

KATEDRA POČÍTAČOVÉ GRAFIKY A INTERAKCE

# Introduction to 3D geometry

Jiří Bittner

# Outline

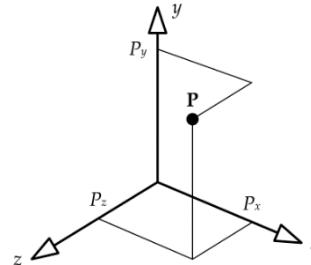
- Points, Vectors, Transformations MPG – chapter 21
  - Camera and Projection MPG – chapter 9
  - 3D Scene Representation MPG - chapters 5.11, 5.12, 5.13, 6-8, 14

# Points in 3D

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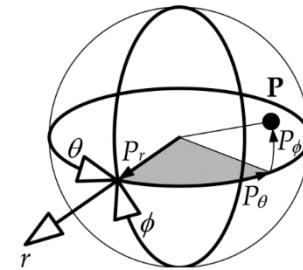
- Point is a location in 3D space

$$P = \begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$$



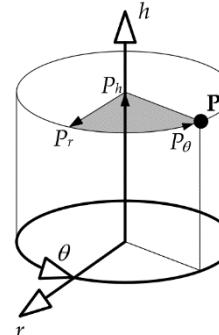
- Cartesian coordinates
  - Orthonormal basis

$$P = \begin{bmatrix} 90^\circ \\ 20^\circ \\ 1 \end{bmatrix}$$



- Spherical coordinates

$$P = \begin{bmatrix} 90^\circ \\ 3 \\ 1 \end{bmatrix}$$



- Cylindrical coordinates

(3)

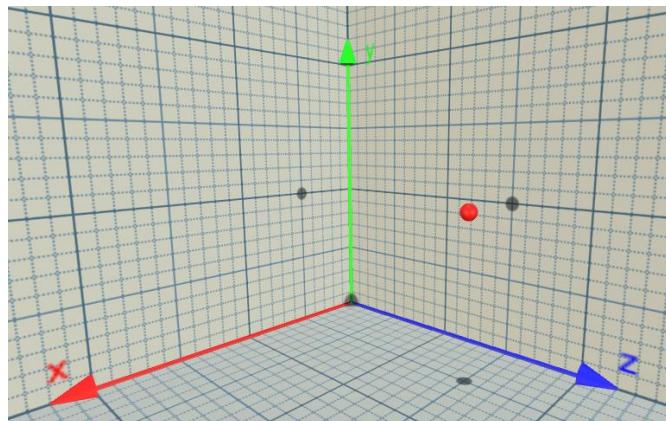
# Cartesian coordinates

- Axes (René Descartes, 1596-1650)

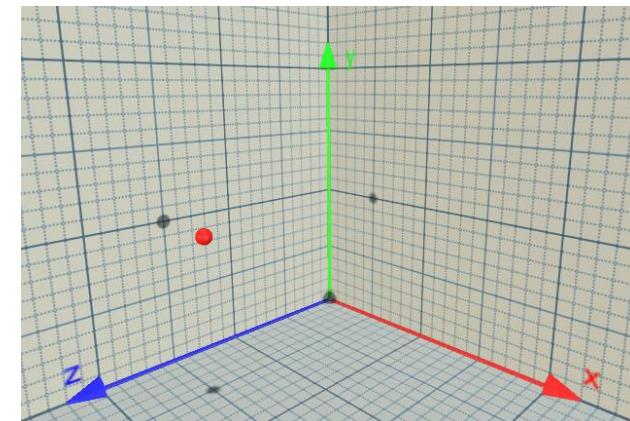
- Orthogonal directions
- Meet at origin
- Uniform scale
- Orthogonal basis

$$A = [5, 10, 15]$$

$$A = \begin{bmatrix} 5 \\ 10 \\ 15 \end{bmatrix}$$



LHS  
Direct3D, Unity, ...



RHS  
OpenGL

# Linear Transformations

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- Scale (Uniform + Non-uniform)
- Mirror
- Shear
- Rotation

$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} 3 \times 3 \\ transformation \\ matrix \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

# Homogeneous coordinates

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- Need also: translation, perspective projection
- Add 4-th coordinate

$$\begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \rightarrow \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} \approx \begin{bmatrix} x_h \\ y_h \\ z_h \\ w \end{bmatrix} \quad x = \frac{x_h}{w}, y = \frac{y_h}{w}, z = \frac{z_h}{w}$$

- For directions (points in infinity)  $w = 0$

# Transformation in homogeneous coordinates

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- Finally normalize (divide by w)
  - Perspective division

$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} & 4 \times 4 \\ transformation & matrix \\ & \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

$$\begin{bmatrix} x'' \\ y'' \\ z'' \\ \end{bmatrix} = \begin{bmatrix} \frac{x'}{w'} \\ \frac{y'}{w'} \\ \frac{z'}{w'} \end{bmatrix}$$

# Composing transformations

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- Matrix multiplication

$$M = R \cdot T \cdot S \dots$$

- Associative

$$A \cdot (B \cdot C) = (A \cdot B) \cdot C$$

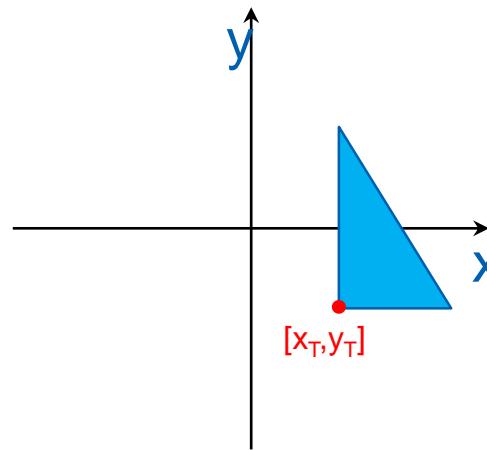
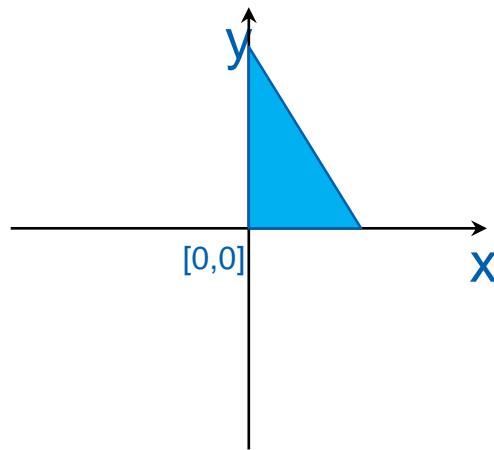
- Non-commutative: Transformation order matters!

$$A \cdot B \neq B \cdot A$$

- Transformations applied from right to left

# Translation

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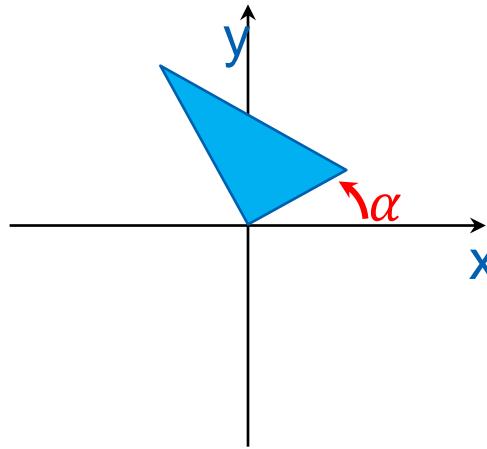
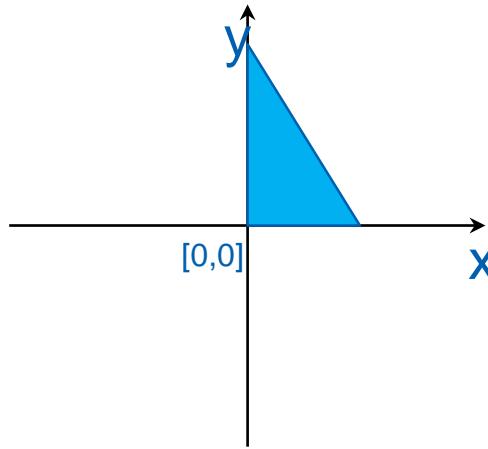
$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = M_T \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix},$$

$$M_T = \begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

(9)

# Rotation

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$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = M_{R_z} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix},$$

$$M_{R_z} = \begin{bmatrix} \cos \alpha & -\sin \alpha & 0 & 0 \\ \sin \alpha & \cos \alpha & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

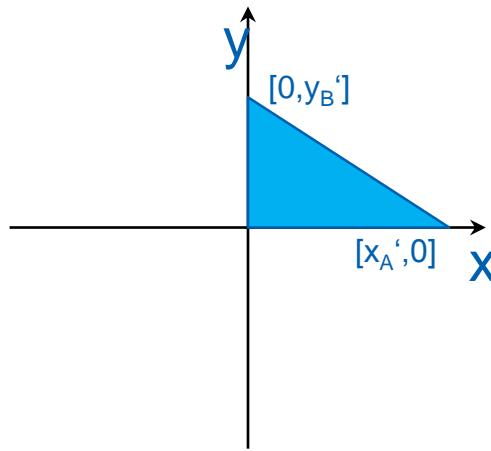
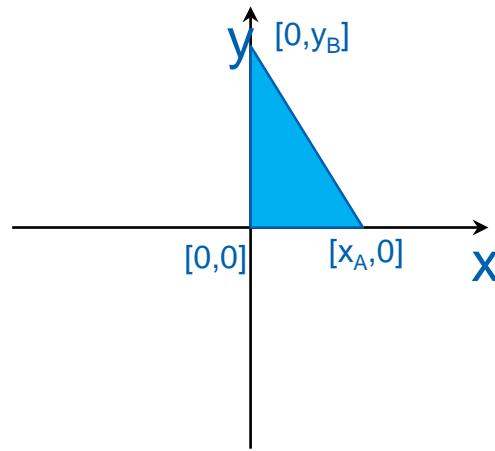
Euler angles

$$M = M_{R_x} M_{R_y} M_{R_z}$$

(10)

# Scaling

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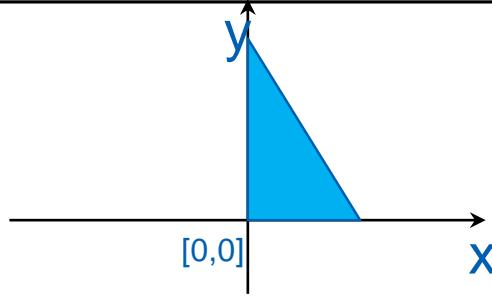


$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = M_S \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix},$$

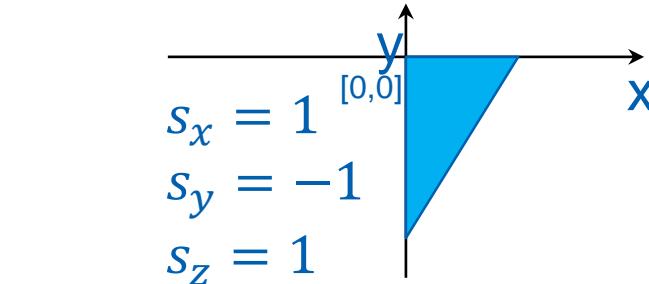
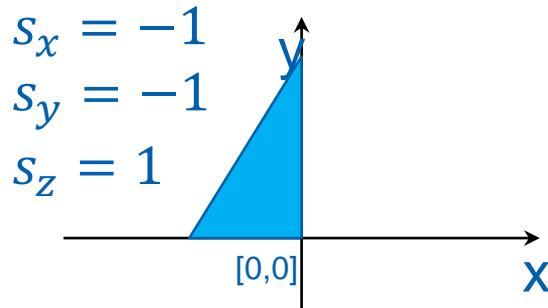
$$M_S = \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

(11)

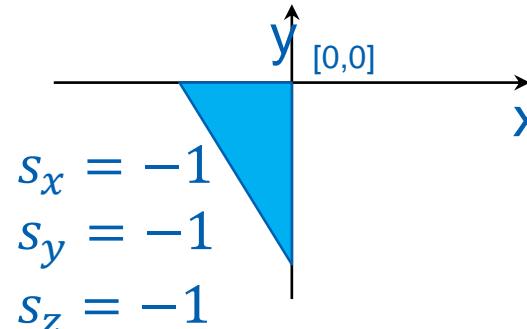
# Symmetry



$$M_S = \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

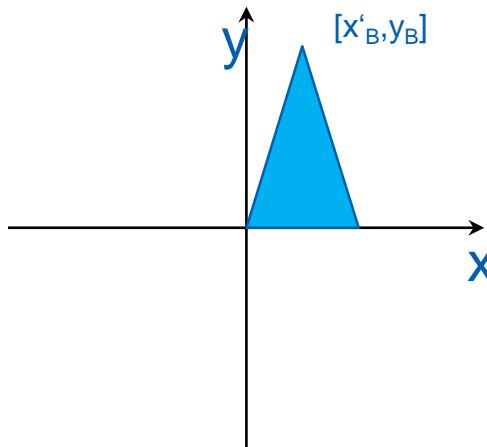
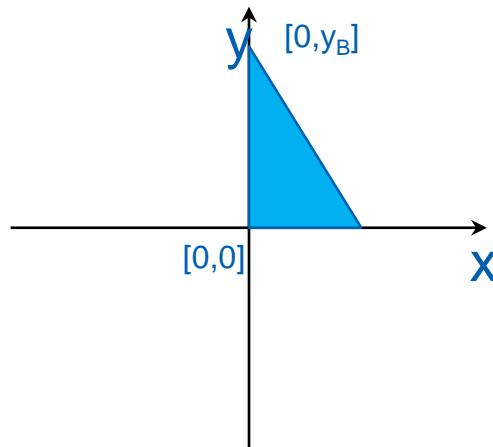


Try to avoid: Odd number of -1  
flips polygon orientations!



# Shear

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$$M_{SH_x} = \begin{bmatrix} 1 & SH_x & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

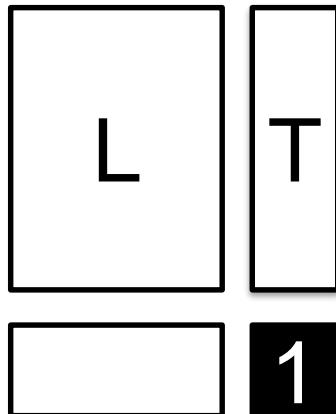
$$SH_x = \frac{x'_B}{y_B}$$

(13)

# Transformation matrix

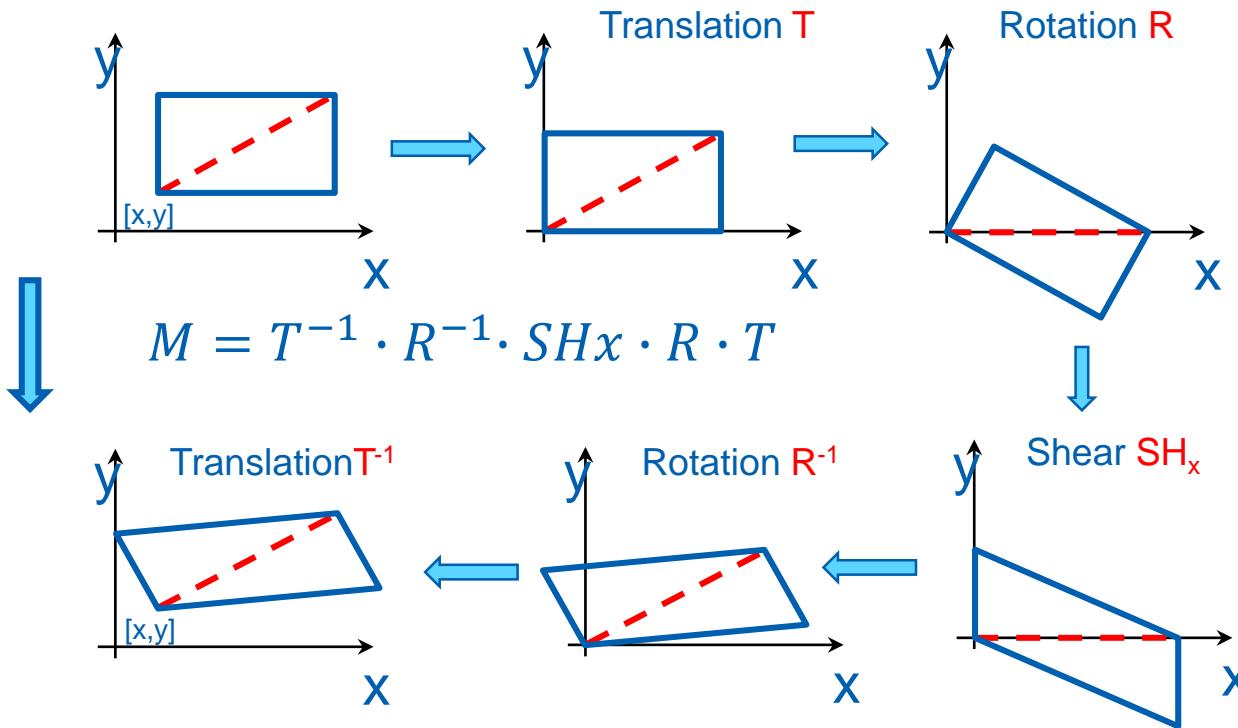
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- L: linear transformation
- T: translation
- Last row (0, 0, 0, 1) for all affine transformations



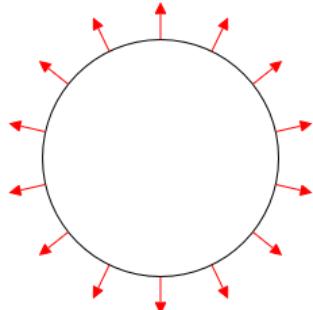
# Example – shear along a diagonal

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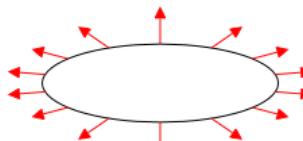


# Transforming normals

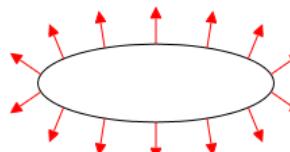
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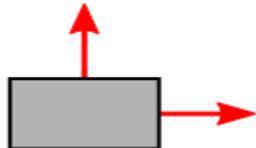
non-uniform scale



wrong



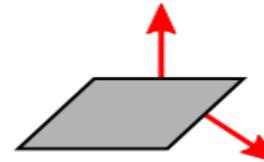
correct



shear



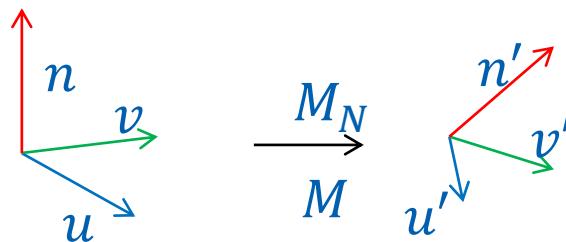
wrong



correct

# Transforming normals

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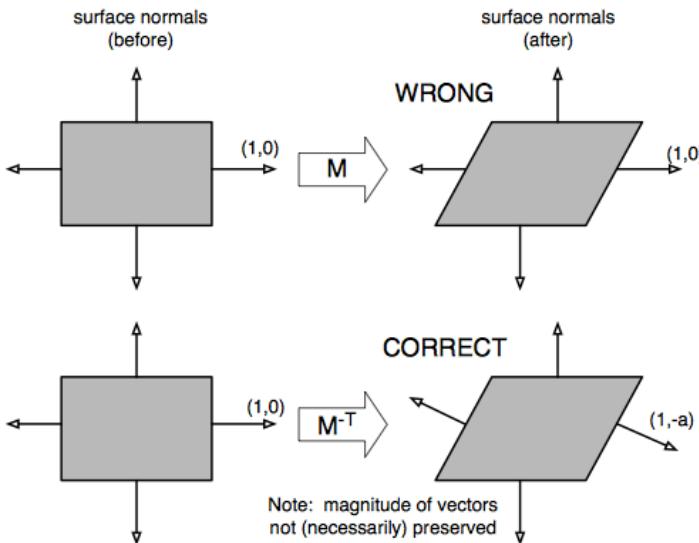
$$\begin{aligned}n^T u &= 0 \\n'^T u' &= 0 \\n'^T M u &= 0 \\n'^T M u &= n^T u \\n'^T M &= n^T \\M^T n' &= n \\n' &= M^{-T} n \\n' &= M^{-1T} n\end{aligned}$$

$$\begin{bmatrix} n_x \\ n_y \\ n_z \\ 0 \end{bmatrix}' = M_N \begin{bmatrix} n_x \\ n_y \\ n_z \\ 0 \end{bmatrix}$$

Can use just  $3 \times 3$  submatrix of  $M$  !

# Transforming normals - example

$$M = \begin{bmatrix} 1 & a \\ 0 & 1 \end{bmatrix} \quad M^{-T} = \begin{bmatrix} 1 & 0 \\ -a & 1 \end{bmatrix}$$

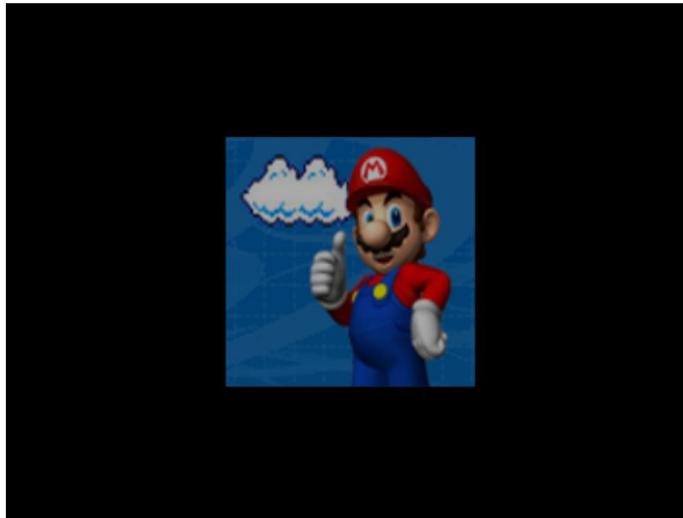


Zdroj: Stack Overflow

# DEMO

<https://cent.felk.cvut.cz/predmety/39PHA/demos/transformations.html>

Transformation example



Model matrix

|   |   |   |   |
|---|---|---|---|
| 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 0 | 0 | 1 |

View matrix (read only)

|   |   |   |   |
|---|---|---|---|
| 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 0 | 0 | 1 |

# Quaternions

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- Alternative rotation representation
- Generalization of complex numbers
  - three basis elements  $i, j, k$
  - $i^2 = j^2 = k^2 = i j k = -1, ij = -ji = k, jk = -kj = i, ki = -ik = j$
- Quaternion is a 4-tuple

$$\mathbf{q} = [x, y, z, w]$$

$$\mathbf{q} = i x + j y + k z + w = [\mathbf{v}, w]$$

$$\mathbf{v} = [x, y, z] = i x + j y + k z$$

$$\mathbf{q} = (x, y, z, w) = (\mathbf{v}, r), \mathbf{v} = xi + yj + zk$$

# Quaternions and Rotation

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- Unit quaternion ( $|q| = 1$ ) represents rotation in 3D

$$q = [a \sin \frac{\alpha}{2}, \cos \frac{\alpha}{2}]$$

3D rotation about axis  $a$  by angle  $\alpha$

# Quaternion Operations

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- Sum

$$\mathbf{q}_1 + \mathbf{q}_2 = [\mathbf{v}_1 + \mathbf{v}_2, w_1 + w_2]$$

- Dot product

$$\mathbf{q}_1 \cdot \mathbf{q}_2 = \mathbf{v}_1 \cdot \mathbf{v}_2 + w_1 \cdot w_2$$

- **Multiplication** (Hamilton product)

$$\mathbf{q}_1 * \mathbf{q}_2 = [\mathbf{v}_1, r_1] * [\mathbf{v}_2, r_2] = [r_1 \mathbf{v}_2 + r_2 \mathbf{v}_1 + \mathbf{v}_1 \times \mathbf{v}_2, r_1 r_2 - \mathbf{v}_1 \cdot \mathbf{v}_2]$$

- *Composition of rotations* (associative, non-commutative)
- **Conjugate**

$$q^* = [-\mathbf{v}, r]$$

- Inverse rotation

# Transformation with quaternion

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- Express vector as quaternion

$$\mathbf{u} = (x, y, z, 0)$$

- Rotation of  $\mathbf{u}$  using  $\mathbf{q}$

$$\mathbf{u}' = (x', y', z', 0) = \boxed{\mathbf{q} * \mathbf{u} * \mathbf{q}^*}$$

- Two quaternion multiplications + conjugate

# Quaternion to Rotation Matrix

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- Quaternion  $q = [x, y, z, w]$  corresponds to rotation matrix

$$R = \begin{pmatrix} 1 - 2y^2 - 2z^2 & 2xy - 2wz & 2xz + 2wy \\ 2xy + 2wz & 1 - 2x^2 - 2z^2 & 2yz - 2wx \\ 2xz - 2wy & 2yz + 2wx & 1 - 2x^2 - 2y^2 \end{pmatrix}$$

- Rotation composition faster with quaternions
- Vector transformation faster with matrix

# Rotation Interpolation

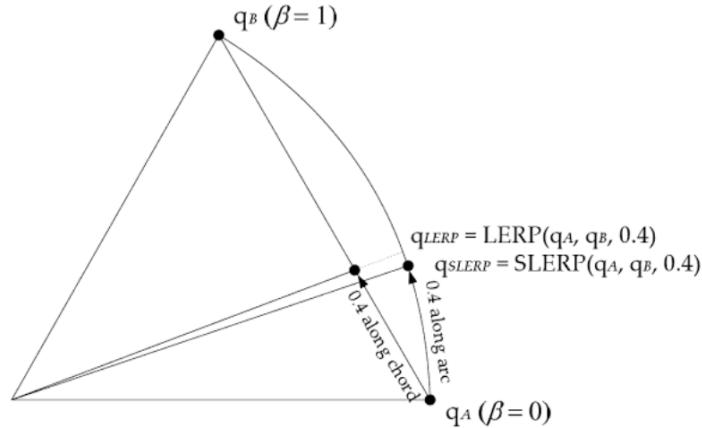
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- Matrix interpolation
  - breaks orthonormality - artefacts
- Quaternion interpolation
  - Linear interpolation (LERP)
  - Spherical linear interpolation (SLERP) - constant angular step

# LERP and SLERP

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$$q = \frac{w_A q_A + w_B q_B}{|w_A q_A + w_B q_B|}$$



J. Gregory, Game Engine Architecture

## LERP

$$\begin{aligned} w_A &= 1 - \beta \\ w_B &= \beta \end{aligned}$$

## SLERP

$$\begin{aligned} w_A &= \frac{\sin (1 - \beta)\theta}{\sin \theta} \\ w_B &= \frac{\sin \beta\theta}{\sin \theta} \\ \theta &= \arccos q_A q_B \end{aligned}$$

(26)

# Transformation Representation - SQT

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- SQT (SRT)
  - Scale, Quaternion, Translation
- Uniform scale:  $1+4+3 = 8$  scalars
  - Sequence of SQT can be composed to SQT
- Non-uniform scale:  $3+4+3=10$  scalars
- Correct interpolation of rotation, scale and translation !
- Compact representation
- Fast composition of transformations
- Slower application of transformation

# Transformation Representation - Matrix

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- Matrix 4x4
- General affine transformation + perspective
- Simple concatenation (matrix multiplication)
- Fast application of transformation

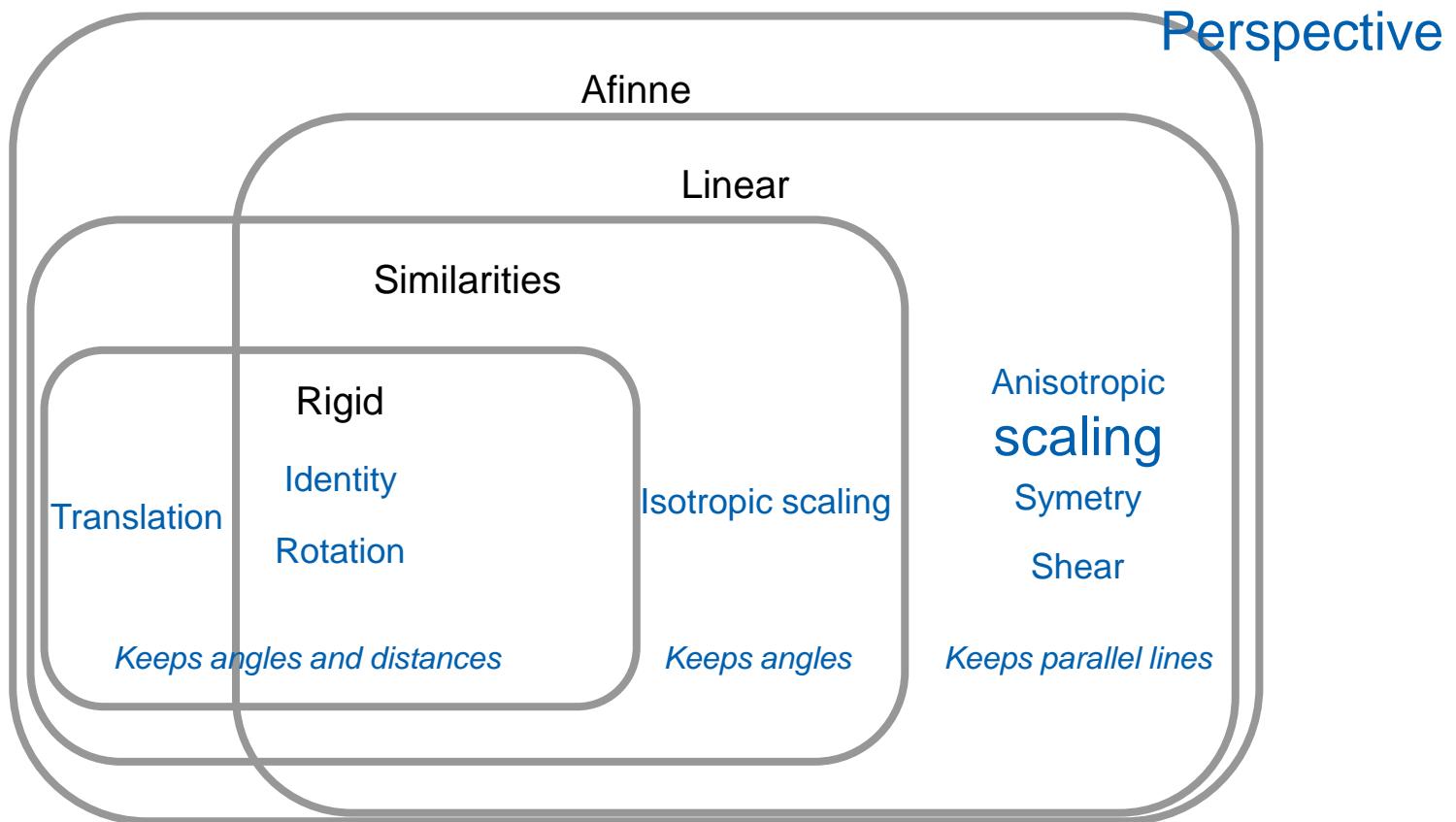
# Transformation – Summary

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- Interpolace a skládání rotací pomocí kvaternionů (animace)
- Transformace vektorů pomocí matic (zobrazování)
- Conversions between representations

# Transformations

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# Outline

- Points, Vectors, Transformations MPG – chapter 21
  - Camera and Projection MPG – chapter 9
  - 3D Scene Representation MPG - chapters 5.11, 5.12, 5.13, 6-8, 14

# Camera

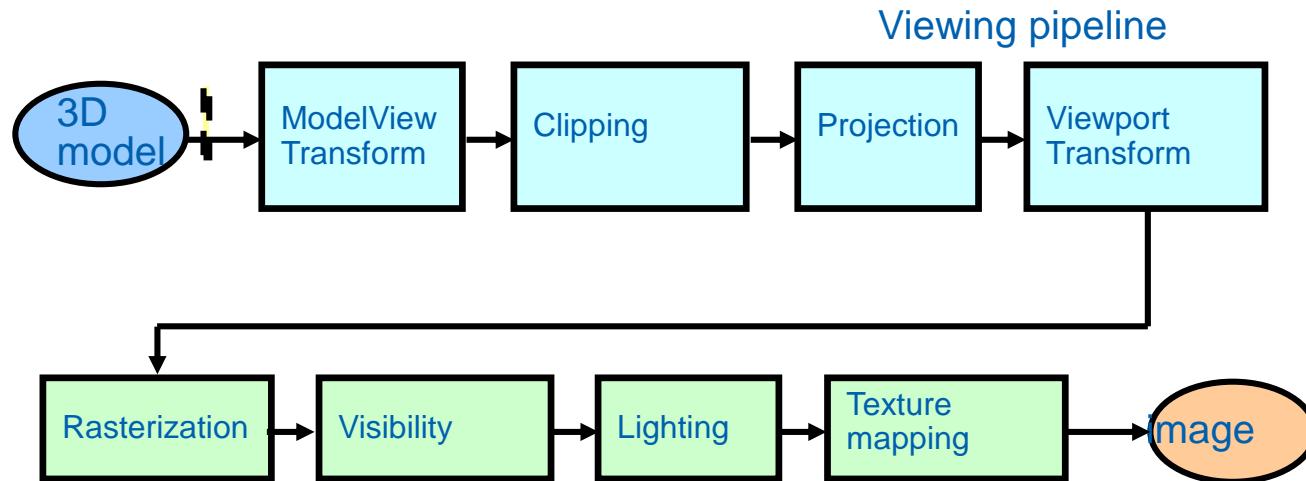
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- Idealized camera (pin-hole)
  - Idealized geometric optics
  - Realistic effects as post process
- Camera description
  - Explicit parameters (position, orientation)
  - Node in a scene graph
  - Other parameters – viewing angle, viewport, rendering setup, ...
- Series of transformations
  - Viewing transformation (camera position / orientation)
  - Projection transformation (viewing volume)
  - Viewport transformation (viewport on the screen)
  - Composed with the modeling transformation

# Rendering Pipeline

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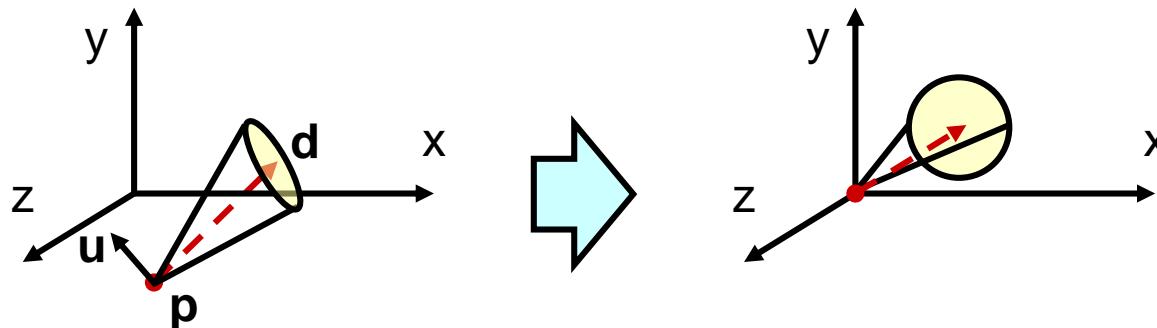
- 1. part – transformations (*viewing pipeline*)
- 2. part – further operations



# View transformation

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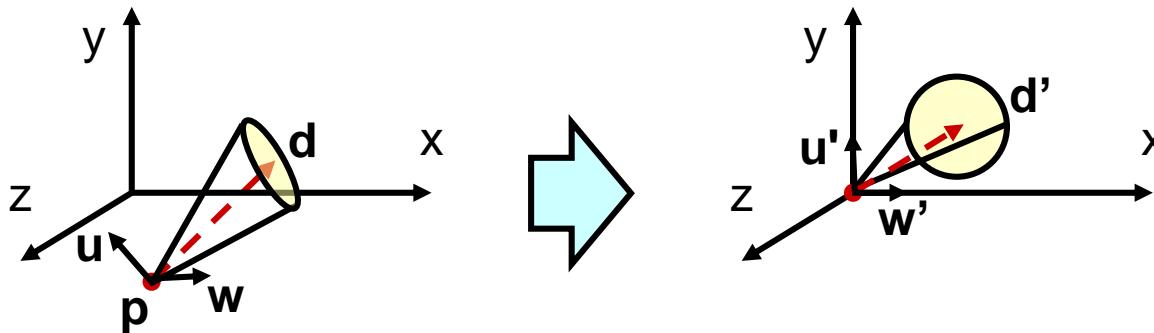
- Transformation of scene to unified position



- **Camera position  $p$**  to  $[0,0,0]$  ... translation
- **View direction  $d$**  // with  $z$  axis ... rotation
- **Up vector  $u$**  // with  $y$  axis ... rotation around  $z$  axis
- Camera matrix  $M$ : Viewing transformation =  $M^{-1}$

# View transformation matrix

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- $M_V = M_C^{-1}$  ( $M_C$  camera matrix)

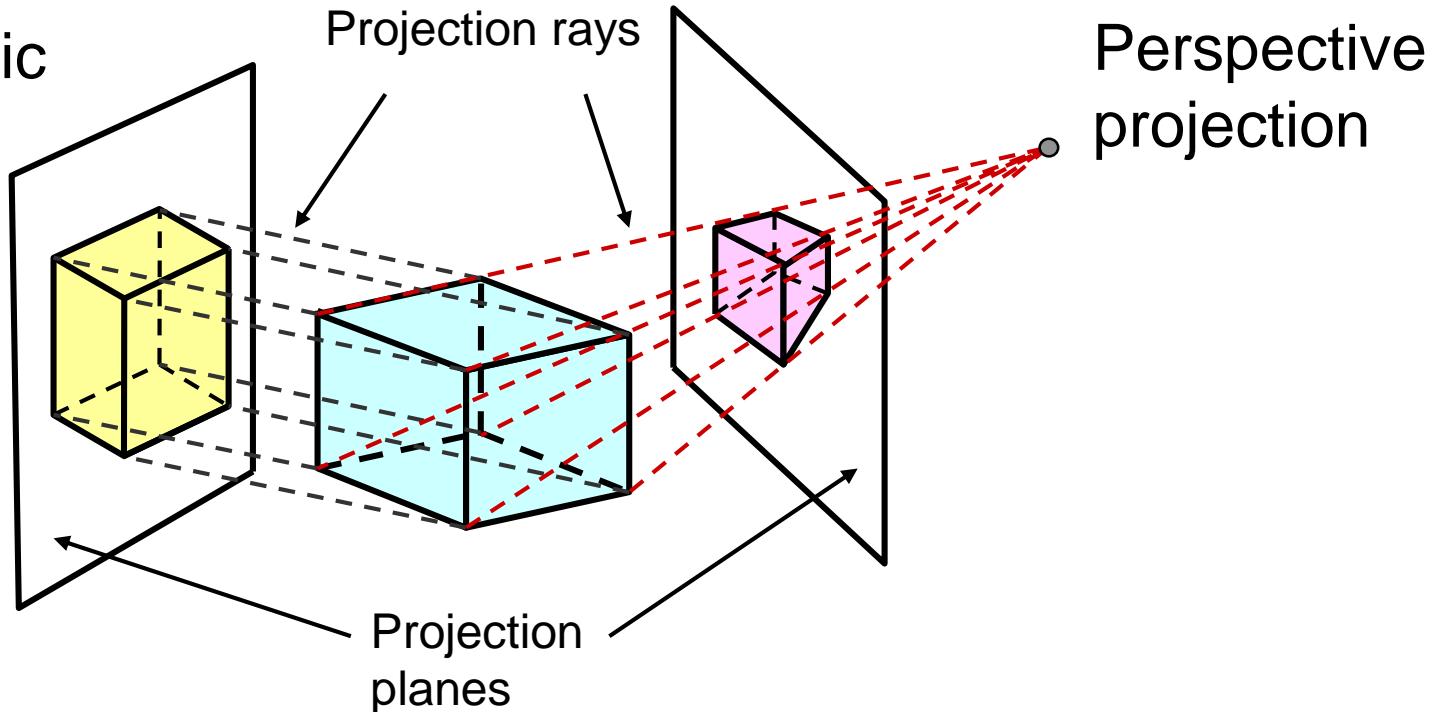
$$w = d \times u$$

$$M_V = \begin{bmatrix} w_x & u_x & d_x & -p_x \\ w_y & u_y & d_y & -p_y \\ w_z & u_z & d_z & -p_z \\ 0 & 0 & 0 & 1 \end{bmatrix}^{-1}$$

# Orthographic and perspective projection

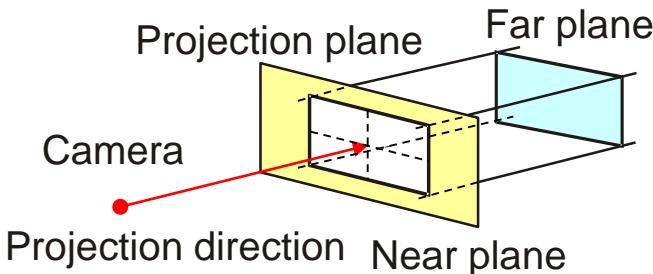
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Orthographic  
projection

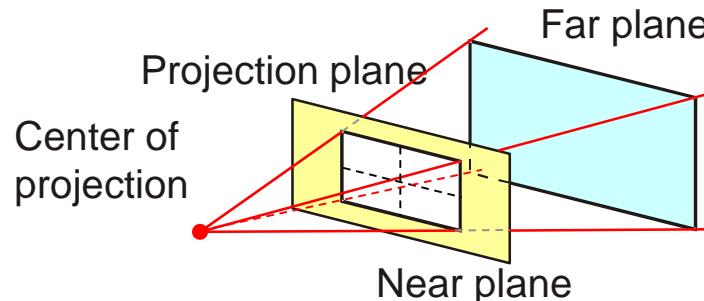


# Camera – projection transformation

- Transformation from 3D space to 2D projection plane
- *Viewing volume / frustum (záběr)*



Orthographic projection  
view volume = cuboid



Perspective projection  
view volume = pyramid frustum

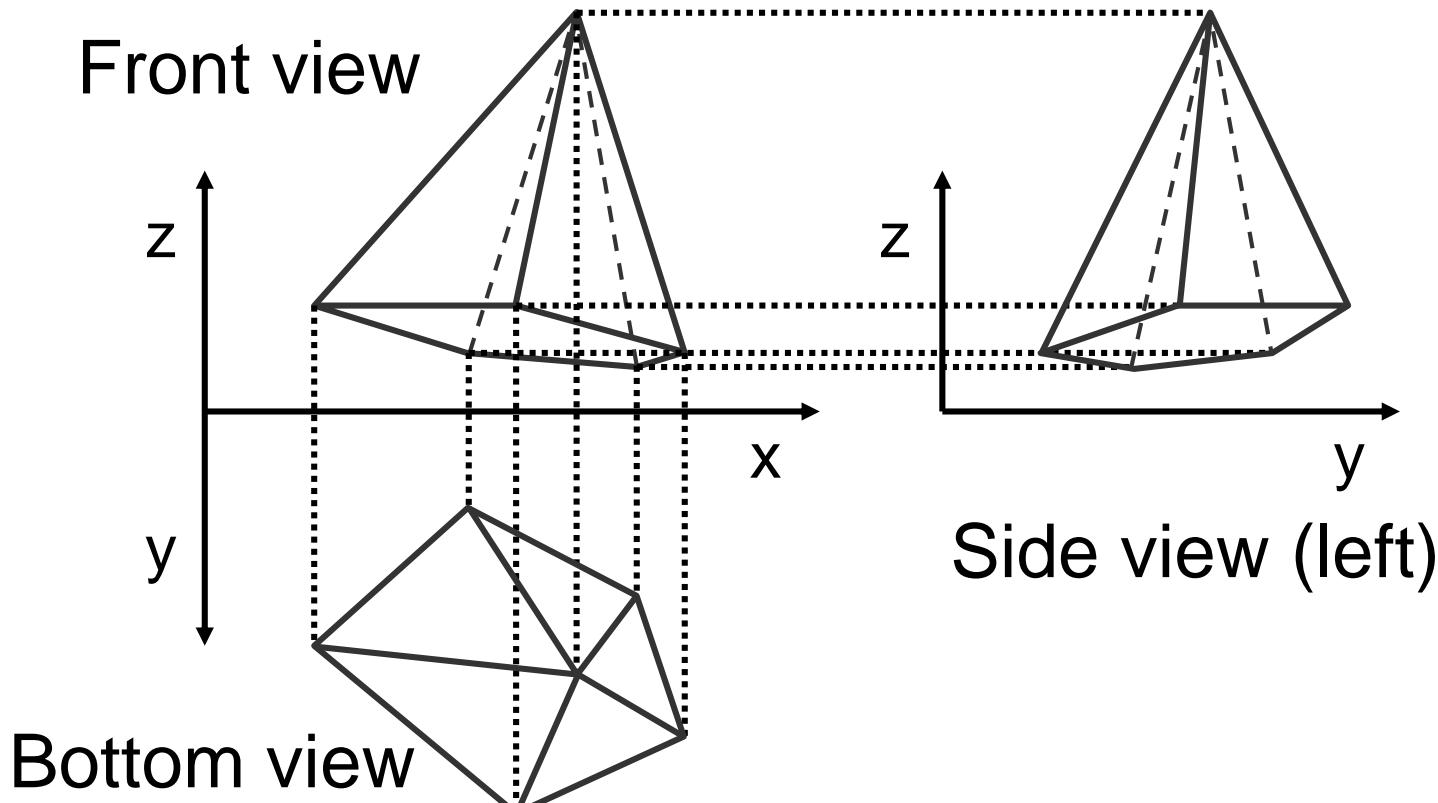
# Orthographic Projection

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- All rays parallel!
- Rays **orthogonal** to projection plane
  - Monge's projection: top, front, side
  - Axonometry (arbitrary projection plane)
- Rays **non-orthogonal** to projection plane (oblique projection)
  - Cavalier projection (the same scale on axes)
  - Cabinet projection ( $z$  axis scale = 1/2)

# Monge's projection

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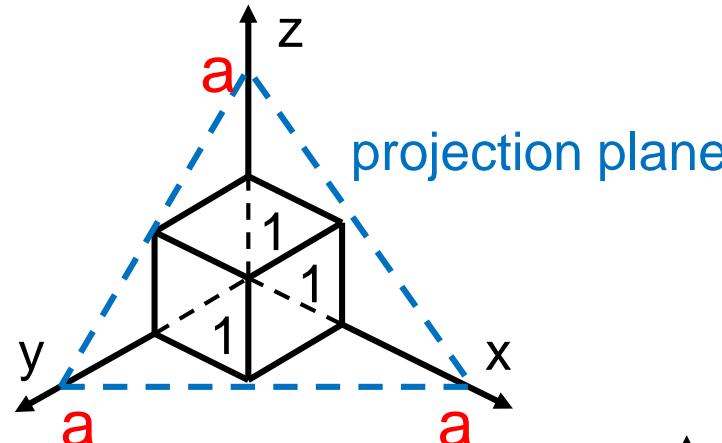


Gaspard Monge (1746 - 1818) 39

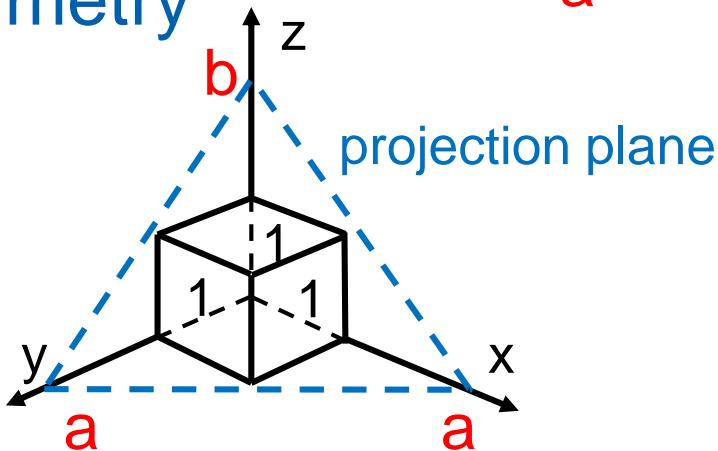
# Axonometry

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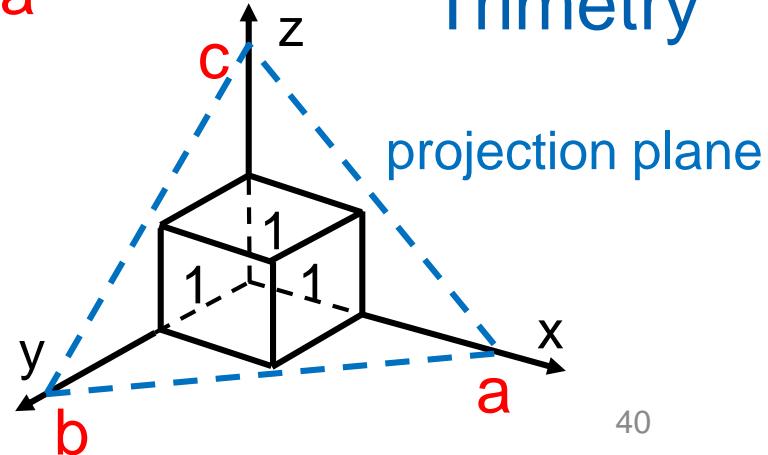
## Isometry



## Dimetry



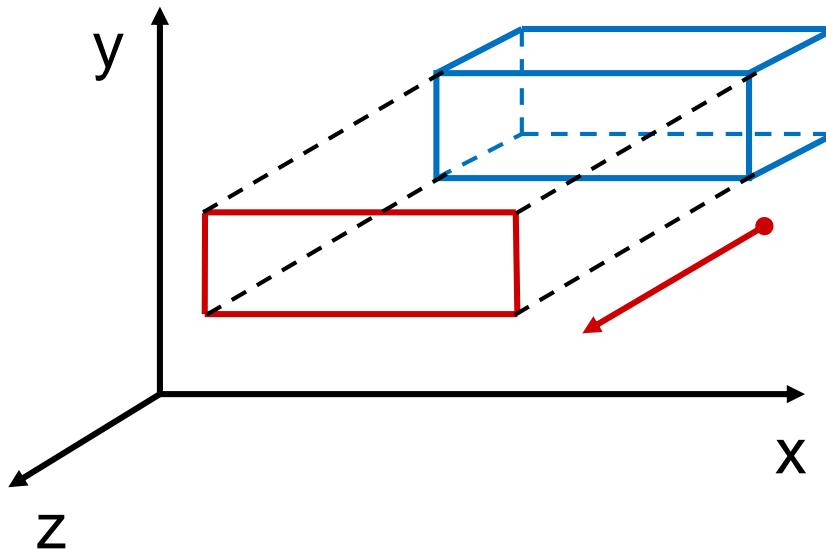
## Trimetry



# Projection: Matrix Form

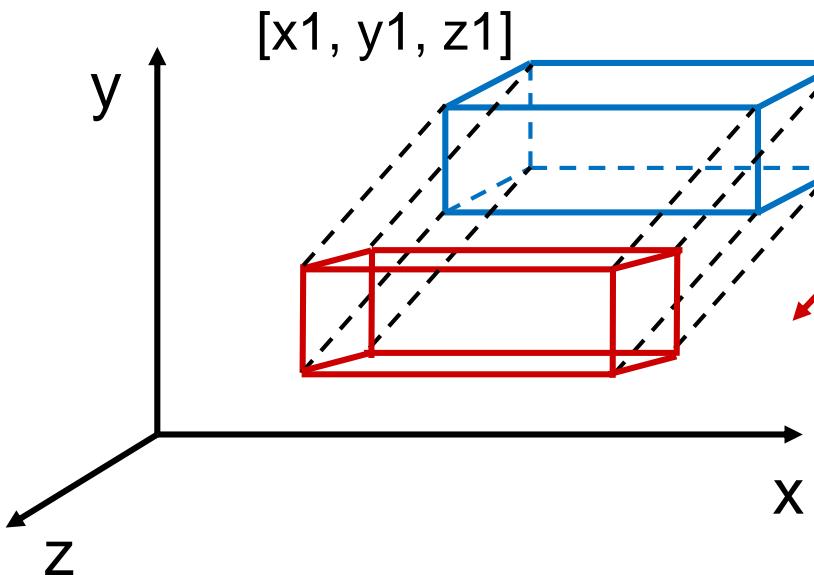
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- Align projection direction to  $z$  axis (rotation)
- Projection plane =  $xy$



$$M_{//} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

# Oblique Projection



$$\begin{aligned}x &= x_1 + x_p \cdot t \\y &= y_1 + y_p \cdot t \\z &= z_1 + z_p \cdot t\end{aligned}$$

$$\underline{z = 0 \Rightarrow t = -z_1 / z_p}$$

Projection direction  $[x_p, y_p, z_p]$

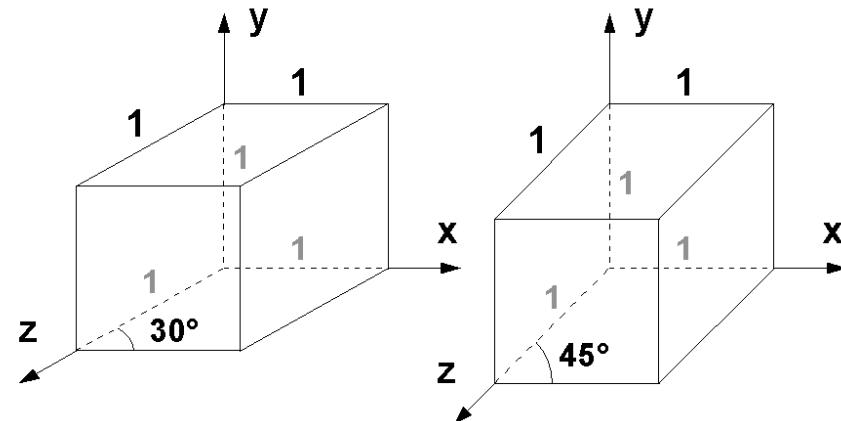
$$M = \begin{bmatrix} 1 & 0 & -\frac{x_p}{z_p} & 0 \\ 0 & 1 & -\frac{y_p}{z_p} & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$M = M_{//} \cdot M_{zk}$$

# Oblique Projection

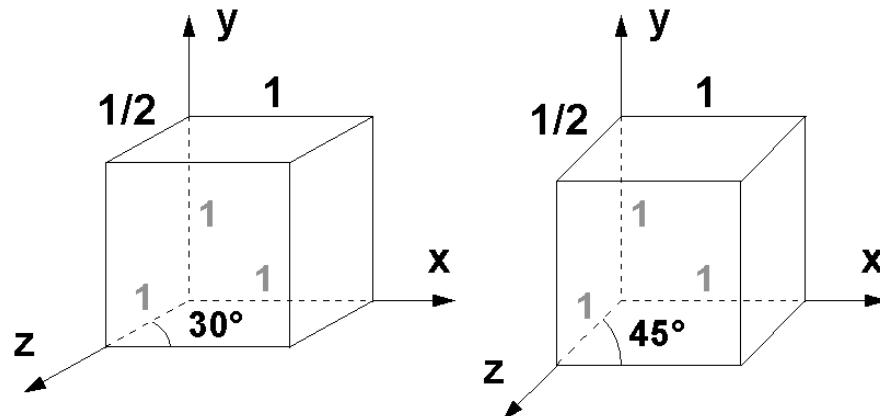
## Cavalier

$$M = \begin{bmatrix} 1 & 0 & -\cos \beta & 0 \\ 0 & 1 & -\sin \beta & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

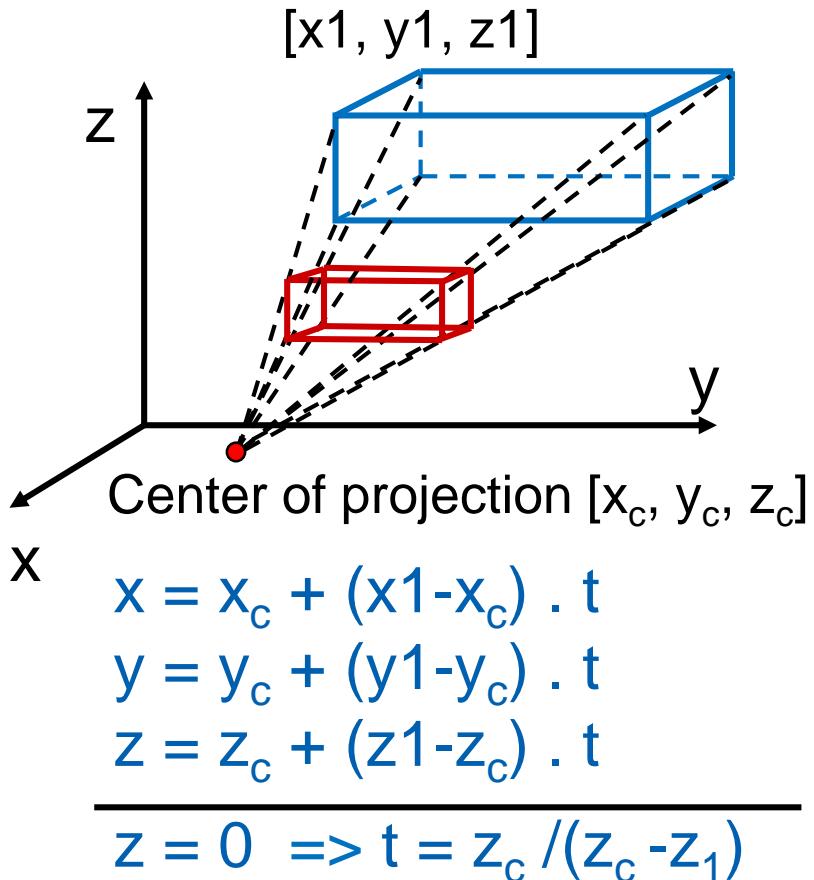


## Cabinet

$$M = \begin{bmatrix} 1 & 0 & \frac{-\cos \beta}{2} & 0 \\ 0 & 1 & \frac{-\sin \beta}{2} & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



# Perspective Projection



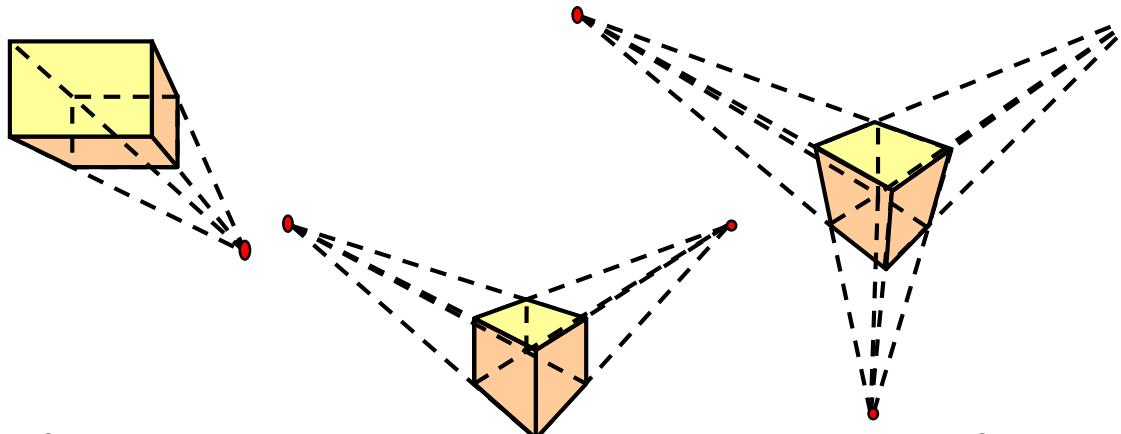
$M =$

$$\begin{bmatrix} 1 & 0 & -\frac{x_c}{z_c} & 0 \\ 0 & 1 & -\frac{y_c}{z_c} & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & -\frac{1}{z_c} & 1 \end{bmatrix}$$

# Vanishing Points (Úběžníky)

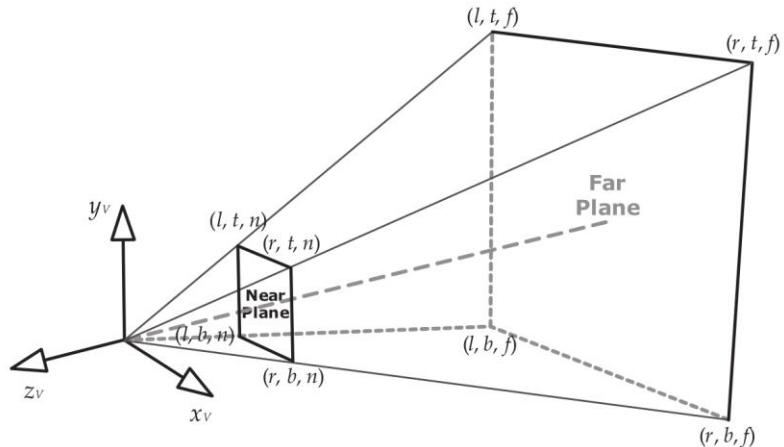
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- Perspective projection does not keep parallelism
- Lines parallel to coordinate axes meet in **primary vanishing points**
  - 1-, 2-, 3-point perspective



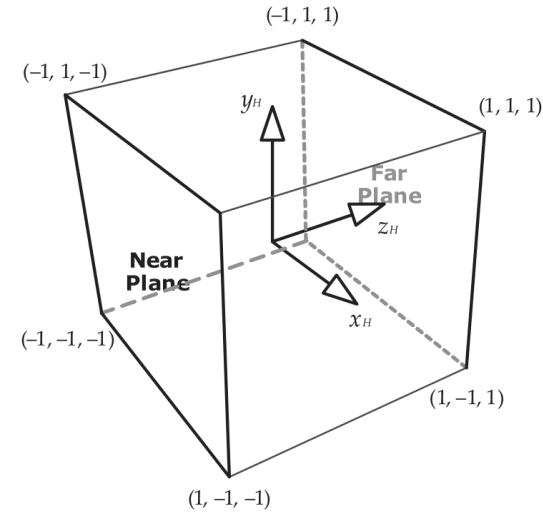
- Number of primary vanishing points = number of projection plane intersections with coordinate axes

# Perspective Projection (OpenGL)



camera / eye space

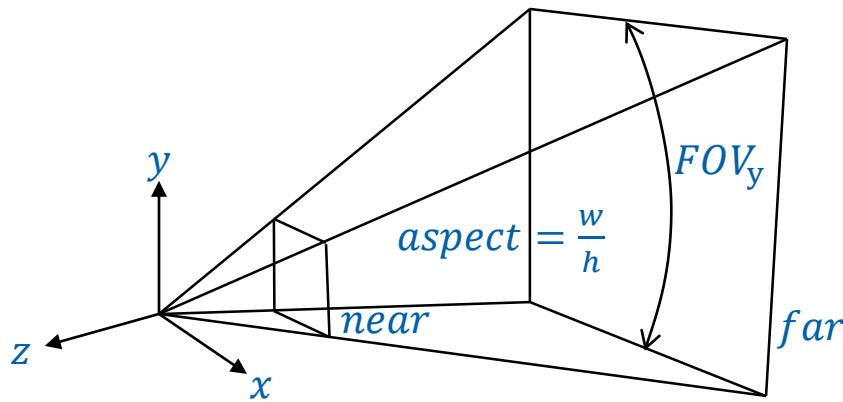
$$P = \begin{bmatrix} \frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\ 0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\ 0 & 0 & -\frac{f+n}{f-n} & -\frac{2nf}{f-n} \\ 0 & 0 & -1 & 0 \end{bmatrix}$$



NDC / clip space

# Symmetrical Perspective Projection

---



$$P = \begin{bmatrix} \cot \frac{FOV_y}{2} & 0 & 0 & 0 \\ \frac{0}{\text{aspect}} & \cot \frac{FOV_y}{2} & 0 & 0 \\ 0 & 0 & -\frac{f+n}{f-n} & -\frac{2nf}{f-n} \\ 0 & 0 & -1 & 0 \end{bmatrix}$$

# Camera – Viewport Transformation

---

- Size and position of the viewport

$$x' = (x_{\text{NDC}} + 1) \frac{W}{2} + X$$

$$y' = (y_{\text{NDC}} + 1) \frac{H}{2} + Y$$

- $x_{\text{NDC}}$  and  $y_{\text{NDC}}$  result of previous transf. (range -1..1)

# Coordinate systems overview

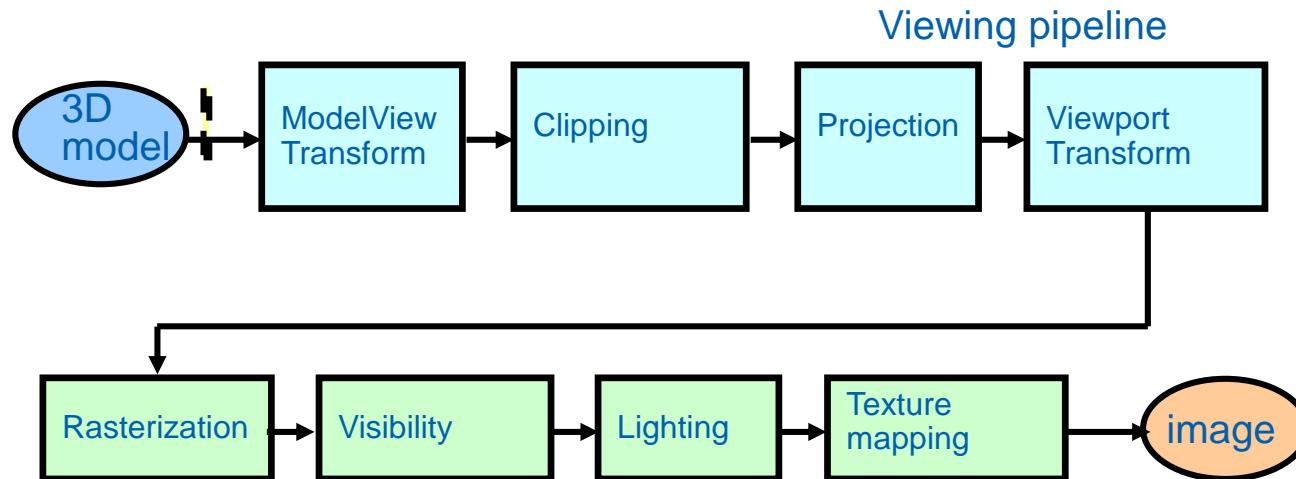
---

- Object / Modeling / Local coordinates
  - Relative to object origin
- World coordinates
  - Global scene coordinates
- Camera / Eye / View coordinates
  - Camera in the origin, looks along  $-z$
- Clip coordinates
  - After multiplication by projection matrix
- Normalized device coordinates
  - Cuboid after perspective division  $[-1,-1,-1] - [1,1,1]$
- Screen / Window coordinates
  - x, y pixel position, z in 0..1 range

# Rendering Pipeline

---

- 1. part – transformations (*viewing pipeline*)
- 2. part – further operations



# Outline

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- Points, Vectors, Transformations MPG – chapter 21
- Camera and Projection MPG – chapter 9
- 3D Scene Representation MPG - chapters  
5.11, 5.12, 5.13, 6-8, 14

# Introduction to 3D geometry

---

- Scene = mathematical model of *the world* in computer
  - Rendering
  - Animation
  - Collisions
  - ...
- Geometry (3D models)
- Materials
- Lights
- Camera
- ...



# 3D Models

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- Boundary representation (B-rep)
- Volumetric representation
- Constructive solid geometry (CSG)
- Implicit surfaces
- Point clouds
- ...

# Polygonal Mesh

---

- Classical boundary representation
- Describes object surface (vertices, edges, faces)
- List of polygons defining object boundary (surface)
  - Better convex polygons
  - Even better just triangles (triangulation)
- Different representations
  - Sequence of vertices (separator)
  - Vertex array + index array
  - ...

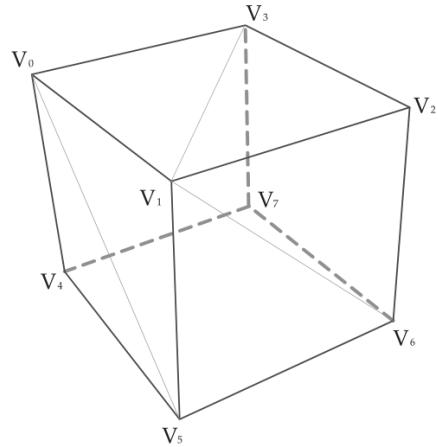
# Triangle Mesh

---

- Just triangles
  - HW friendly !
  - Simplified rendering, clipping, collisions, ...
- Mathematics of a triangle
  - In visibility / ray intersection lecture...

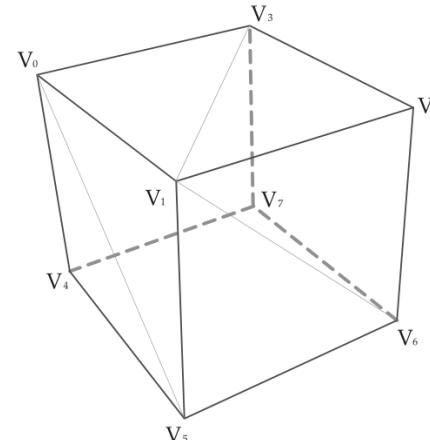
# Triangle Mesh

---



`V0 | V1 | V3 | V1 | V2 | V3 | V0 | V5 | V1 ... | V5 | V7 | V6`

triangle list



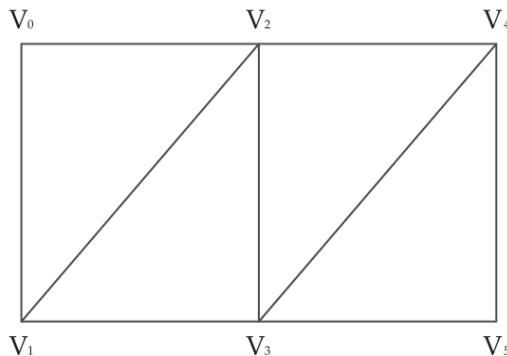
Vertices `V0 | V1 | V2 | V3 | V4 | V5 | V6 | V7`

Indices `0 | 1 | 3 | 1 | 2 | 3 | 0 | 5 | 1 ... | 5 | 7 | 6`

indexed triangle list

# Triangle Mesh – Compact Representation

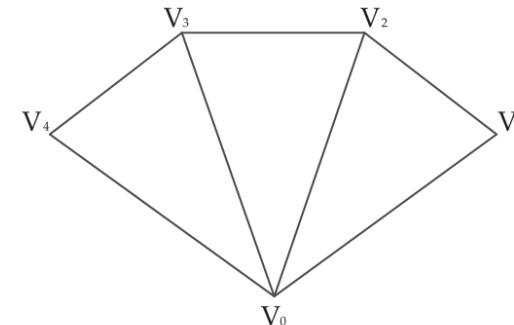
---



Vertices [V<sub>0</sub> | V<sub>1</sub> | V<sub>2</sub> | V<sub>3</sub> | V<sub>4</sub> | V<sub>5</sub>]

Interpreted  
as triangles:  
[0 1 2] [1 3 2] [2 3 4] [3 5 4]

triangle strip



Vertices [V<sub>0</sub> | V<sub>1</sub> | V<sub>2</sub> | V<sub>3</sub> | V<sub>4</sub>]

Interpreted  
as triangles:  
[0 1 2] [0 2 3] [0 3 4]

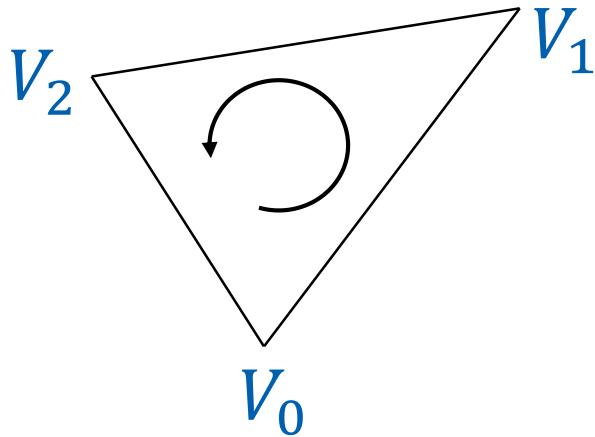
triangle fan

No indices – saves memory!

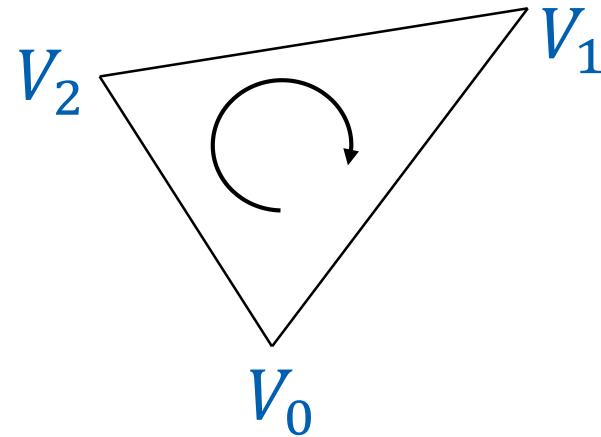
# Triangle Mesh – Winding Order

---

- Defining front and back faces



$V_0V_1V_2$   
CCW (counter clock wise)



$V_0V_2V_1$   
CW (clock wise)

# Storing Other Information

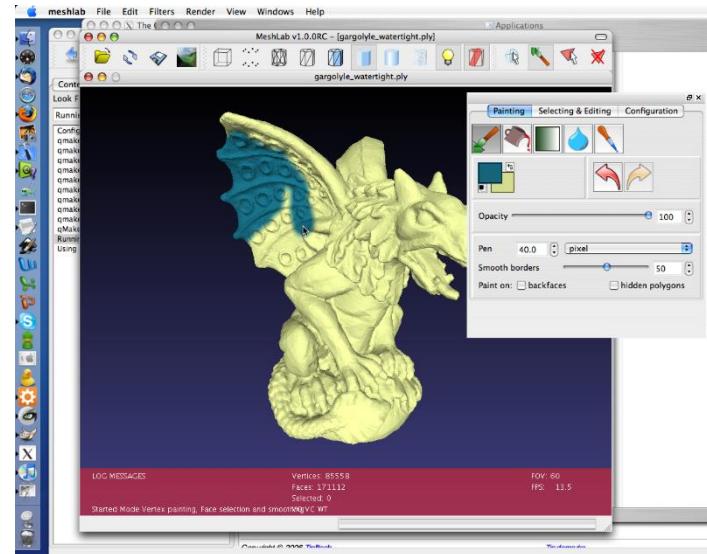
---

- Vertices
  - Position, normal, texture coordinates, color, ...
- Edges
  - sharp, auxiliary
- Faces
  - normal, material
- Solids
  - material, texture

# Triangle Mesh

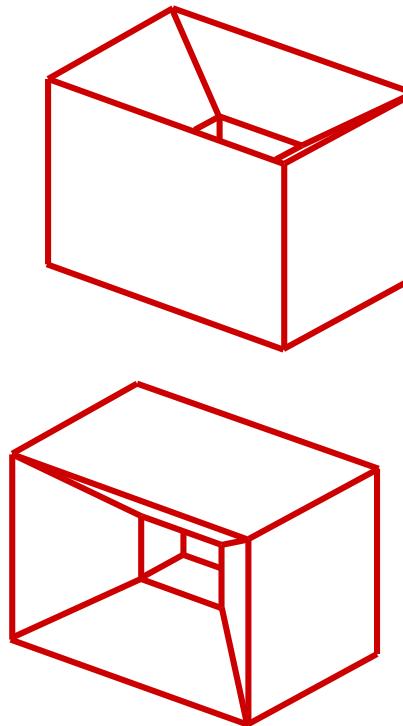
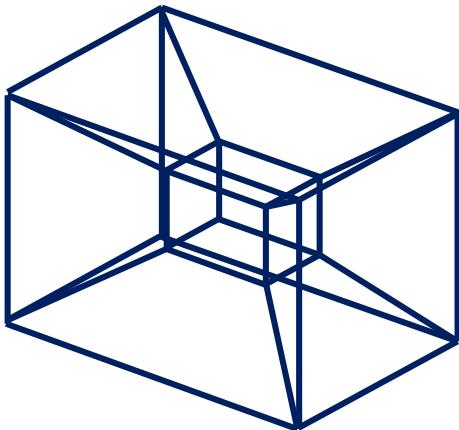
---

- Modeling
  - Maya, 3DS Max, Blender, Cinema
- Editing / Optimization
  - MeshLab
  - NvTriStrip
  - ...



# Wireframe Model

---

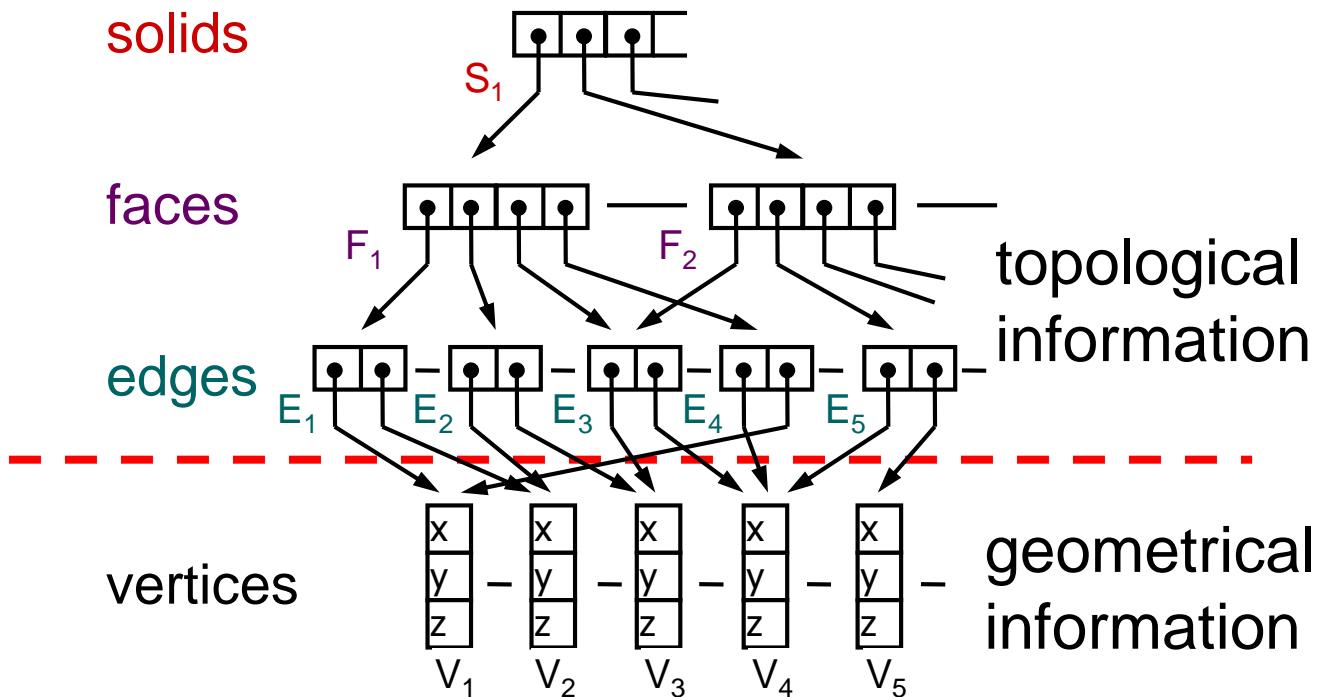


But very useful  
for debugging!

Ambiguous interpretation

# Mesh Graph

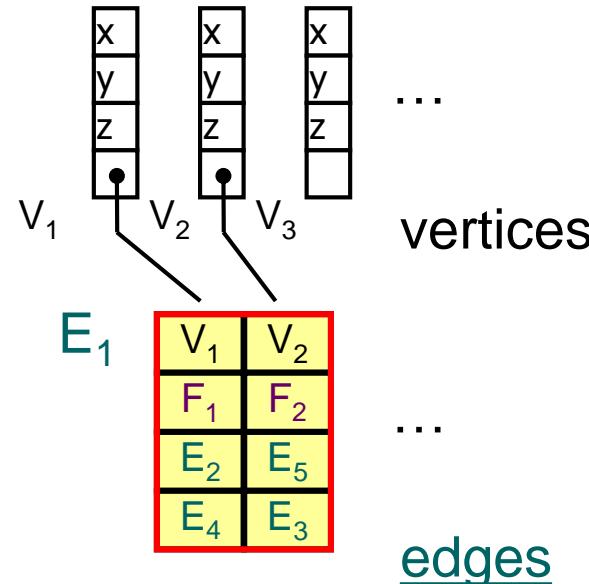
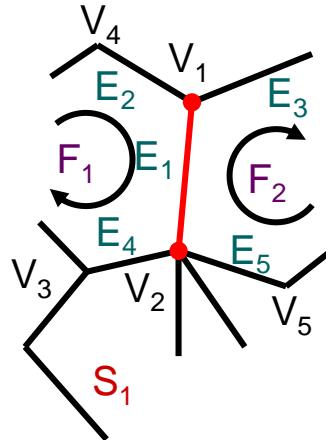
Hierarchical representation



# Winged-Edge

---

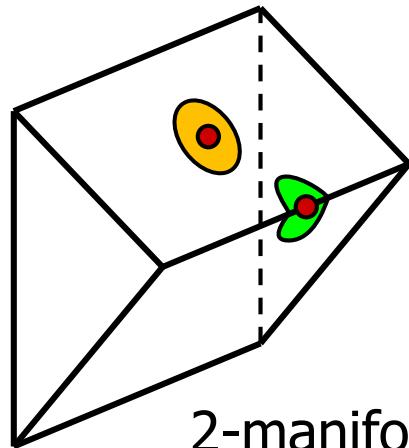
- Information about the neighborhood
- Useful for **editing & maintaining consistency**



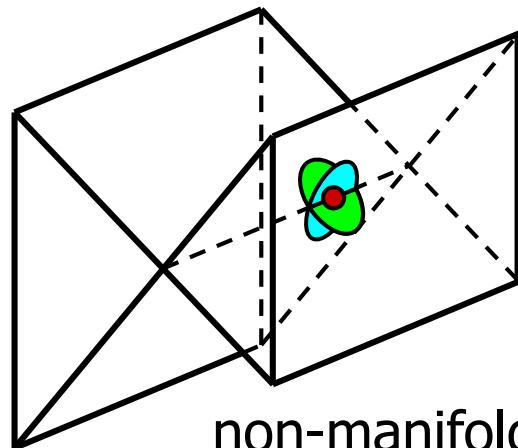
# Model Unambiguity

---

- Manifold (rozvinutelný)
- 2-manifold: for every surface point there is a neighborhood topologically equivalent with plane
- Important for manufacturing, CAD/CAM



2-manifold



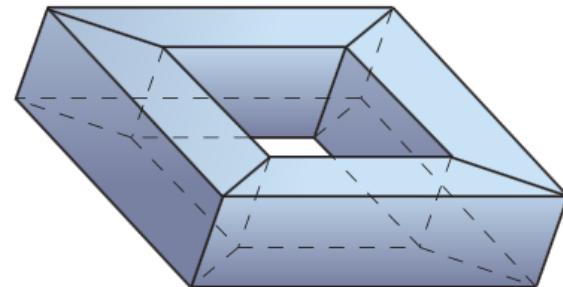
non-manifold

# Euler-Poincare Formula for Manifolds

---

$$V - E + F - R = 2(S - H)$$

- V #vertices
- E #edges
- F #faces
- R #rings (holes in faces)
- H #holes (holes through object)
- S #shells (separate objects)

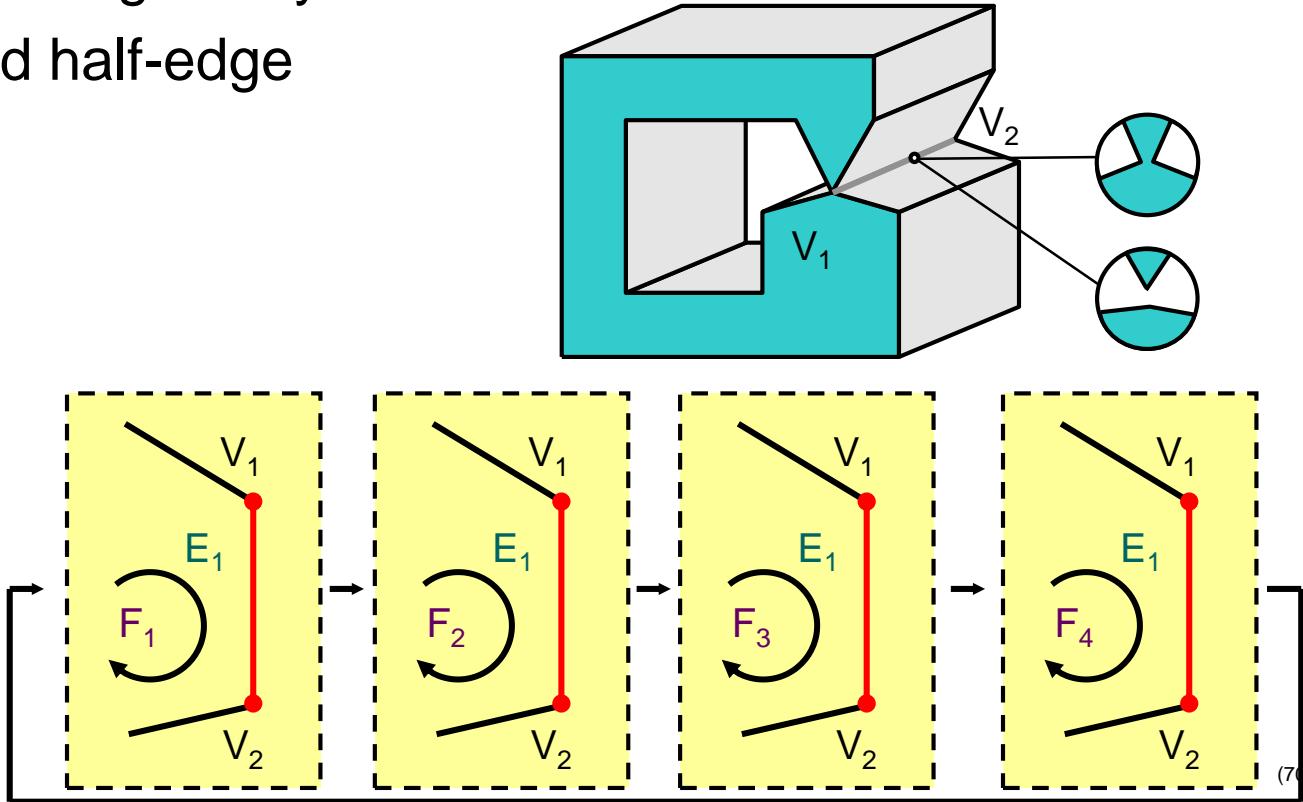


$$\begin{aligned}V &= 16 \\E &= 32 \\F &= 16 \\R &= 0 \\H &= 1 \\S &= 1\end{aligned}$$

(69)

# Representing non-manifolds

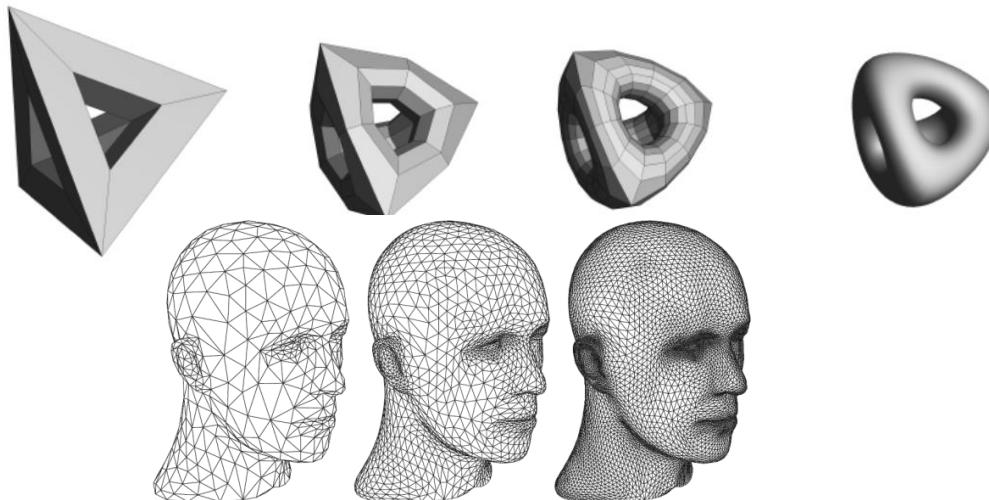
- Winged-edge: only manifolds
- Winged half-edge



# Subdivision Surfaces

---

- Progressively subdivide coarse mesh
- Different subdivision schemes
  - Loop, Catmull-Clark, Doo-Sabin
  - HW support: hull+tesselation shaders

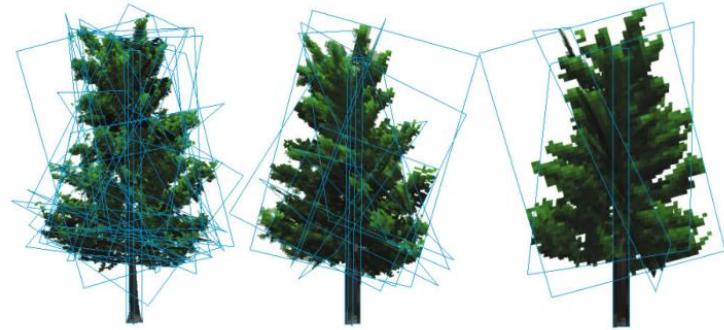
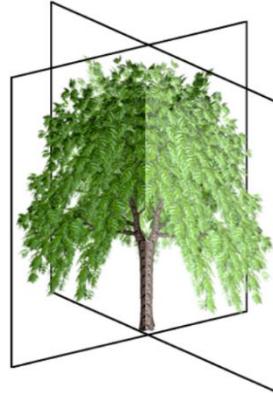


Zorin & Schroeder, SIGGRAPH 99

# Sprites, Billboards

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- Replacing geometry with images – sprites / billboards/ impostors
- Billboard: oriented sprite
  - towards a camera or based on object features ...



# Other B-reps

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- Parametric surfaces
  - Bezier surface, Coons surface, NURBS
- Height fields
  - Regular / irregular
  - Terrains
- Impostors with depth
- LODs
  - Multiresolution representation

# B-rep: Summary

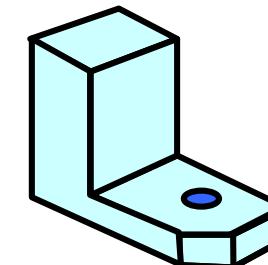
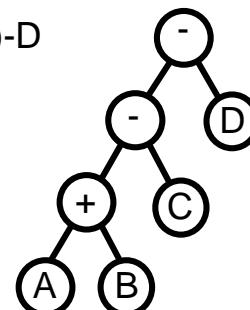
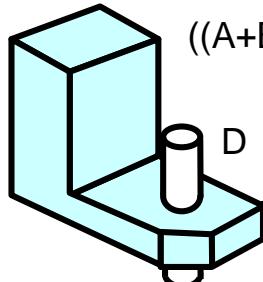
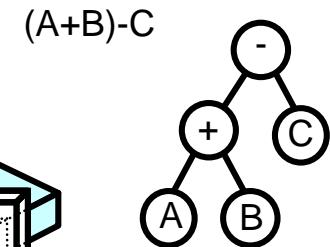
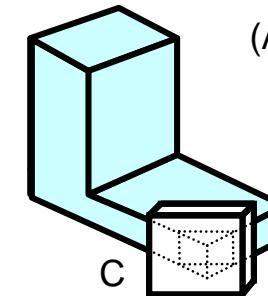
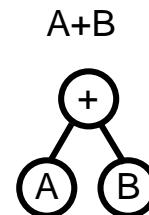
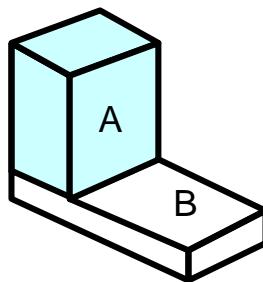
---

- Easy (GPU) rendering
- Complicated operations on solids
  - No explicit information on what is the interior

# CSG Tree

---

- Leaves: geometric primitives
- Inner nodes: set operations, transformations
- Root = model



# CSG Tree - Properties

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- Easy „point in solid“ test
- Modeling resembles manufacturing
  - Popular for 3D printing!
- Memory compact (primitives defined analytically)
- More complex rendering

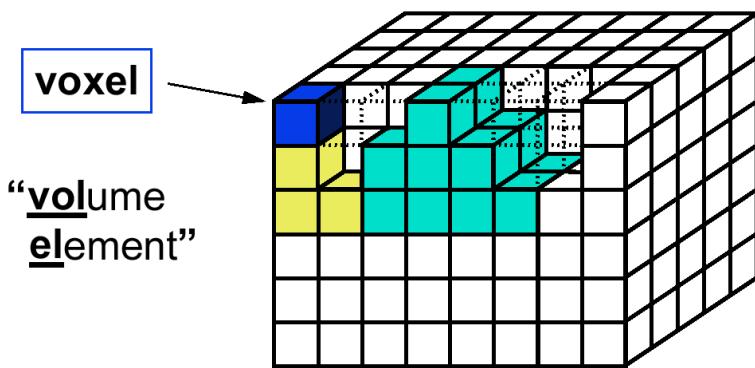


DP: Markéta Karaffová 2016

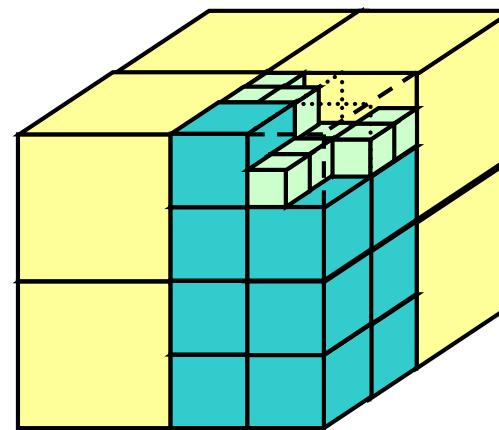
# Volumetric representation

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3D grid (regular structure)



Octree (hierarchical structure)



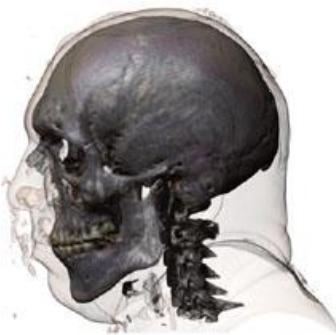
# Volumetric rep.- properties

---

- Easy „point in solid“ test
- More difficult rendering (ray casting)



Source: Ikits et al. GPU Gems 2

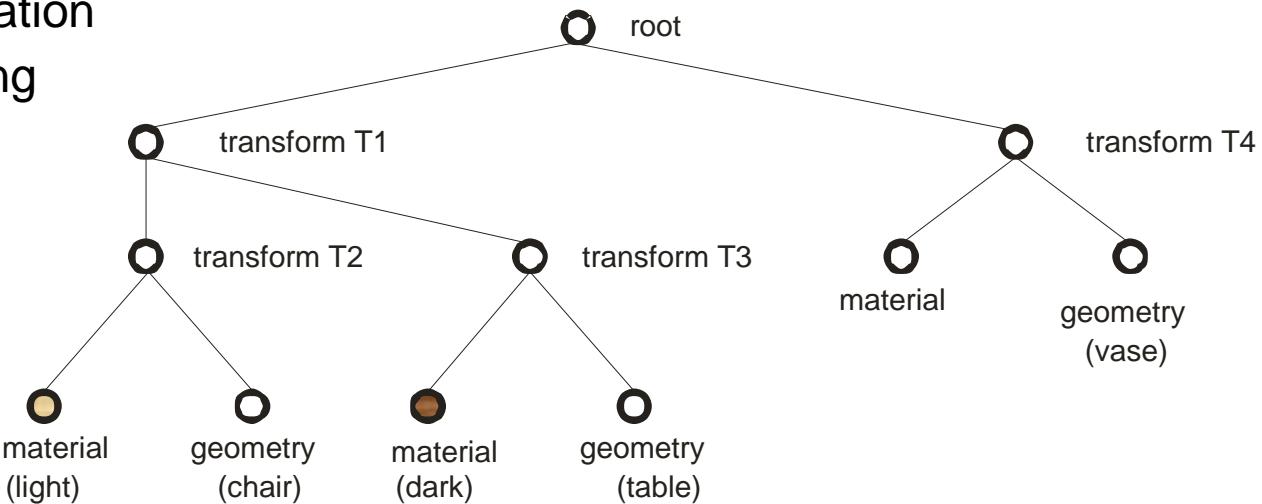


DP: M. Benatsky 2011

# Scene Graph

---

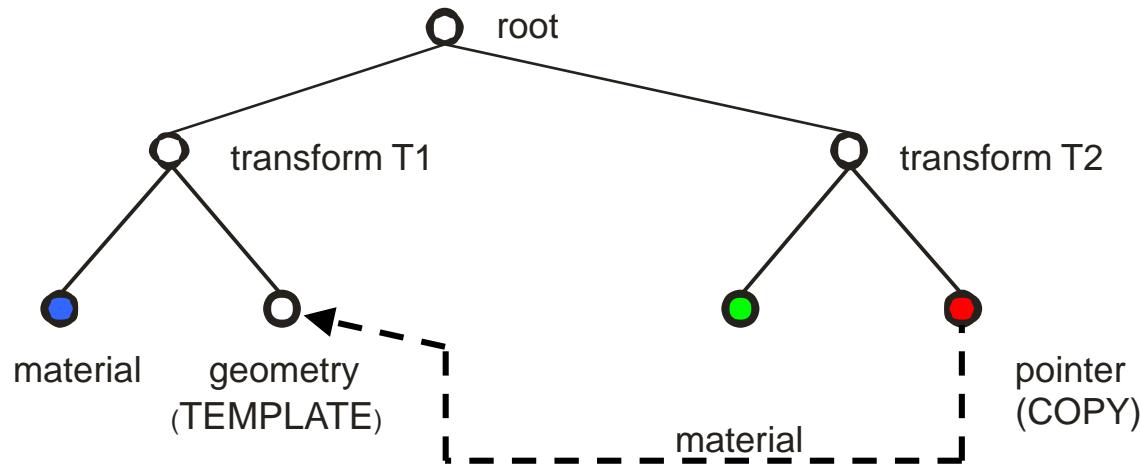
- Logical / Semantical grouping
  - Transformation composition
  - Naming
  - Activation / deactivation
  - Partial spatial sorting



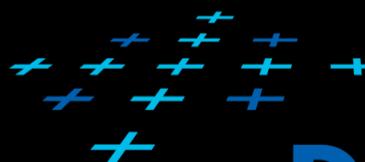
# Scene graph - Instancing

---

- One Template / Many copies



- Saving memory, propagating changes
- Not a tree anymore: DAG!
  - Implications for a renderer



**DCGI**

KATEDRA POČÍTAČOVÉ GRAFIKY A INTERAKCE

Questions?