

# Partially observable Markov decision processes

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<https://cw.fel.cvut.cz/wiki/courses/b4b36zui/prednasky>







# Partial observability

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- MDPs work with the assumption of complete observability
  - assumption that the actual state  $s$  is always known is often non realistic,
  - examples
    - \* physical processes such as a nuclear reactor, complex machines,
    - \* we do know the physical laws that underlie the process,
    - \* we know the structure and characteristics of the machine and its parts,
    - \* however, do not know the initial state and subsequent states, can only measure temperature,
    - \* or have signals from various (unreliable) sensors.



# Partial observability

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- partially observable Markov decision process (POMDP)
  - MDP generalization, states guessed from observations coupled with them,
  - POMDP =  $\{S, A, P, R, O, \Omega\}$ ,
    - \*  $O$  is a set of observations,
    - \*  $\Omega$  is a sensoric model that defines conditional observation probs

$$\Omega_{s'o}^a = Pr\{o_{t+1} = o \mid s_{t+1} = s', a_t = a\}$$

- instead of  $s$  agent internally keeps prob distribution  $b$  (**belief**) across states
  - \* we perform  $a$  in unknown  $s$  (knowing  $b(s)$  only) and observe  $o$ ,
  - \* then we update our belief

$$b'(s') = \eta \Omega_{s'o}^a \sum_{s \in S} P_{ss'}^a b(s)$$

- \*  $\eta$  is a normalization constant such that  $\sum_{s' \in S} b'(s') = 1$ .

# Partial observability

- consequences of partial observability
  - it makes no sense to concern policy  $\pi : S \rightarrow A$ , shift to  $\pi : B \rightarrow A$ ,
  - commonly computationally intractable, approximate solutions only
    - \* for  $n$  states,  $b$  is an  $n$ -dimensional real vector,
    - \* PSPACE-hard, worse than NP.

























