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Frequent itemsets, association rules

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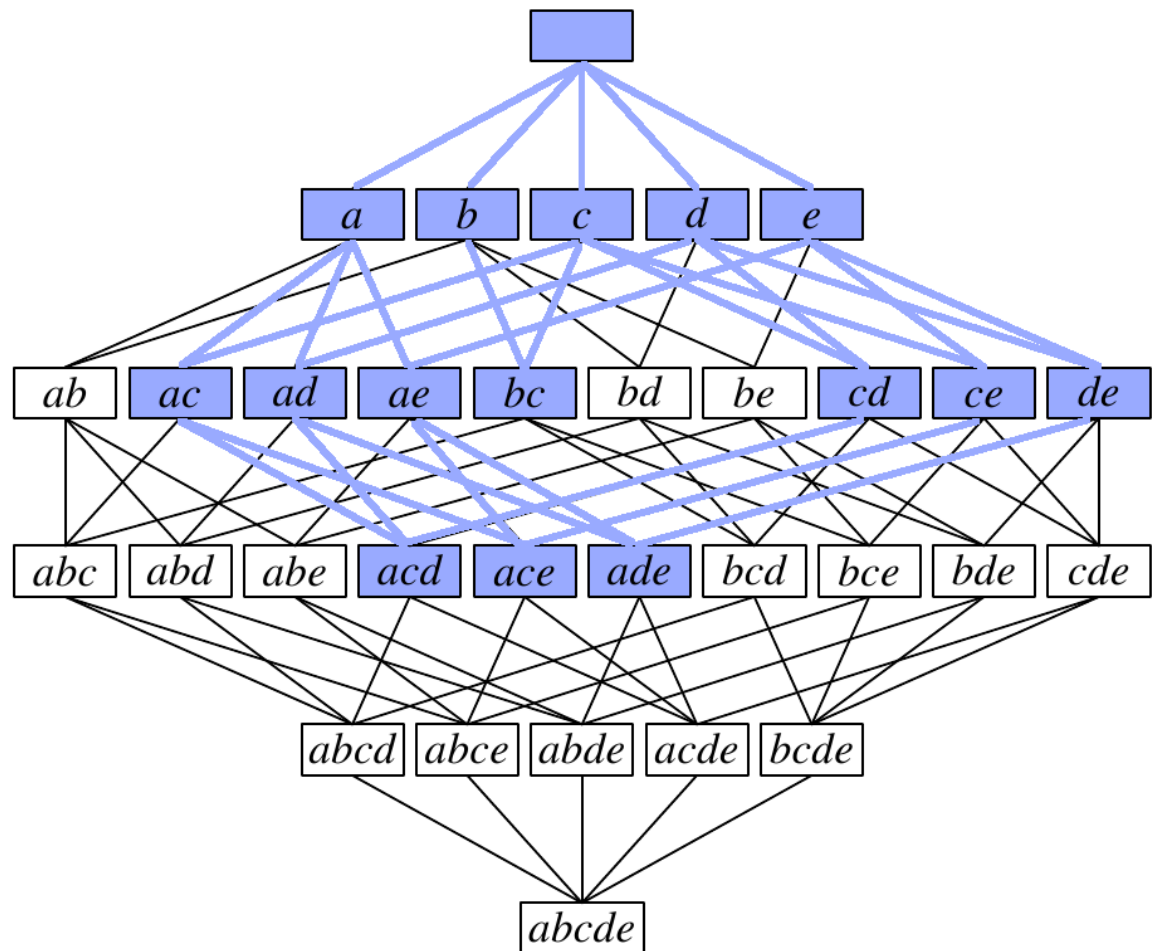
APRIORI algorithm – the basic idea

- pioneering, the most well-known, but not the most efficient,
- based on the elemental characteristic of any frequent itemset:
Each subset of a frequent itemset is frequent.
- as we proceed bottom-up from subsets to supersets
the logical **contraposition** principle
$$(p \Rightarrow q) \Leftrightarrow (\neg q \Rightarrow \neg p)$$
- the anti-monotone property transformed to a monotone property, consequence:
No superset of an infrequent itemset can be frequent.
- candidate itemsets
 - potentially frequent – all the subsets are known to be frequent.
- APRIORI categories: breath-first search, horizontal transaction representation.

Frequent itemset mining – example

the lattice with frequent itemsets for $s_{min} = 3$

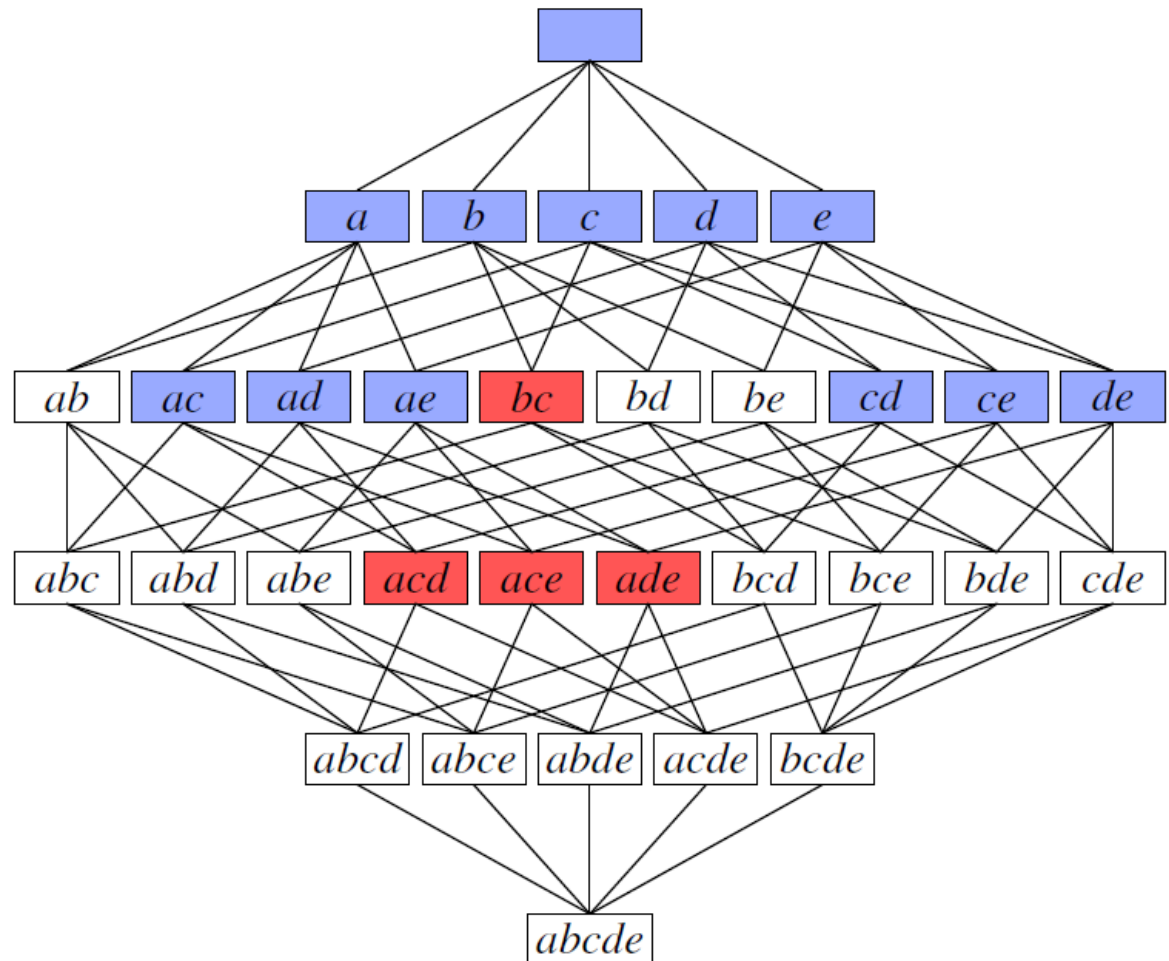
Transakce	Položky
t_1	a, d, e
t_2	b, c, d
t_3	a, c, e
t_4	a, c, d, e
t_5	a, e
t_6	a, c, d
t_7	b, c
t_8	a, c, d, e
t_9	b, c, e
t_{10}	a, d, e



Reducing the output – illustration

- the frequent itemsets for $s_{min} = 3$ (blue), the maximal itemsets (red),
- how many frequent itemsets are not closed?, which itemsets?

Transactions	Items
t_1	a, d, e
t_2	b, c, d
t_3	a, c, e
t_4	a, c, d, e
t_5	a, e
t_6	a, c, d
t_7	b, c
t_8	a, c, d, e
t_9	b, c, e
t_{10}	a, d, e



Example: the study plan

- Aim: find out whether the real study plans correspond with recommendations/study programs
- Courses: RZN (Knowledge representation), PAH (Planning and games), VI (Computational intelligence), MAS (Multi-agent systems), SAD (Machine learning and data analysis), AU (Automatic reasoning)

Transactions	Items
t_1	RZN
t_2	VI, SAD, AU
t_3	PAH, AU
t_4	PAH, VI, AU
t_5	PAH, MAS
t_6	VI, AU
t_7	PAH, SAD
t_8	PAH, VI, MAS, AU
t_9	PAH
t_{10}	PAH, VI, AU

Transactions	Items
t_{11}	AU
t_{12}	RZN, PAH, VI, SAD, AU
t_{13}	PAH, VI, MAS, AU
t_{14}	VI, SAD, AU
t_{15}	PAH, AU
t_{16}	SAD, AU
t_{17}	RZN, PAH, SAD
t_{18}	PAH, VI, MAS, AU
t_{19}	PAH
t_{20}	PAH, VI, MAS, AU

Recommended reading, lecture resources

:: Reading

- Agrawal, Srikant: **Fast Algorithms for Mining Association Rules.**
 - the article that introduced the task and proposed APRIORI algorithm,
 - <http://rakesh.agrawal-family.com/papers/vldb94apriori.pdf>,
- Borgelt: **Frequent Pattern Mining.**
 - slides, a detailed course, including a formal notation,
 - <http://www.borgelt.net/teach/fpm/slides.html>,
- Hájek, Havránek: **Mechanizing Hypothesis Formation.**
 - a pioneering theory from 1966, decades before Agrawal,
 - <http://www.cs.cas.cz/hajek/guhabook/>.





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