

Environment Representation Frontier-based Exploration MRE Information Theoretic Approaches Robotic Information Gathering Search Robotic Information Gathering Environment Representation Frontier-based Exploration MRE Information Theoretic Approaches Robotic Exploration of Unknown Environment Mobile Robot Exploration Robotic exploration is a fundamental problem of robotic information gathering. Create a map of the environment. How to efficiently utilize a group of mobile robots **Frontier**-based approach. Yamauchi (1997) to create a map of an unknown environment autonomously? Occupancy grid map. Moravec and Elfes (1985) Performance indicators vs constraints. Laser scanner sensor. Indicators – time, energy, map quality. Next-best-view approach. Select the next robot goal Constraints – no. of robots, communication.

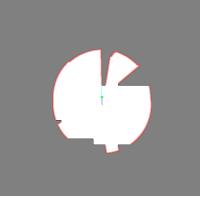
- Performance in a real mission depends on the on lin
- Performance in a real mission depends on the on-line decision-making.
- It includes multiple challenges:
 - Map building and localization;
 - Determination of the navigational waypoints; Where to go next?

Environment Representation

- Path planning and navigation to the waypoints;
- Coordination of the actions (multi-robot team).



- Performance metric, e.g., Time to create a map of the whole environment
 - vs. time to search entity in a search-and-rescue mission.



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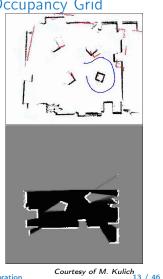
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Environment Representation – Mapping and Occupancy Grid

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- The robot uses its sensors to build a map of the environment.
- The robot should be localized to integrate new sensor measurements into a globally consistent map.
- Simultaneous Localization and Mapping (SLAM).
 - The robot uses the map being built to localize itself.
 - The map is primarily to help to localize the robot.
 - The map is a "side product" of SLAM.
- Grid map discretized world representation.
 - A cell is **occupied** (an obstacle) or **free**.
- Occupancy grid map Each cell is a binary random variable modeling the occupancy of the cell.



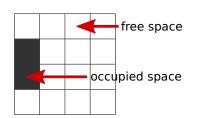
Occupancy Grid

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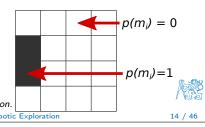
- Assumptions
 - The area of a cell is either completely free or occupied.
 - Cells (random variables) are independent of each other.
 - The state is static.
- A cell is a binary random variable modeling the occupancy of the cell, e.g.,
 - Cell m_i is occupied $p(m_i) = 1$;
 - Cell m_i is not occupied $p(m_i) = 0$;
 - Unknown $p(m_i) = 0.5$.
- Probability distribution of the map *m*
 - $p(m) = \prod_i p(m_i).$
- Estimation of the map from sensor data z_{1:t} and robot poses x_{1:t}

$$p(m|z_{1:t}, x_{1:t}) = \prod_i p(m_i|z_{1:t}, x_{1:t}).$$

Binary Bayes filter – Bayes rule and Markov process assumption.



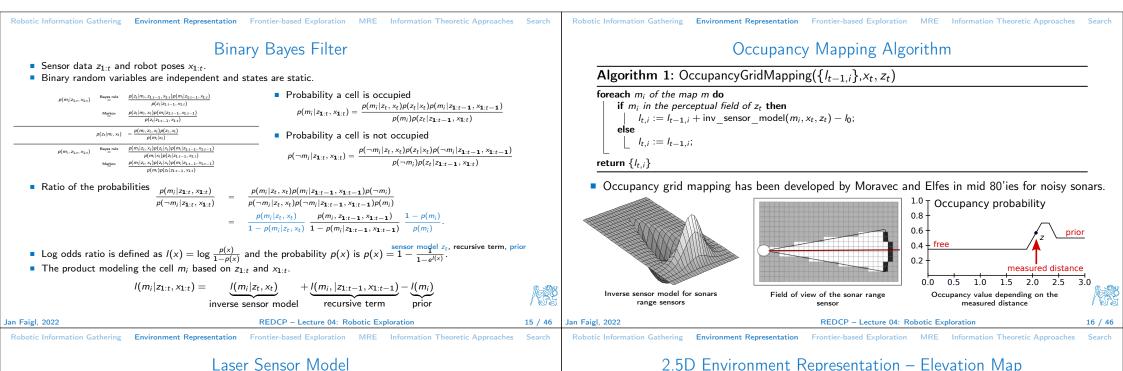
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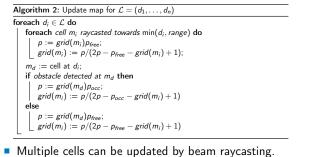
Robotic Information Gathering

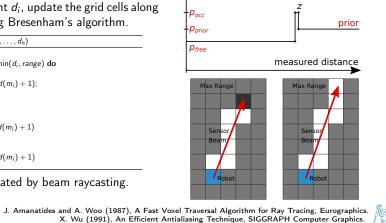


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Laser Sensor Model

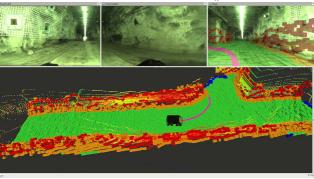
- The model is "sharp" with the precise obstacle detection.
- For the range measurement d_i , update the grid cells along a sensor beam, e.g., using Bresenham's algorithm.





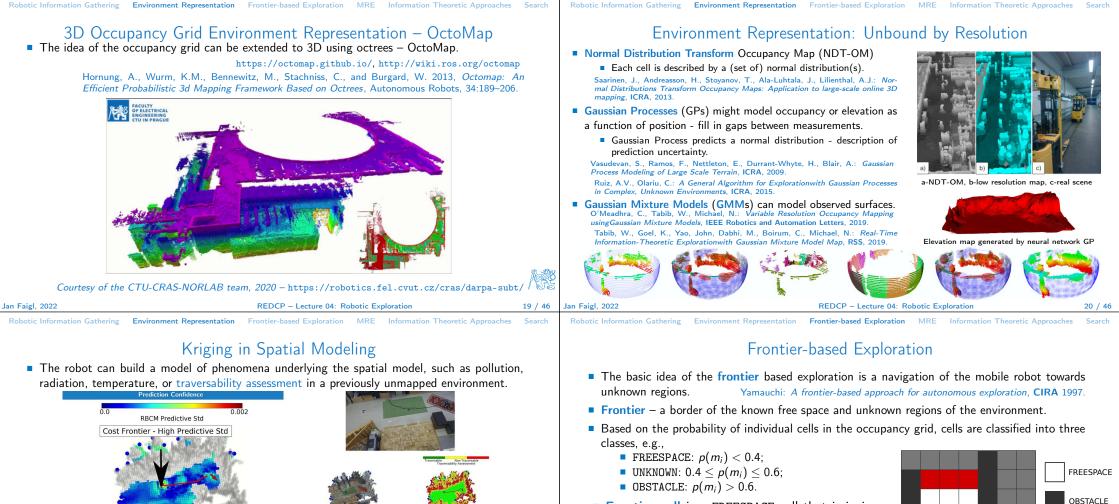
Occupancy probability

• An extension of the 2*D* occupancy map to 2.5D elevation map, where each cell includes information about the terrain elevation, e.g., using $h_k = \frac{\sigma_k^2 h_{k-1} + \sigma_{k-1}^2 z_k}{\sigma_k^2 + \sigma_{k-1}^2}$ $\sigma_k^2 = \frac{\sigma_k^2 \sigma_{k-1}^2}{\sigma_k^2 + \sigma_{k-1}^2}$ Kalman filter update for the elevation h after observation z_k



Bayer, J. and Faigl, J.: Speeded Up Elevation Map for Exploration of Large-Scale Subterranean Environ 2019 Modelling and Simulation for Autonomous Systems (MESAS), 2020, pp. 190-202.

C. Schulz and A. Zell (2019), Sub-Pixel Resolution Techniques for Ray Casting in Low-Resolution Occupancy Grid Maps, ECMR. Jan Faigl, 2022 REDCP - Lecture 04: Robotic Exploration 17 / 46



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The fidelity of the traversal cost model is improved by deliberately navigating low confidence areas, represented by high predictive std.

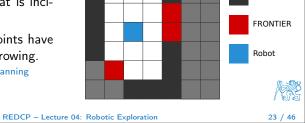
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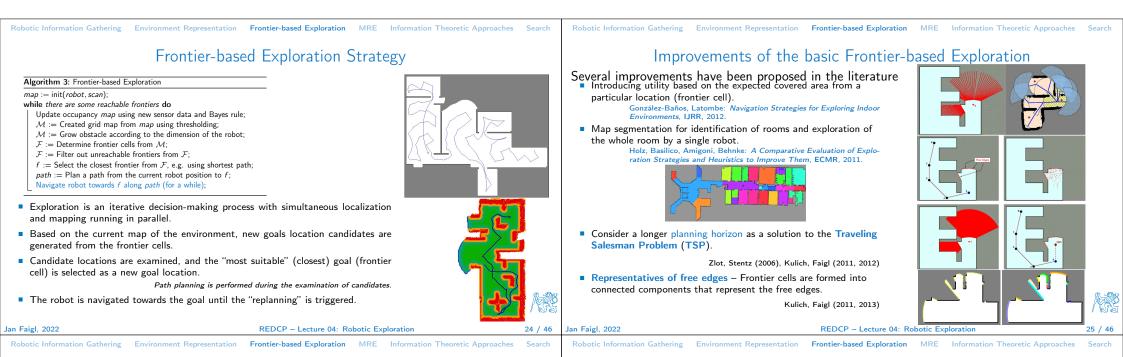
Robotics: Science and Systems (RSS), 2019.

Prágr, Čížek, Bayer, Faigl: Online Incremental Learning of the Terrain Traversal Cost in Autonomous Explorat

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- Frontier cell is a FREESPACE cell that is incident with an UNKNOWN cell.
- Frontier cells as the navigation waypoints have to be reachable, e.g., after obstacle growing. Use grid-based path planning





Variants of the Distance Cost

■ Simple robot-goal distance – *next-best view*.

- Evaluate all goals using the robot-goal distance. A length of the path from the robot position to the goal candidate.
- Greedy goal selection the closest one.
- Using frontier representatives improves the performance a bit.

TSP distance cost – Non-myopic next-best view.

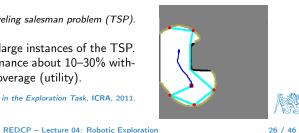
Consider visitations of all goals.

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Solve the associated traveling salesman problem (TSP).

- A length of the tour visiting all goals.
- Use frontier representatives to avoid large instances of the TSP.
- the TSP distance cost improves performance about 10–30% without further heuristics, e.g., expected coverage (utility).

Kulich, M., Faigl, J. Přeučil, L.: On Distance Utility in the Exploration Task, ICRA, 2011.



Frontier Representatives – Frontier Clusters

- An omnidirectional sensor with a non-zero sensing range can cover multiple frontier cells.
- Group frontier cells to the so-called free-edges single connected components.

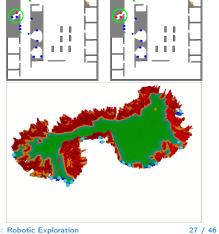


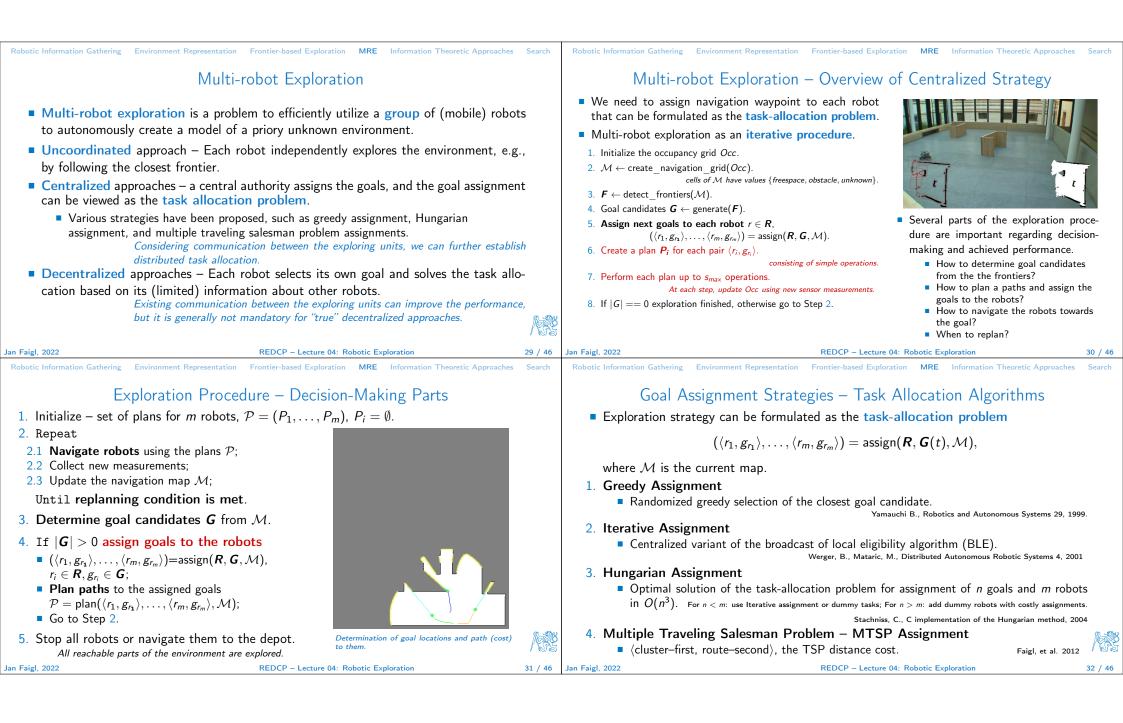
Split large clusters (of the size f) to smaller clusters that can be covered by the sensor range D; determine the number of subclusters n_r and use k-means clustering.

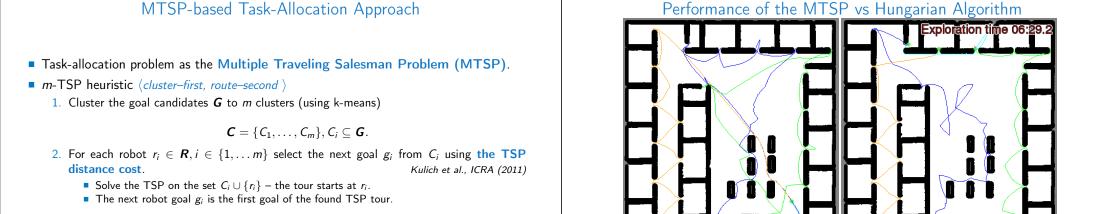
$$n_r = 1 + \left\lfloor rac{f}{1.8D} + 0.5
ight
floor$$
 .

- Faigl, J., Kulich, M., and Přeučil, L.: Goal assignment using distance cost in multi-robot exploration IROS 2012
- It reduces the number of goal candidates and yields navigation towards middle locations of the free-edges.

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Search

Faigl, J., Kulich, M., Přeučil, L.: Goal Assignment using Distance Cost in Multi-Robot Exploration, IROS 2012.

Environment Representation Frontier-based Exploration MRE Information Theoretic Approaches



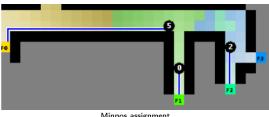
MinPos: Decentralized Exporation Strategy

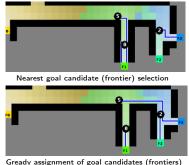
- The robot solves the task allocation based on its (limited) information about other robots.
- Assumption: the distance cost matrix C between robots R and frontiers F are known to all robots.
 In practice, it requires the robots to share the map of the whole environment, which might not be feasible, and therefore, approximations can be employed.
- Each robot ranks each frontier using the relative distance of the robots to the frontier cell (goal candidate).

Robotic Information Gathering

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• The robot is assigned the goal with the minimum rank.





Bautin, A., Simonin, O., Charpillet, F.: MinPos: A Novel Frontier Allocation Algorithmfor Multi-robot Exploration, ICIRA, 2012. Faigl, J., Simonin, O., Charpillet, F.: Comparison of Task-Allocation Algorithms in Frontier-Based Multi-robot Exploration, European Conference on Multi-Agent Systems, EUMAS, 2014. REDCP – Lecture 04: Robotic Exploration 35 / 46

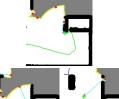
Influence of Decision-Making – Exploration Strategy

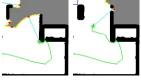
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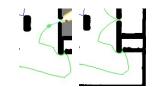
- The exploration performance depends on the whole solution, albeit we can have "best" possible solutions of each part.
- Locally optimal Hungarian algorithm might not necessarily provide better solutions than for example the MTSP-based approach.
- A solution of the particular sub-task (i.e., goal candidate selection) might have side effects that are exhibited during the missions depending on the utilized exploring technic.
 - depending on the utilized navigation technique.
 - Vector Field Histogram (VFH) slows down the robot close to the obstacles.

Borenstein, J. and Koren, Y.: The vector field histogram-fast obstacle avoidance for mobile robots, IEEE Transactions on Robotics, 1991.

A side effect of the representatives of free edges is that goal candidates are "in the middle of free-edges" and the robot is navigated towards them, which results in faster motion because it is relatively far from the obstacles.







Robotic Information Gathering Environment Representation Frontier-based Exploration MRE Information Theoretic Approaches Search

Information Theory in Robotic Information Gathering

- Frontier-based exploration assumes perfect knowledge about the robot states and the utility function depends only on the map.
- We can avoid such assumption by defining the control policy as a rule how to select the robot action that reduces the uncertainty of estimate by learning measurements:

 $\operatorname{argmax}_{a \in A} I_{MI}[x; z|a],$

where A is a set of possible actions, x is a future estimate, and z is future measurement

Mutual information – how much uncertainty of x will be reduced by learning z

$$I_{MI}[x;z] = H[x] - H[x|z],$$

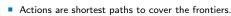
where H[x] is the current entropy, and H[x|z] is future/predicted entropy.

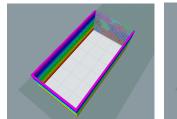
• Conditional Entropy H[x|z] is the expected uncertainty of x after learning unknown z (collecting new measurements).

Actions

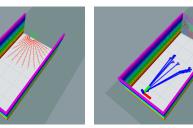
• Entropy – uncertainty of x: $H[x] = -\int p(x) \log p(x) dx$.

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Detect and cluster frontiers Sampled poses to cover a cluster Select an action (a path) that maximizes the rate of Cauchy-Schwarz Quadratic Mutual Information

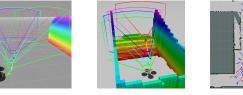


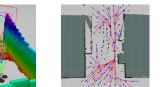
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Computing Mutual Information in Exploration

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- Sensor placement approach with raycasting of the sensor beam and determination of the distribution over the range returns.
- Precise computing of the mutual information is usually not computationally feasible given the size of the action set and the uncertainty of action results.
- We can assume that observation removes all uncertainty from observed areas

$$H_{MI}[x;z] = H[x] - H[x|z] \approx H[x].$$

- Then, we can decrease the computational requirements by using simplified approach where the action is selected to maximize the entropy over the sensed regions in the current map.
- We are maximizing mutual information in the sensor placement problem of observing the region with maximum entropy

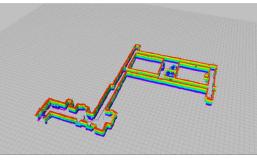
$$\operatorname{argmax}_{a \in A} \sum_{x \in \mathcal{R}(a)} H[p(x)],$$

where R(a) represents the region sensed by the action a. Bourgault, F., Makarenko, A.a., Williams, S.B., Grocholsky, B., Durrant-Whyte, H.F.: Information based

adaptive robotic exploration, IROS, 2002. Computational cost can be decreased using Cauchy-Schwarz Quadratic Mutual Information (CSQMI) defined similarly to mutual information. Can be evaluated analytically for occupancy grid mapping. Charrow, B., Liu, S., Kumar, V., Michael, N.: Information-theoretic mapping using Cauchy-Schwarz Quadratic Mutual Information, ICRA 2015.

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Example of Autonomous Exploration using CSQMI





Ground vehicle

Aerial vehicle

Planning with trajectory optimization – determine trajectory maximizing I_{CS}.

Charrow, B., Kahn, G., Patil, S., Liu, S., Goldberg, K., Abbeel, P., Michael, N., Kumar, V.: Information-Theoretic Planning with Trajectory Optimization for Dense 3D Mapping. Robotics: Science and Systems (RSS), 2015.

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