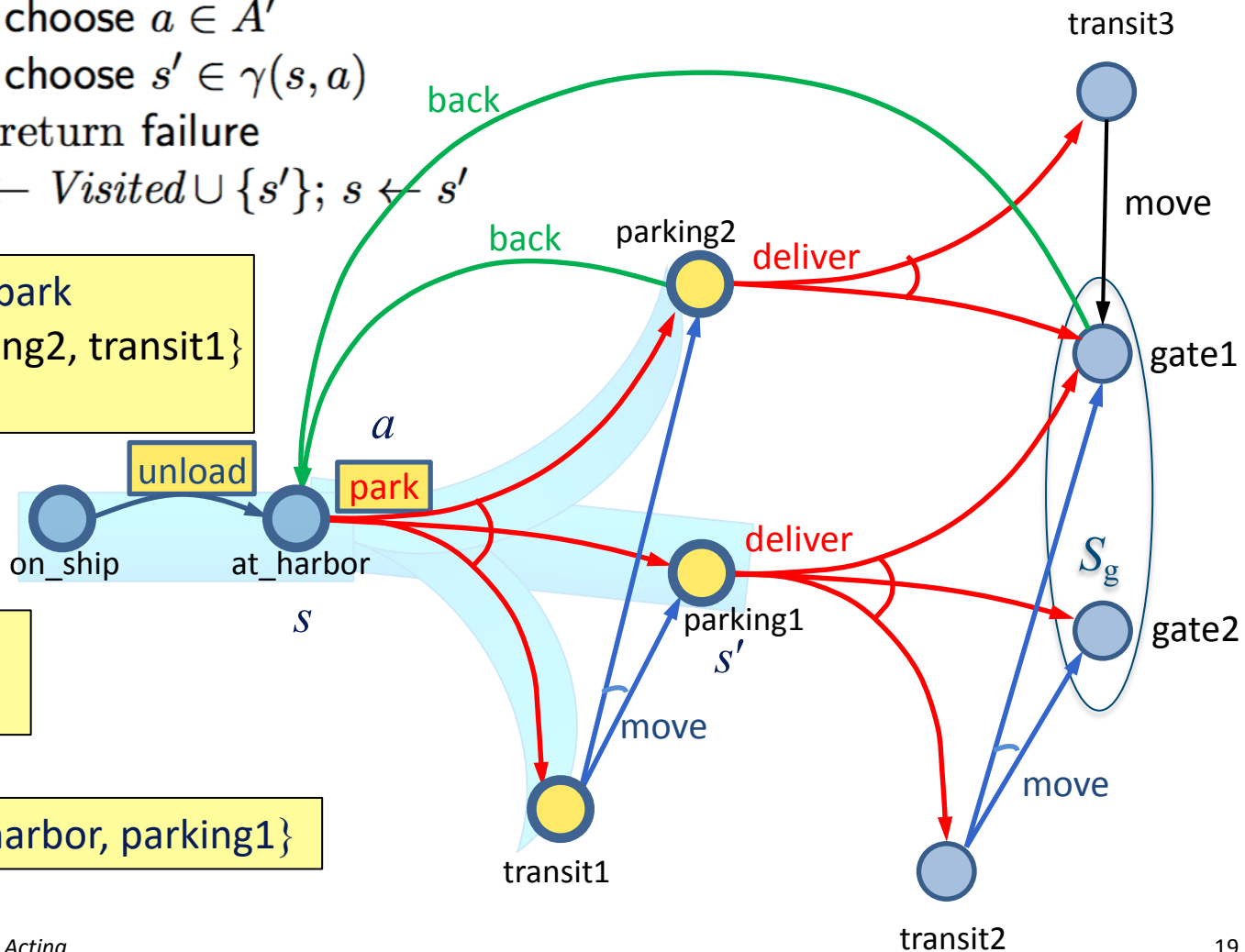
$\pi(s) \leftarrow a; Visited \leftarrow Visited \cup \{s'\}; s \leftarrow s'$

## Example

$s = \text{at\_harbor}, a = \text{park}$   
 $\gamma(s, a) = \{\text{parking1}, \text{parking2}, \text{transit1}\}$   
 $s' = \text{parking1}$

$\pi = \{(\text{on\_ship}, \text{unload}),$   
 $(\text{at\_harbor}, \text{park})\}$

$Visited = \{\text{on\_ship}, \text{at\_harbor}, \text{parking1}\}$



# Find-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset; s \leftarrow s_0; Visited \leftarrow \{s_0\}$

loop

if  $s \in S_g$  then return  $\pi$

$A' \leftarrow \text{Applicable}(s)$

if  $A' = \emptyset$  then return failure

nondeterministically choose  $a \in A'$

nondeterministically choose  $s' \in \gamma(s, a)$

if  $s' \in Visited$  then return failure

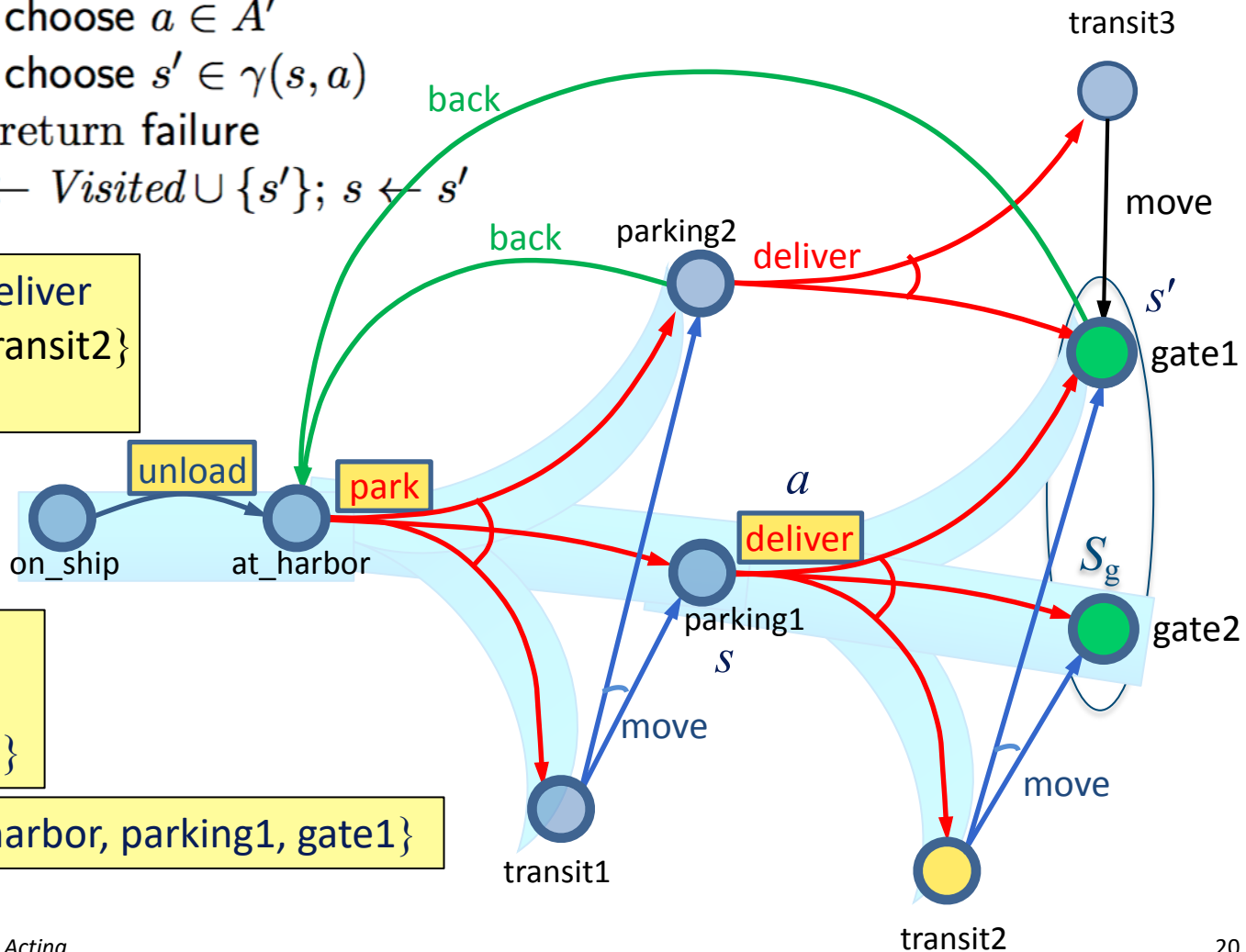
$\pi(s) \leftarrow a; Visited \leftarrow Visited \cup \{s'\}; s \leftarrow s'$

## Example

$s = \text{parking1}, a = \text{deliver}$   
 $\gamma(s, a) = \{\text{gate1}, \text{gate2}, \text{transit2}\}$   
 $s' = \text{gate1}$

$\pi = \{(\text{on\_ship}, \text{unload}),$   
 $(\text{at\_harbor}, \text{park}),$   
 $(\text{parking1}, \text{deliver})\}$

$Visited = \{\text{on\_ship}, \text{at\_harbor}, \text{parking1}, \text{gate1}\}$



# Find-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$ ;  $s \leftarrow s_0$ ;  $Visited \leftarrow \{s_0\}$

loop

if  $s \in S_g$  then return  $\pi$

$A' \leftarrow \text{Applicable}(s)$

if  $A' = \emptyset$  then return failure

nondeterministically choose  $a \in A'$

nondeterministically choose  $s' \in \gamma(s, a)$

if  $s' \in Visited$  then return failure

$\pi(s) \leftarrow a$ ;  $Visited \leftarrow Visited \cup \{s'\}$ ;  $s \leftarrow s'$

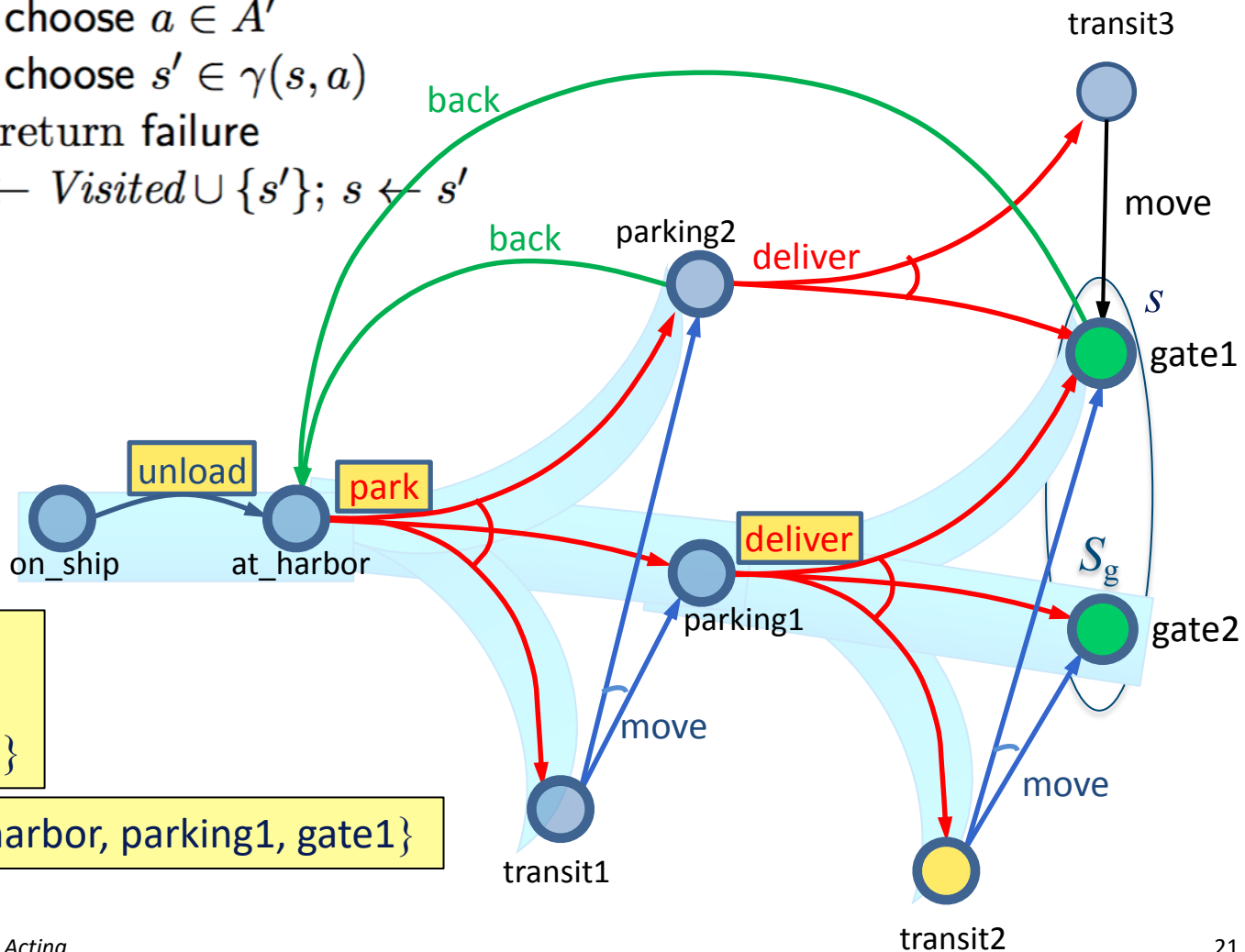
## Example

$s = \text{gate1}$

gate1 is a goal,  
so return  $\pi$

$\pi = \{(\text{on\_ship}, \text{unload}),$   
 $(\text{at\_harbor}, \text{park}),$   
 $(\text{parking1}, \text{deliver})\}$

$Visited = \{\text{on\_ship}, \text{at\_harbor}, \text{parking1}, \text{gate1}\}$



# Finding Acyclic Safe Solutions

Find-Acyclic-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

if  $Applicable(s) = \emptyset$  then return failure

nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if  $has-loops(\pi, a, Frontier)$  then return failure

return  $\pi$

*Check for cycles:*

For each  $s' \in \gamma(s, a) \cap Dom(\pi)$ , is  $s \in \hat{\gamma}(s', \pi)$ ?

# Find-Acyclic-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

    if  $Applicable(s) = \emptyset$  then return failure

    nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

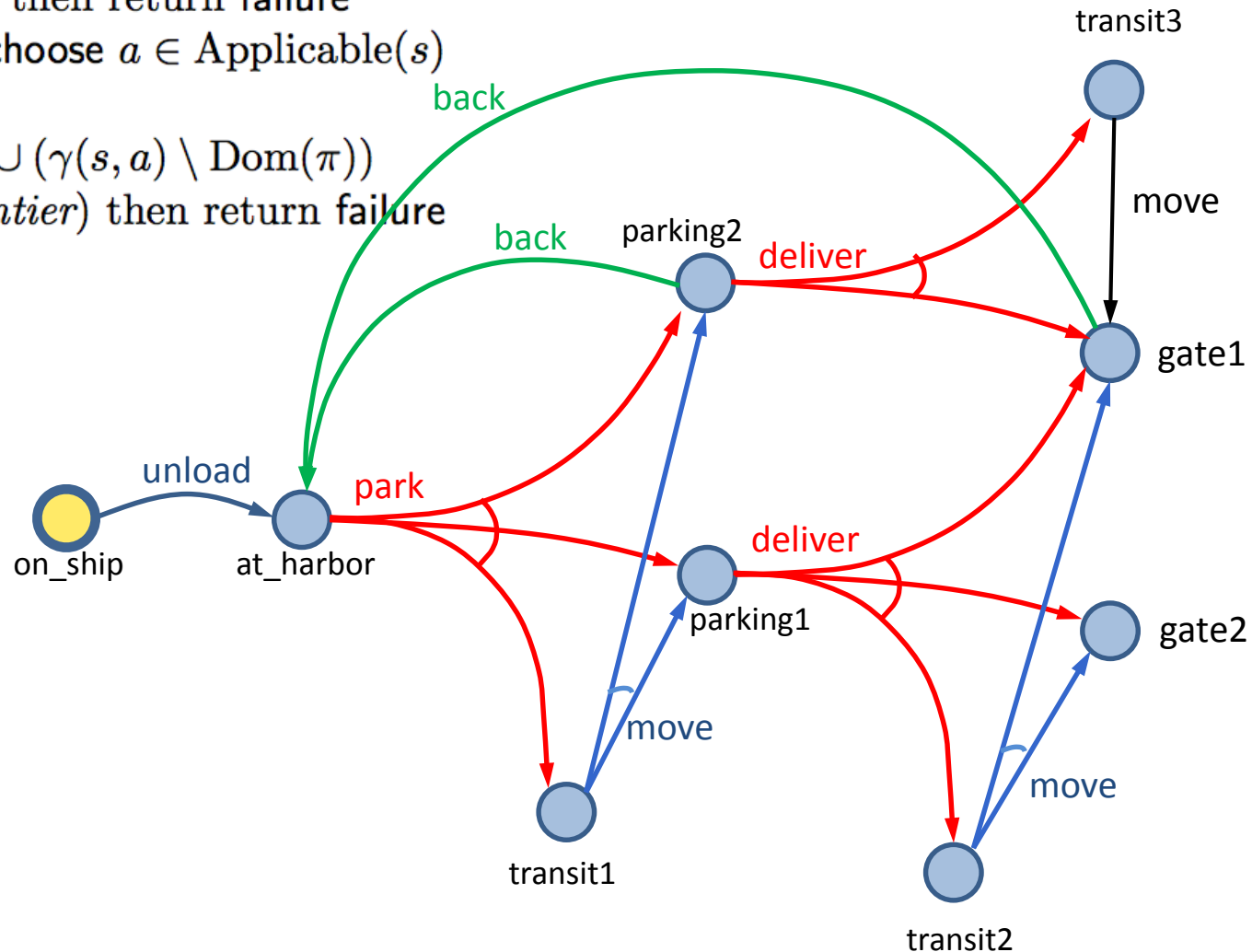
    if  $has-loops(\pi, a, Frontier)$  then return failure

return  $\pi$

# Example

$Frontier \setminus S_g = \{on\_ship\}$

$\pi = \{\}$



# Find-Acyclic-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

    if  $Applicable(s) = \emptyset$  then return failure

    nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

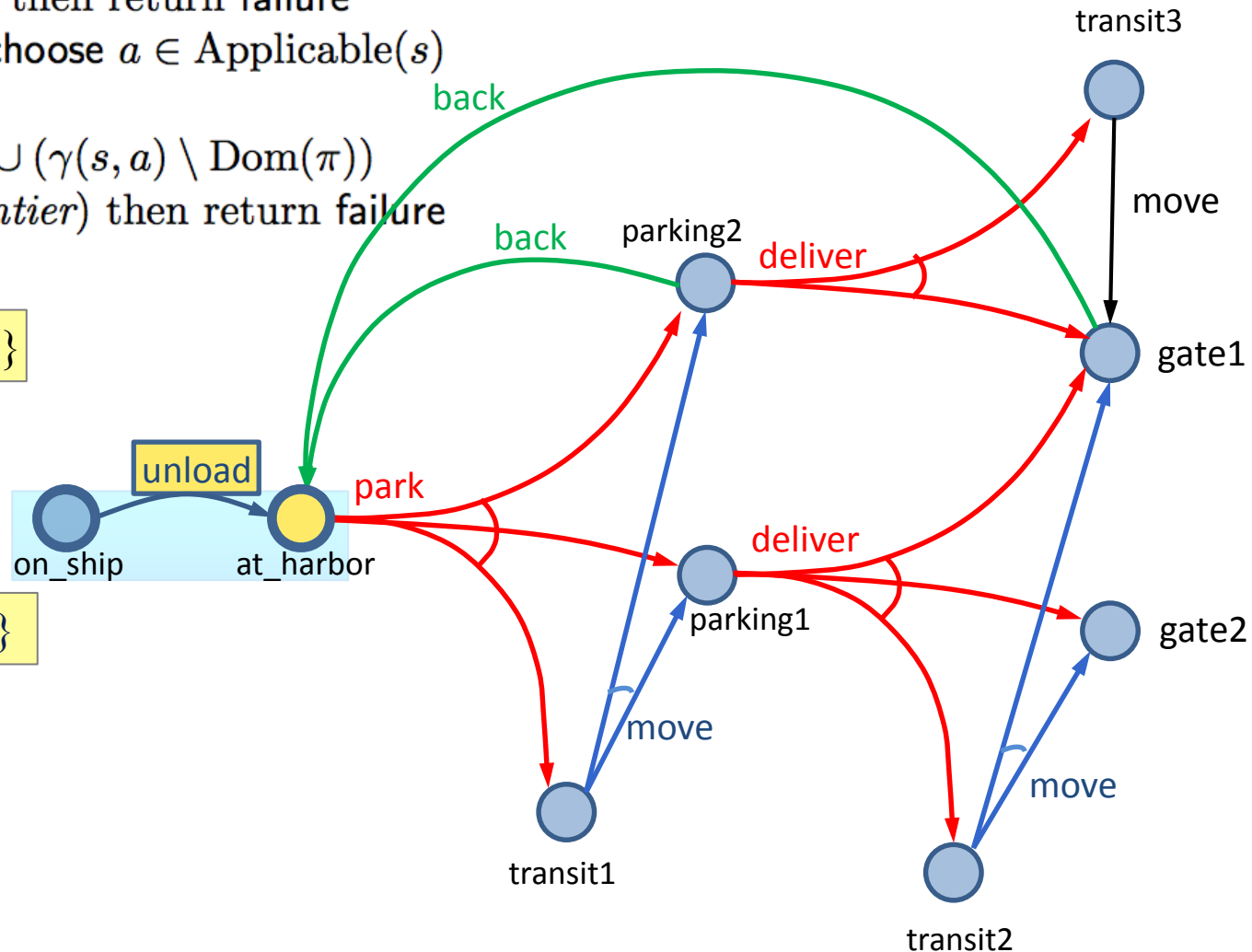
    if  $has-loops(\pi, a, Frontier)$  then return failure

return  $\pi$

# Example

$Frontier \setminus S_g = \{at\_harbor\}$

$\pi = \{(on\_ship, unload)\}$





# Find-Acyclic-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

    if  $Applicable(s) = \emptyset$  then return failure

    nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

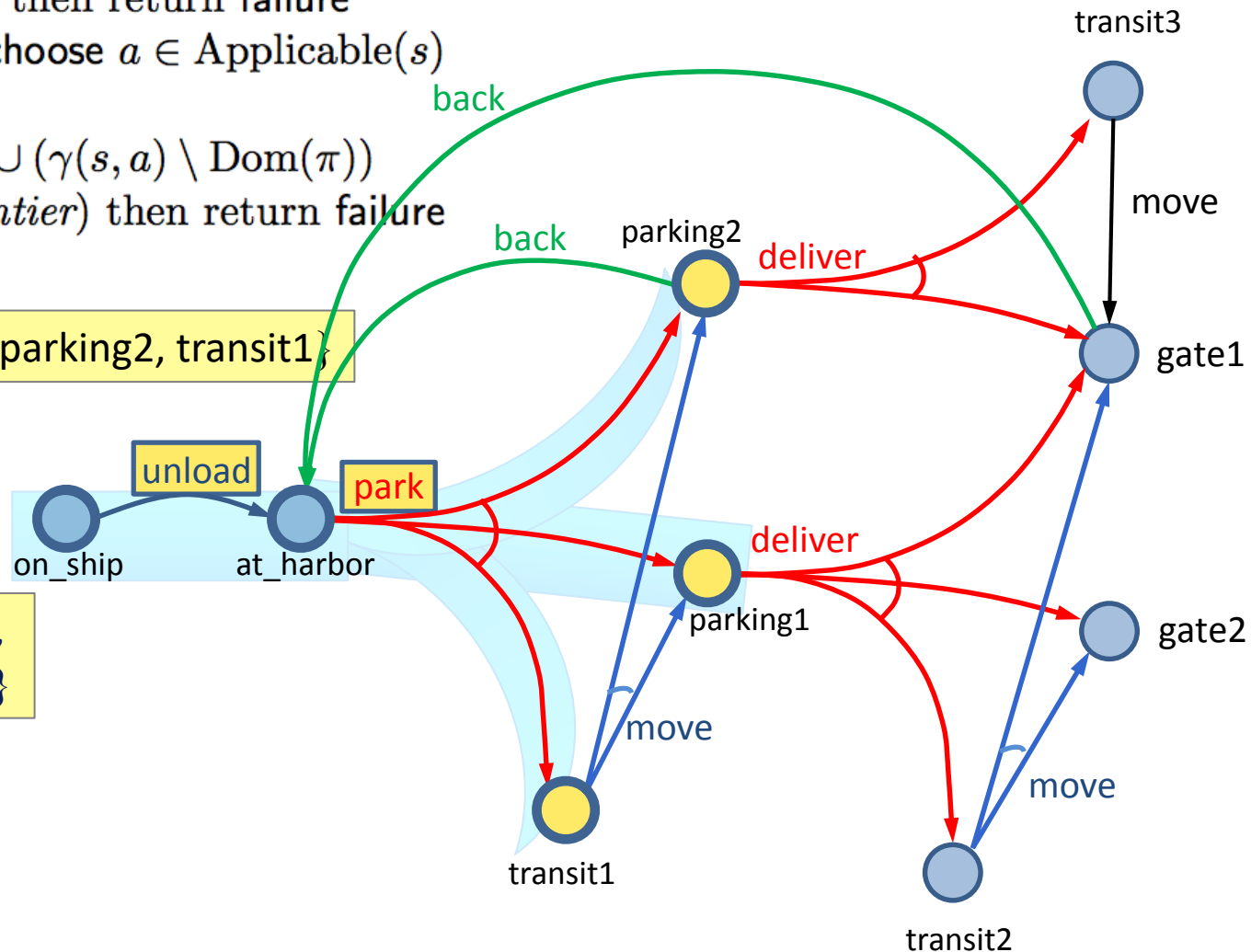
    if  $has-loops(\pi, a, Frontier)$  then return failure

return  $\pi$

# Example

$Frontier \setminus S_g = \{\text{parking1, parking2, transit1}\}$

$\pi = \{(\text{on\_ship}, \text{unload}),$   
 $(\text{at\_harbor}, \text{park})\}$



# Find-Acyclic-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

    if  $Applicable(s) = \emptyset$  then return failure

    nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

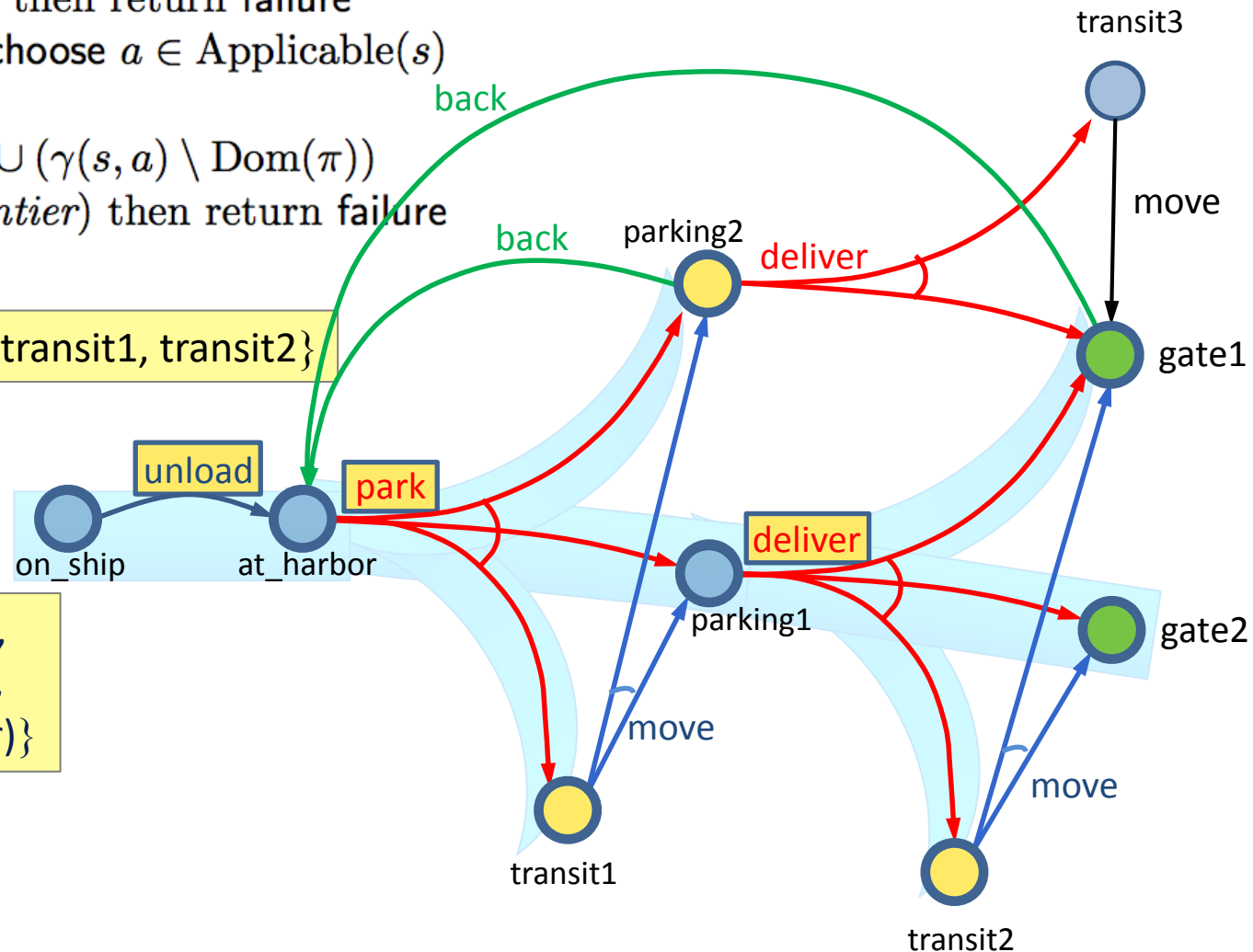
    if  $has-loops(\pi, a, Frontier)$  then return failure

return  $\pi$

# Example

$Frontier \setminus S_g = \{\text{parking2}, \text{transit1}, \text{transit2}\}$

$\pi = \{(\text{on\_ship}, \text{unload}),$   
 $(\text{at\_harbor}, \text{park}),$   
 $(\text{parking1}, \text{deliver})\}$



# Find-Acyclic-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

if  $Applicable(s) = \emptyset$  then return failure

nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if  $has-loops(\pi, a, Frontier)$  then return failure

return  $\pi$

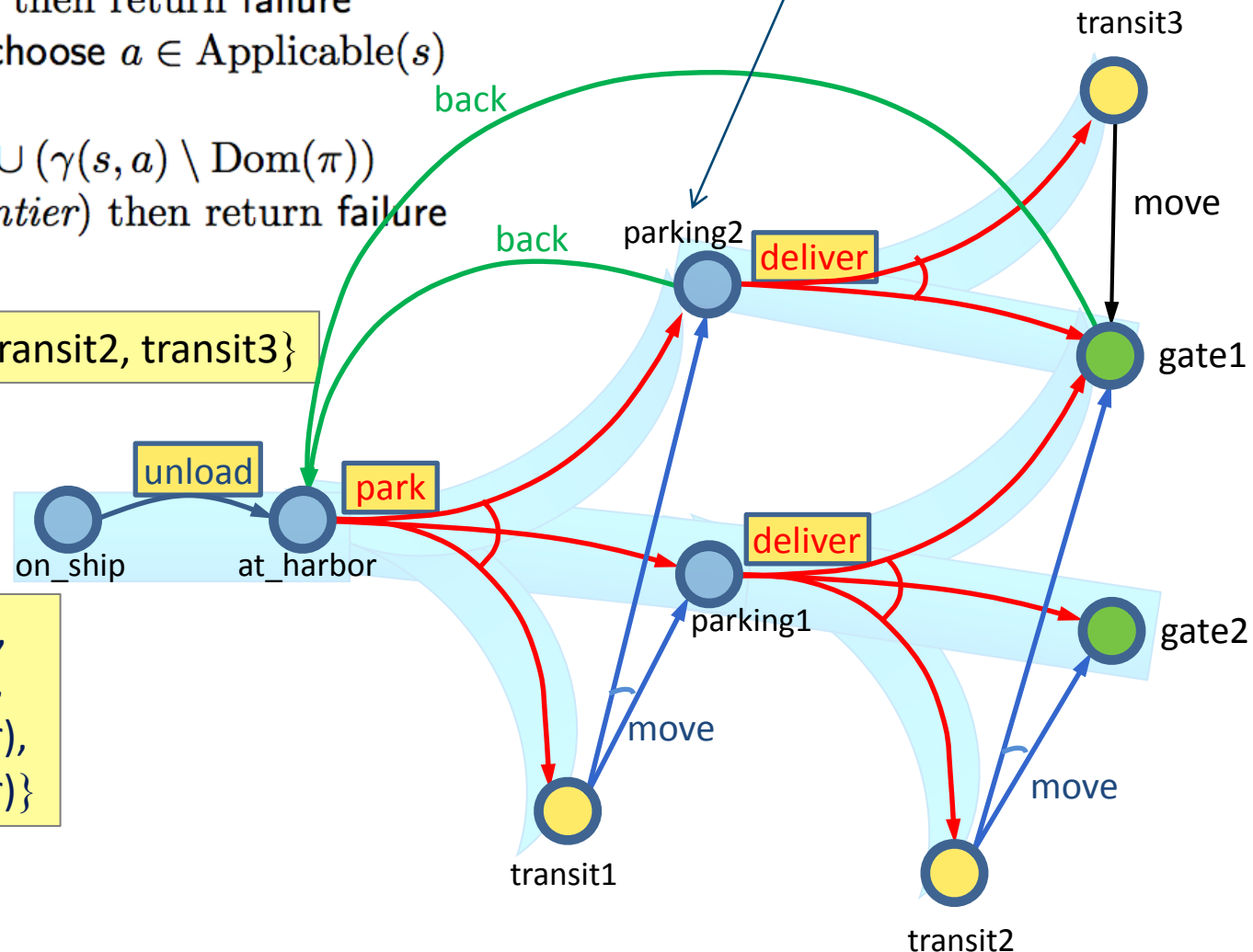
## Example

nondeterministically choose back or deliver

- back  $\Rightarrow$  cycle, so return failure
- deliver  $\Rightarrow$  no cycle, so continue

$Frontier \setminus S_g = \{transit1, transit2, transit3\}$

$\pi = \{(on\_ship, unload),$   
 $(at\_harbor, park),$   
 $(parking1, deliver),$   
 $(parking2, deliver)\}$



# Find-Acyclic-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

    if  $Applicable(s) = \emptyset$  then return failure

    nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

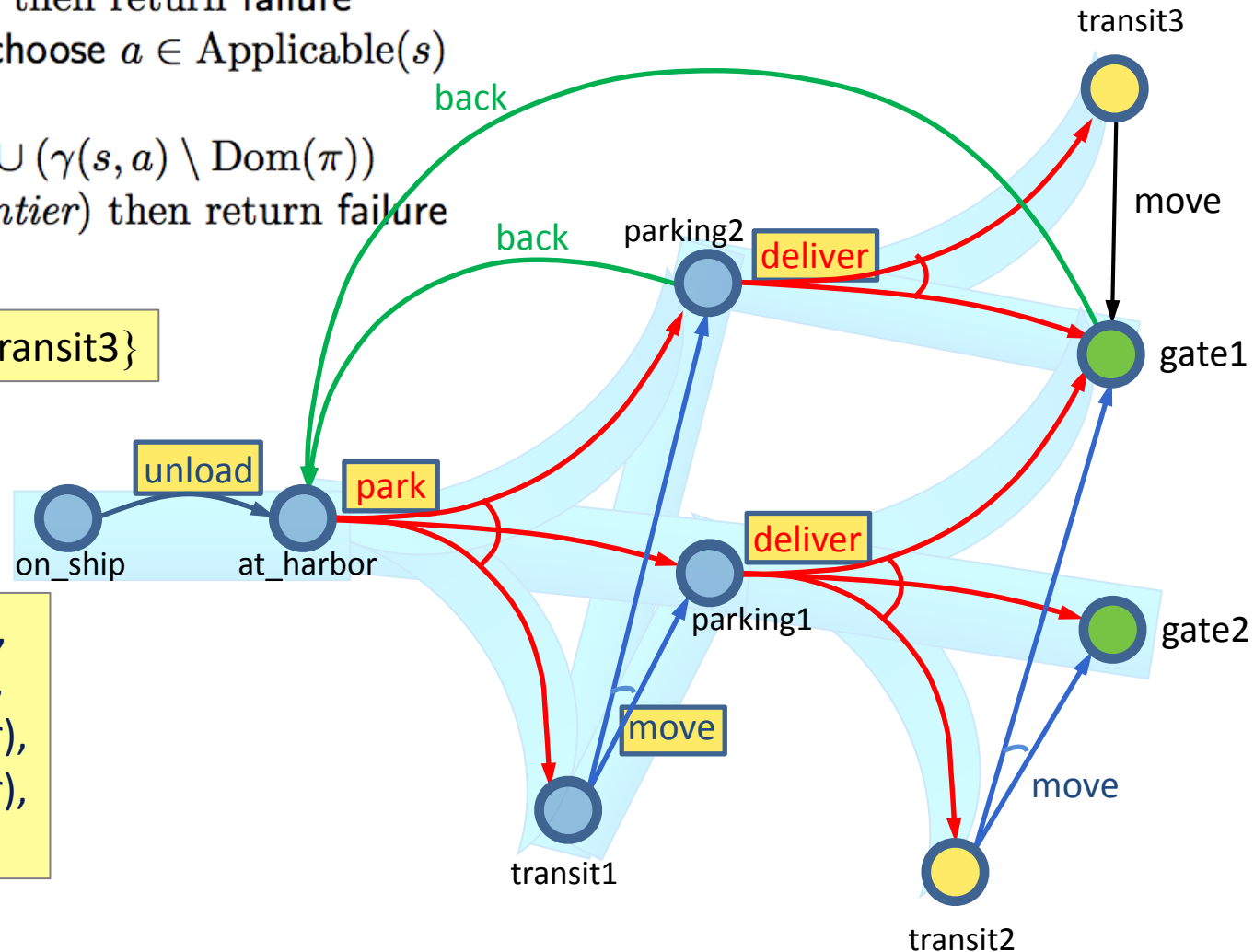
    if  $has-loops(\pi, a, Frontier)$  then return failure

return  $\pi$

# Example

$Frontier \setminus S_g = \{\text{transit2}, \text{transit3}\}$

$\pi = \{(\text{on\_ship}, \text{unload}),$   
 $(\text{at\_harbor}, \text{park}),$   
 $(\text{parking1}, \text{deliver}),$   
 $(\text{parking2}, \text{deliver}),$   
 $(\text{transit1}, \text{move})\}$



# Find-Acyclic-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

    if  $Applicable(s) = \emptyset$  then return failure

    nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

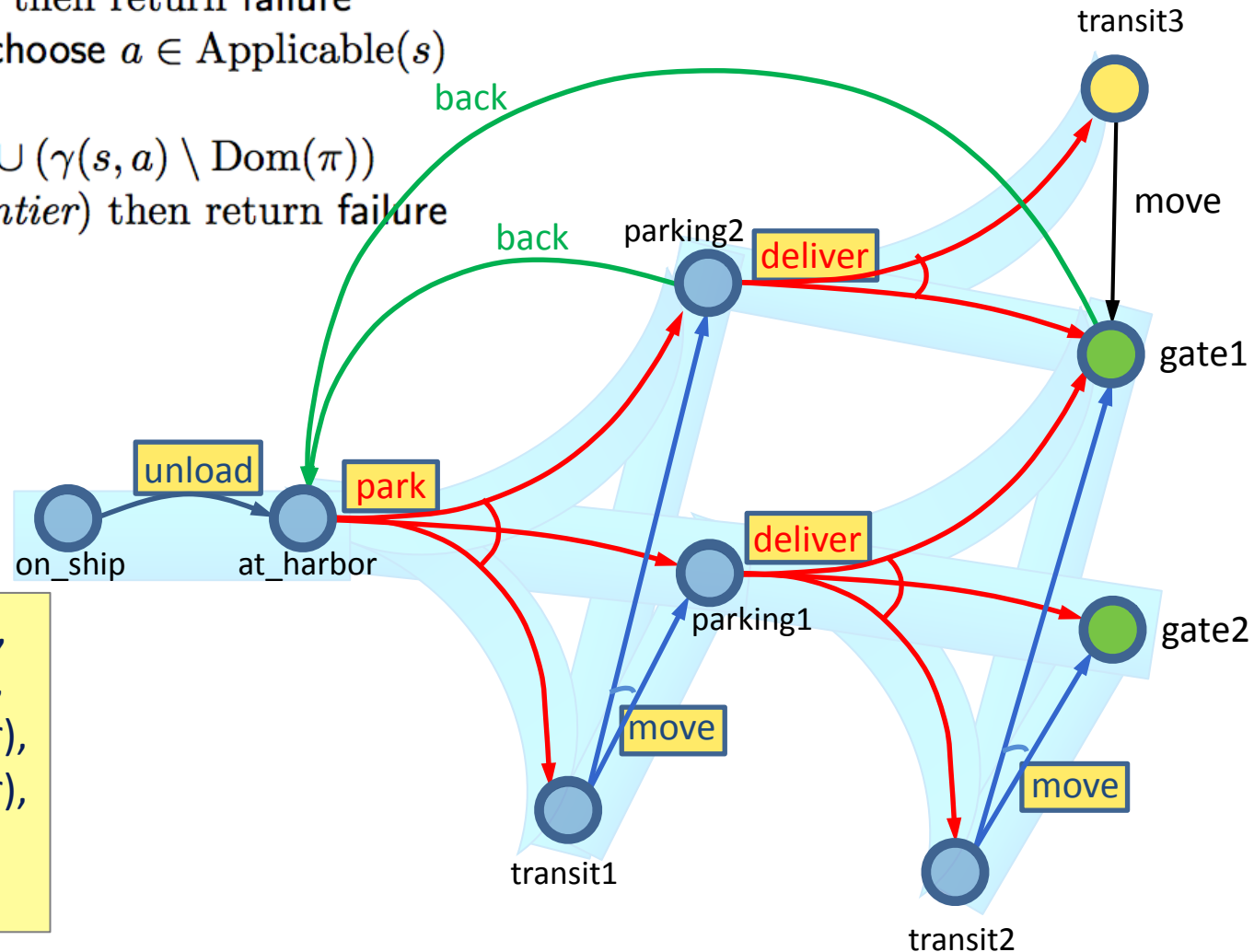
    if  $has-loops(\pi, a, Frontier)$  then return failure

return  $\pi$

# Example

$Frontier \setminus S_g = \{transit3\}$

$\pi = \{(on\_ship, unload),$   
 $(at\_harbor, park),$   
 $(parking1, deliver),$   
 $(parking2, deliver),$   
 $(transit1, move),$   
 $(transit2, move)\}$



# Find-Acyclic-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

    if  $Applicable(s) = \emptyset$  then return failure

    nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

    if  $has-loops(\pi, a, Frontier)$  then return failure

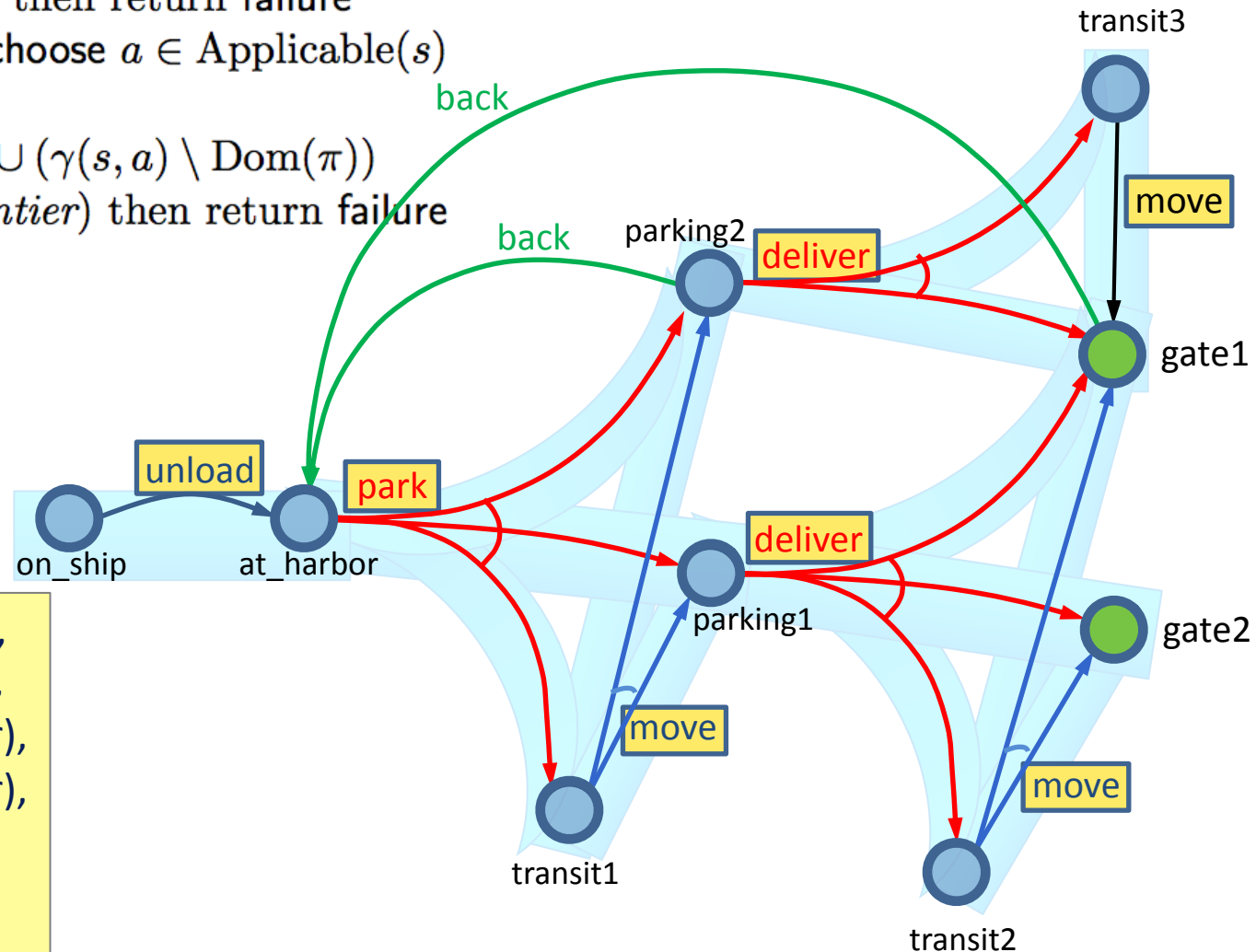
return  $\pi$

# Example

$Frontier \setminus S_g = \emptyset$

Found a solution

$\pi = \{(on\_ship, unload),$   
 $(at\_harbor, park),$   
 $(parking1, deliver),$   
 $(parking2, deliver),$   
 $(transit1, move),$   
 $(transit2, move),$   
 $(transit3, move)\}$



# Find-Safe-Solution

Find-Safe-Solution  $(\Sigma, s_0, S_g)$

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

*Keep track of unexpanded states, like  $A^*$*

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

if  $Applicable(s) = \emptyset$  then return failure

nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

*Add all outcomes that  $\pi$  doesn't already handle*

if  $has\_unsafe\_loops(\pi, a, Frontier)$  then return failure

return  $\pi$

- Same as Find-Acyclic-Solution except for one difference:
- has-unsafe-loops instead of has-loops
  - Check whether  $\pi$  contains any cycles that can't be escaped:
  - For each  $s' \in \gamma(s, a) \cap Dom(\pi)$ , is  $\hat{\gamma}(s', \pi) \cap Frontier = \emptyset$ ?

# Example

Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

if  $Applicable(s) = \emptyset$  then return failure

nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

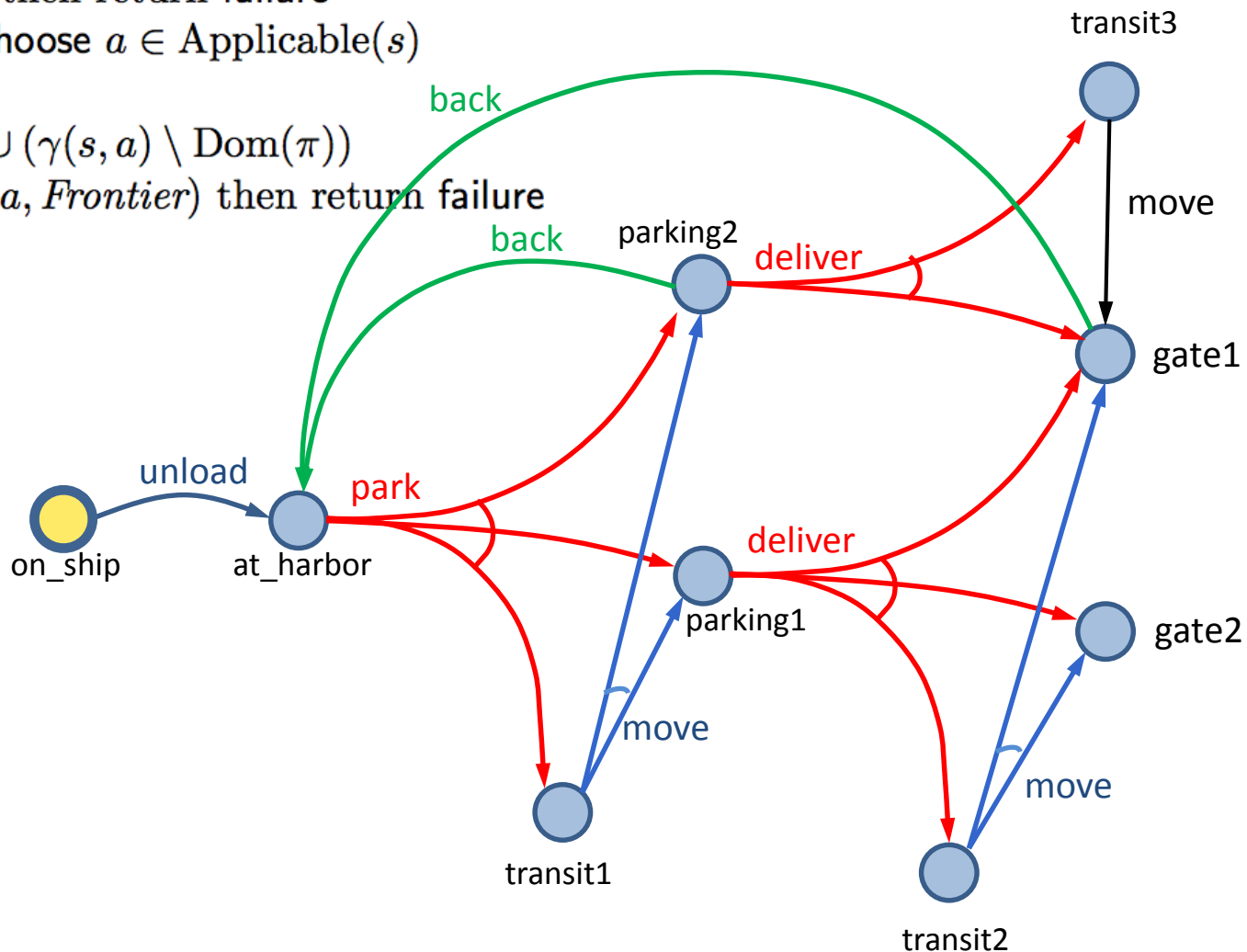
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if  $has\_unsafe\_loops(\pi, a, Frontier)$  then return failure

return  $\pi$

$Frontier \setminus S_g = \{on\_ship\}$

$\pi = \{\}$





# Example

Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

if  $Applicable(s) = \emptyset$  then return failure

nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

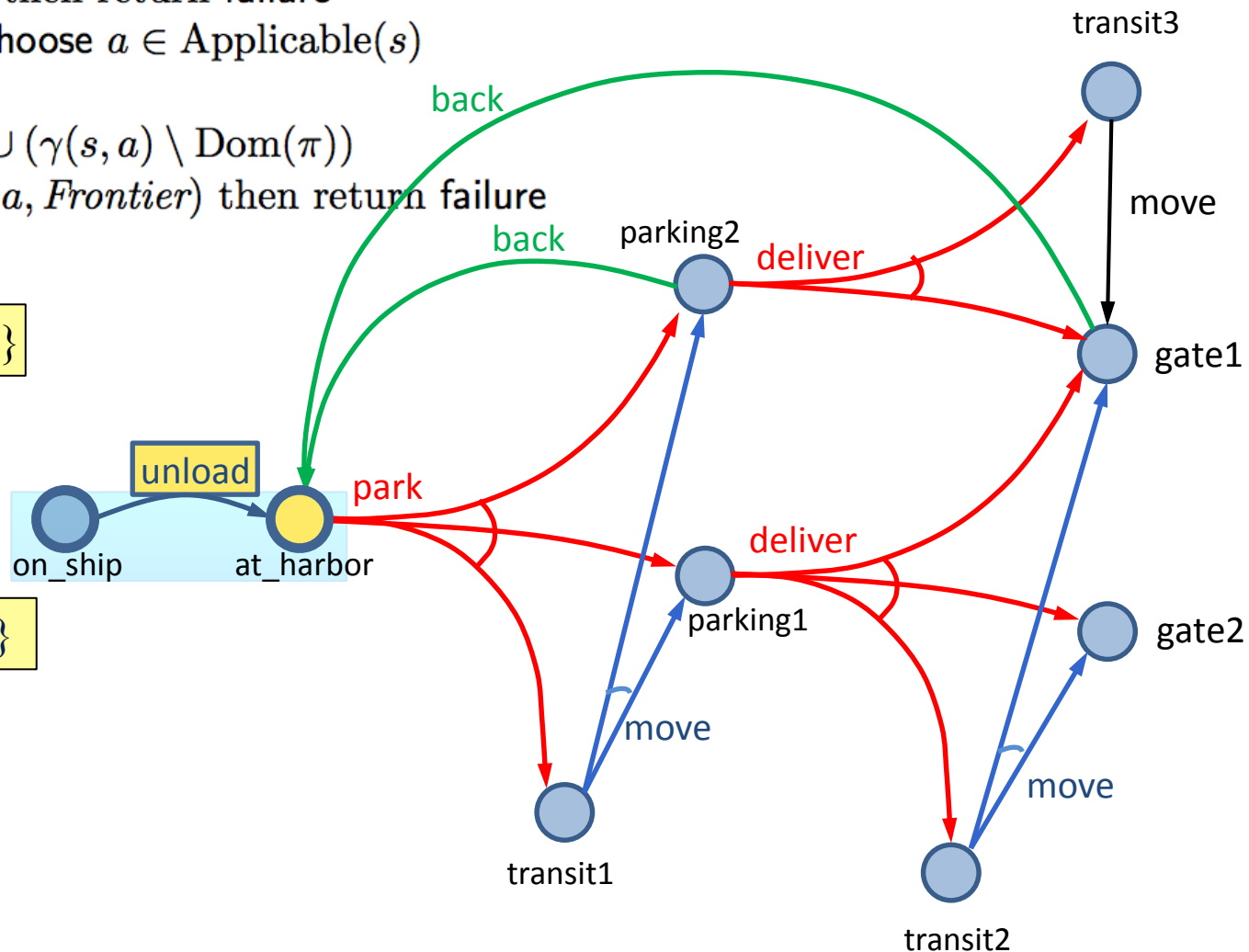
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if  $has\_unsafe\_loops(\pi, a, Frontier)$  then return failure

return  $\pi$

$Frontier \setminus S_g = \{at\_harbor\}$

$\pi = \{(on\_ship, unload)\}$



# Example

Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

if  $Applicable(s) = \emptyset$  then return failure

nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

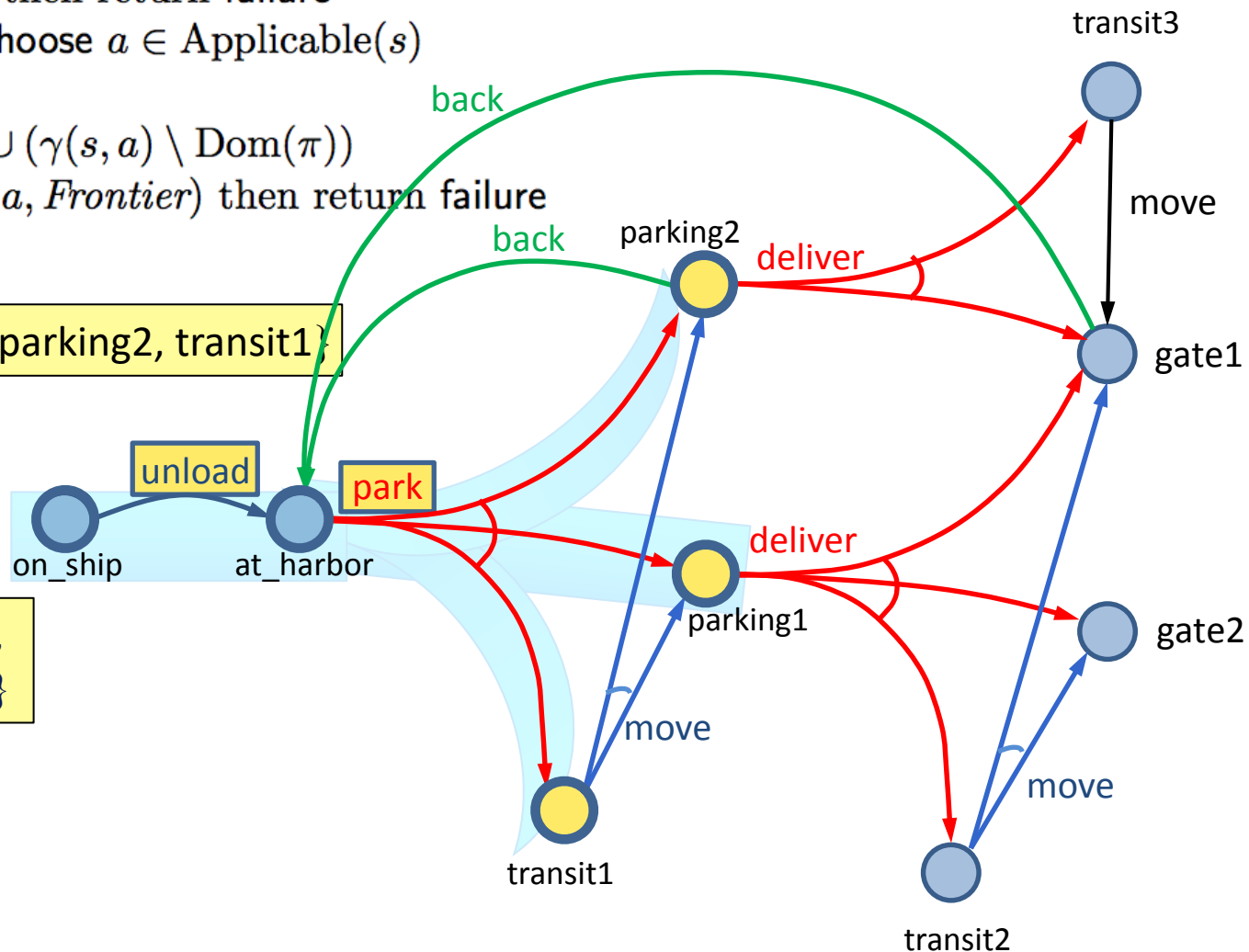
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if  $has\_unsafe\_loops(\pi, a, Frontier)$  then return failure

return  $\pi$

$Frontier \setminus S_g = \{parking1, parking2, transit1\}$

$\pi = \{(on\_ship, unload), (at\_harbor, park)\}$



# Example

Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

if  $Applicable(s) = \emptyset$  then return failure

nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

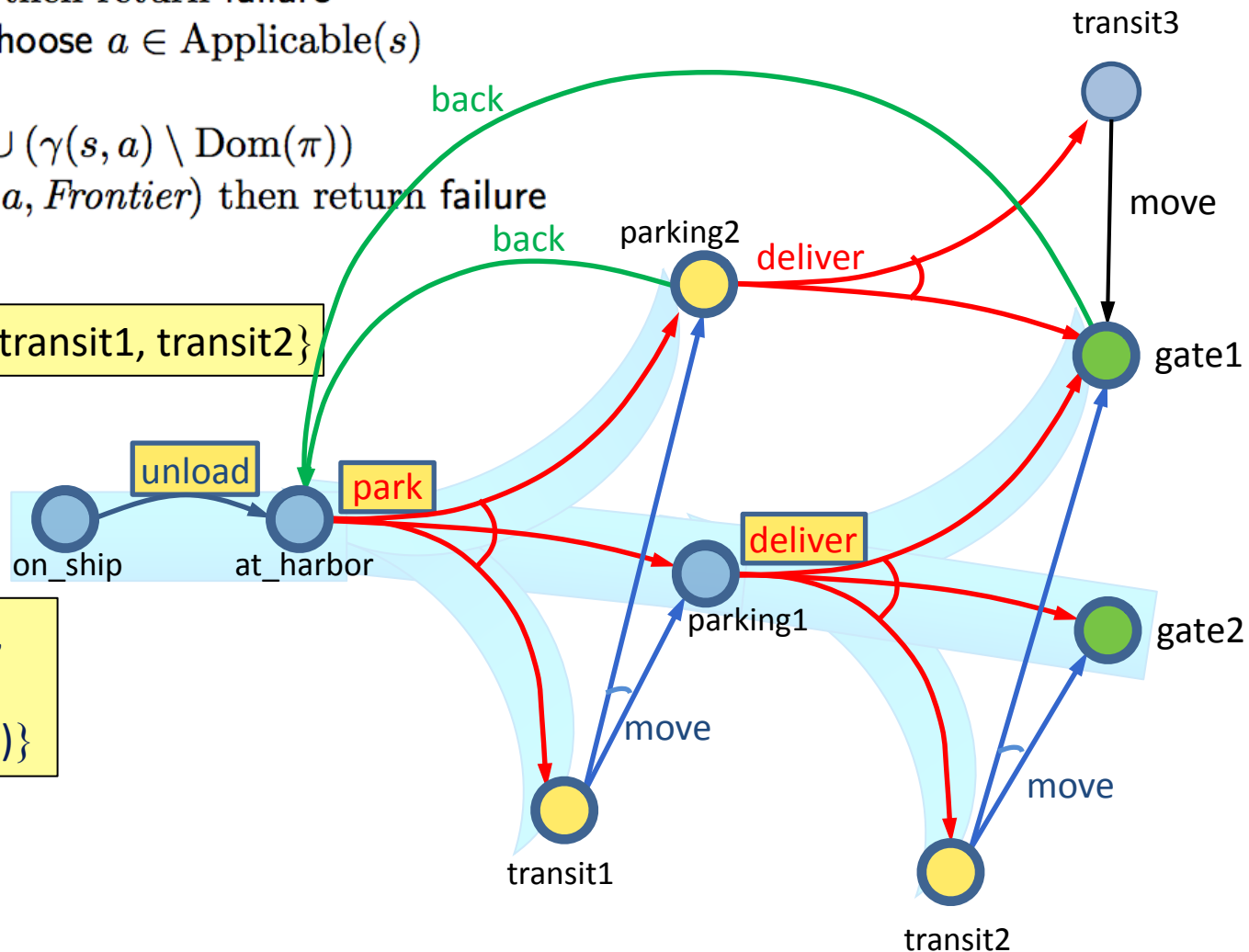
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if  $has\_unsafe\_loops(\pi, a, Frontier)$  then return failure

return  $\pi$

$Frontier \setminus S_g = \{parking2, transit1, transit2\}$

$\pi = \{(on\_ship, unload),$   
 $(at\_harbor, park),$   
 $(parking1, deliver)\}$



# Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

if  $Applicable(s) = \emptyset$  then return failure

nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if  $has\_unsafe\_loops(\pi, a, Frontier)$  then return failure

return  $\pi$

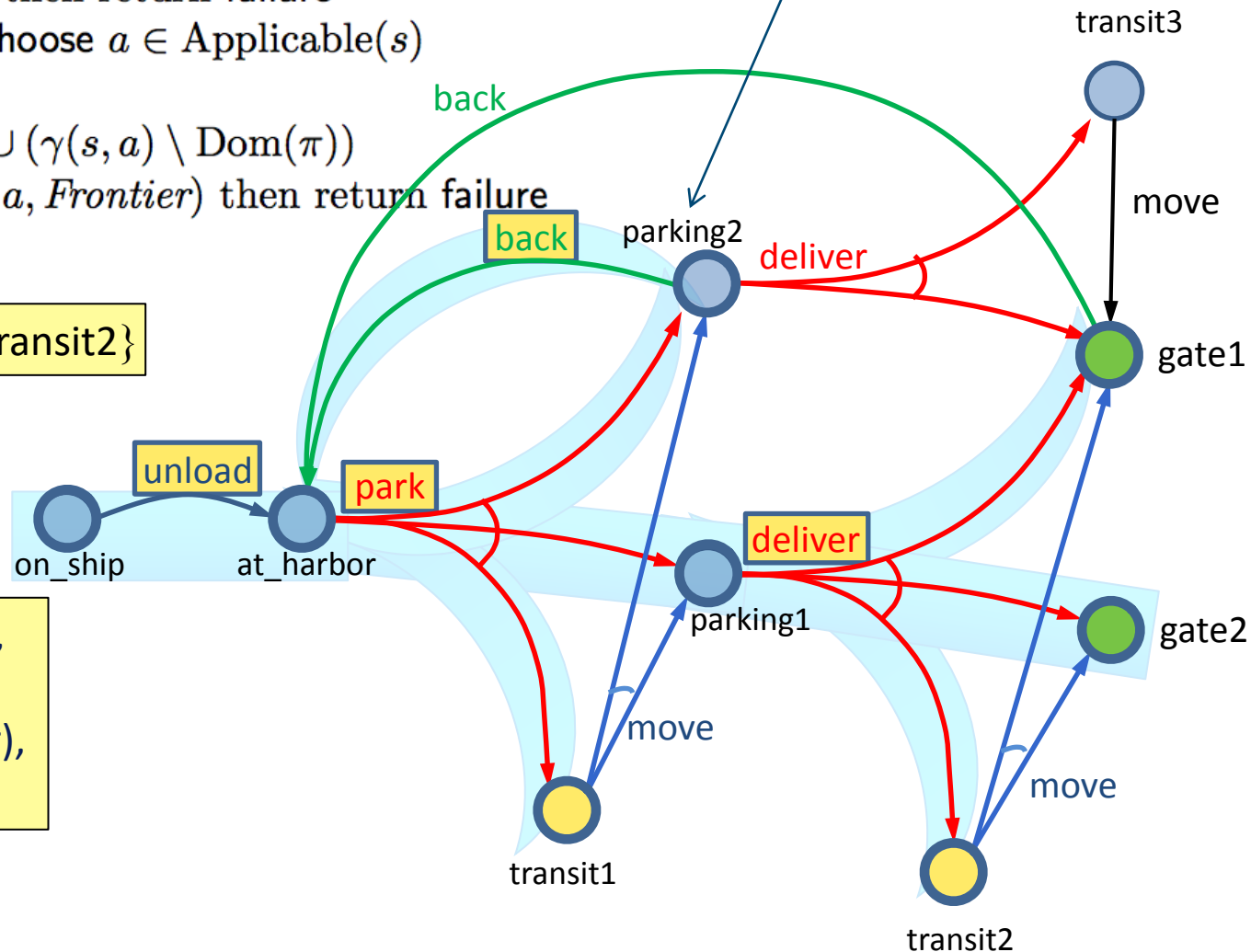
# Example

Nondeterministically choose back or deliver

- back is OK: escapable cycle

$Frontier \setminus S_g = \{transit1, transit2\}$

$\pi = \{(on\_ship, unload), (at\_harbor, park), (parking1, deliver), (parking2, back)\}$



# Example

Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

if  $Applicable(s) = \emptyset$  then return failure

nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

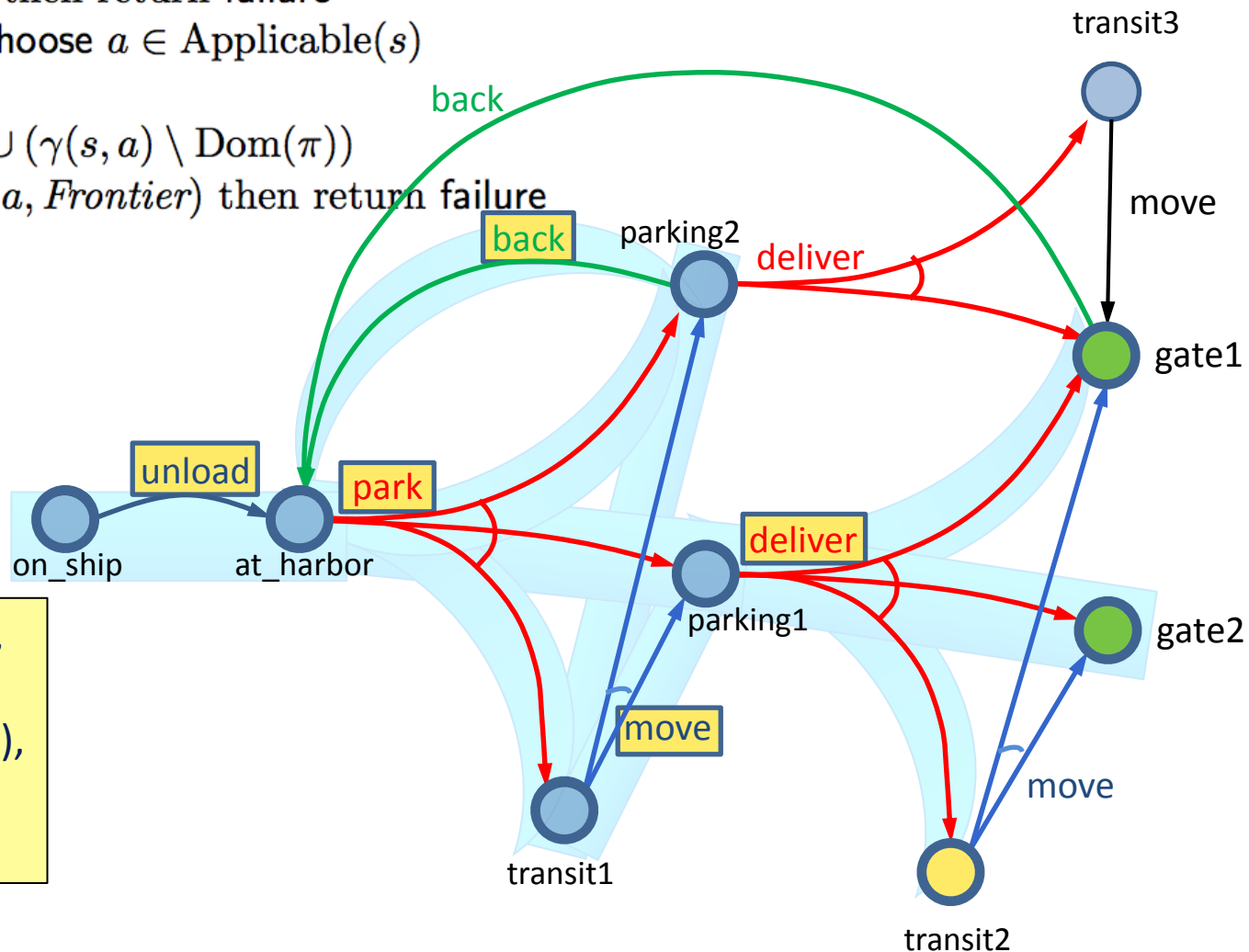
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if  $has\_unsafe\_loops(\pi, a, Frontier)$  then return failure

return  $\pi$

$Frontier \setminus S_g = \{transit2\}$

$\pi = \{(on\_ship, unload),$   
 $(at\_harbor, park),$   
 $(parking1, deliver),$   
 $(parking2, back),$   
 $(transit1, move)\}$



# Example

Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

if  $Applicable(s) = \emptyset$  then return failure

nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

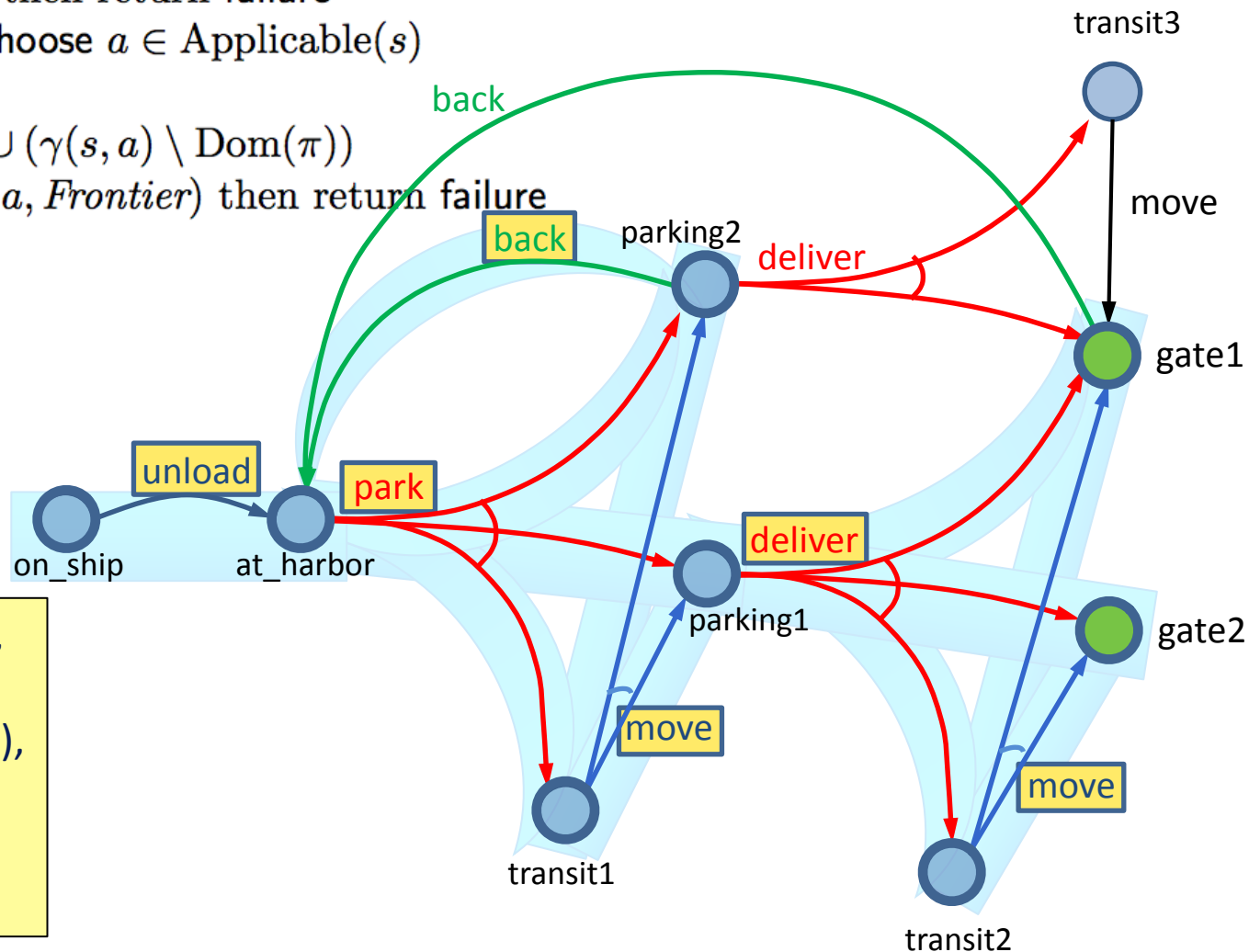
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if  $has\_unsafe\_loops(\pi, a, Frontier)$  then return failure

return  $\pi$

$Frontier \setminus S_g = \emptyset$

$\pi = \{(on\_ship, unload),$   
 $(at\_harbor, park),$   
 $(parking1, deliver),$   
 $(parking2, back),$   
 $(transit1, move),$   
 $(transit2, move)\}$



# Guided-Find-Safe-Solution

- Motivation:
  - Much easier to find solutions if they don't have to be safe
  - Find-Safe-Solution needs plans for all possible outcomes of actions
  - Find-Solution only needs a plan for one of them
- Idea:
  - loop
    - Find a solution  $\pi$
    - Look at each leaf node of  $\pi$ 
      - ▶ If the leaf node isn't a goal, find a solution and incorporate it into  $\pi$

# Guided-Find-Safe-Solution

Guided-Find-Safe-Solution  $(\Sigma, s_0, S_g)$

if  $s_0 \in S_g$  then return( $\emptyset$ )

if  $Applicable(s_0) = \emptyset$  then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if  $Q = \emptyset$  then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return( $\pi$ )

select arbitrarily  $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

if  $\pi' \neq failure$  then do

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else if  $s = s_0$  then return failure *(not in book)*

else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make  $a$  not applicable in  $s'$

$\pi$  is a solution. Return the part that's reachable from  $s_0$ .

Choose any leaf  $s$  that isn't a goal. Find a solution  $\pi'$  for  $s$ .

For each  $(s, a)$  in  $\pi'$ , add to  $\pi$  unless  $\pi$  already has an action at  $s$

$s$  is unsolvable. For each  $(s', a)$  that can produce  $s$ , modify  $\pi$  and  $\Sigma$  so we'll never use  $a$  at  $s'$



# Guided-Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

if  $s_0 \in S_g$  then return( $\emptyset$ )

if  $Applicable(s_0) = \emptyset$  then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if  $Q = \emptyset$  then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return( $\pi$ )

select arbitrarily  $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

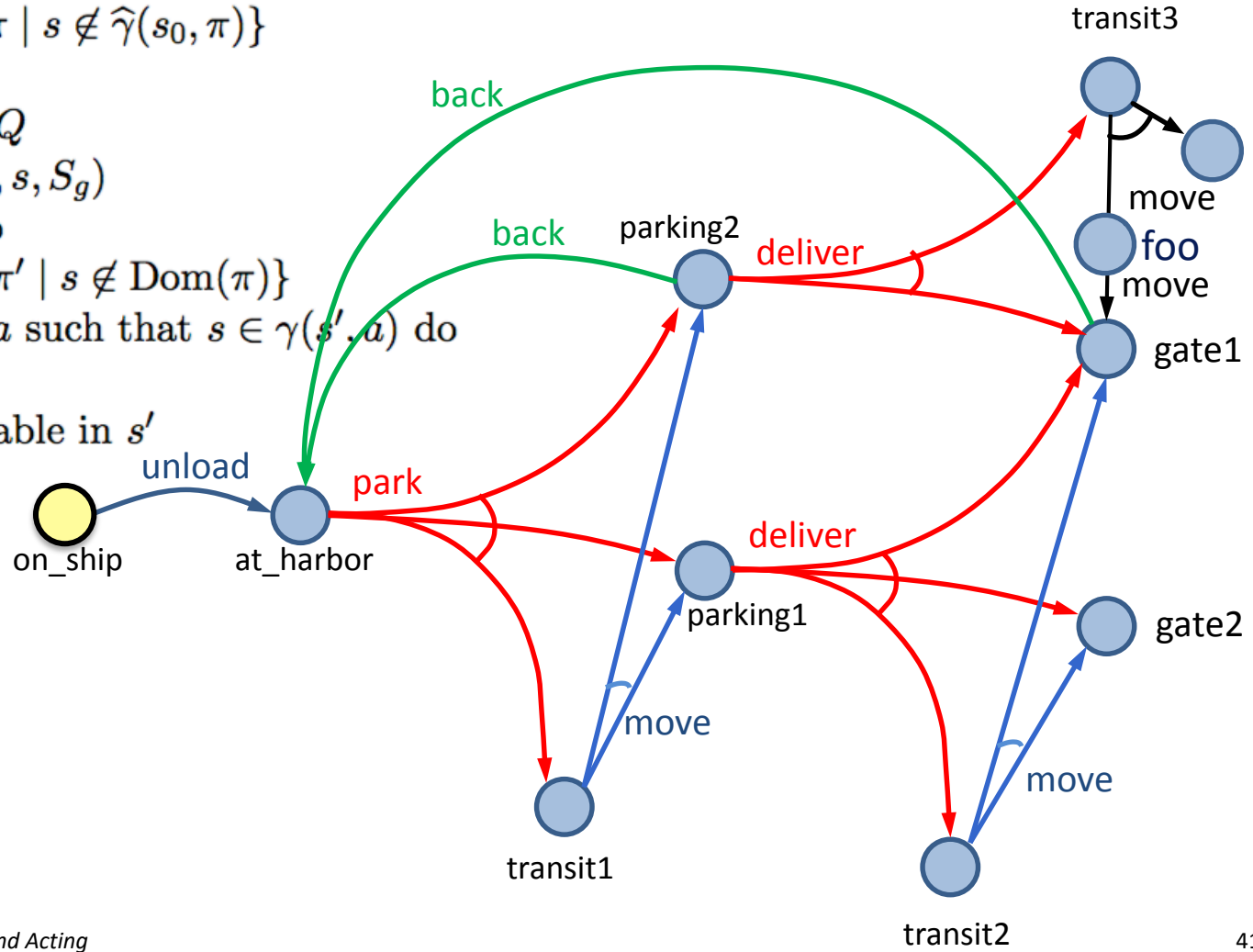
if  $\pi' \neq failure$  then do

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make  $a$  not applicable in  $s'$



## Example

# Guided-Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

if  $s_0 \in S_g$  then return( $\emptyset$ )  
if  $Applicable(s_0) = \emptyset$  then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if  $Q = \emptyset$  then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return( $\pi$ )

select arbitrarily  $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

if  $\pi' \neq failure$  then do

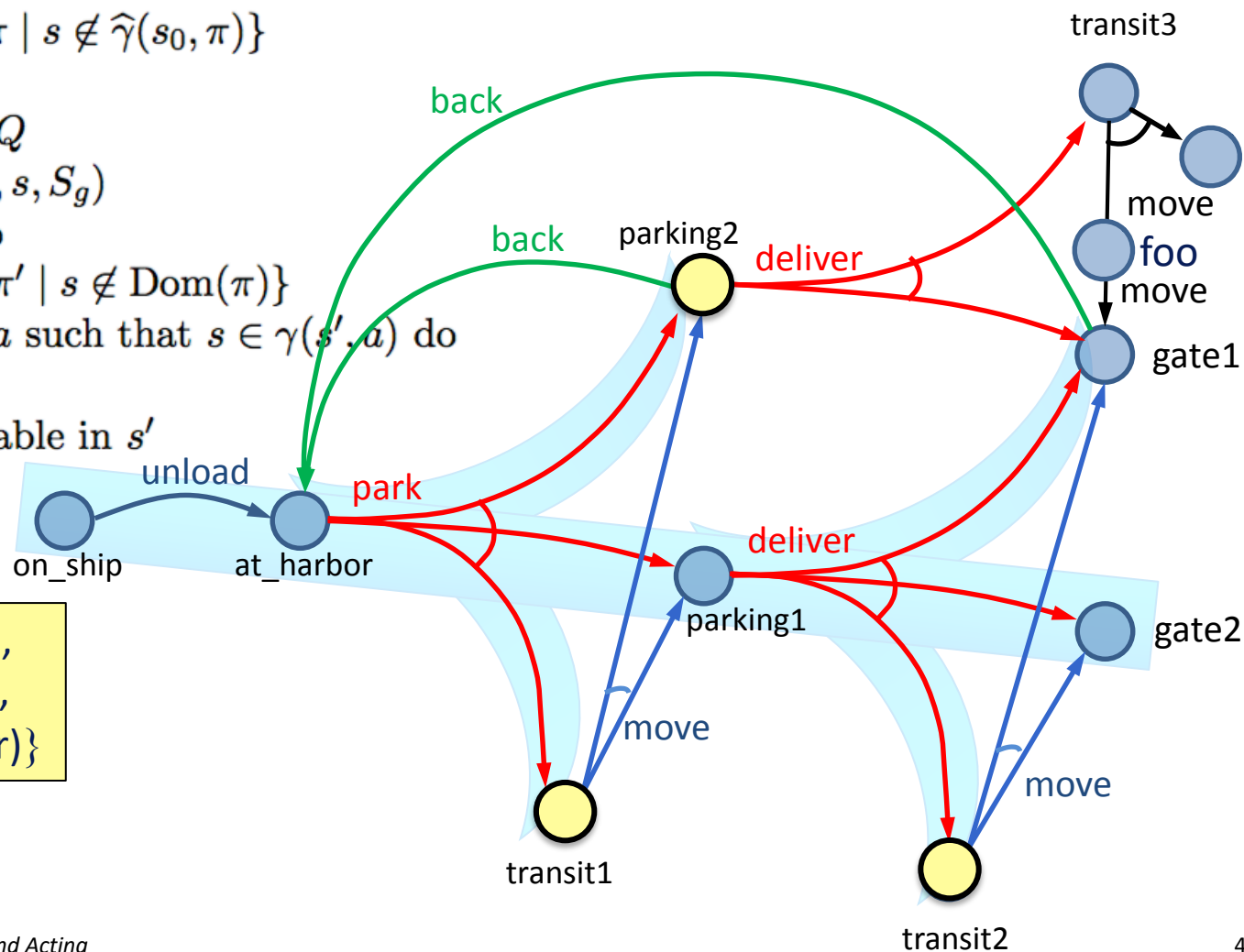
$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make  $a$  not applicable in  $s'$

## Example



# Guided-Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

if  $s_0 \in S_g$  then return( $\emptyset$ )  
if  $Applicable(s_0) = \emptyset$  then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if  $Q = \emptyset$  then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return( $\pi$ )

select arbitrarily  $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

if  $\pi' \neq failure$  then do

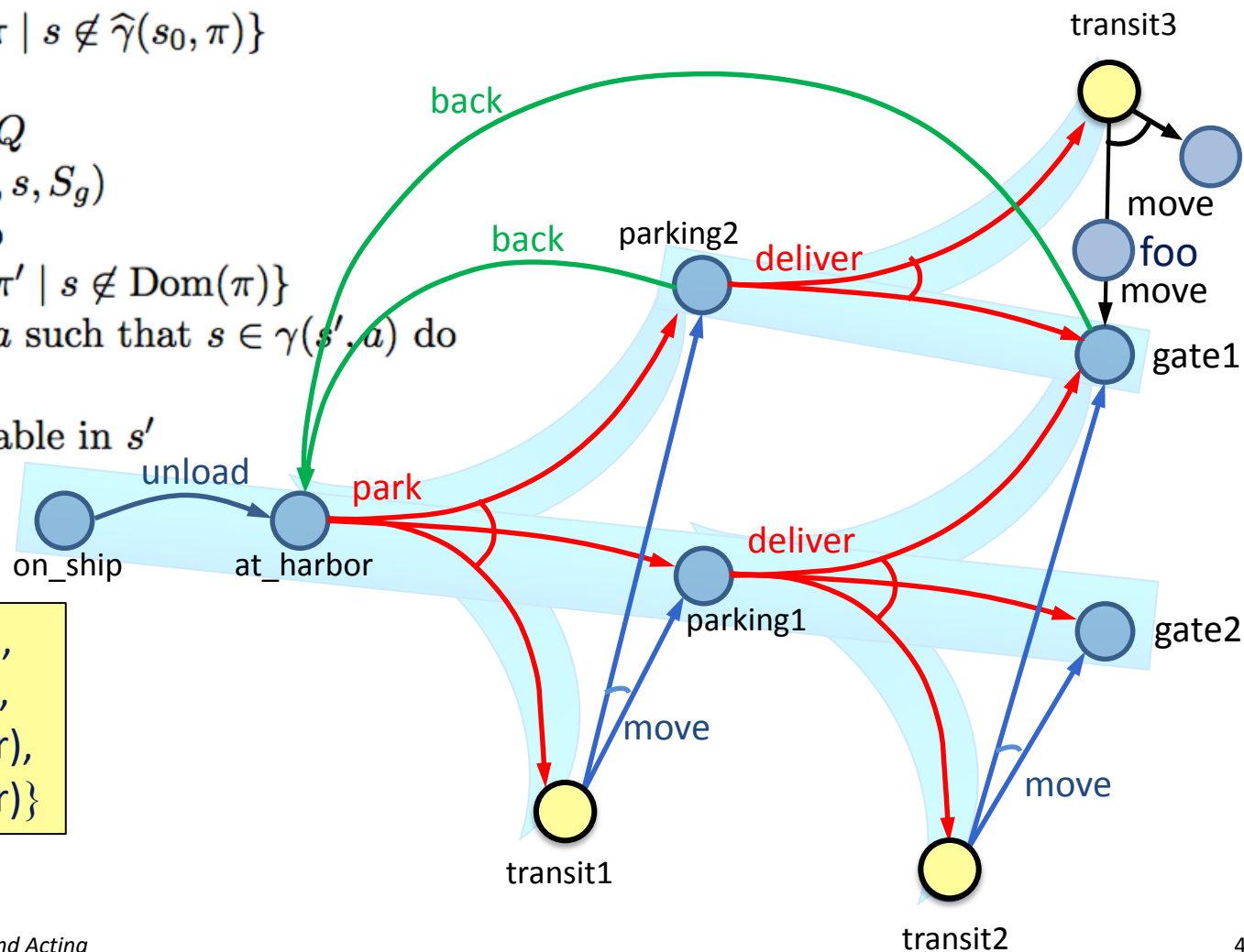
$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make  $a$  not applicable in  $s'$

## Example



$\pi = \{(on\_ship, unload),$   
 $(at\_harbor, park),$   
 $(parking1, deliver),$   
 $(parking2, deliver)\}$



# Guided-Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

if  $s_0 \in S_g$  then return( $\emptyset$ )

if  $Applicable(s_0) = \emptyset$  then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if  $Q = \emptyset$  then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return( $\pi$ )

select arbitrarily  $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

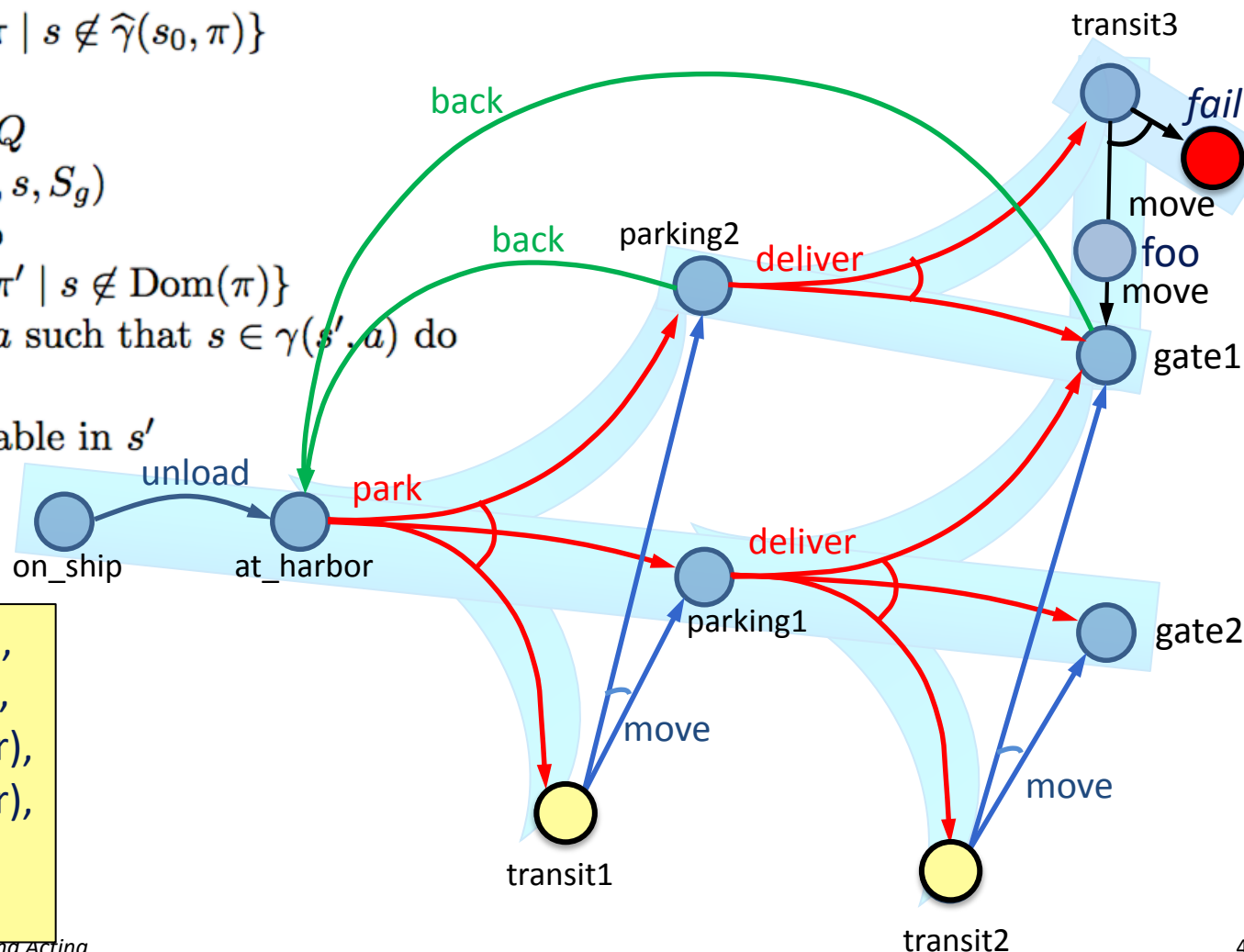
if  $\pi' \neq failure$  then do

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make  $a$  not applicable in  $s'$



$\pi = \{(on\_ship, unload),$   
 $(at\_harbor, park),$   
 $(parking1, deliver),$   
 $(parking2, deliver),$   
 $(transit3, move),$   
 $(foo, move)\}$

## Example

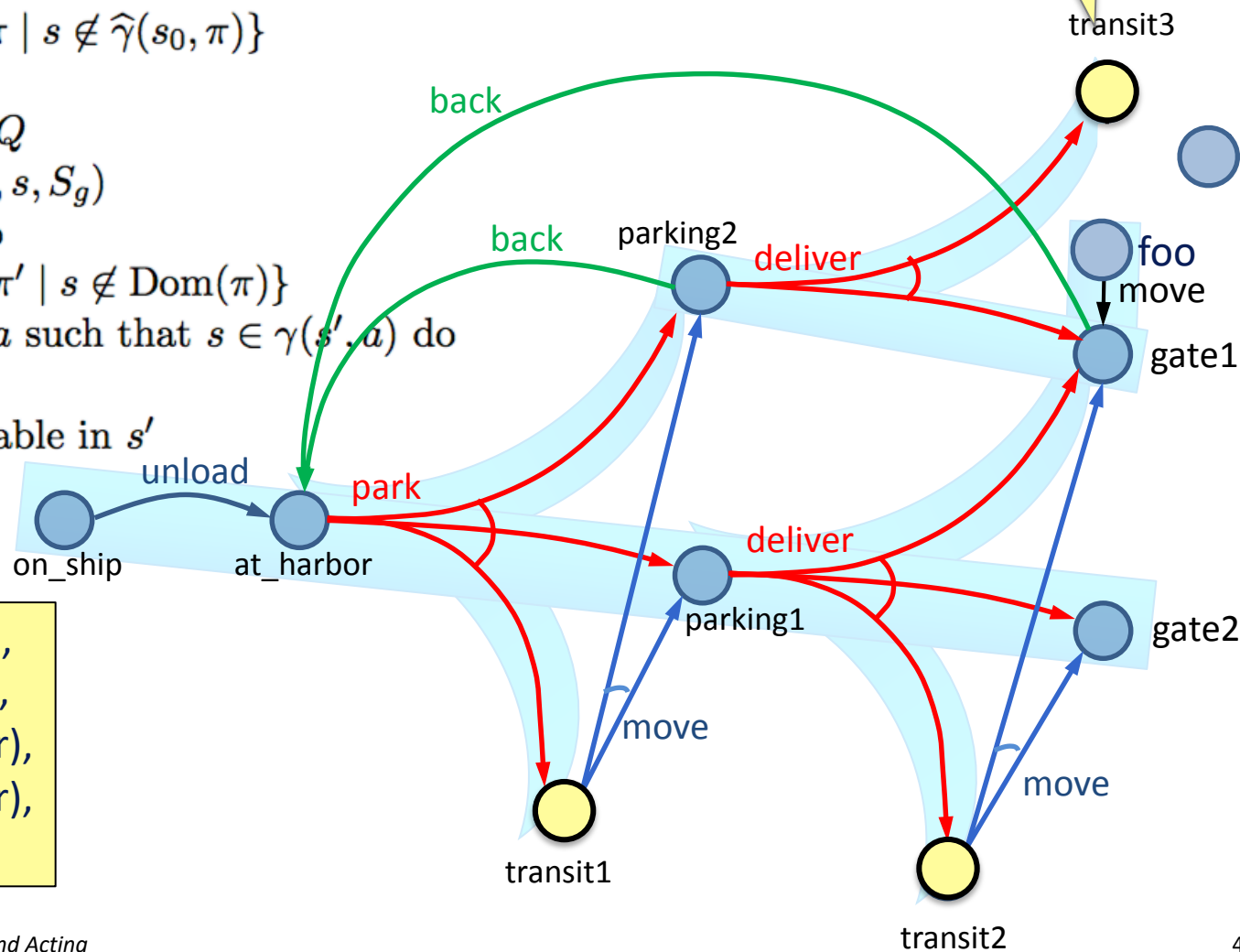
# Guided-Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

```
if  $s_0 \in S_g$  then return( $\emptyset$ )  
if  $Applicable(s_0) = \emptyset$  then return(failure)  
 $\pi \leftarrow \emptyset$   
loop  
   $Q \leftarrow leaves(s_0, \pi) \setminus S_g$   
  if  $Q = \emptyset$  then do  
     $\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$   
    return( $\pi$ )  
  select arbitrarily  $s \in Q$   
   $\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$   
  if  $\pi' \neq failure$  then do  
     $\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$   
  else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do  
     $\pi \leftarrow \pi \setminus \{(s', a)\}$   
    make  $a$  not applicable in  $s'$ 
```

$\pi = \{(on\_ship, unload),$   
 $(at\_harbor, park),$   
 $(parking1, deliver),$   
 $(parking2, deliver),$   
 $(foo, move)\}$

## Example

Modify  $\Sigma_d$  to make move inapplicable



# Guided-Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

if  $s_0 \in S_g$  then return( $\emptyset$ )

if  $Applicable(s_0) = \emptyset$  then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if  $Q = \emptyset$  then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return( $\pi$ )

select arbitrarily  $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

if  $\pi' \neq failure$  then do

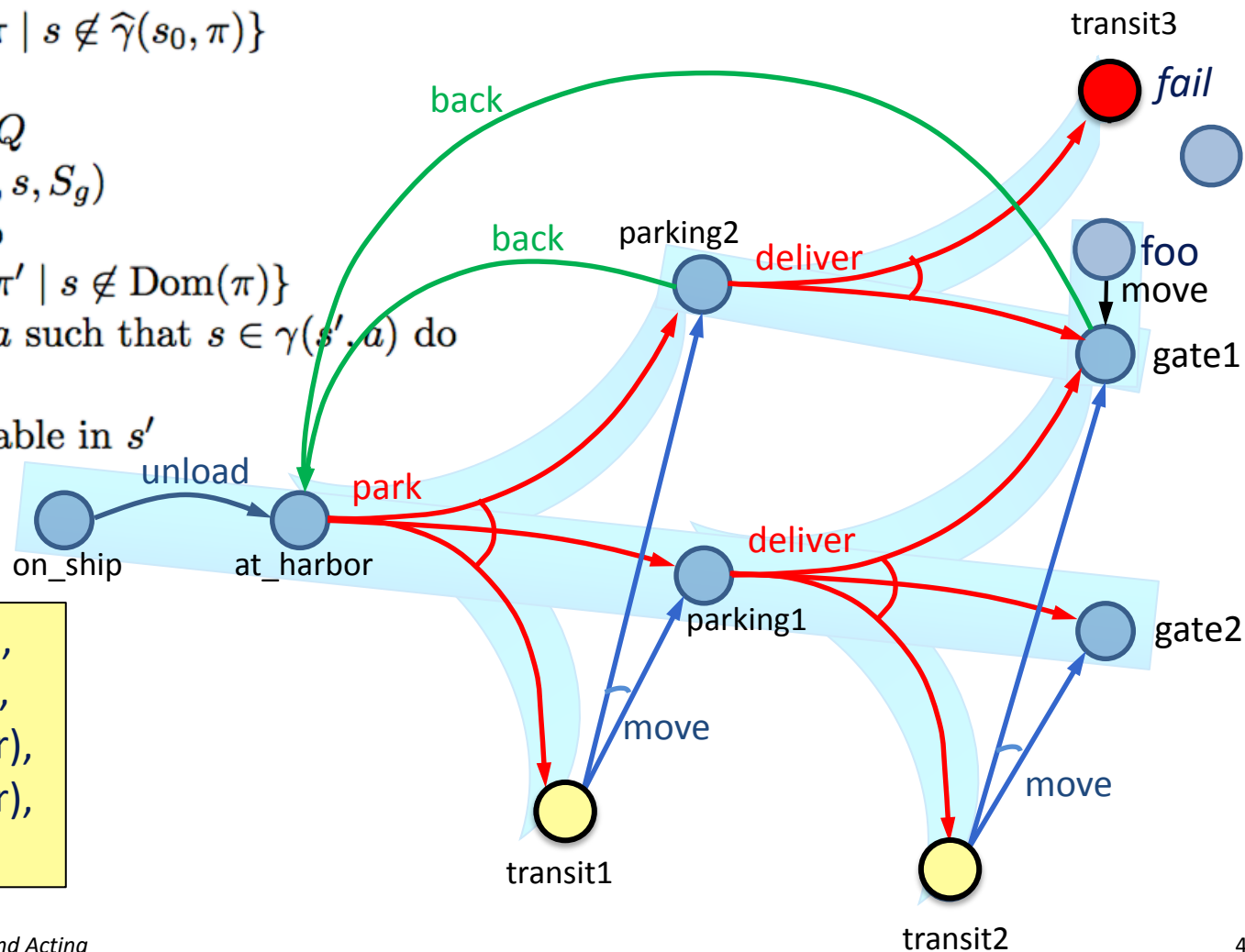
$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make  $a$  not applicable in  $s'$

## Example



$\pi = \{(on\_ship, unload),$   
 $(at\_harbor, park),$   
 $(parking1, deliver),$   
 $(parking2, deliver),$   
 $(foo, move)\}$

# Guided-Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

if  $s_0 \in S_g$  then return( $\emptyset$ )

if  $Applicable(s_0) = \emptyset$  then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if  $Q = \emptyset$  then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return( $\pi$ )

select arbitrarily  $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

if  $\pi' \neq failure$  then do

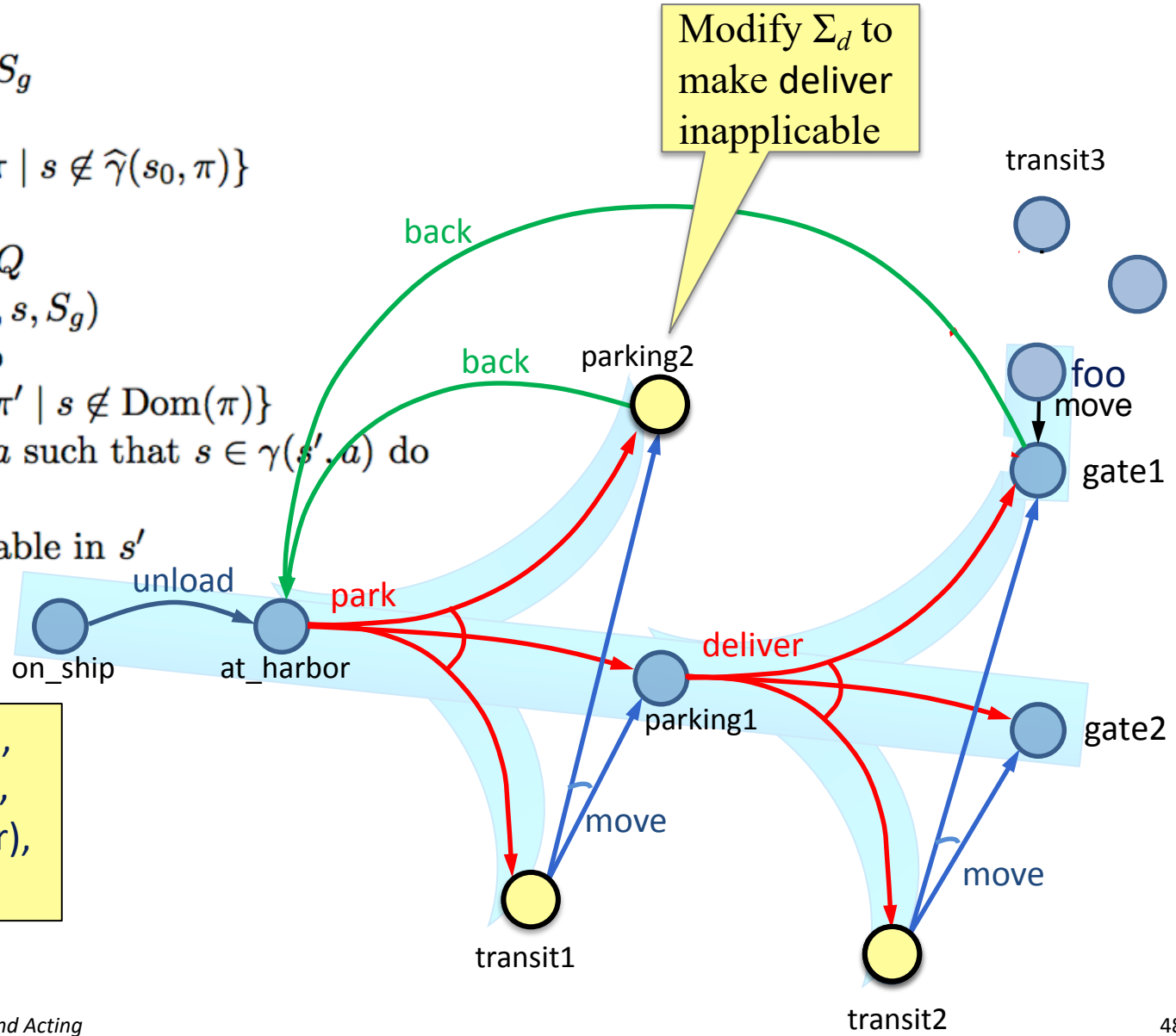
$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make  $a$  not applicable in  $s'$

## Example



$\pi = \{(on\_ship, unload), (at\_harbor, park), (parking1, deliver), (foo, move)\}$





# Guided-Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

```
if  $s_0 \in S_g$  then return( $\emptyset$ )  
if  $Applicable(s_0) = \emptyset$  then return(failure)
```

```
 $\pi \leftarrow \emptyset$ 
```

```
loop
```

```
   $Q \leftarrow leaves(s_0, \pi) \setminus S_g$ 
```

```
  if  $Q = \emptyset$  then do
```

```
     $\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$ 
```

```
    return( $\pi$ )
```

```
  select arbitrarily  $s \in Q$ 
```

```
   $\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$ 
```

```
  if  $\pi' \neq failure$  then do
```

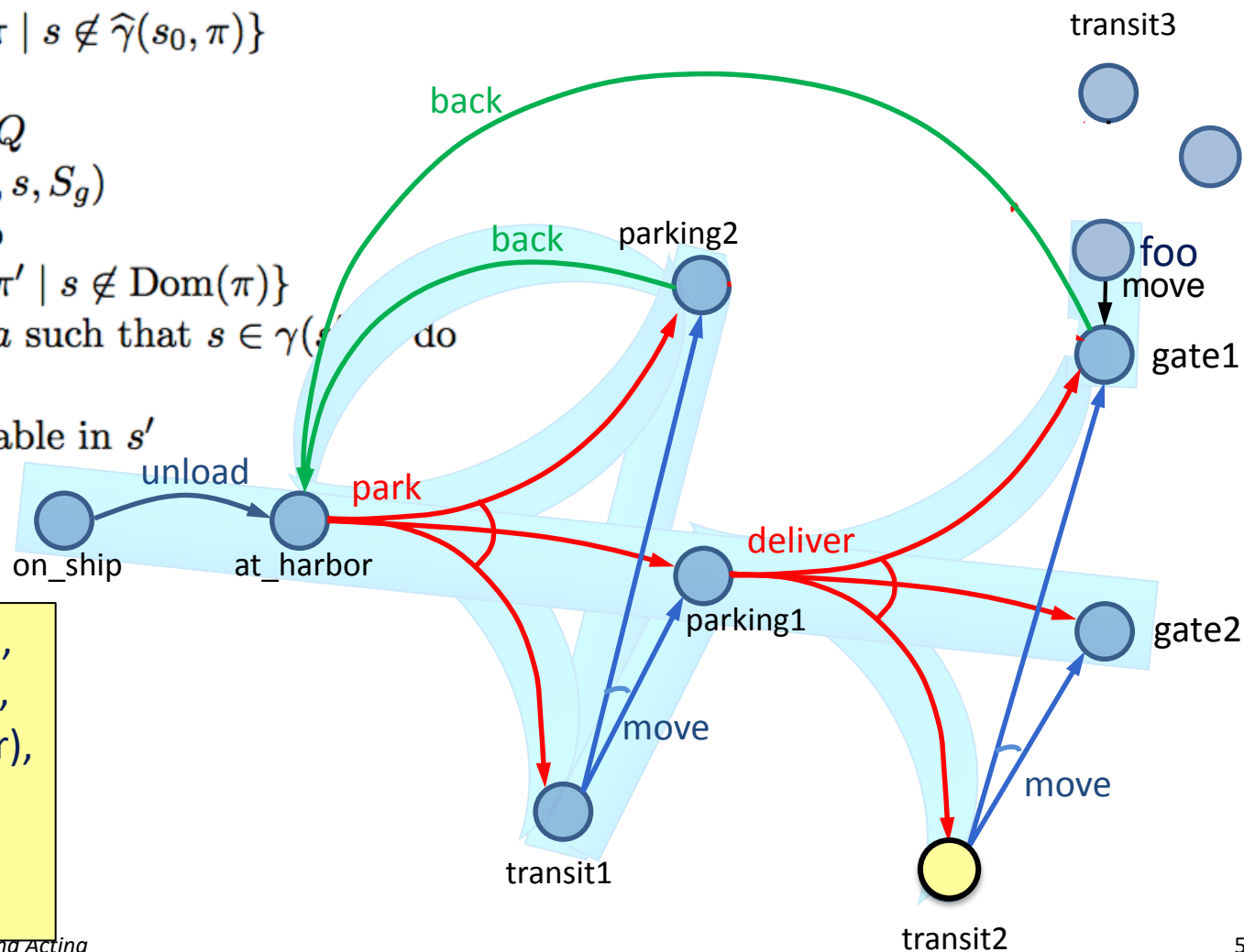
```
     $\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$ 
```

```
  else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do
```

```
     $\pi \leftarrow \pi \setminus \{(s', a)\}$ 
```

```
    make  $a$  not applicable in  $s'$ 
```

## Example



```
 $\pi = \{(on\_ship, unload),$   
 $(at\_harbor, park),$   
 $(parking1, deliver),$   
 $(foo, move),$   
 $(parking2, back),$   
 $(transit1, move)\}$ 
```

# Guided-Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

if  $s_0 \in S_g$  then return( $\emptyset$ )  
if  $Applicable(s_0) = \emptyset$  then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if  $Q = \emptyset$  then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return( $\pi$ )

select arbitrarily  $s \in Q$

$\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$

if  $\pi' \neq failure$  then do

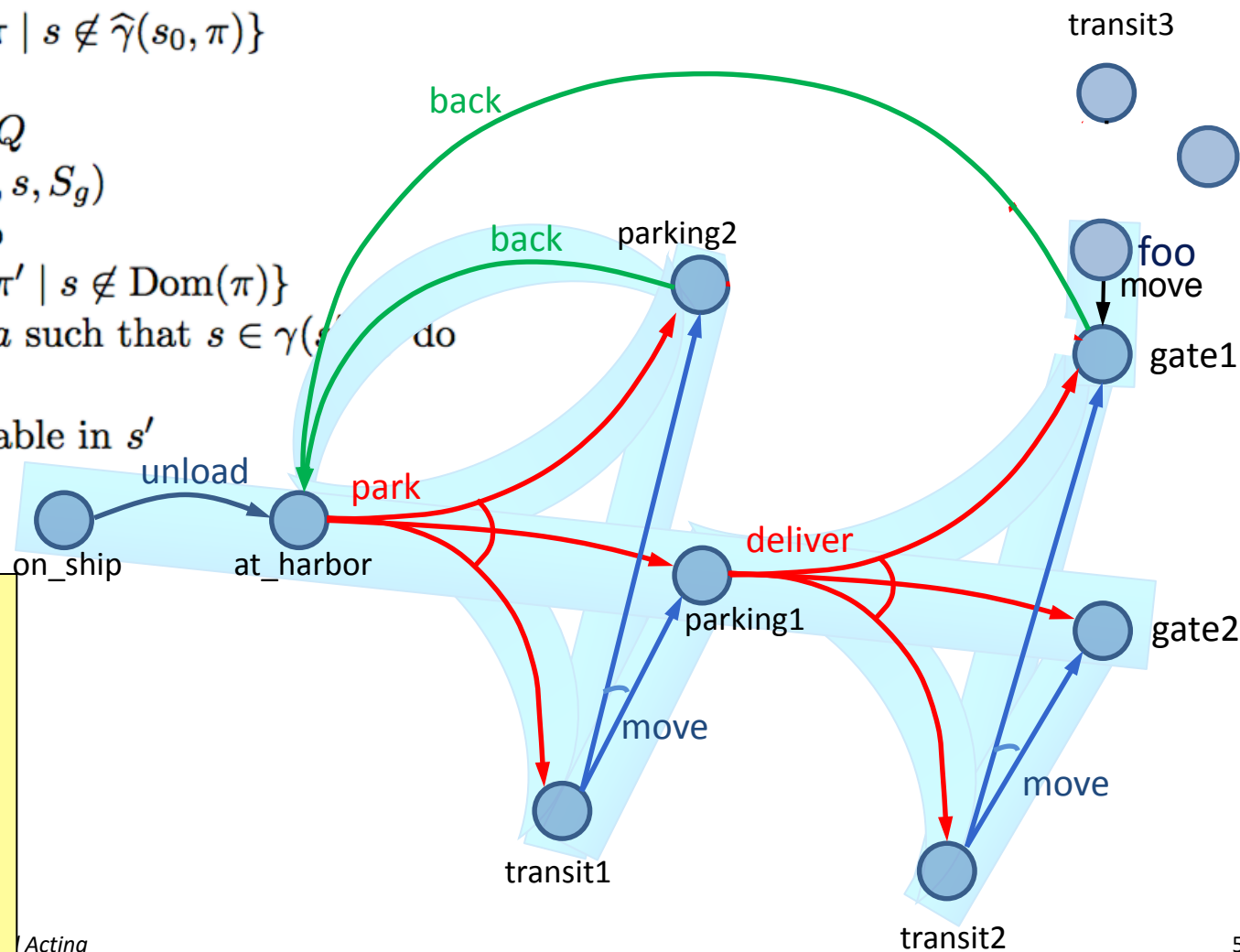
$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make  $a$  not applicable in  $s'$

## Example

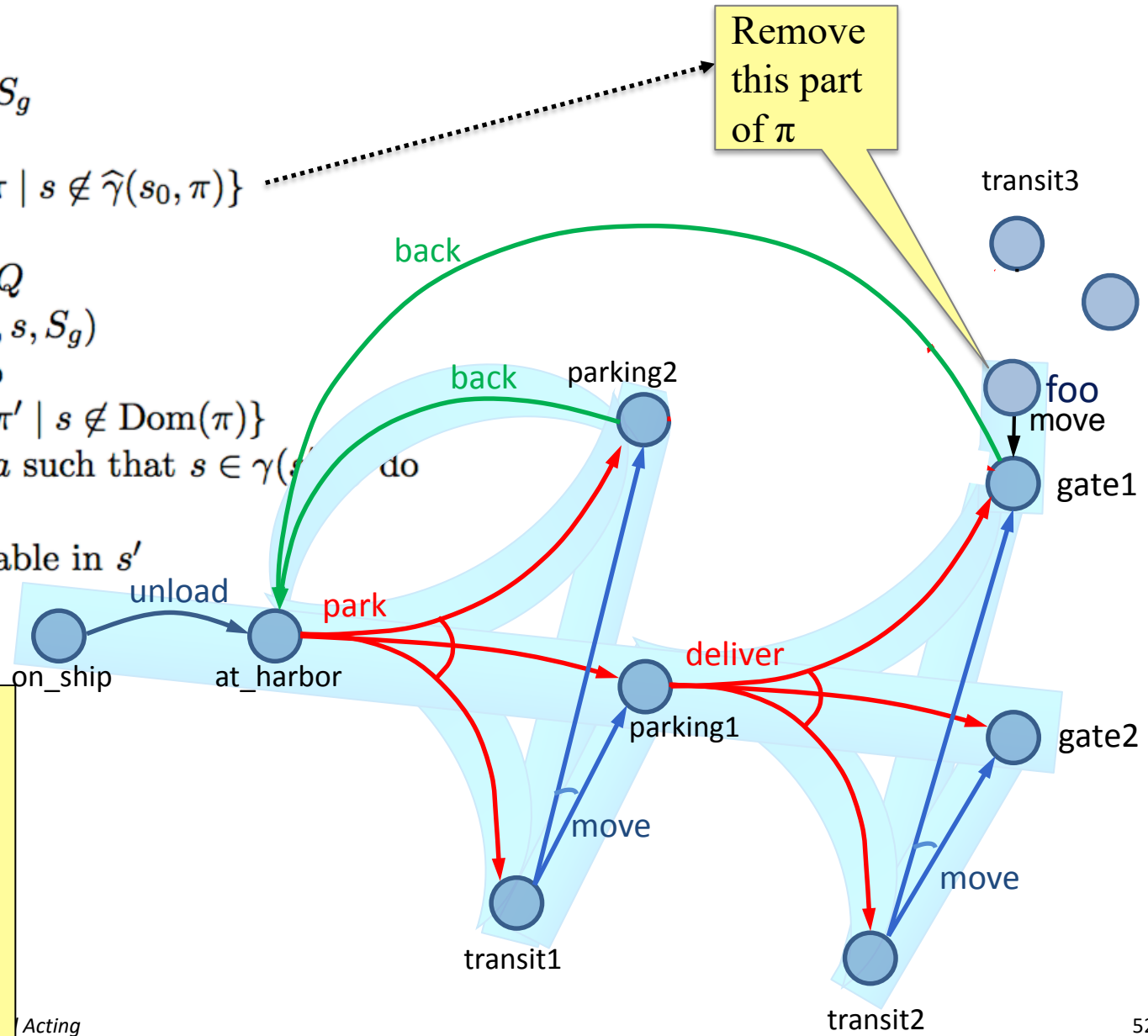


# Guided-Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

```
if  $s_0 \in S_g$  then return( $\emptyset$ )  
if  $Applicable(s_0) = \emptyset$  then return(failure)  
 $\pi \leftarrow \emptyset$   
loop  
   $Q \leftarrow leaves(s_0, \pi) \setminus S_g$   
  if  $Q = \emptyset$  then do  
     $\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$   
    return( $\pi$ )  
  select arbitrarily  $s \in Q$   
   $\pi' \leftarrow Find-Solution(\Sigma, s, S_g)$   
  if  $\pi' \neq failure$  then do  
     $\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$   
  else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do  
     $\pi \leftarrow \pi \setminus \{(s', a)\}$   
    make  $a$  not applicable in  $s'$ 
```

## Example

Remove this part of  $\pi$



$\pi = \{(on\_ship, unload),$   
 $(at\_harbor, park),$   
 $(parking1, deliver),$   
 ~~$(foo, move),$~~   
 $(parking2, back),$   
 $(transit1, move),$   
 $(transit2, move)\}$

Acting

## Guided-Find-Safe-Solution ( $\Sigma, s_0, S_g$ )

if  $s_0 \in S_g$  then return( $\emptyset$ )

if  $Applicable(s_0) = \emptyset$  then return(failure)

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow leaves(s_0, \pi) \setminus S_g$

if  $Q = \emptyset$  then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return( $\pi$ )

select arbitrarily  $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if  $\pi' \neq \text{failure}$  then do

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

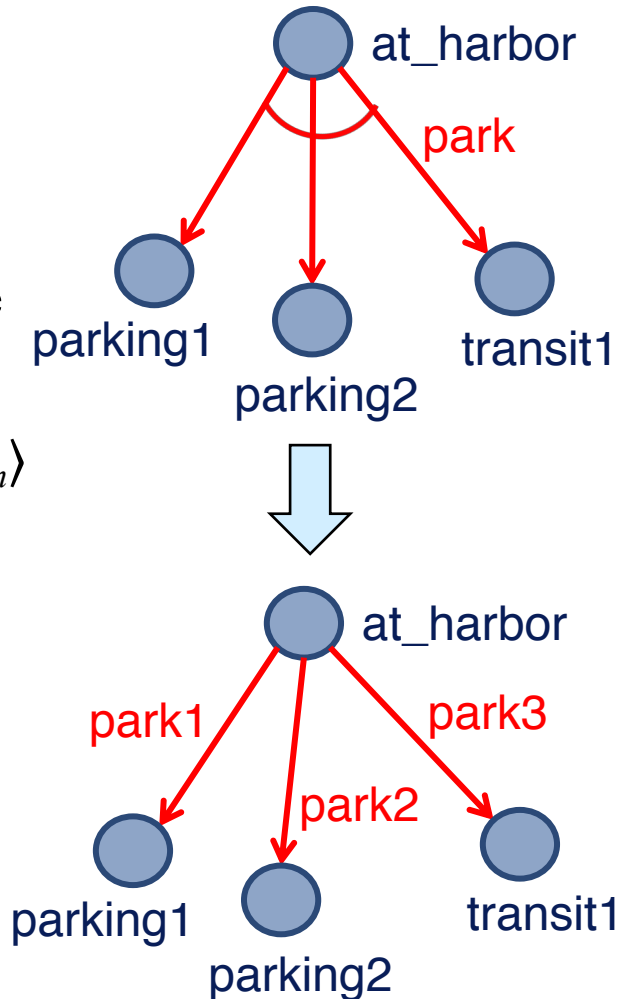
make  $a$  not applicable in  $s'$

## Determinization

- How to implement it?
  - Need implementation of Find-Solution
  - Need it to be very efficient
    - We'll call it many times
- Idea: instead of Find-Solution, use a classical planner
  - Any of the algorithms from Chapter 2
  - Efficient algorithms, search heuristics

# Determinization

- Convert the nondeterministic actions into something the classical planner can use
- *Determinize*
  - Suppose  $a_i$  has  $n$  possible outcomes
  - $n$  deterministic actions, one for each outcome
- Classical planner returns a plan  $p = \langle a_1, a_2, \dots, a_n \rangle$
- If  $p$  is acyclic, can convert it to a policy
  - (unsafe) solution for  $P$
  - $\{(s_0, \mathbf{a}_1), (s_1, \mathbf{a}_2), \dots, (s_{n-1}, \mathbf{a}_n)\}$   
where
    - each  $\mathbf{a}_i$  is the nondeterministic action whose determinization includes  $a_i$
    - $s_i \in \gamma(s_{i-1}, \mathbf{a}_i)$



# Determinization

- Nondeterministic planning problem  $P = (\Sigma, s_0, S_g)$
- Determinization  $P_d = (\Sigma_d, s_0, S_g)$
- Classical planner returns a solution for  $P$ 
  - a plan  $p = \langle a_1, a_2, \dots, a_n \rangle$
- If  $p$  is acyclic, can convert it to an (unsafe) solution for  $P$ 
  - $\{(s_0, \mathbf{a}_1), (s_1, \mathbf{a}_2), \dots, (s_{n-1}, \mathbf{a}_n)\}$   
where each  $\mathbf{a}_i$  is the nondeterministic action whose determinization includes  $a_i$
  - each  $s_i \in \gamma(s_{i-1}, \mathbf{a}_i)$

```
Plan2policy( $p = \langle a_1, \dots, a_n \rangle, s$ )  
   $\pi \leftarrow \emptyset$   
  loop for  $i$  from 1 to  $n$  do  
     $\pi \leftarrow \pi \cup (s, \text{det2nondet}(a_i))$   
     $s \leftarrow \gamma_d(s, a_i)$   
  return  $\pi$ 
```

# Determinization

Find-Safe-Solution-by-Determinization ( $\Sigma, s_0, S_g$ )

if  $s_0 \in S_g$  then return( $\emptyset$ )

if  $Applicable(s_0) = \emptyset$  then return(failure)

$\pi \leftarrow \emptyset$

$\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if  $Q = \emptyset$  then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return( $\pi$ )

select  $s \in Q$

$p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$

if  $p' \neq \text{fail}$  then do

$\pi' \leftarrow \text{Plan2policy}(p', s)$

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make the actions in the determinization of  $a$   
not applicable in  $s'$

Same as  
Guided-Find-Safe-Solution

Any classical planner that  
doesn't return cyclic plans

Convert  $p'$  to a policy. Add each  $(s, a)$   
to  $\pi$  unless  $\pi$  already has an action at  $s$

$s$  is unsolvable. For each  $(s', a)$   
that can produce  $s$ , modify  $\pi$   
and  $\Sigma_d$  so we'll never use  $a$  at  $s'$



# Example

Find-Safe-Solution-by-Determinization ( $\Sigma, s_0, S_g$ )

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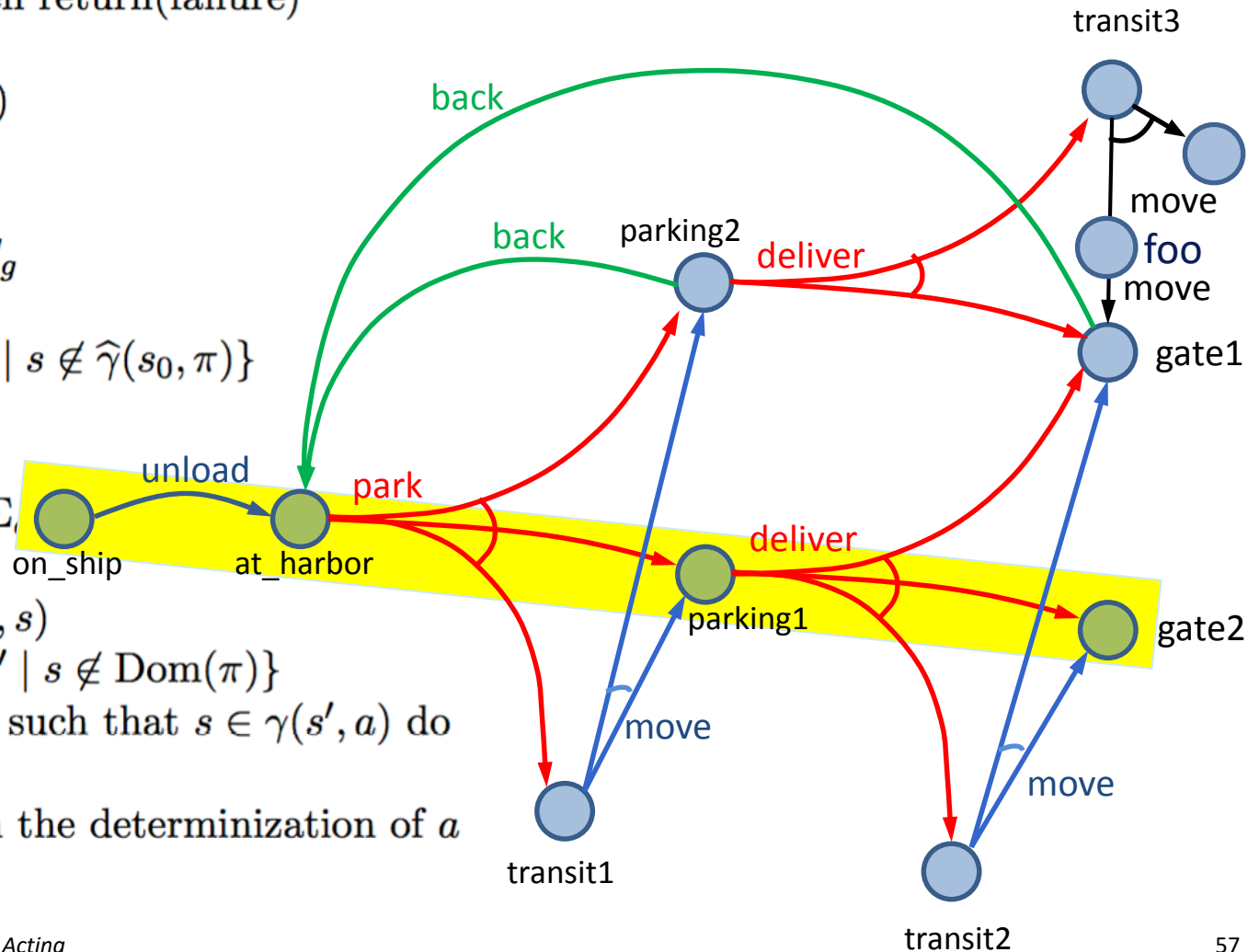
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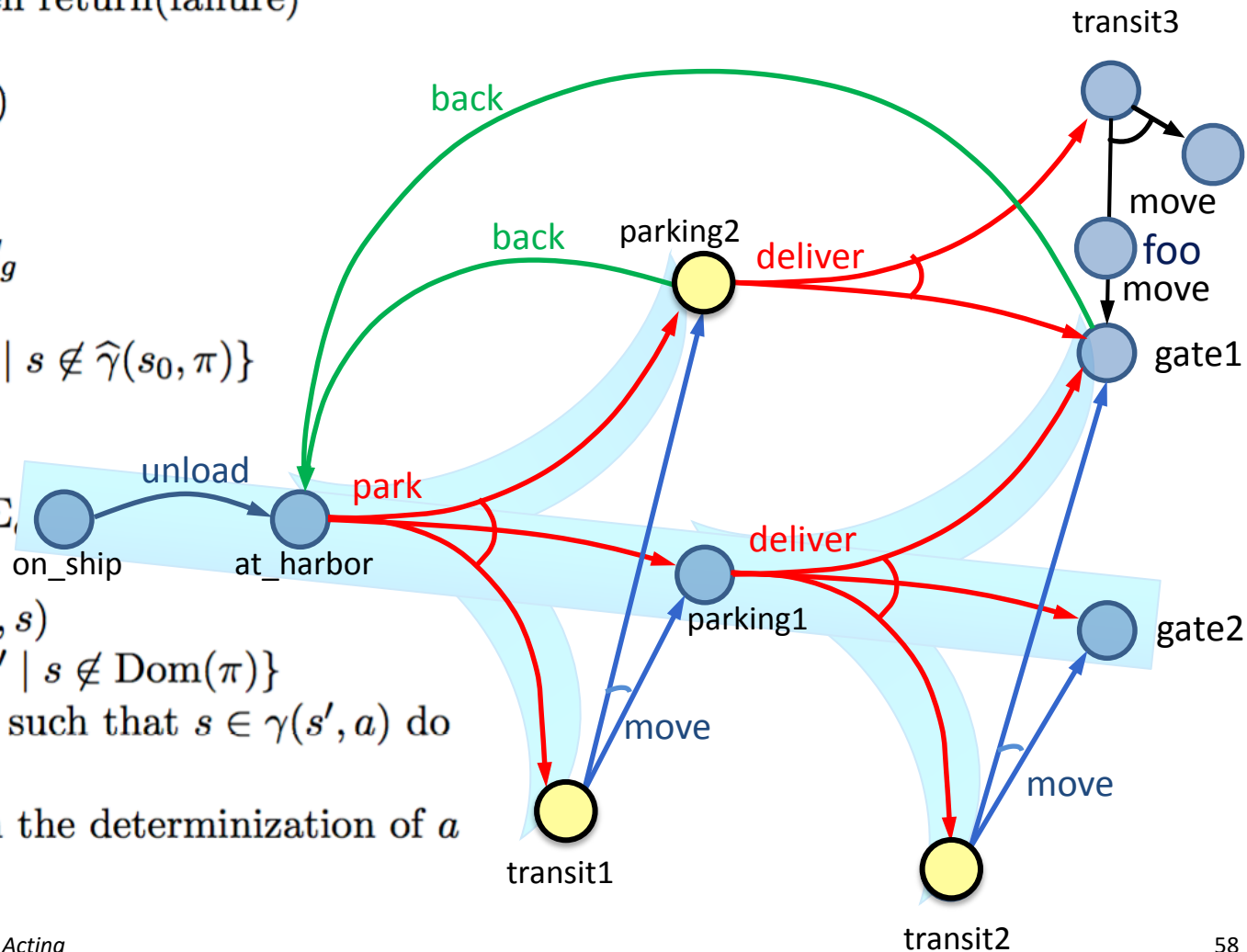
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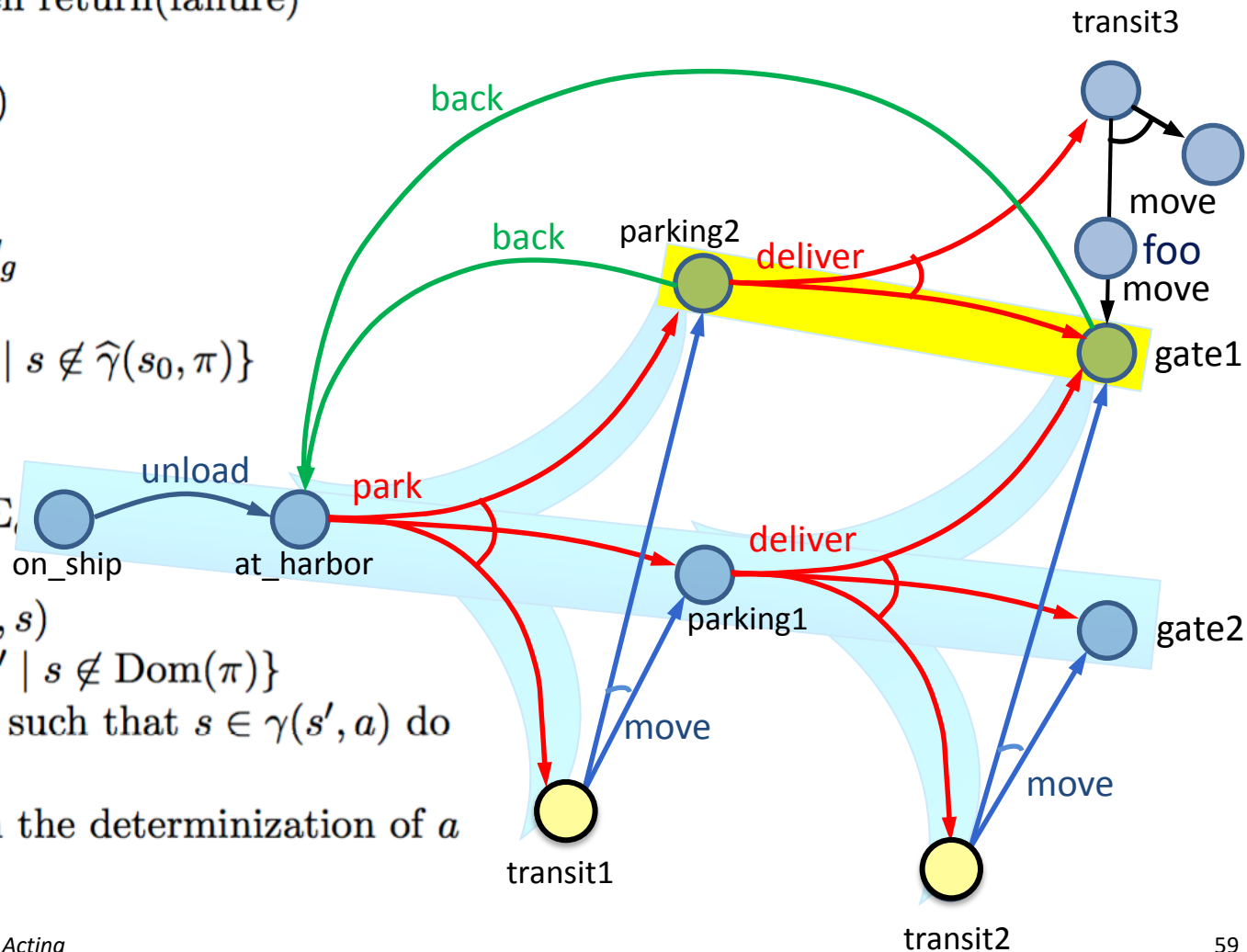
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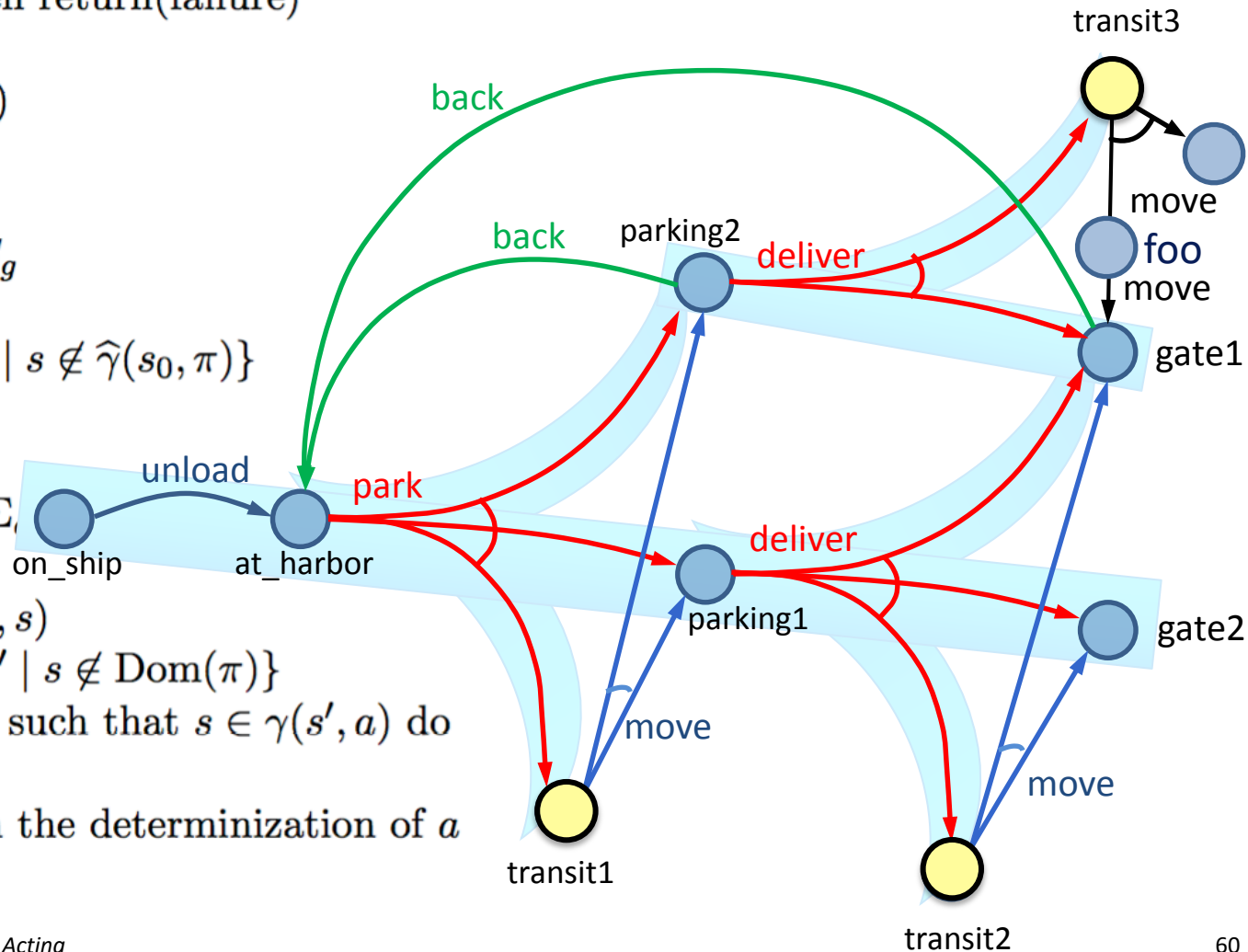
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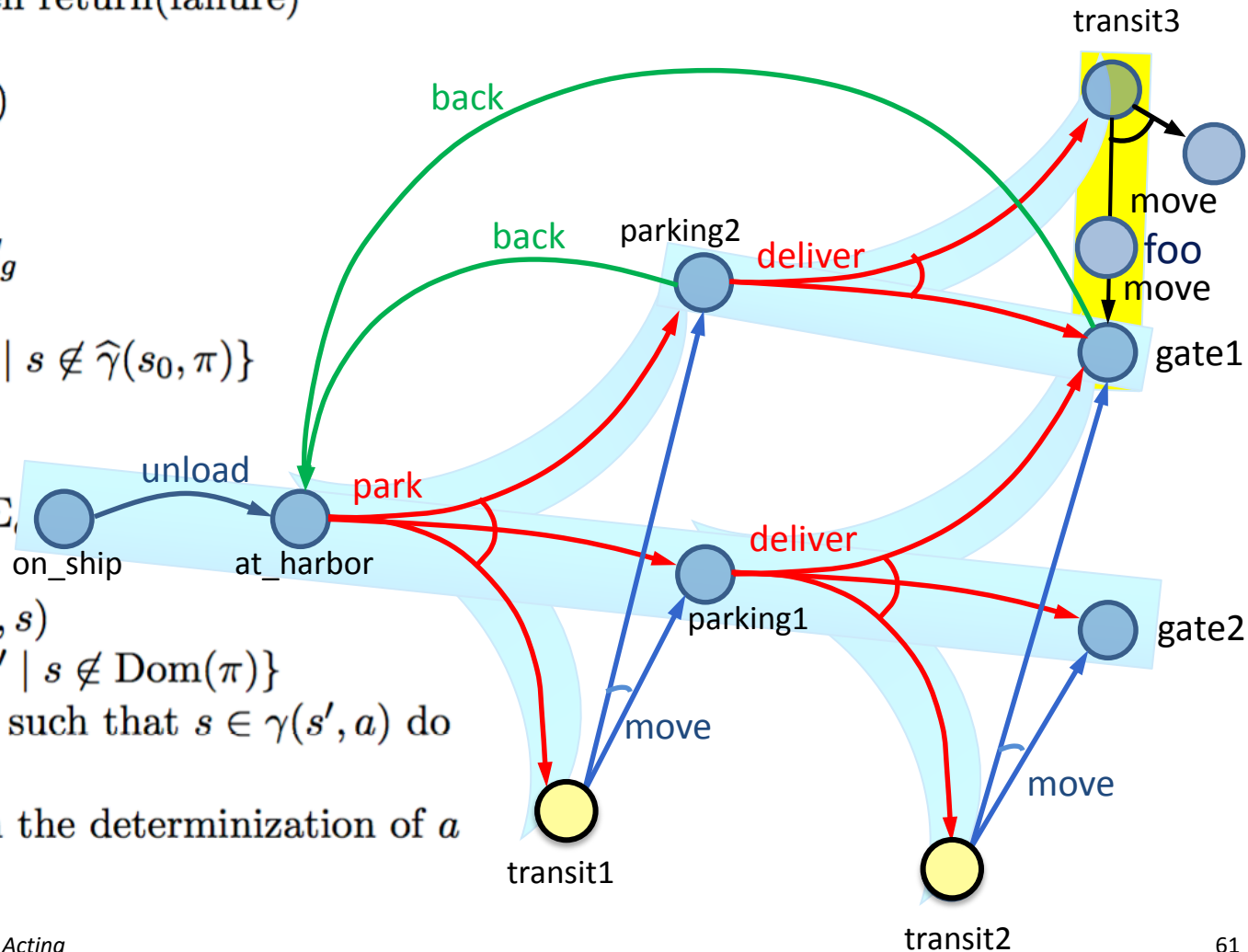
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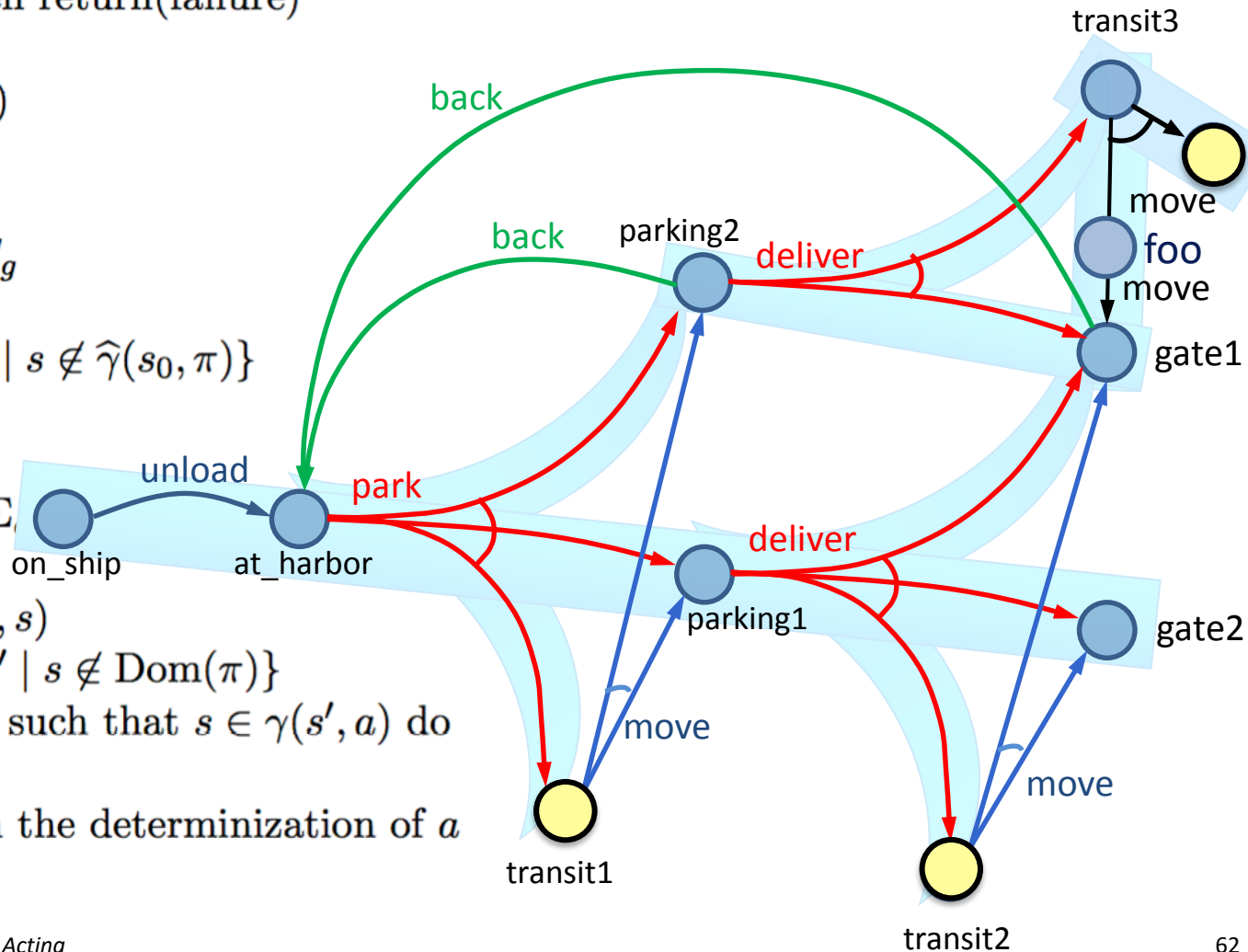
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return( $\pi$ )

select  $s \in Q$

$p' \leftarrow Forward\text{-search}(\Sigma, s)$

if  $p' \neq fail$  then do

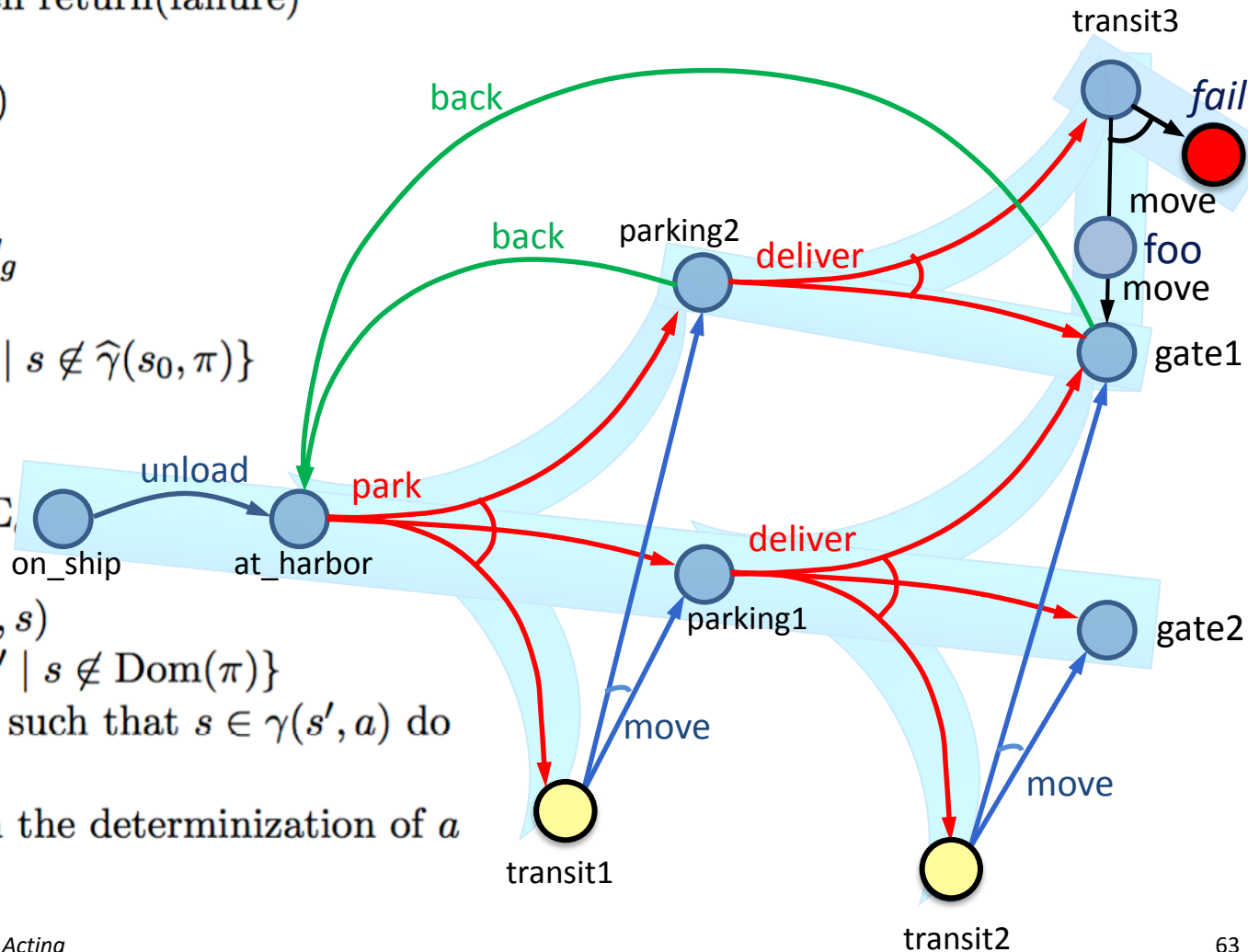
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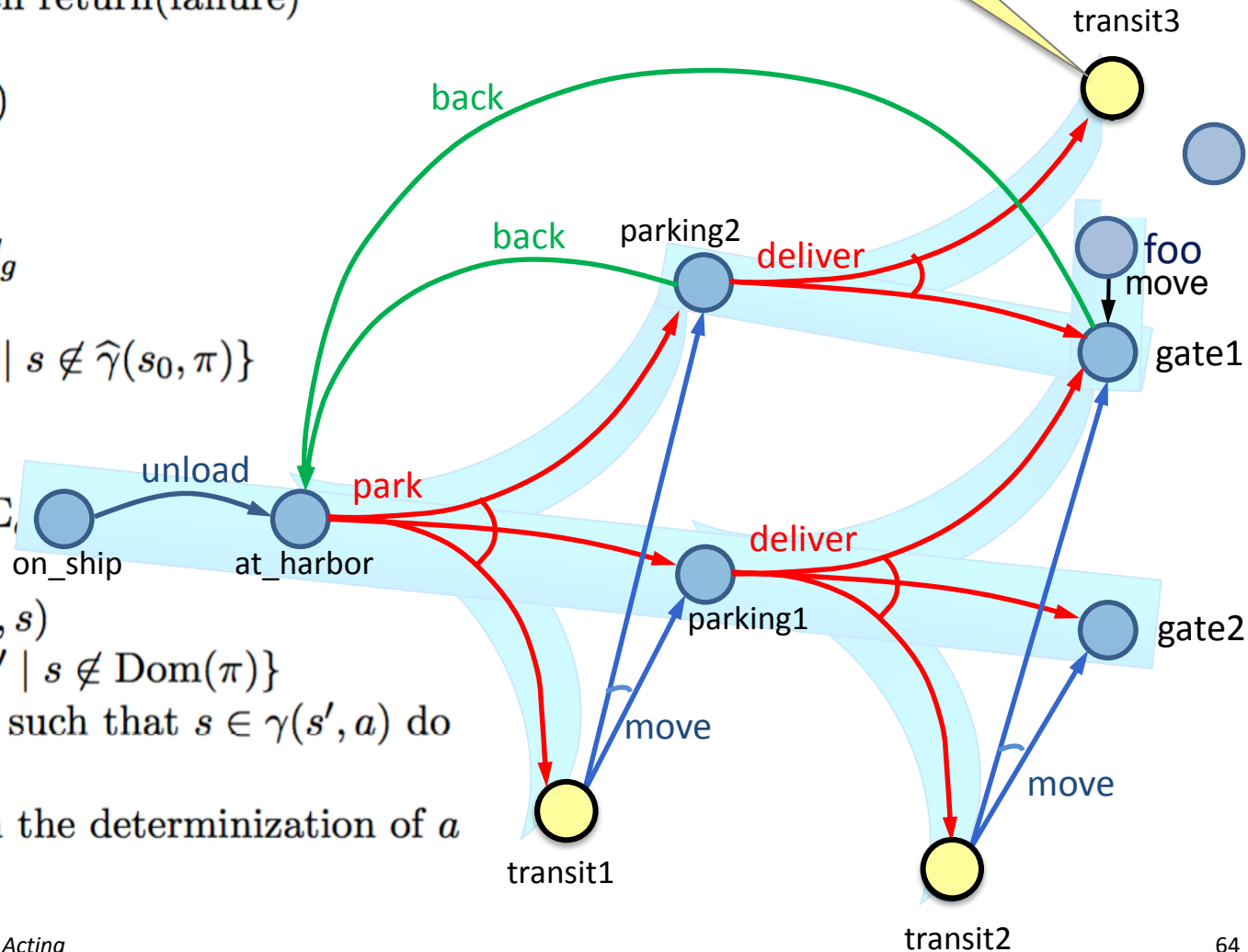
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make the actions in the determinization of  $a$  not applicable in  $s'$

Modify  $\Sigma_d$  to make move inapplicable





# Example

Find-Safe-Solution-by-Determinization  $(\Sigma, s_0, S_g)$

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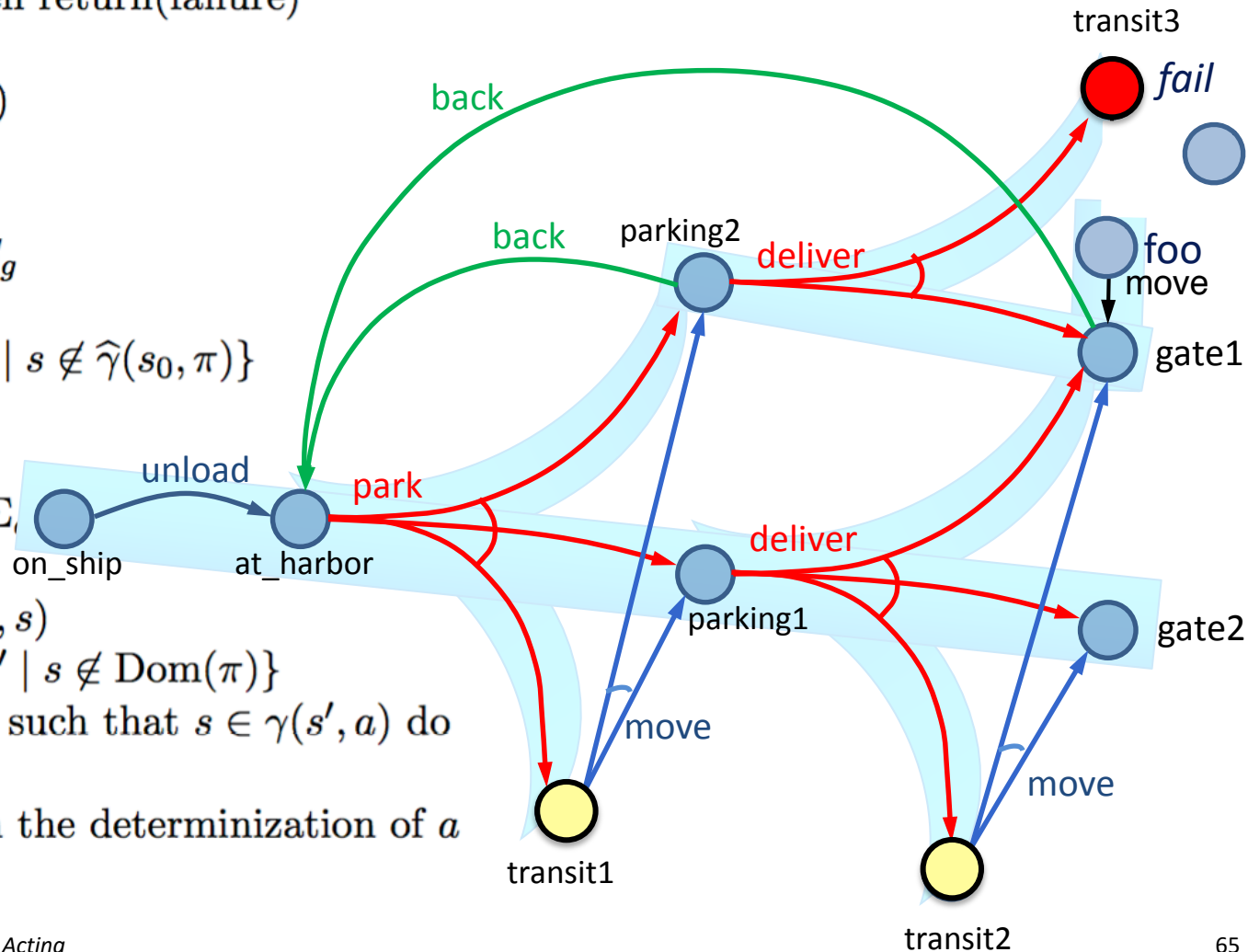
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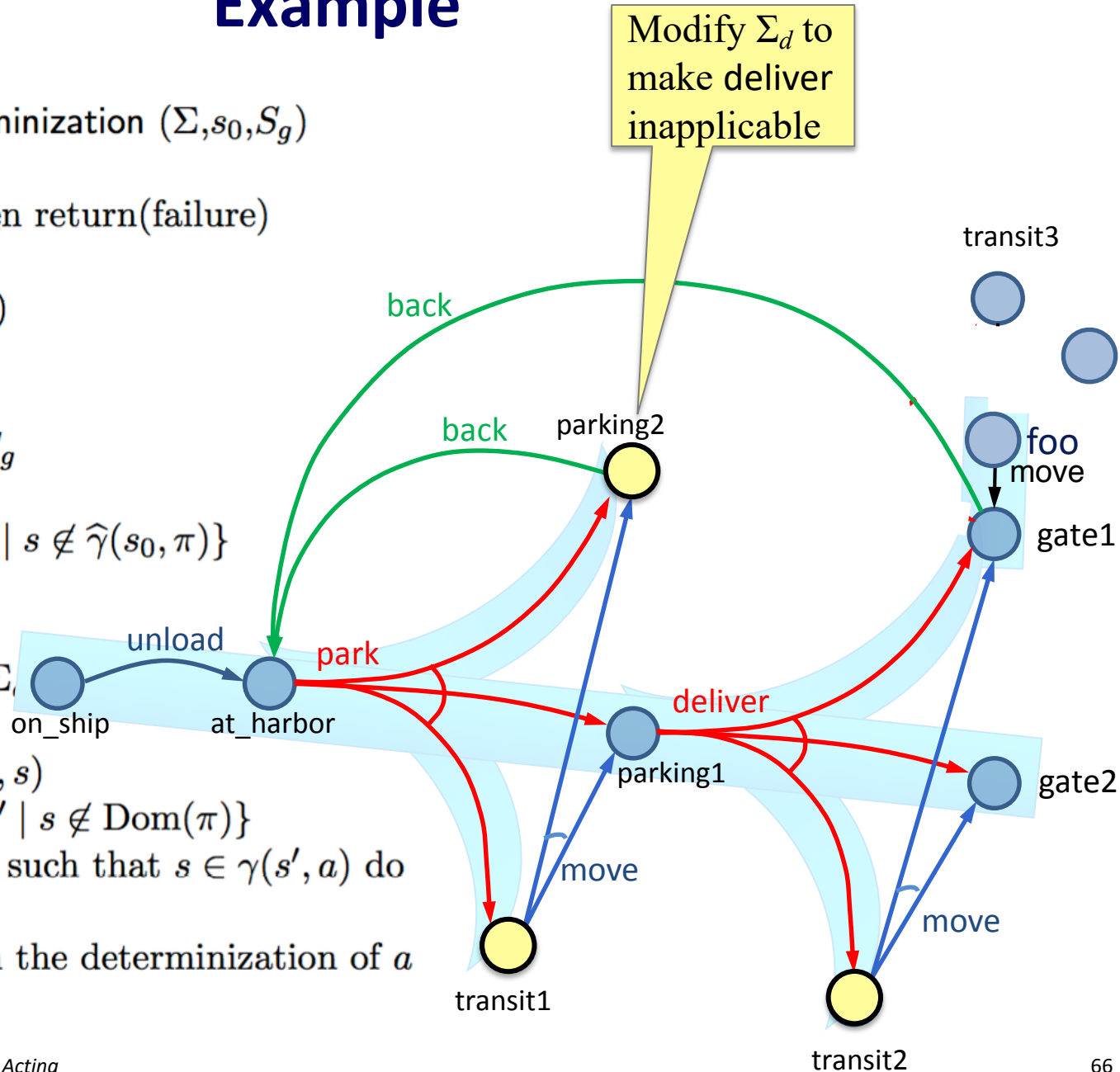
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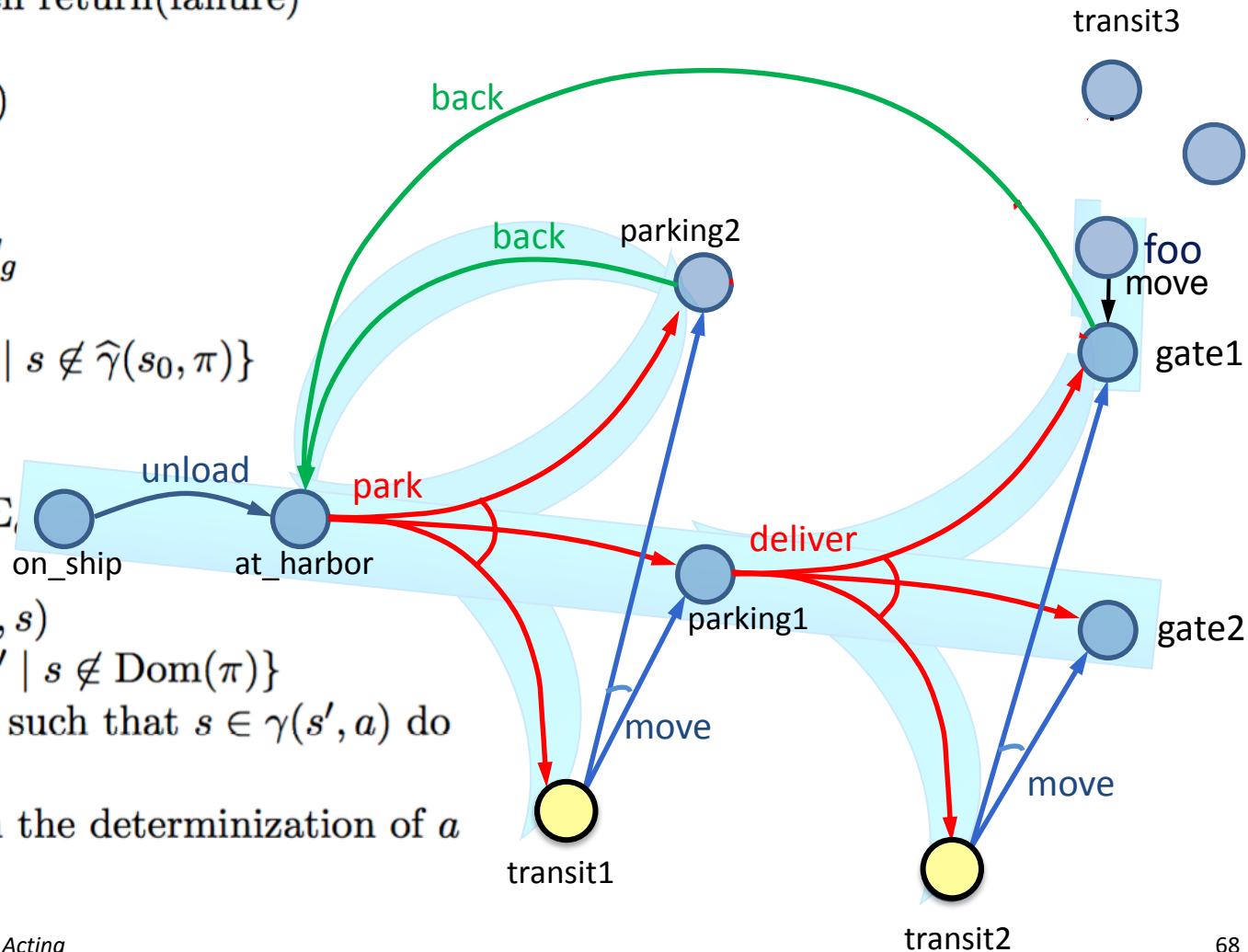
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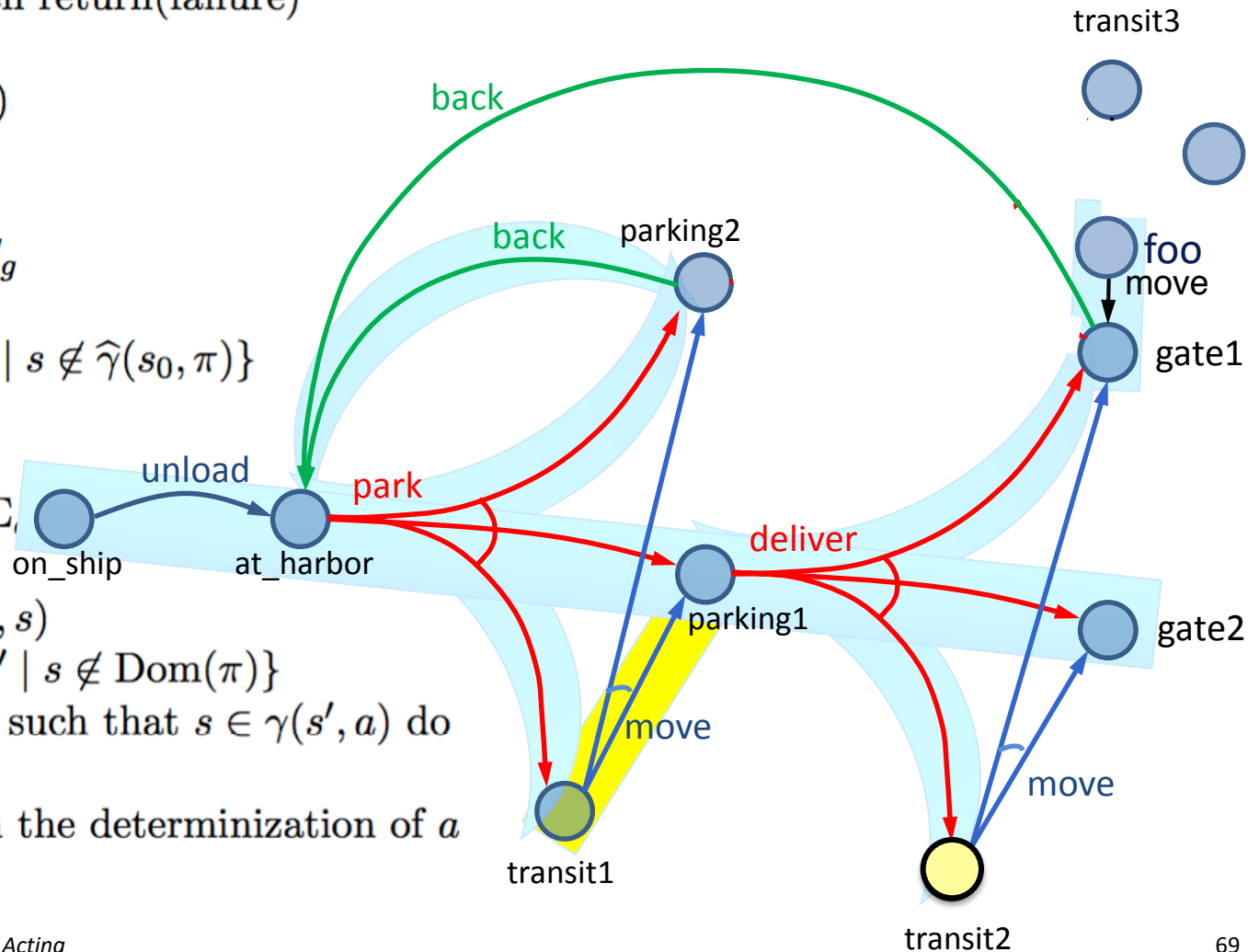
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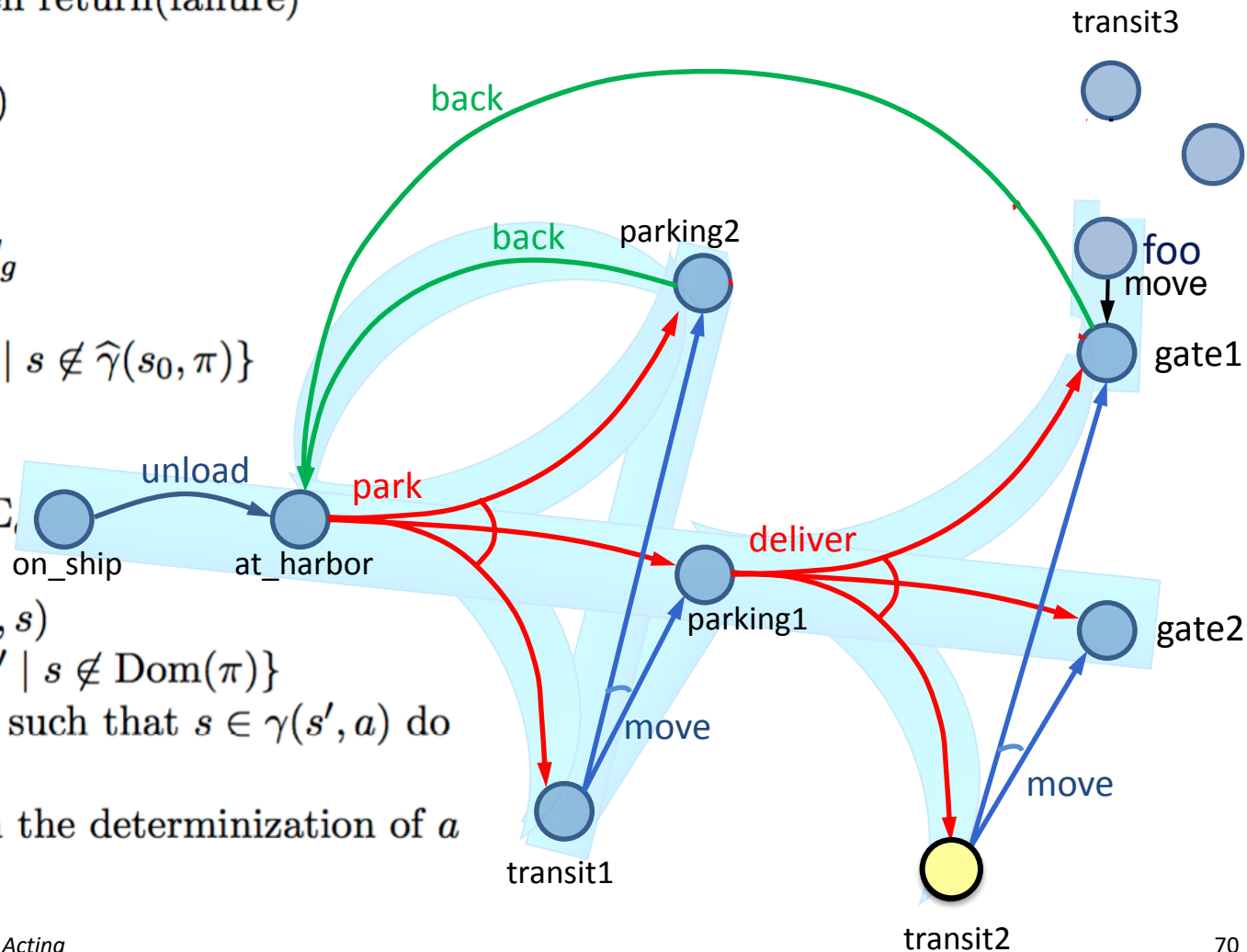
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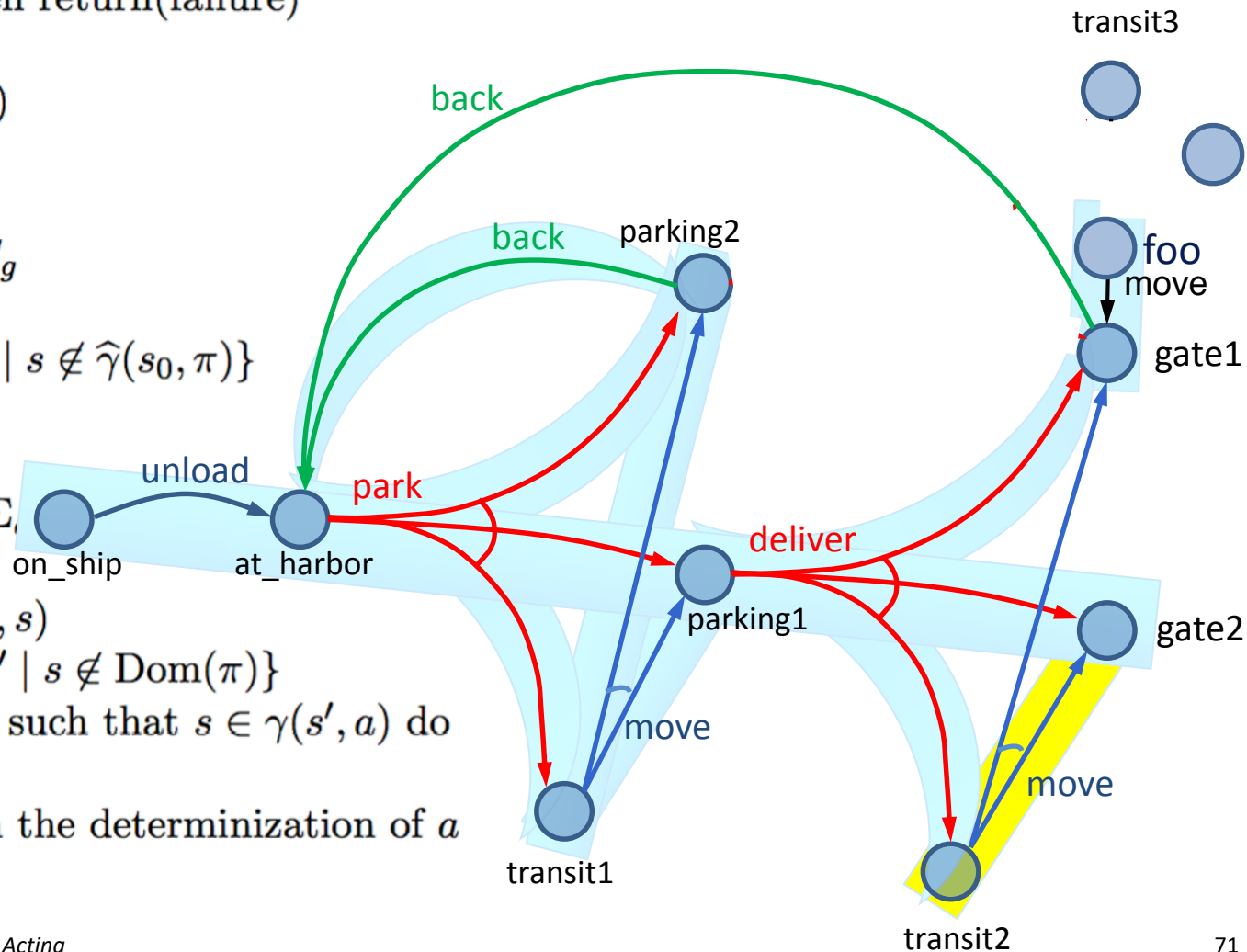
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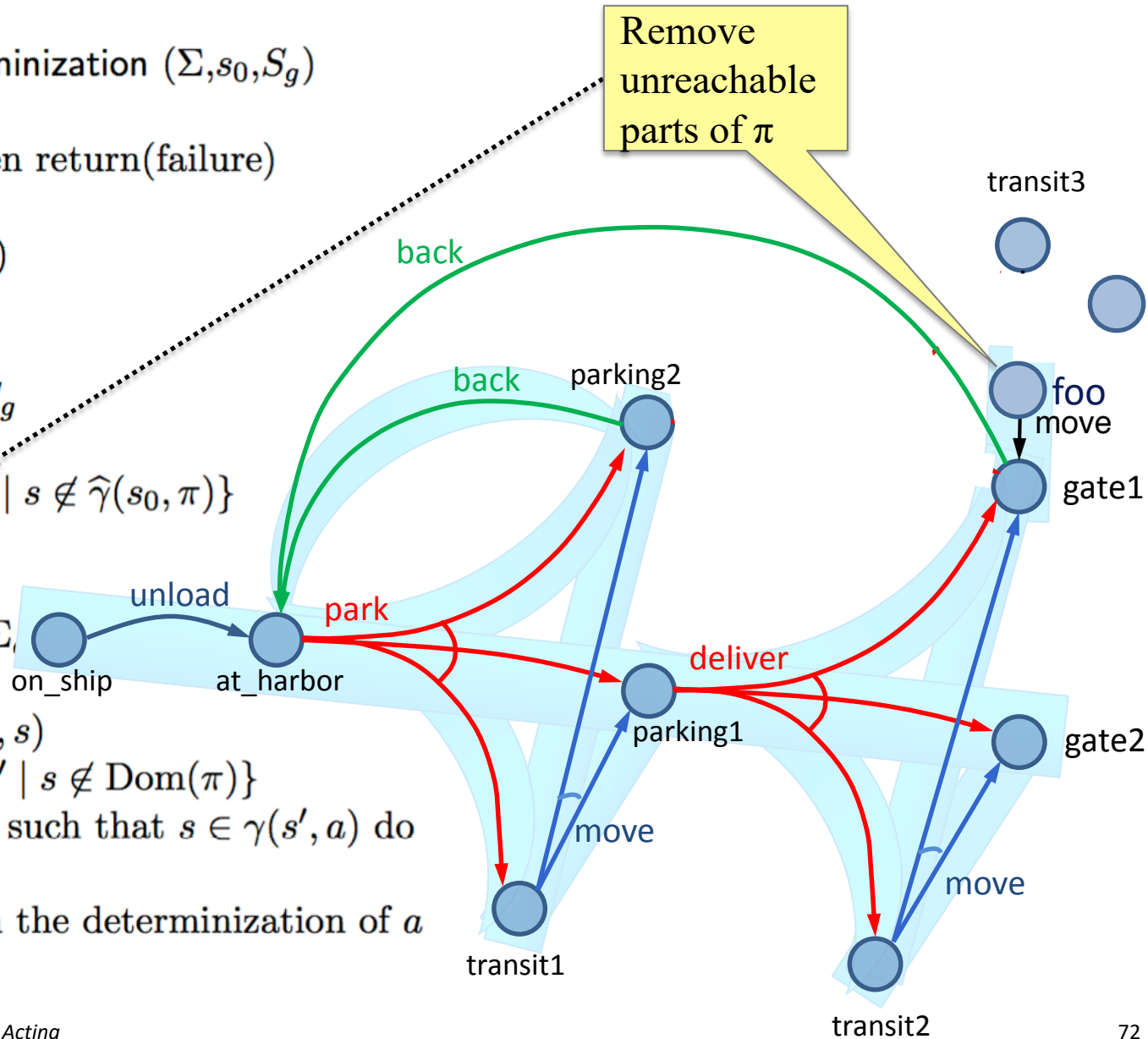
$\pi' \leftarrow Plan2policy(p', s)$

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin Dom(\pi)\}$

else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make the actions in the determinization of  $a$  not applicable in  $s'$





# Making Actions Inapplicable

Find-Safe-Solution-by-Determinization  $(\Sigma, s_0, S_g)$

if  $s_0 \in S_g$  then return( $\emptyset$ )

if  $Applicable(s_0) = \emptyset$  then return(failure)

$\pi \leftarrow \emptyset$

$\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if  $Q = \emptyset$  then do

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return( $\pi$ )

select  $s \in Q$

$p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$

if  $p' \neq \text{fail}$  then do

$\pi' \leftarrow \text{Plan2policy}(p', s)$

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else for every  $s'$  and  $a$  such that  $s \in \gamma(s', a)$  do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make the actions in the determinization of  $a$   
not applicable in  $s'$

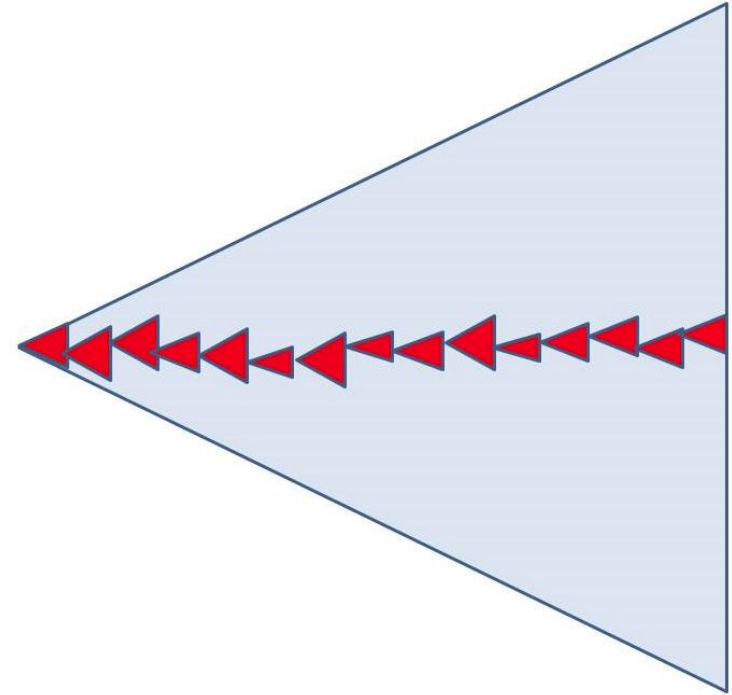
- Modify  $\Sigma_d$  to make actions inapplicable
  - worst-case exponential time
- Better: table of bad state-action pairs
  - For every  $(s', a)$  such that  $s \in \gamma(s', a)$ ,  $Bad[s'] \leftarrow Bad[s'] \cup \text{determinization}(a)$
  - Modify classical planner to take the table as an argument
    - if  $s$  is current state, only choose actions in  $Applicable(s) \setminus Bad(s)$

# Skip Ahead

- Several topics I'll skip for now
  - will come back later if there's time
  - Other kinds of search algorithms
    - min-max search
  - Symbolic model checking techniques
    - Backward search
    - BDD representation
      - ▶ Reduce search-space size by planning over sets of states

## 5.6 Online Approaches

- Motivation
  - Planning models are approximate – execution seldom works out as planned
  - Large problems may require too much planning time
- 2<sup>nd</sup> motivation even more stronger in nondeterministic domains
  - Nondeterminism makes planning exponentially harder
    - Exponentially more time, exponentially larger policies



Offline vs Runtime  
Search Spaces

# Online Approaches

- Need to identify *good* actions without exploring entire search space
  - Can be done using heuristic estimates
- Some domains are *safely explorable*
  - Safe to create partial plans, because goal states are reachable from all situations
- Other domains contain dead-ends, partial planning won't guarantee success
  - Can get trapped in dead ends that we would have detected if we had planned fully
    - No applicable actions
      - ▶ robot goes down a steep incline and can't come back up
    - Applicable actions, but caught in a loop
      - ▶ robot goes into a collection of rooms from which there's no exit
  - However, partial planning can still make success more likely

# Lookahead-Partial-Plan

- Adaptation of Run-Lazy-Lookahead (Chapter 2)
- Lookahead is any planning algorithm that returns a policy  $\pi$ 
  - $\pi$  may be partial solution, or unsafe solution
  - Lookahead-Partial-Plan executes  $\pi$  as far as it will go, then calls Lookahead again

```
Lookahead-Partial-Plan( $\Sigma, s_0, S_g$ )  
   $s \leftarrow s_0$   
  while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do  
     $\pi \leftarrow \text{Lookahead}(s, \theta)$   
    if  $\pi = \emptyset$  then return failure  
    else do  
      perform partial plan  $\pi$   
       $s \leftarrow$  observe current state
```

# FS-Replan

- Adaptation of Run-Lookahead (Chapter 2)
- Calls Forward-Search (Chapter 2) on determinized domain, converts to a policy
  - Unsafe solution

FS-Replan ( $\Sigma, s, S_g$ )

$\pi_d \leftarrow \emptyset$

while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do

if  $\pi_d$  undefined for  $s$  then do

$\pi_d \leftarrow \text{Plan2policy}(\text{Forward-search}(\Sigma_d, s, S_g), s)$

if  $\pi_d = \text{failure}$  then return failure

perform action  $\pi_d(s)$

$s \leftarrow$  observe resulting state

- Generalization:
  - Lookahead can be any planning algorithm that returns a policy  $\pi$

FS-Replan ( $\Sigma, s, S_g$ ) (*generalize*)

$\pi_d \leftarrow \emptyset$

while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do

if  $\pi_d$  undefined for  $s$  then do

$\pi_d \leftarrow \text{Lookahead}(s, \theta)$

if  $\pi_d = \text{failure}$  then return failure

perform action  $\pi_d(s)$

$s \leftarrow$  observe resulting state

# Possibilities for Lookahead

- Lookahead could be one of the algorithms we discussed earlier

Find-Safe-Solution

Find-Acyclic-Solution

Guided-Find-Safe-Solution

Find-Safe-Solution-by-Determinization

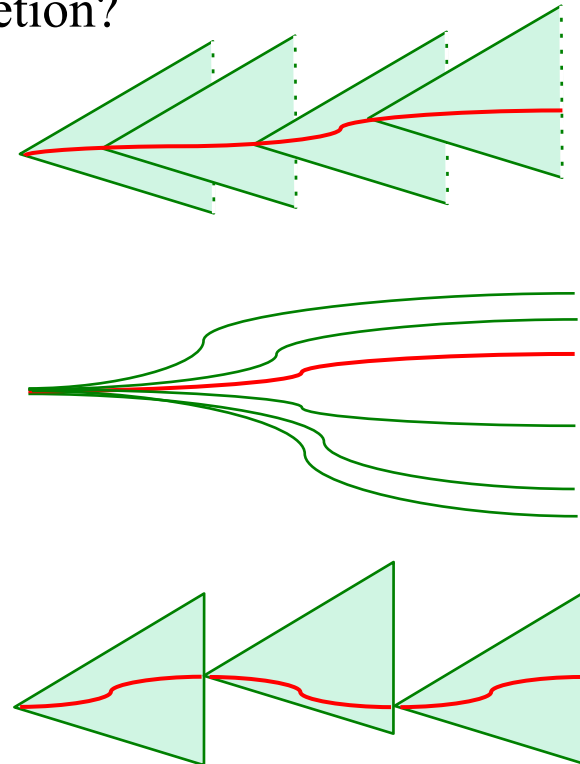
Planning

Acting

- What if it doesn't have time to run to completion?

- Can use the same techniques we discussed in Chapter 3

- Receding horizon
- Sampling
- Subgoaling
- Iterative deepening



# Possibilities for Lookahead

- *Full horizon, limited breadth:*
  - look for solution that works for *some* of the outcomes
  - E.g., modify Find-Acyclic-Solution to examine  $i$  outcomes of every action
- *Iterative broadening:*
  - for  $i = 1$  by 1 until time runs out
  - look for a solution that handles  $i$  outcomes per action

Find-Acyclic-Solution ( $\Sigma, s_0, S_g$ )

$\pi \leftarrow \emptyset$

$Frontier \leftarrow \{s_0\}$

for every  $s \in Frontier \setminus S_g$  do

$Frontier \leftarrow Frontier \setminus \{s\}$

if  $Applicable(s) = \emptyset$  then return failure

nondeterministically choose  $a \in Applicable(s)$

$\pi \leftarrow \pi \cup (s, a)$

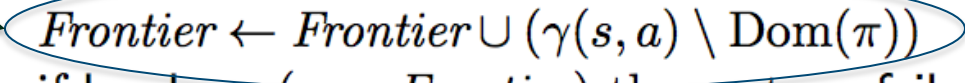
$Frontier \leftarrow Frontier \cup (\gamma(s, a) \setminus Dom(\pi))$

if  $has-loops(\pi, a, Frontier)$  then return failure

return  $\pi$

$T \leftarrow i$  elements of  $\gamma(s, a) \setminus Dom(\pi)$

$Frontier \leftarrow Frontier \cup T$





# Safely Explorable Domains

- *Safely explorable* domain
  - for every state  $s$ , at least one goal state is reachable from  $s$
- Suppose
  - We use Lookahead-Partial-Plan or FS-Replan in a safely explorable domain
  - Lookahead never returns failure
  - No “unfair” executions
- Then we will eventually reach a goal
- What would happen if we just chose a random action each time?

# Online Approaches

Min-Max LRTA\* ( $\Sigma, s_0, S_g$ )

$s \leftarrow s_0$

while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do

$a \leftarrow \operatorname{argmin}_{a \in \text{Applicable}(s)} \max_{s' \in \gamma(s,a)} h(s')$

$h(s) \leftarrow \max\{h(s), 1 + \max_{s' \in \gamma(s,a)} h(s')\}$

perform action  $a$

$s \leftarrow$  the current state

Assumes each action has cost 1  
Can easily be modified to use cost  $\neq 1$

- loop
  - choose an action  $a$  that (according to  $h$ ) has optimal worst-case cost
    - Update  $h(s)$  to use  $a$ 's worst-case cost
    - Perform  $a$
- In safely explorable domains with no “unfair” executions, guaranteed to reach a goal

# Example

Min-Max LRTA\* ( $\Sigma, s_0, S_g$ )

$s \leftarrow s_0$

while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do

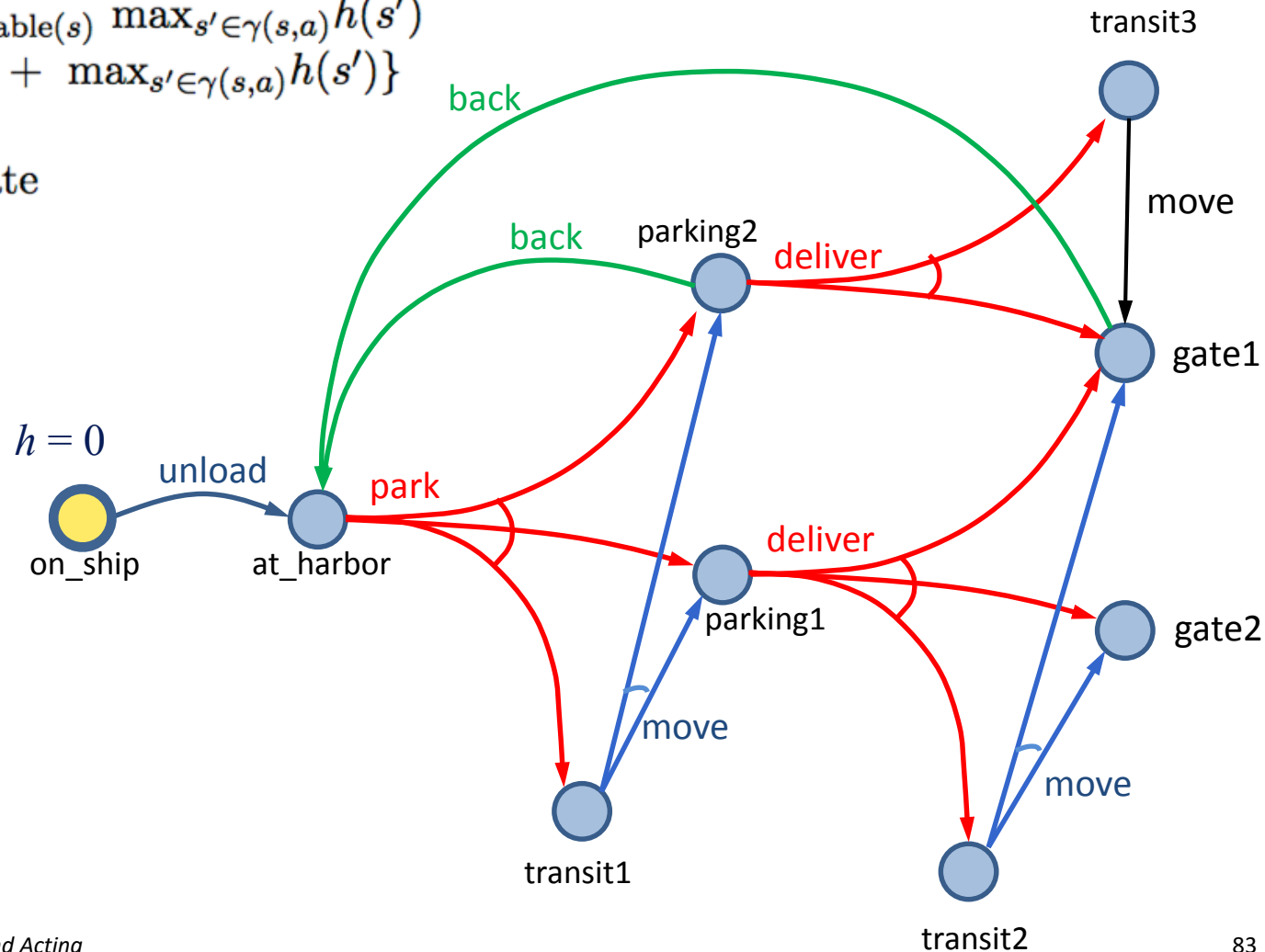
$a \leftarrow \text{argmin}_{a \in \text{Applicable}(s)} \max_{s' \in \gamma(s,a)} h(s')$

$h(s) \leftarrow \max\{h(s), 1 + \max_{s' \in \gamma(s,a)} h(s')\}$

perform action  $a$

$s \leftarrow$  the current state

- Suppose that initially,  $h(s) = 0$  for every state  $s$



# Example

Min-Max LRTA\* ( $\Sigma, s_0, S_g$ )

$s \leftarrow s_0$

while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do

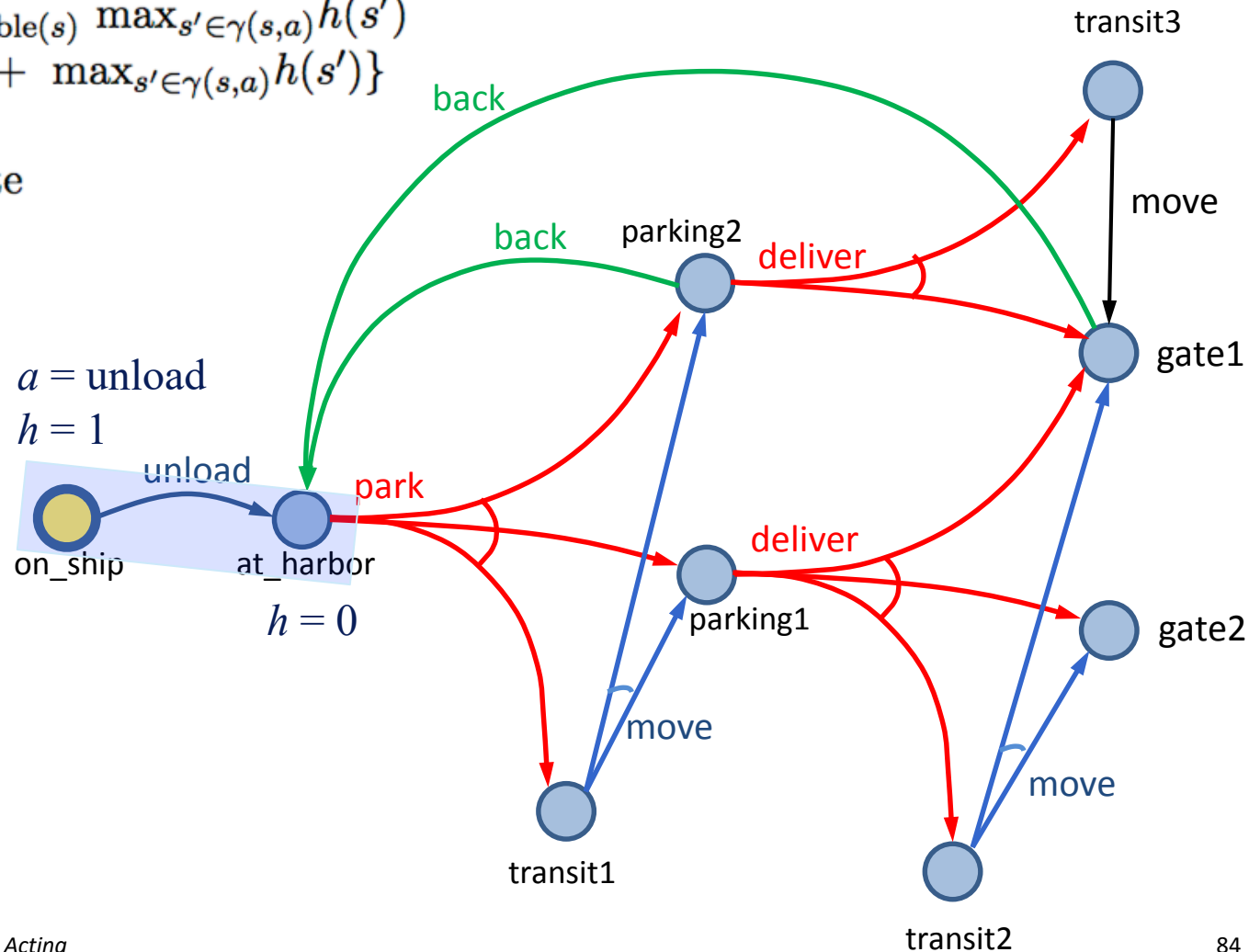
$a \leftarrow \operatorname{argmin}_{a \in \text{Applicable}(s)} \max_{s' \in \gamma(s,a)} h(s')$

$h(s) \leftarrow \max\{h(s), 1 + \max_{s' \in \gamma(s,a)} h(s')\}$

perform action  $a$

$s \leftarrow$  the current state

- Suppose that initially,  $h(s) = 0$  for every state  $s$



# Example

Min-Max LRTA\* ( $\Sigma, s_0, S_g$ )

$s \leftarrow s_0$

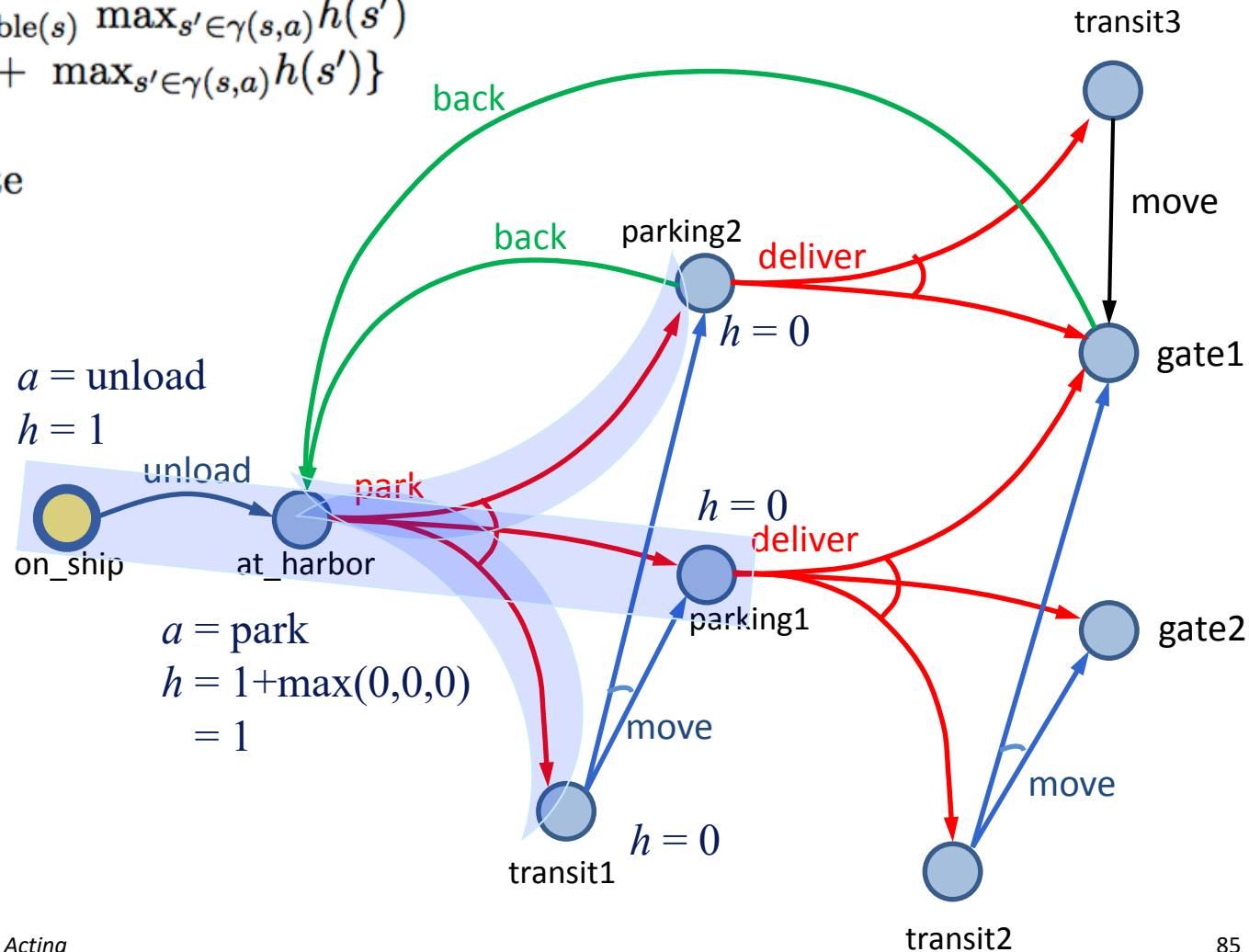
while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do

$a \leftarrow \text{argmin}_{a \in \text{Applicable}(s)} \max_{s' \in \gamma(s,a)} h(s')$

$h(s) \leftarrow \max\{h(s), 1 + \max_{s' \in \gamma(s,a)} h(s')\}$

perform action  $a$

$s \leftarrow$  the current state



# Example

Min-Max LRTA\* ( $\Sigma, s_0, S_g$ )

$s \leftarrow s_0$

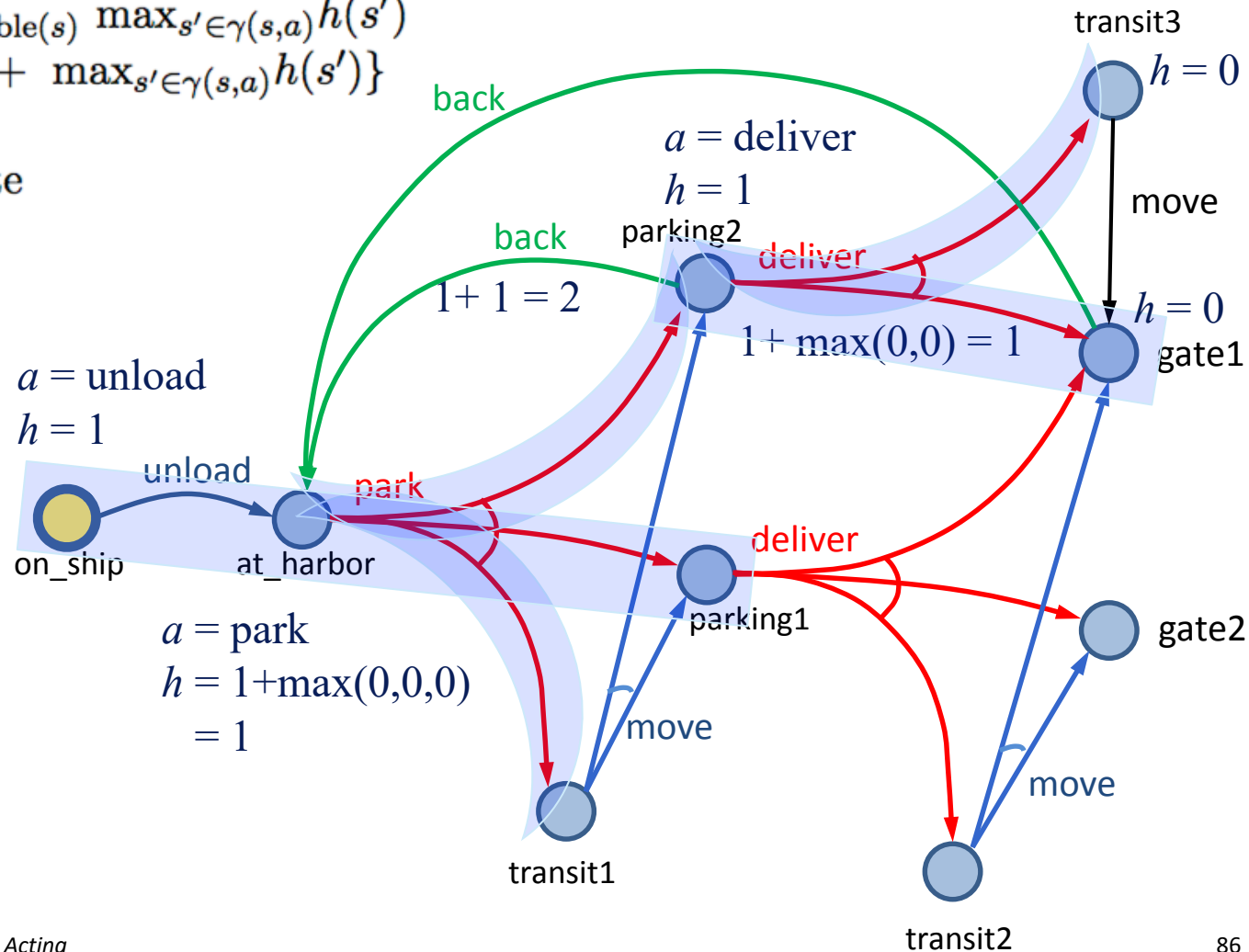
while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do

$a \leftarrow \text{argmin}_{a \in \text{Applicable}(s)} \max_{s' \in \gamma(s,a)} h(s')$

$h(s) \leftarrow \max\{h(s), 1 + \max_{s' \in \gamma(s,a)} h(s')\}$

perform action  $a$

$s \leftarrow$  the current state



## 5.7 Refinement Methods

- Differences to refinement methods in Chapter 3:
  - Tasks refine into automata
  - Need to combine the automata
- Important work, but the concepts are complicated
  - We won't have time to cover them

# Summary

- Actions, plans, policies, planning problems
- types of solutions: unsafe, cyclic safe, acyclic safe
  - algorithms for each
- Guided-find-safe-solution
  - call find-solution to get an unsafe solution
  - call find-solution additional times on the leaves
- find-safe-solution-by-determinization
  - use determinized actions
  - call classical planner rather than find-solution
  - if dead-ends are encountered, modify actions that lead to them
  
- continued on next page



# Summary

- Online approaches
  - Lookahead-partial-plan
    - adaptation of Run-Lazy-Lookahead
  - FS-replan
    - adaptation of Run-Lookahead
- ways to do the lookahead
  - full breadth with limited depth,
    - iterative deepening
  - full depth with limited breadth
    - iterative broadening
  - convergence in safely explorable domains
- min-max-LRTA\*

Can also adapt  
Run-Concurrent-Lookahead

Can put bounds on both  
depth and breadth