

# The Catering Problem

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## 1 The Catering Problem

### 1.1 Motivation

A catering company to cook  $n$  dishes, but has only one available oven. At most a single dish can be inside the oven at one time.

Each dish  $i$  has its earliest time when it can be put into the oven  $r_i$  (since it needs to be prepared before it is put into the oven), the latest time it should be taken from the oven  $d_i$  (since the customers do not want to wait too long), and the time it needs to stay in the oven  $p_i$ . The goal is to find the vector of times  $\mathbf{s} = (s_0, \dots, s_{n-1})$  (denoting the times when each dish is put into the oven) such that the finish time of the last dish is minimal.

### 1.2 Input

You are given the following: \* number of dishes  $n$  \* parameters  $r_i$ ,  $d_i$  and  $p_i$  for each dish  $i$

For the testing purposes, you can experiment with the following instance:

```
[1]: n = 5
      params = {
          0: {'r': 20, 'd': 45, 'p': 15},
          1: {'r': 4, 'd': 30, 'p': 19},
          2: {'r': 5, 'd': 80, 'p': 20},
          3: {'r': 17, 'd': 70, 'p': 8},
          4: {'r': 27, 'd': 66, 'p': 7}
      }

      # Note: parameter d_1 can be obtained by params[1]["d"]
```

### 1.3 Output

You are expected to find the vector  $\mathbf{s} = (s_0, \dots, s_{n-1})$  denoting the times when each dish should be put into the oven.

The optimal solution vector for the given instance is  $\mathbf{s} = (23, 4, 53, 38, 46)$ .

## 1.4 Exercise

Your task is to formulate the ILP model of the catering problem, solve it, and extract the vector  $s$ . The example solution follows:

Hint: to ensure that any two dishes  $i$  and  $j$  are not overlapping in the oven, you need to ensure that one of the following constraints holds:  $s_i + p_i \leq s_j$  or  $s_j + p_j \leq s_i$ . This might be perhaps done using big-M...

```
[5]: import gurobipy as grb # import Gurobi module

# model -----
model = grb.Model()

# - ADD VARIABLES
# TODO

# - ADD CONSTRAINTS
# TODO

# - SET OBJECTIVE
# TODO

# call the solver -----
model.optimize()

# print the solution -----
print('\nSOLUTION:')
# TODO
```

Optimize a model with 0 rows, 0 columns and 0 nonzeros

Coefficient statistics:

```
Matrix range      [0e+00, 0e+00]
Objective range   [0e+00, 0e+00]
Bounds range      [0e+00, 0e+00]
RHS range         [0e+00, 0e+00]
```

Presolve time: 0.01s

Presolve: All rows and columns removed

Iteration	Objective	Primal Inf.	Dual Inf.	Time
0	0.0000000e+00	0.000000e+00	0.000000e+00	0s

Solved in 0 iterations and 0.01 seconds

Optimal objective 0.000000000e+00

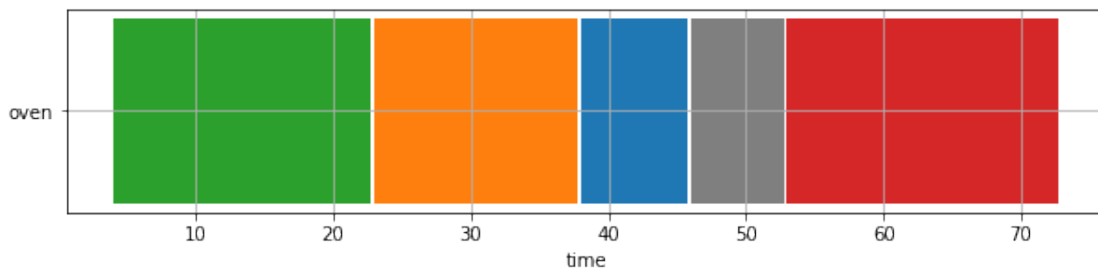
SOLUTION:

## 1.5 Solution visualization

```
[6]: import matplotlib.pyplot as plt

def plot_solution(s, p):
    """
    s: solution vector
    p: processing times
    """
    fig = plt.figure(figsize=(10,2))
    ax = plt.gca()
    ax.set_xlabel('time')
    ax.grid(True)
    ax.set_yticks([2.5])
    ax.set_yticklabels(["oven"])
    eps = 0.25 # just to show spaces between the dishes
    ax.broken_barh([(s[i], p[i]-eps) for i in range(len(s))], (0, 5),
                   facecolors=('tab:orange', 'tab:green', 'tab:red', 'tab:
→blue', 'tab:gray'))

    # TODO: plot your solution
    plot_solution([23.0, 4.0, 53.0, 38.0, 46.0], [params[i]["p"] for i in range(n)])
```



```
[ ]:
```