



DCGI

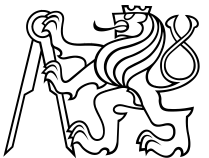
KATEDRA POČÍTAČOVÉ GRAFIKY A INTERAKCE

APG – Color

JIŘÍ ŽÁRA

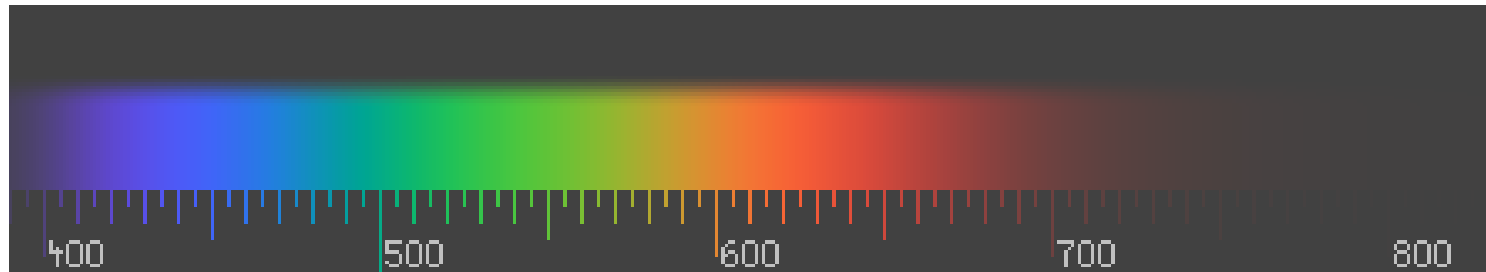
Contents

- 1) Principles of color perception, colorimetry
 - Light, color, perception
 - Colorimetry, comparison of colors
- 2) Color models in technical applications
 - RGB, CMY(K), HSV, HLS, YUV, YC_bC_r
 - CIE L^*a^*b , CIE Luv



Visible light

- EM (electro-magnetic) radiation cca 380nm – 720nm
- Retina (human eye) is sensitive to



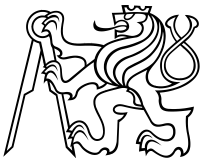
- Light is a *physical phenomenon*
- Physics can describe light properties and behavior
[Physics \Leftarrow 😊 \Rightarrow Computer Graphics]



Color

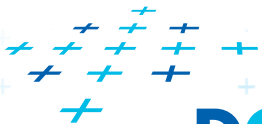
- Perception (individual)
- No (direct) relation with physics
- Color description relates to psychology

- *What is “dark blue”? “army green”? “rosy”?*



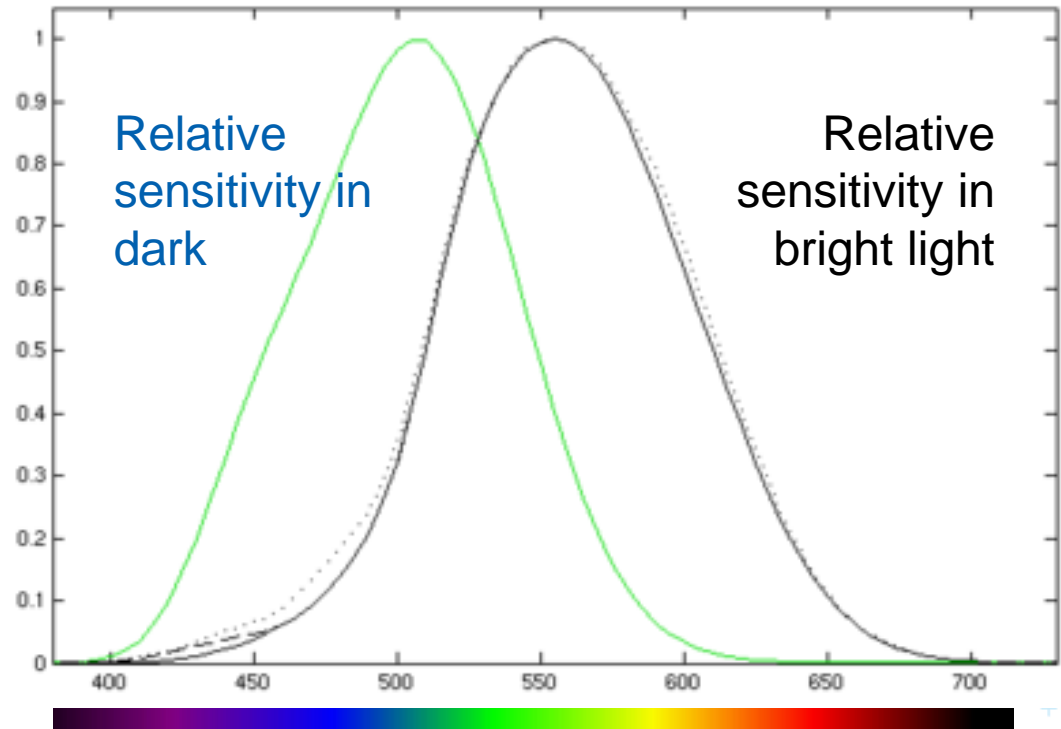
Human Eye

- Light passes through lens and falls to **retina** (array of photoreceptor **cells**):
 - Cone cells [*čípky*]
 - 3 kinds responsive to three different wavelengths - L / M / S (long / medium / short wavelength) – approx. Red/ Green / Blue
 - Essential for **color perception**
 - Bright light is required
 - Rod cells [*tyčinky*]
 - Activated in low intensity of light – *scotopic* (night) vision
 - Saturated during the day light (*photopic* intensity) – no signal produced
 - 1 kind only – monochrome, black & white vision => impossible to distinguish colors in dark



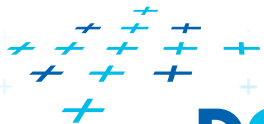
Luminance curve

- How we perceive intensity according to wavelength



- *Purkyně shift:*

- Change in the brightness of red and blue colors as light intensity decreases
- Example: Red paper looks brighter than the blue one during the day, while reversely in the dark.



Jan Evangelista Purkyně

* 1787, Libochovice

† 1869, Praha

- Medicine, poetry, philosophy, ...
- Idea: „*Cell is the most important entity for a life*“ [1837, Prague]

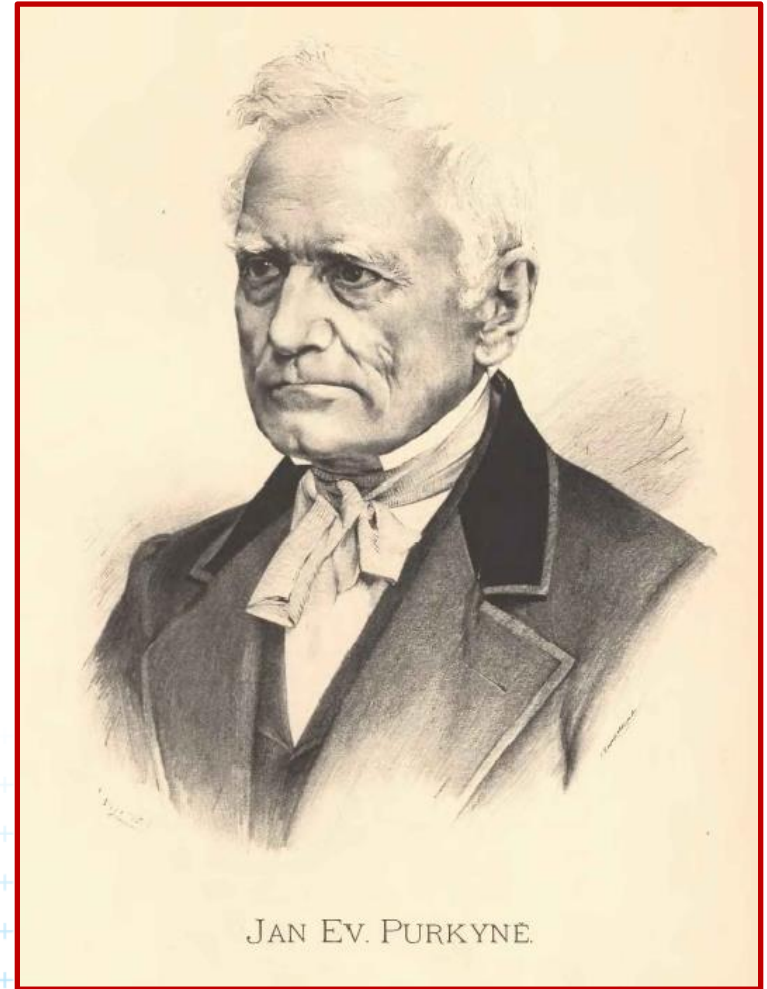
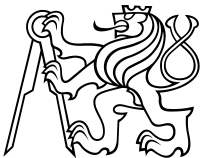


Image source: Wikipedia



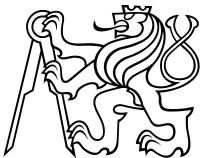
What influences the color perception?

■ A. Light Source

- **Spectral radiance**, $L(\lambda)$: quantity of (emitted) radiation of specific wavelength λ within a given angle in a given direction. [$\text{W sr}^{-1} \text{m}^{-2} \text{Hz}^{-1}$] [$\text{W sr}^{-1} \text{m}^{-2} \text{nm}^{-1}$] [záře]
 - **Radiance**: total emission (non-spectral), [$\text{W sr}^{-1} \text{m}^{-2}$]
- Influences human eye adaptation
 - People tend to consider light as white, even if it is not

■ B. Material properties of lighted object(s)

■ C. Perceptual processes in an eye and a brain

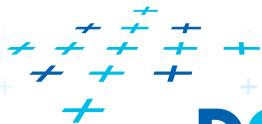


What influences the color perception?

- A. Light source
- B. Material properties of lighted object(s)
 - Spectral reflectivity, reflectance $\rho(\lambda)$ [*odrazivost*]

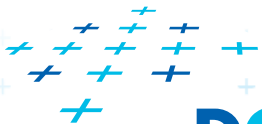
$$L_{\text{reflected}}(\lambda) = L_{\text{incoming}}(\lambda) \rho(\lambda)$$

- C. Perceptual processes in an eye and a brain
 - Radiance $L(\lambda)$ falling in the eye (i.e. function of wavelengths) is „decoded“ by brain as something like:
 - **Hue** – dominant color [*odstín*]
 - **Saturation** – how far is the color from gray of equal intensity [*sytost*]
 - **Lightness** – perceived intensity of reflecting object [*jas*]
Note: **Brightness** – when object is emitter



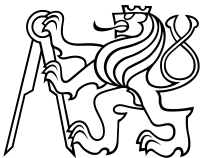
Colorimetry

- Studies human perception of colors – how spectral radiance is interpreted by humans
- (Historical) questions:
 - a) Are 2 different spectral radiances perceived as 2 colors?
 - No! Human eye is not a perfect spectrophotometer.
 - b) Under which conditions 2 spectral radiances are perceived as the same color?
 - c) Is it possible to find „clear“, basic colors (**primaries**) and make all visible colors by mixing these primaries?
 - d) If yes, how to define the intensities of primaries for a given spectral radiance, which make the same color perception?



Colorimetry

- The key is the characteristics of cones in retina:
 - What are responses of S, M, L cones for a given radiance?
- Answers to previous questions:
 - Ad b)
 - If responses of S, M, L cones to different spectral radiances are equal then the same color is perceived.
 - Ad c) + d)
 - **GOOD NEWS:** Since we have 3 types of cones, human perception is 3-dimensional (only!), thus we can use/mix 3 primaries to define all visible colors.
 - **BAD NEWS:** Those primaries need to have also negative coefficients/intensities! (physically impossible)

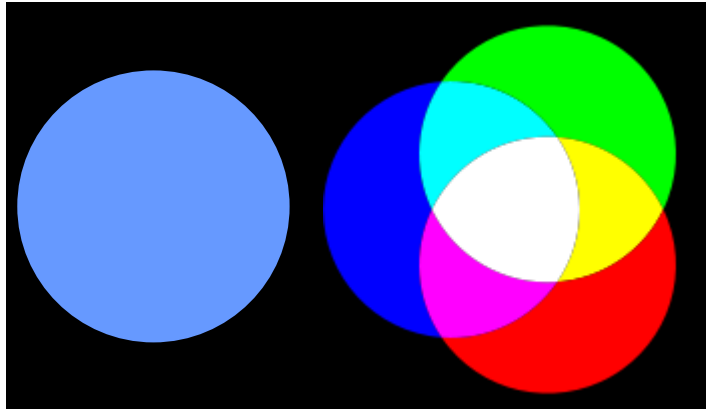


Color matching experiment

- Colorimetry tool used in the 19th and 20th century:

Left:

Real color
projected from
projector



Right:

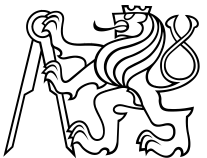
Three primaries
(monochromatic
colors) projected and
overlaid (additive
composition)

- Task for a human: Set the intensities of primaries on the right to reach the same color as on the left.
- Solve the “visual equation”: $C_{\text{real}} = C_R + C_G + C_B$

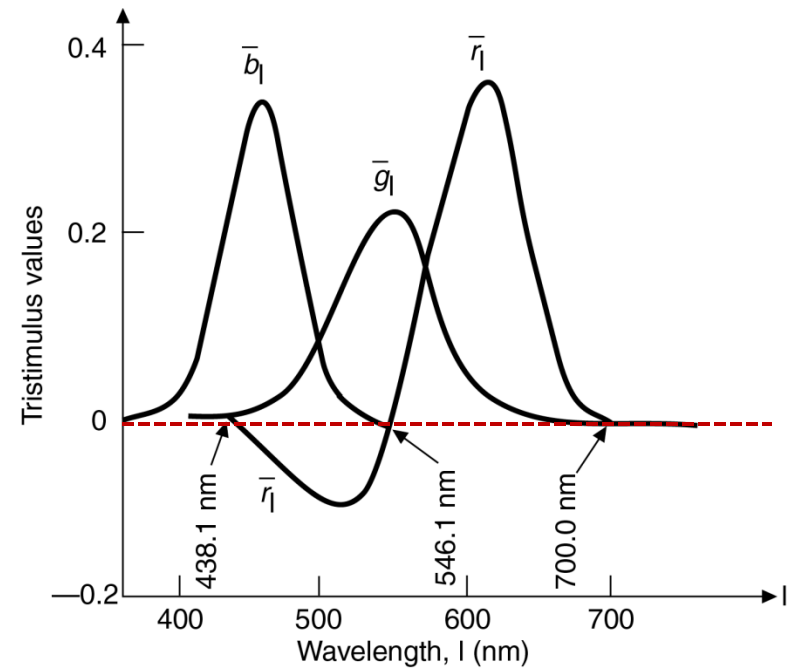
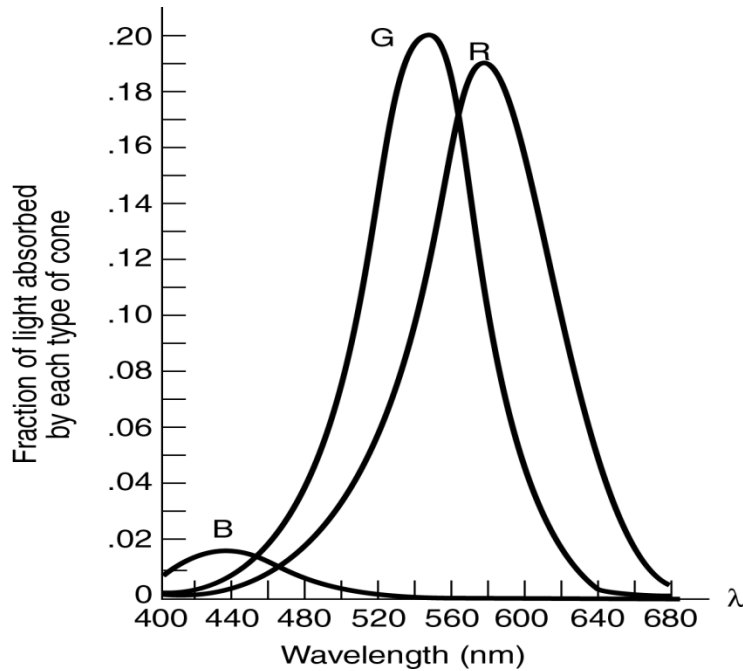


Color matching experiment results

- Two primaries are not enough (as expected...)
- Three primaries are enough, but in some cases the mixed color has a lower saturation than the real color on the right:
 - If red primary is added to **left** color, the same perception is reached.
 - Instead of **adding** red to the left, we could **subtract** red from the **right** => mathematically we add red with **negative** intensity (negative coefficient c_R) to the right.
 - This stands for all possible three primaries ☹.



Cones and Primaries



■ Cone responses

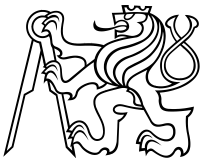
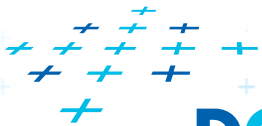
■ Required tri-stimulus values

Images from [Foley, van Dam, 1990]



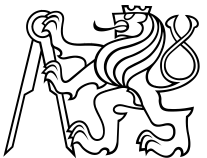
Conclusions

- No triple of primaries (with positive coeffs.) can be found to make **all** visible colors.
- Each triple of primaries defines limited range/amount (**gamut**) of colors.
- Theoretically, having negative coeffs., it would be possible to make **all** colors from only three primaries.

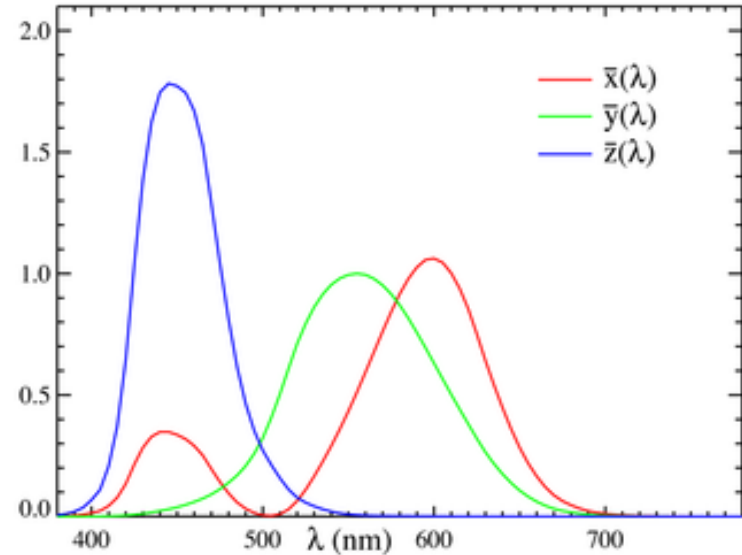
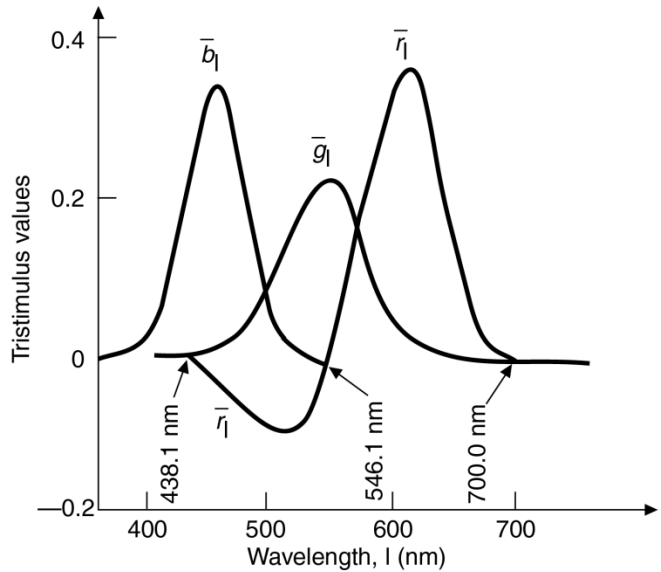


CIE XYZ Color Model

- **CIE: Commission Internationale de l'Eclairage (1931)**
 - Defines international standards
- **Disadvantage of RGB primaries**
 - Composition with positive coeffs. does not make all colors
- **Artificial color space CIE XYZ**
 - Newly designed X, Y, Z color primaries (non-real)
 - All X, Y, Z functions positive
 - The idea: Make all colors by composing X, Y, Z only



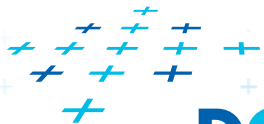
CIE XYZ Color Model



■ Theoretical RGB primaries

■ XYZ primaries

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \frac{1}{b_{21}} \begin{bmatrix} b_{11} & b_{12} & b_{13} \\ b_{21} & b_{22} & b_{23} \\ b_{31} & b_{32} & b_{33} \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix} = \frac{1}{0.17697} \begin{bmatrix} 0.49 & 0.31 & 0.20 \\ 0.17697 & 0.81240 & 0.01063 \\ 0.00 & 0.01 & 0.99 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

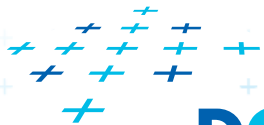
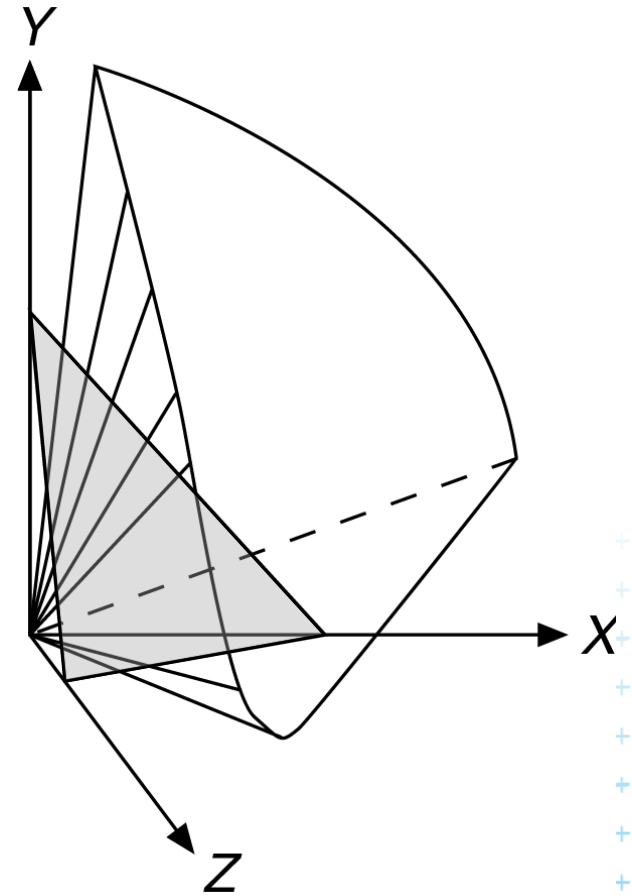


DCGI



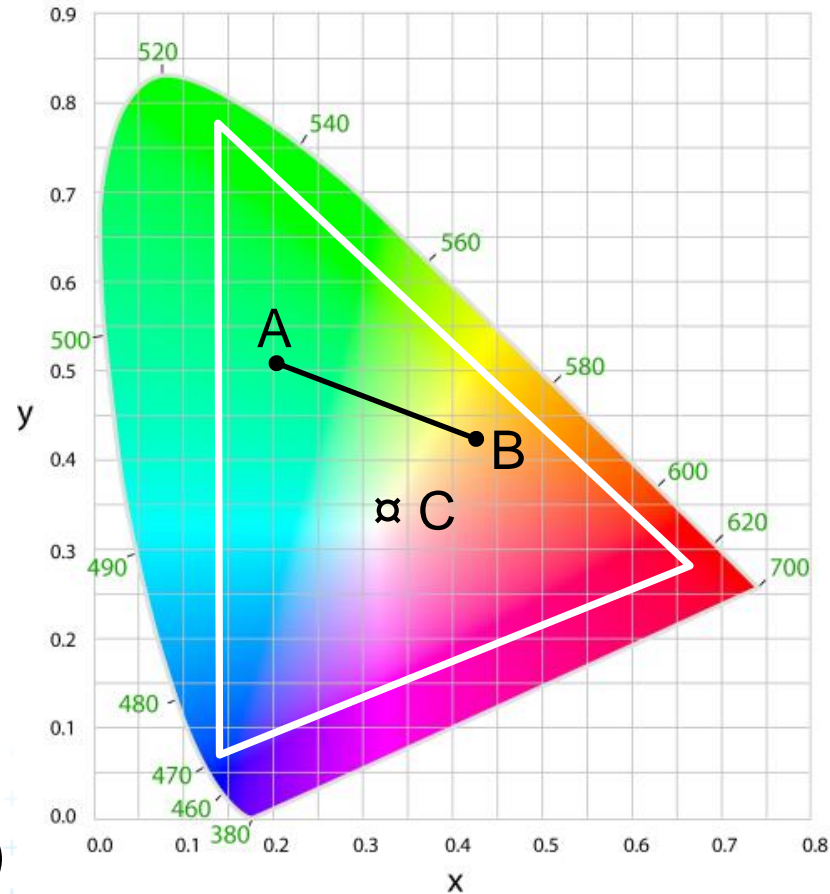
CIE XYZ Color Model

- Cone of visible colors in CIE XYZ space
- $X+Y+Z=1$ plane is shown:
 - Constant luminance
 - Only depends on dominant wavelength and saturation

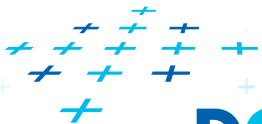


CIE Chromaticity Diagram

- Colors on $X+Y+Z=1$ plane
- Normalization \Rightarrow 2D space:
$$x = \frac{X}{X+Y+Z} \quad y = \frac{Y}{X+Y+Z}$$
- Colors on the right are symbolical only:
 - No chance to show them all on RGB devices.
 - C ... white (grey)
 - Triangle = **gamut**
 - Linear combination (gamut, AB)
 - Outline = discrete spectral colors



[\[http://www.rp-photonics.com/rgb_sources.html\]](http://www.rp-photonics.com/rgb_sources.html)



DCGI



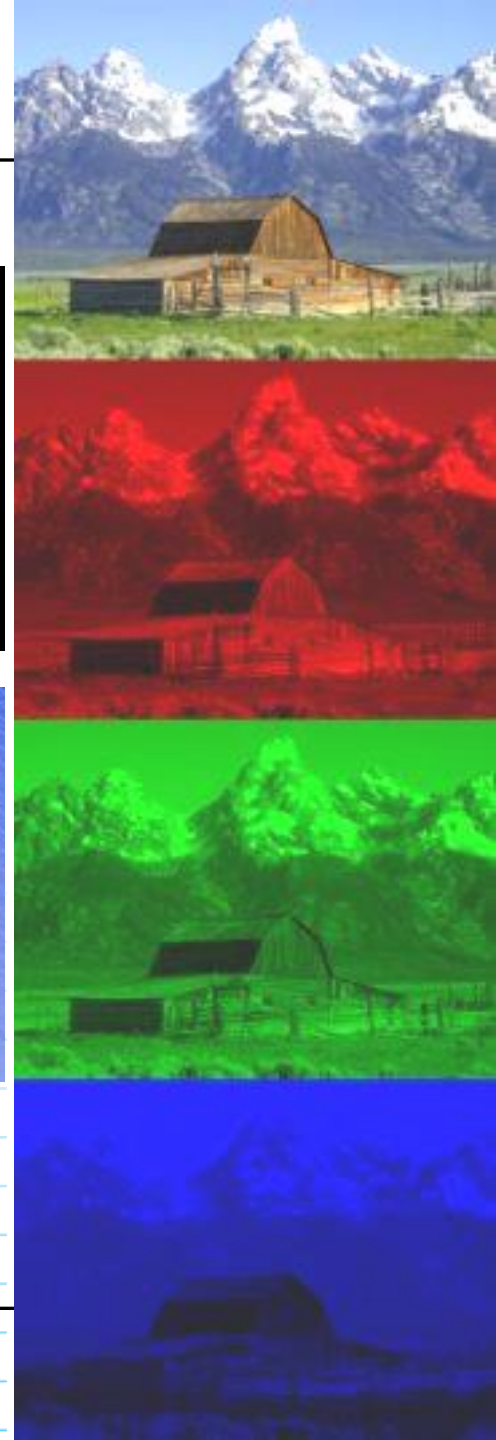
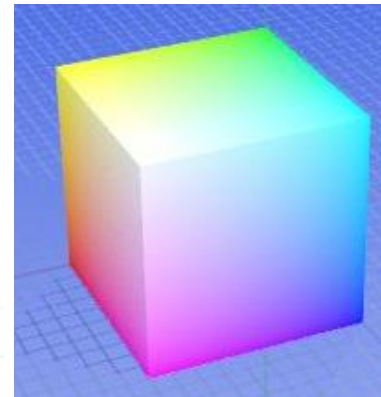
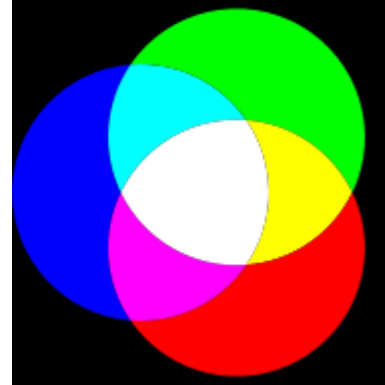
Content

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 - Light, color, perception
 - Colorimetry, comparison of colors
- 2) Color models in technical applications
 - RGB, CMY(K), HSV, HLS, YUV, YC_bC_r
 - CIE L^*a^*b , CIE Luv



RGB = Red Green Blue

- For TVs, monitors, projectors
- Additive color composition
 - Corresponds to adding light (e.g. emitted by LED)
 - $[0,0,0]$ = black
 - $[1,1,1]$ = white
- RGB cube
 - Visualization of RGB space
- Luminance of RGB color:
 - $0.299 r + 0.587 g + 0.114 b$
 - Various formulas in various apps



RGB = Red Green Blue

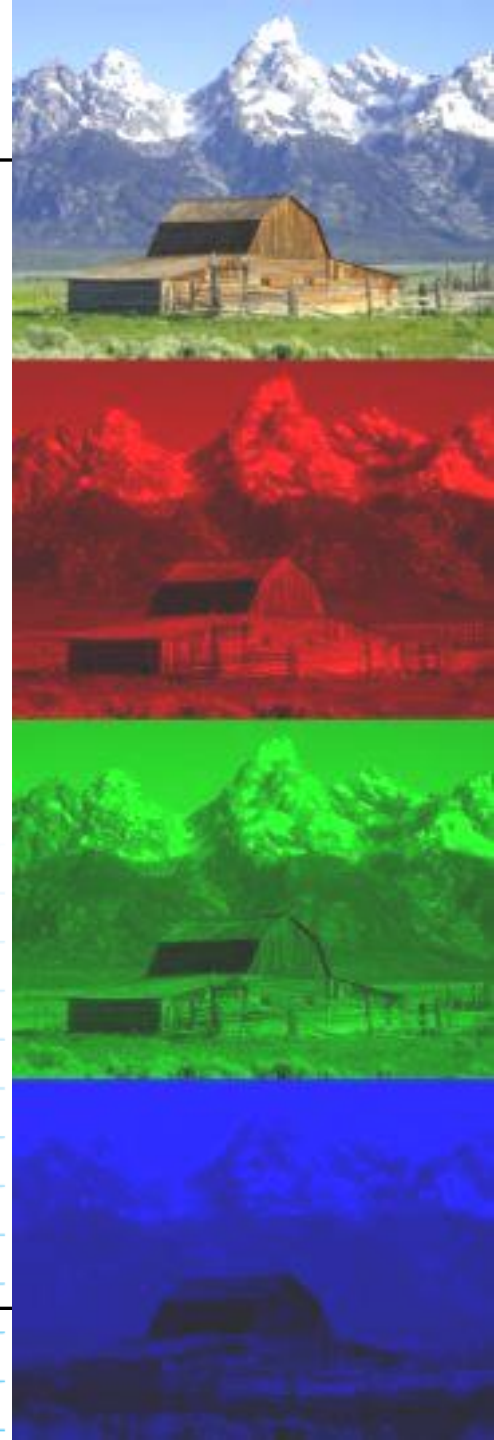
■ Many different RGB spaces:

– Standards

- CIE RGB 1931
- sRGB (for web)

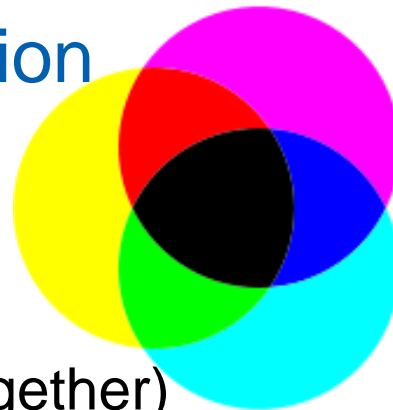
– Every output device has its „own“ RGB space

– RGB image without calibration information is useless (in professional applications).



CMY = Cyan Magenta Yellow

- For printing devices
- Subtractive color composition
 - Corresponds to mixing color pigments in paintings
 - $[0,0,0]$ = white (paper color)
 - $[1,1,1]$ = black (all pigments together)



- Conversion RGB => CMY

$$[C, M, Y] = [1 - R, 1 - G, 1 - B]$$



CMYK = CMY + black

- Low quality of black when mixed from several color pigments
 - Add black pigment among primary colors
 - Save other pigments

- Conversion CMY \Rightarrow CMYK

$$K = \min\{C', M', Y'\}$$

$$t_{CMYK} = \left\{ \frac{C' - K}{1 - K}, \frac{M' - K}{1 - K}, \frac{Y' - K}{1 - K}, K \right\}$$

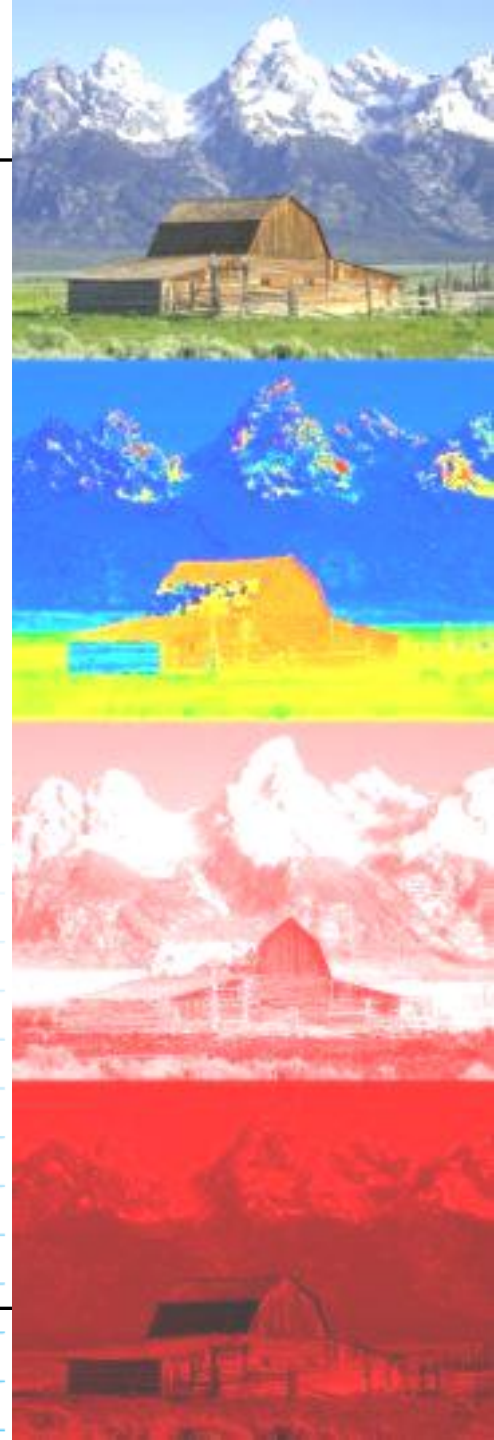


CMY



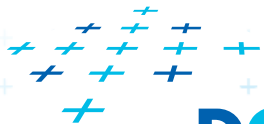
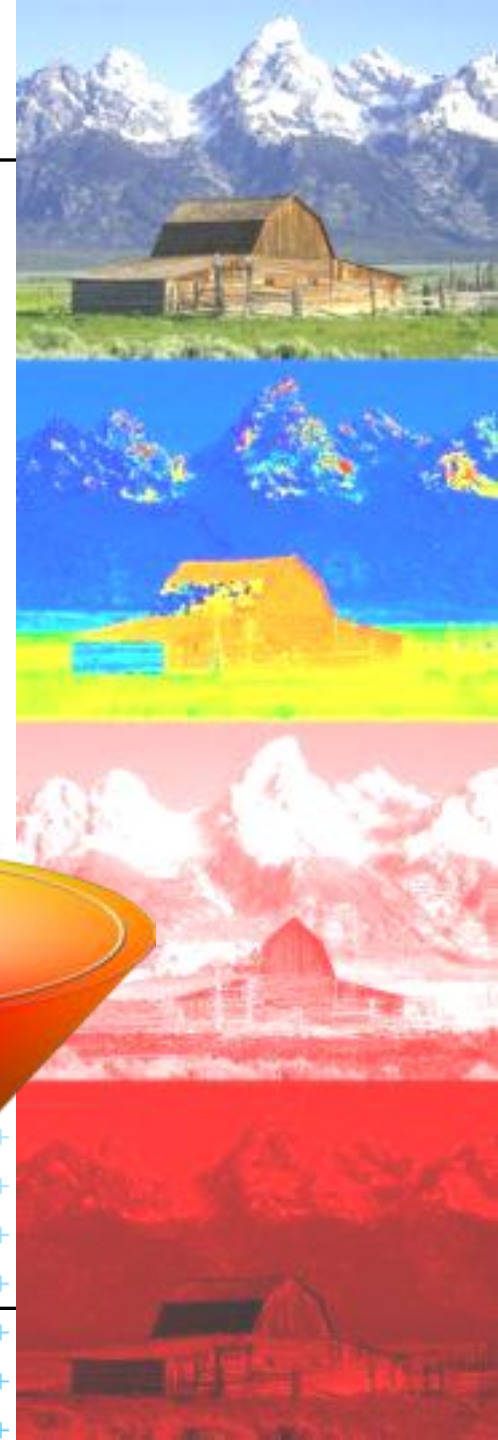
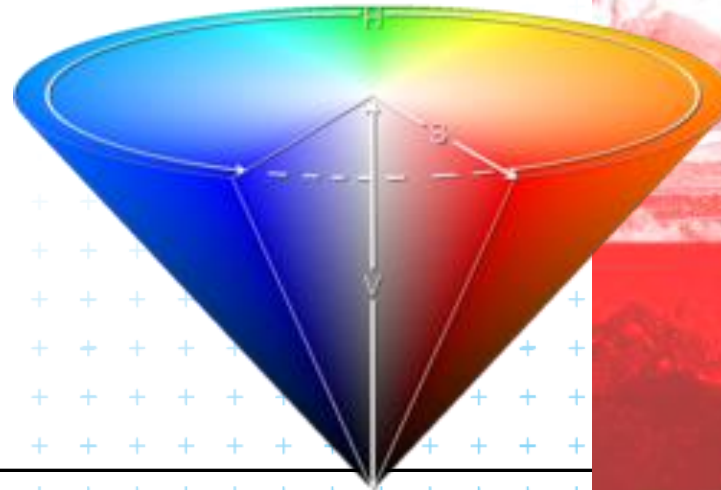
HSV = Hue Saturation Value

- Human-Computer interface for color selection
- Corresponds to human perception terms:
 - H (Hue)
 - S (Saturation)
 - V (Value)



HSV = Hue Saturation Value

- H ... angle
 - Color tones order:
R Y G C B M
- S ... distance from central axis
 - Saturated colors on a surface
 - Grey(s) in axis (where H is undefined!)
- V ... distance from the cone top
 - Top – black
 - Base – the highest lightness



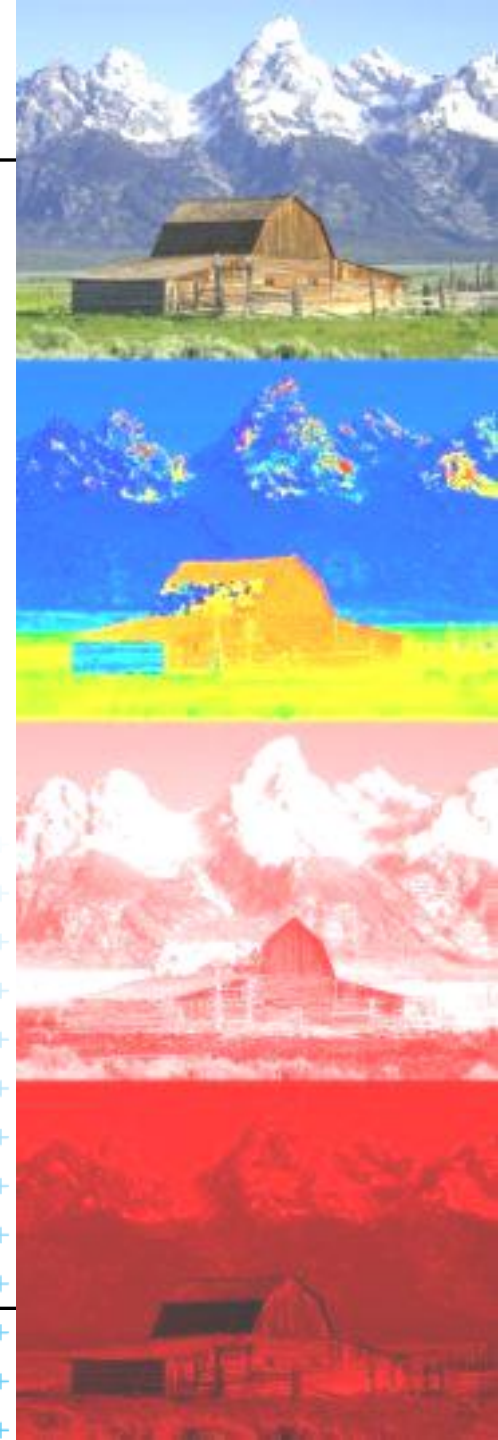
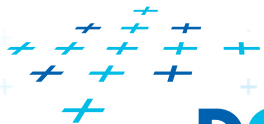
HSV: Conversion

■ RGB => HSV

$$H = \begin{cases} \text{undefined,} & \text{if } MAX = MIN \\ 60 \times \frac{G-B}{MAX-MIN} + 0, & \text{if } MAX = R \text{ and } G \geq B \\ 60 \times \frac{G-B}{MAX-MIN} + 360, & \text{if } MAX = R \text{ and } G < B \\ 60 \times \frac{B-R}{MAX-MIN} + 120, & \text{if } MAX = G \\ 60 \times \frac{R-G}{MAX-MIN} + 240, & \text{if } MAX = B \end{cases}$$

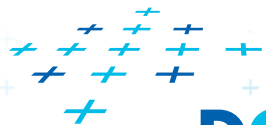
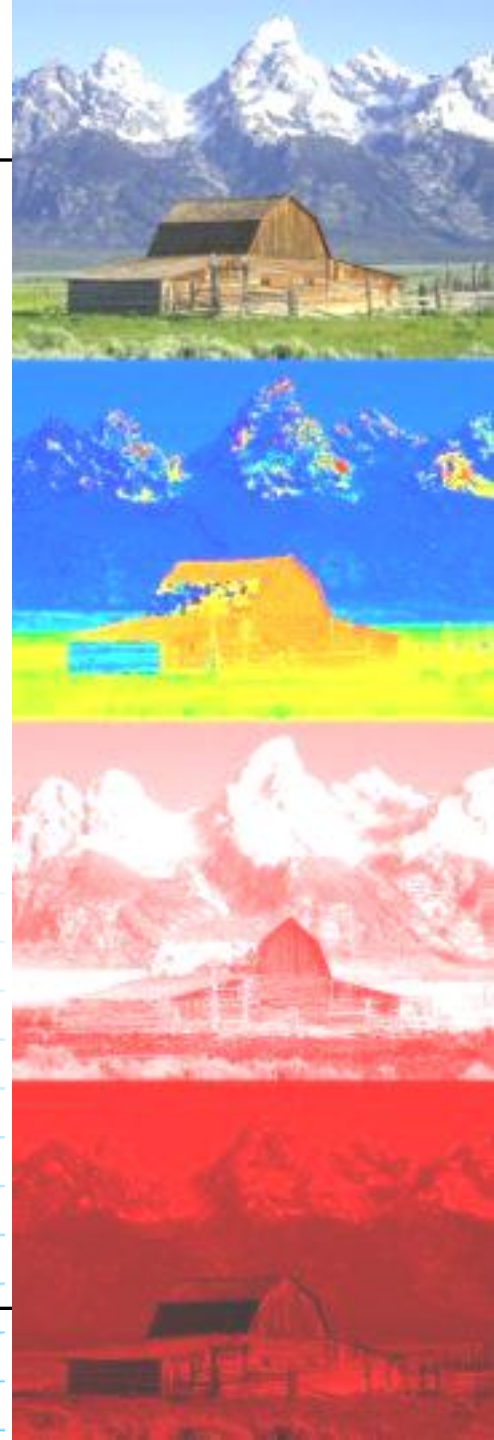
$$S = \begin{cases} 0, & \text{if } MAX = 0 \\ 1 - \frac{MIN}{MAX}, & \text{otherwise} \end{cases}$$

$$V = MAX$$



HSV in user interfaces

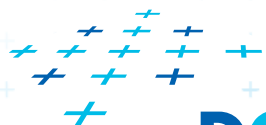
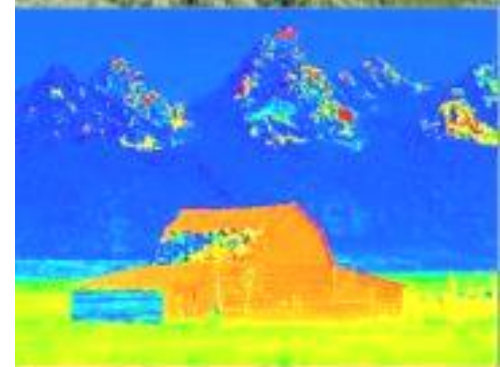
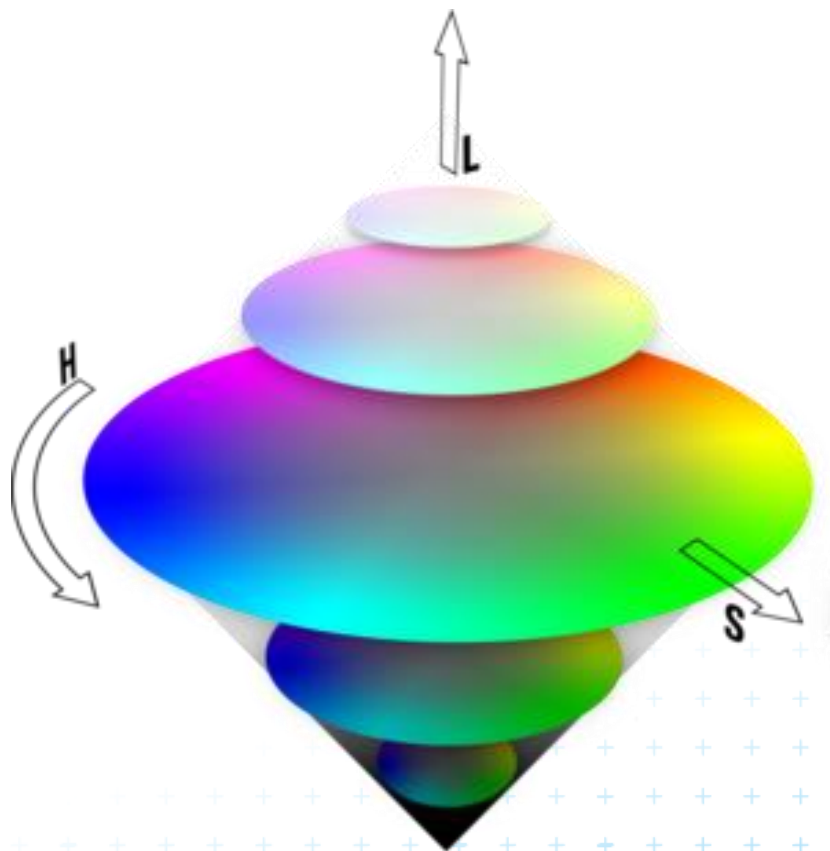
- Orientation of a triangle – H
- Inside a triangle – S, V



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HLS = Hue Lightness Saturation

- Similar to HSV, but symmetrical



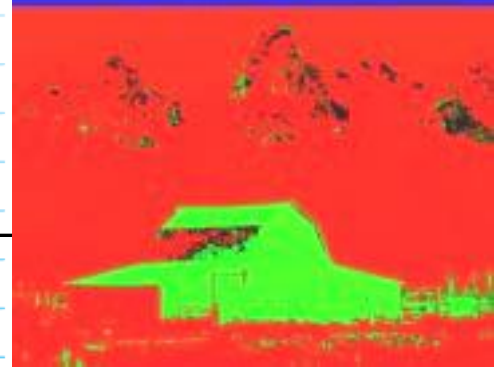
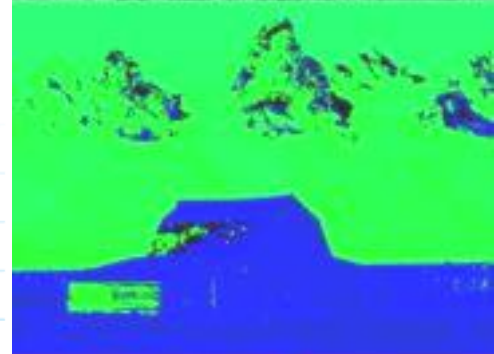
YUV

- TV signal transmission in PAL standard
- **Y** ... brightness
- **UV** ... color/hue components (chroma)
- Conversion RGB => YUV:

$$Y = +0.299 R + 0.587 G + 0.114 B$$

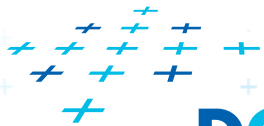
$$U = -0.1471 R - 0.288 G + 0.436 B$$

$$V = +0.615 R - 0.514 G - 0.100 B$$



Y Cb Cr

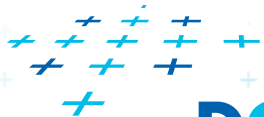
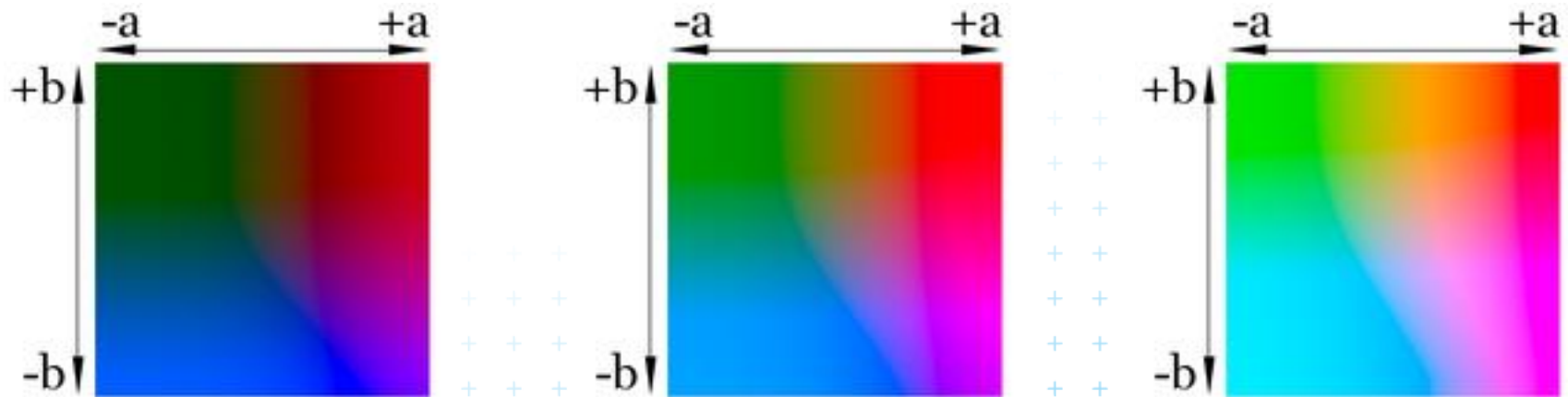
- For digital video
- in JPEG compression algorithm



DCGI

CIE L*a*b (CIELAB)

- Absolute color space (device independent)
- Non-linear compression of CIE XYZ colors
- Perceptually uniform (almost)
 - Euclidian distance in CIELAB corresponds to perceived color differences

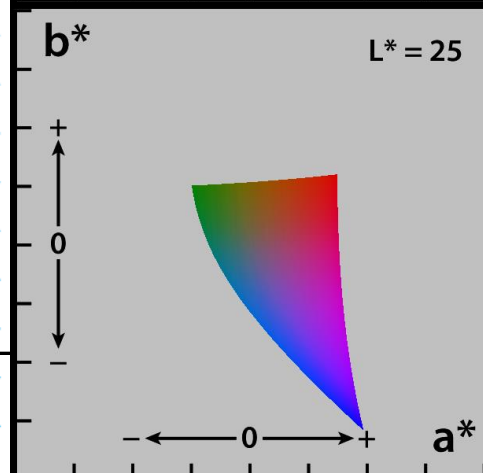
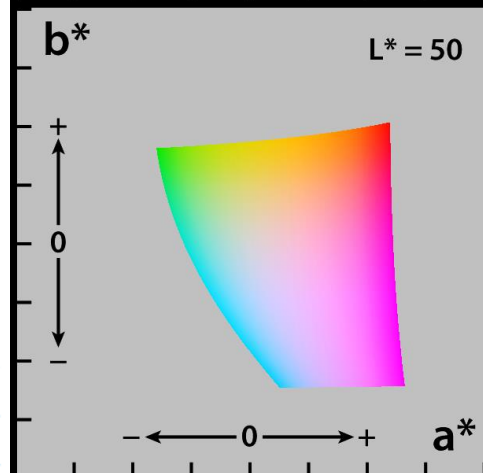
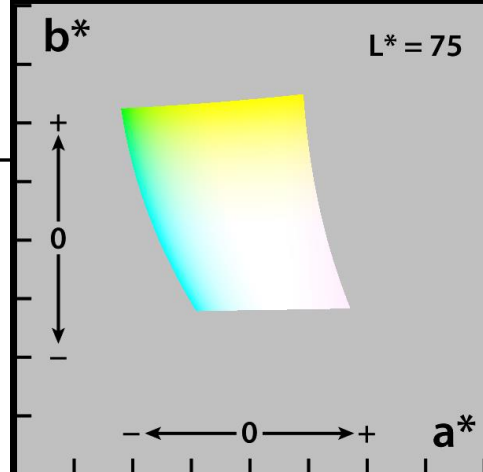


DCGI



CIE L*a*b (CIELAB)

- Impossible to display all CIELAB colors in specific device(s) – due to limited device gamut(s)
- L^* ... brightness
- a^* , b^* ... color opponent dimensions:
 - a^* ... red \Leftrightarrow green
 - b^* ... yellow \Leftrightarrow blue



CIE Luv

- Similar to CIE L*a*b*
- L*a*b* is considered to be better than Luv
- Luv used in historical reasons now (backward compatibility)



Thank you for your attention

Jiří Žára, 25.11.2015

