

**DCGI**

**KATEDRA POČÍTAČOVÉ GRAFIKY A INTERAKCE**

# Introduction to 3D geometry

Jiří Bittner

# Outline

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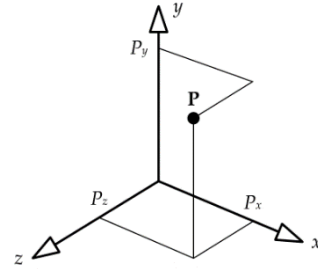
- Points, Vectors, Transformations      MPG – chapter 21
- Camera and Projection      MPG – chapter 9
- 3D Scene Representation      MPG - chapters 5.11,  
5.12, 5.13, 6-8, 14

# Points in 3D

- Point is a location in 3D space

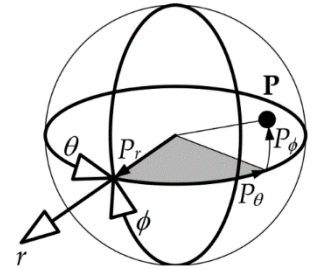
- Cartesian coordinates
  - Orthonormal basis

$$P = \begin{bmatrix} 2 \\ 3 \\ 1 \end{bmatrix}$$



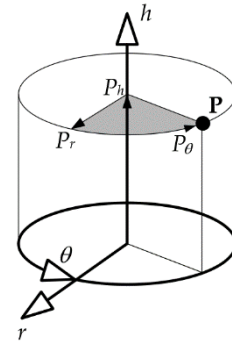
- Spherical coordinates

$$P = \begin{bmatrix} 90^\circ \\ 20^\circ \\ 1 \end{bmatrix}$$



- Cylindrical coordinates

$$P = \begin{bmatrix} 90^\circ \\ 3 \\ 1 \end{bmatrix}$$



# Cartesian coordinates

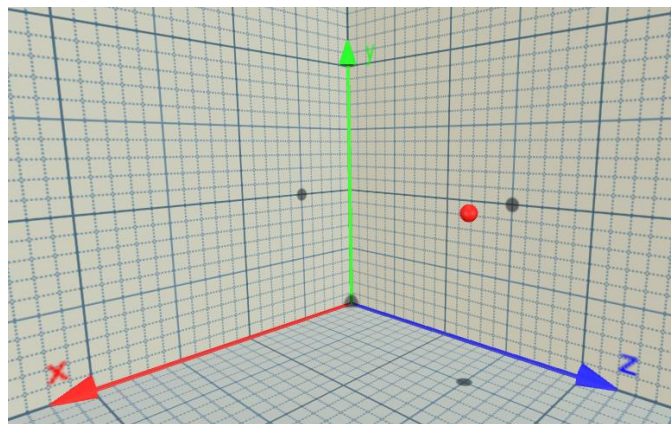
## ■ Axes

- Orthogonal directions
- Meet at origin
- Uniform scale
- Orthogonal basis

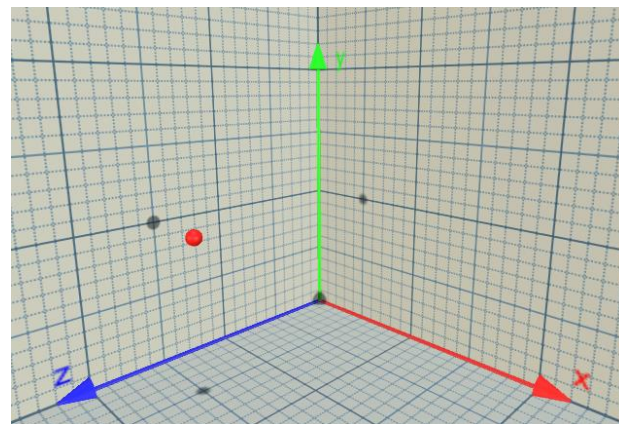
(René Descartes, 1596-1650)

$$A = [5, 10, 15]$$

$$A = \begin{bmatrix} 5 \\ 10 \\ 15 \end{bmatrix}$$



LHS  
Direct3D, Unity, ...



RHS  
OpenGL

# Linear Transformations

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- Scale (Uniform + Non-uniform)
- Mirror
- Shear
- Rotation

$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} 3 \times 3 \\ \text{transformation} \\ \text{matrix} \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

# Homogeneous coordinates

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- Need also: translation, perspective projection
- Add 4-th coordinate

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} \rightarrow \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \approx \begin{bmatrix} x_h \\ y_h \\ z_h \\ w \end{bmatrix} \quad x = \frac{x_h}{w}, y = \frac{y_h}{w}, z = \frac{z_h}{w}$$

- For directions (points in infinity)  $w = 0$

# Transformation in homogeneous coordinates

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- Finally normalize (divide by w)
  - Perspective division

$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} 4 \times 4 \\ \text{transformation} \\ \text{matrix} \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

$$\begin{bmatrix} x'' \\ y'' \\ z'' \end{bmatrix} = \begin{bmatrix} \frac{x'}{w'} \\ \frac{y'}{w'} \\ \frac{z'}{w'} \end{bmatrix}$$

# Composing transformations

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- Matrix multiplication

$$M = R \cdot T \cdot S \dots$$

- Associative

$$A \cdot (B \cdot C) = (A \cdot B) \cdot C$$

- Non-commutative: Transformation order matters!

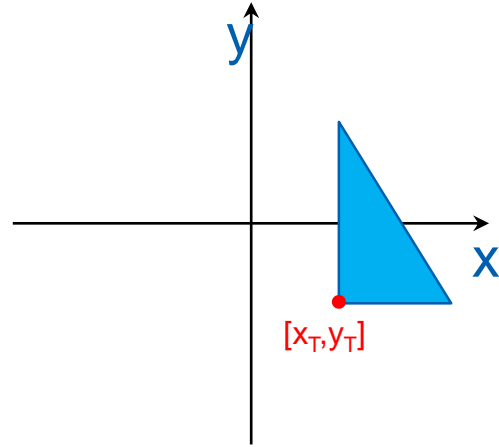
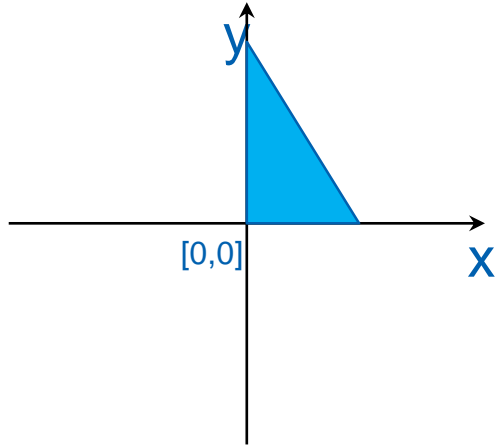
$$A \cdot B \neq B \cdot A$$

- Transformations applied from right to left



# Translation

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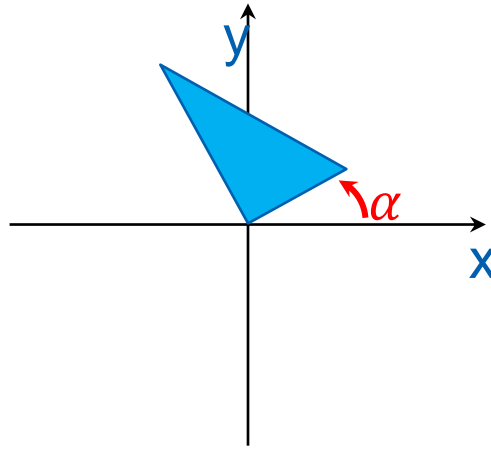
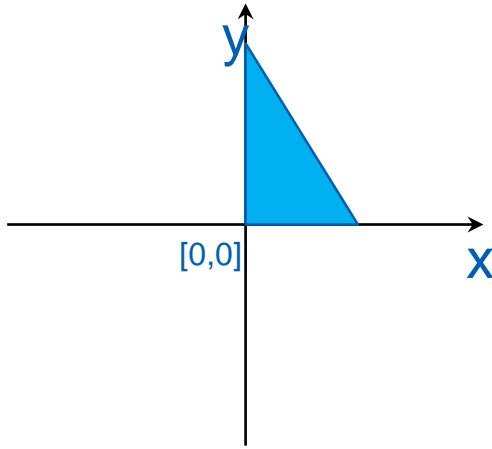


$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = M_T \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix},$$

$$M_T = \begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

# Rotation

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$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = M_{R_z} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix},$$

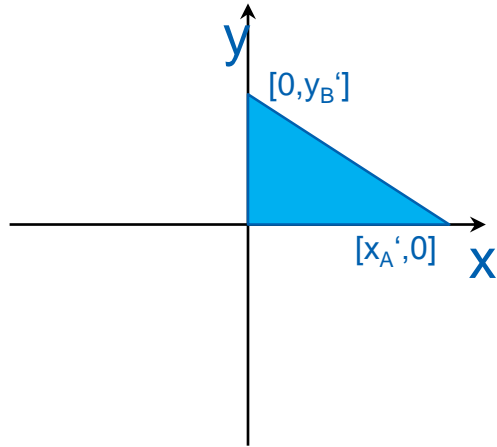
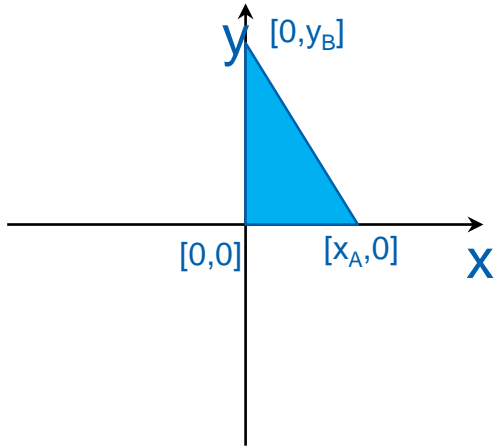
$$M_{R_z} = \begin{bmatrix} \cos \alpha & -\sin \alpha & 0 & 0 \\ \sin \alpha & \cos \alpha & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Euler angles

$$M = M_{R_x} M_{R_y} M_{R_z}$$

# Scaling

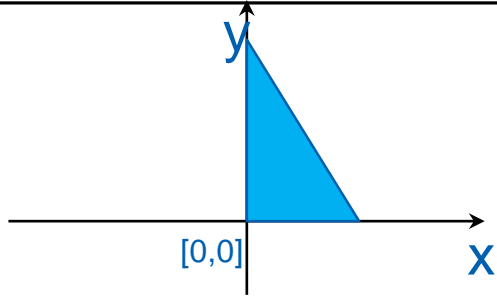
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$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = M_S \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix},$$

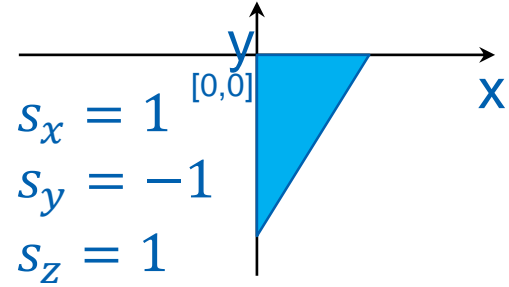
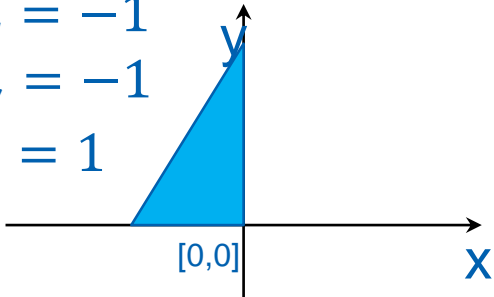
$$M_S = \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

# Symetry



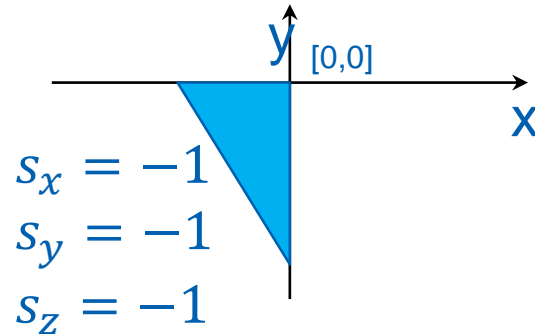
$$M_S = \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{aligned} s_x &= -1 \\ s_y &= -1 \\ s_z &= 1 \end{aligned}$$



$$\begin{aligned} s_x &= 1 \\ s_y &= -1 \\ s_z &= 1 \end{aligned}$$

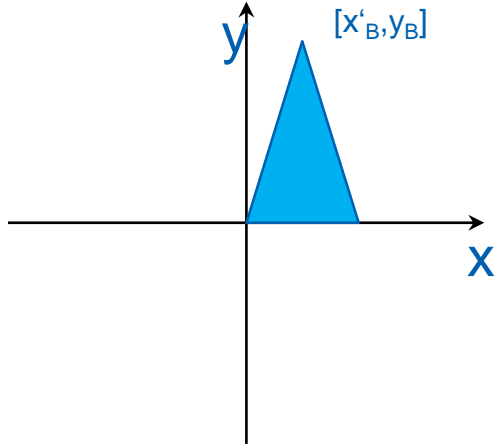
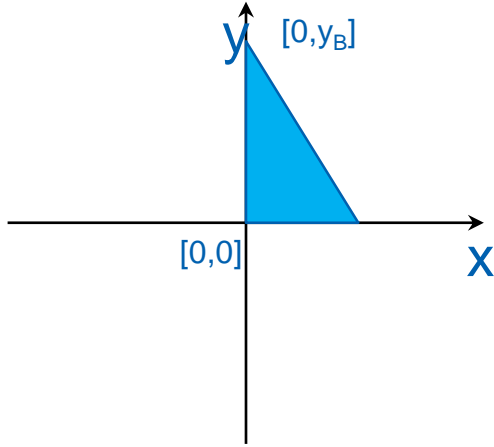
Try to avoid: Odd number of -1 flips polygon orientations!



$$\begin{aligned} s_x &= -1 \\ s_y &= -1 \\ s_z &= -1 \end{aligned}$$

# Shear

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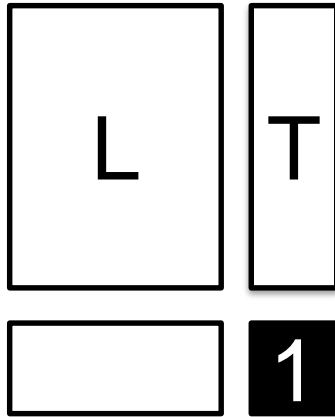
$$M_{SH_x} = \begin{bmatrix} 1 & SH_x & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$SH_x = \frac{x'_B}{y_B}$$

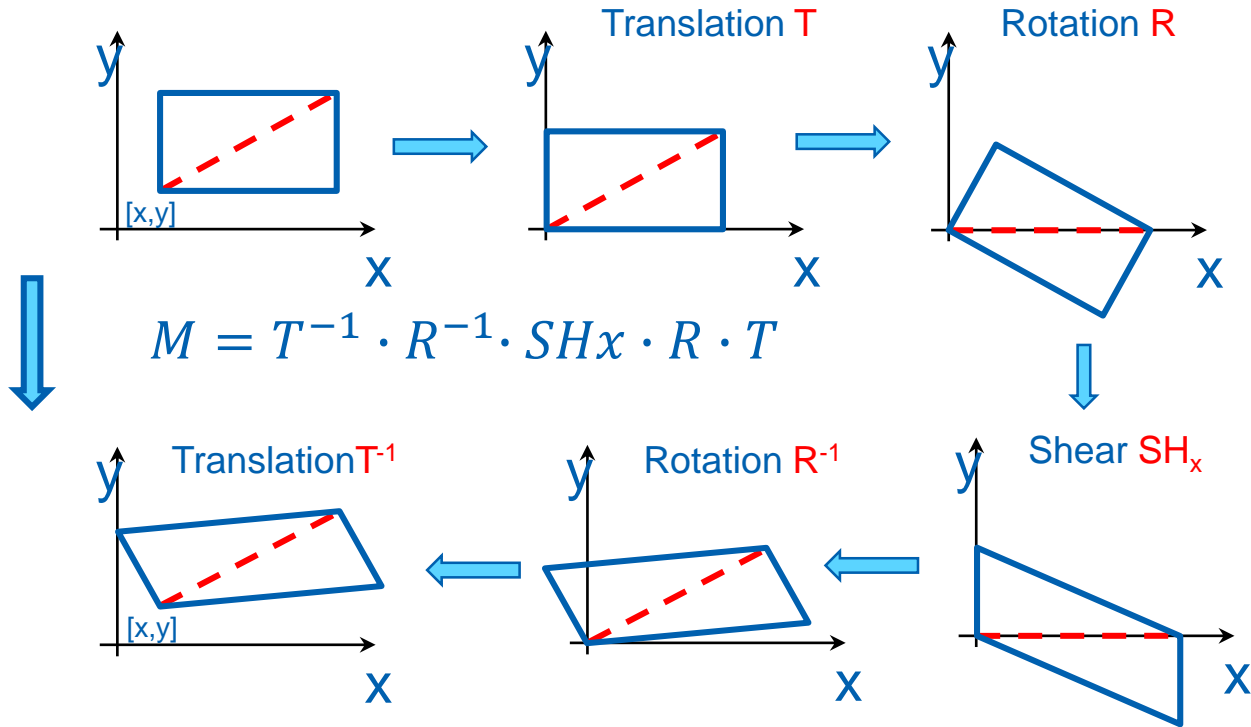
# Transformation matrix

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- L: linear transformation
- T: translation
- Last row (0, 0, 0, 1) for all affine transformations

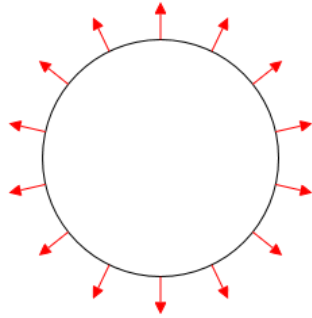


# Example – shear along a diagonal

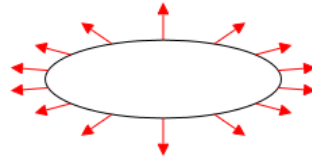


# Transforming normals

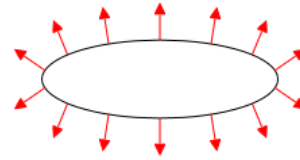
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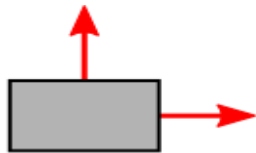
non-uniform scale



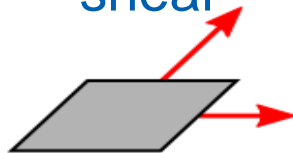
wrong



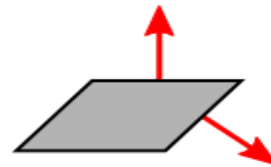
correct



shear



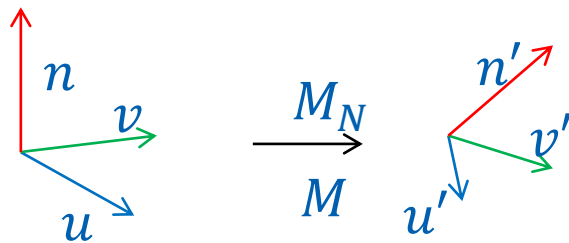
wrong



correct



# Transforming normals



$$\begin{bmatrix} n_x' \\ n_y' \\ n_z' \\ 0 \end{bmatrix} = M_N \begin{bmatrix} n_x \\ n_y \\ n_z \\ 0 \end{bmatrix}$$

$$n^T u = 0$$

$$n'^T u' = 0$$

$$n'^T M u = 0$$

$$n'^T M u = n^T u$$

$$n'^T M = n^T$$

$$M^T n' = n$$

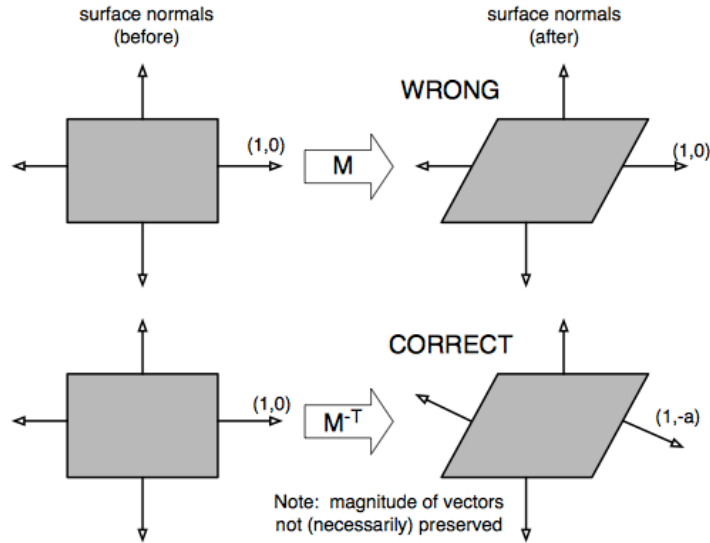
$$n' = M^{T^{-1}} n$$

$$n' = M^{-1T} n$$

Can use just 3x3 submatrix of  $M$  !

# Transforming normals - example

$$M = \begin{bmatrix} 1 & a \\ 0 & 1 \end{bmatrix} \quad M^{-T} = \begin{bmatrix} 1 & 0 \\ -a & 1 \end{bmatrix}$$

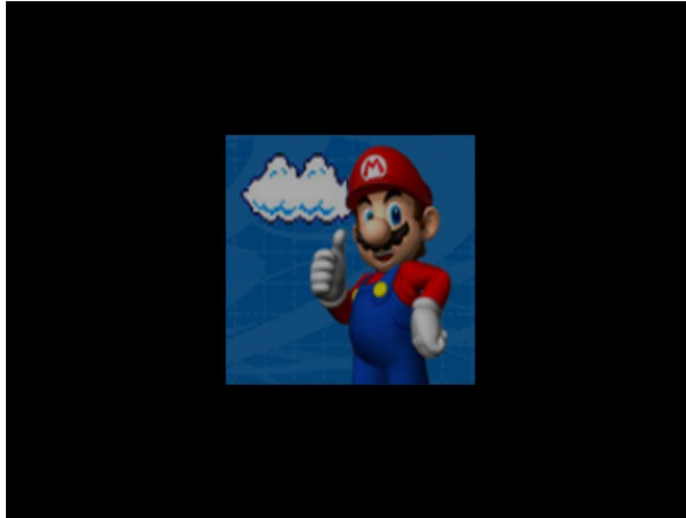


Zdroj: Stack Overflow

# DEMO

<https://cent.felk.cvut.cz/predmety/39PHA/demos/transformations.html>

Transformation example



Model matrix

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Reset

View matrix (read only)

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Reset

# Quaternions

---

- Alternative rotation representation
- Generalization of complex numbers
  - three basis elements  $i, j, k$
  - $i^2 = j^2 = k^2 = i j k = -1, ij = -ji = k, jk = -kj = i, ki = -ik = j$
- Quaternion is a 4-tuple

$$\mathbf{q} = [x, y, z, w]$$

$$\mathbf{q} = i x + j y + k z + w = [\mathbf{v}, w]$$

$$\mathbf{v} = [x, y, z] = i x + j y + k z$$

$$\mathbf{q} = (x, y, z, w) = (\mathbf{v}, r) , \mathbf{v} = xi + yj + zk$$

# Quaternions and Rotation

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- Unit quaternion ( $|q| = 1$ ) represents rotation in 3D

$$q = \left[ a \sin \frac{\alpha}{2}, \cos \frac{\alpha}{2} \right]$$

3D rotation about axis  $a$  by angle  $\alpha$

# Quaternion Operations

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- Sum  $q_1 + q_2 = [v_1 + v_2, w_1 + w_2]$

- Dot product  $q_1 \cdot q_2 = v_1 \cdot v_2 + w_1 \cdot w_2$

- **Multiplication** (Hamilton product)

$$q_1 * q_2 = [v_1, r_1] * [v_2, r_2] = [r_1 v_2 + r_2 v_1 + v_1 \times v_2, r_1 r_2 - v_1 v_2]$$

- *Composition of rotations* (associative, non-commutative)

- **Conjugate**

$$q^* = [-v, r]$$

- Inverse rotation

# Transformation with quaternion

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- Express vector as quaternion

$$\mathbf{u} = (x, y, z, 0)$$

- Rotation of  $\mathbf{u}$  using  $q$

$$\mathbf{u}' = (x', y', z', 0) = q * \mathbf{u} * q^*$$

- Two quaternion multiplications + conjugate

# Quaternion to Rotation Matrix

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- Quaternion  $\mathbf{q} = [x, y, z, w]$  corresponds to rotation matrix

$$\mathbf{R} = \begin{pmatrix} 1 - 2y^2 - 2z^2 & 2xy - 2wz & 2xz + 2wy \\ 2xy + 2wz & 1 - 2x^2 - 2z^2 & 2yz - 2wx \\ 2xz - 2wy & 2yz + 2wx & 1 - 2x^2 - 2y^2 \end{pmatrix}$$

- Rotation composition faster with quaternions
- Vector transformation faster with matrix



# Rotation Interpolation

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- Matrix interpolation
  - breaks orthonormality - artefacts
- Quaternion interpolation
  - Linear interpolation (LERP)
  - Spherical linear interpolation (SLERP) - constant angular step

# LERP and SLERP

$$q = \frac{w_A q_A + w_B q_B}{|w_A q_A + w_B q_B|}$$

## LERP

$$w_A = 1 - \beta$$

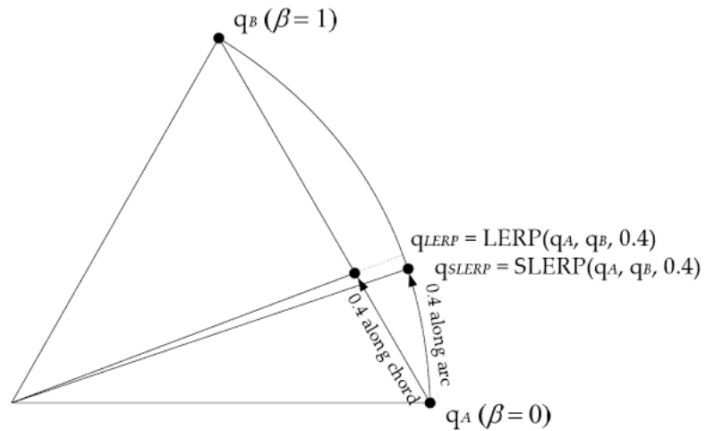
$$w_B = \beta$$

## SLERP

$$w_A = \frac{\sin(1 - \beta)\theta}{\sin \theta}$$

$$w_B = \frac{\sin \beta\theta}{\sin \theta}$$

$$\theta = \arccos q_A q_B$$



J. Gregory, Game Engine Architecture

# Transformation Representation - SQT

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- SQT (SRT)
  - Scale, Quaternion, Translation
- Uniform scale:  $1+4+3 = 8$  scalars
  - Sequence of SQT can be composed to SQT
- Non-uniform scale:  $3+4+3=10$  scalars
- Correct interpolation of rotation, scale and translation !
- Compact representation
- Fast composition of transformations
- Slower application of transformation

# Transformation Representation - Matrix

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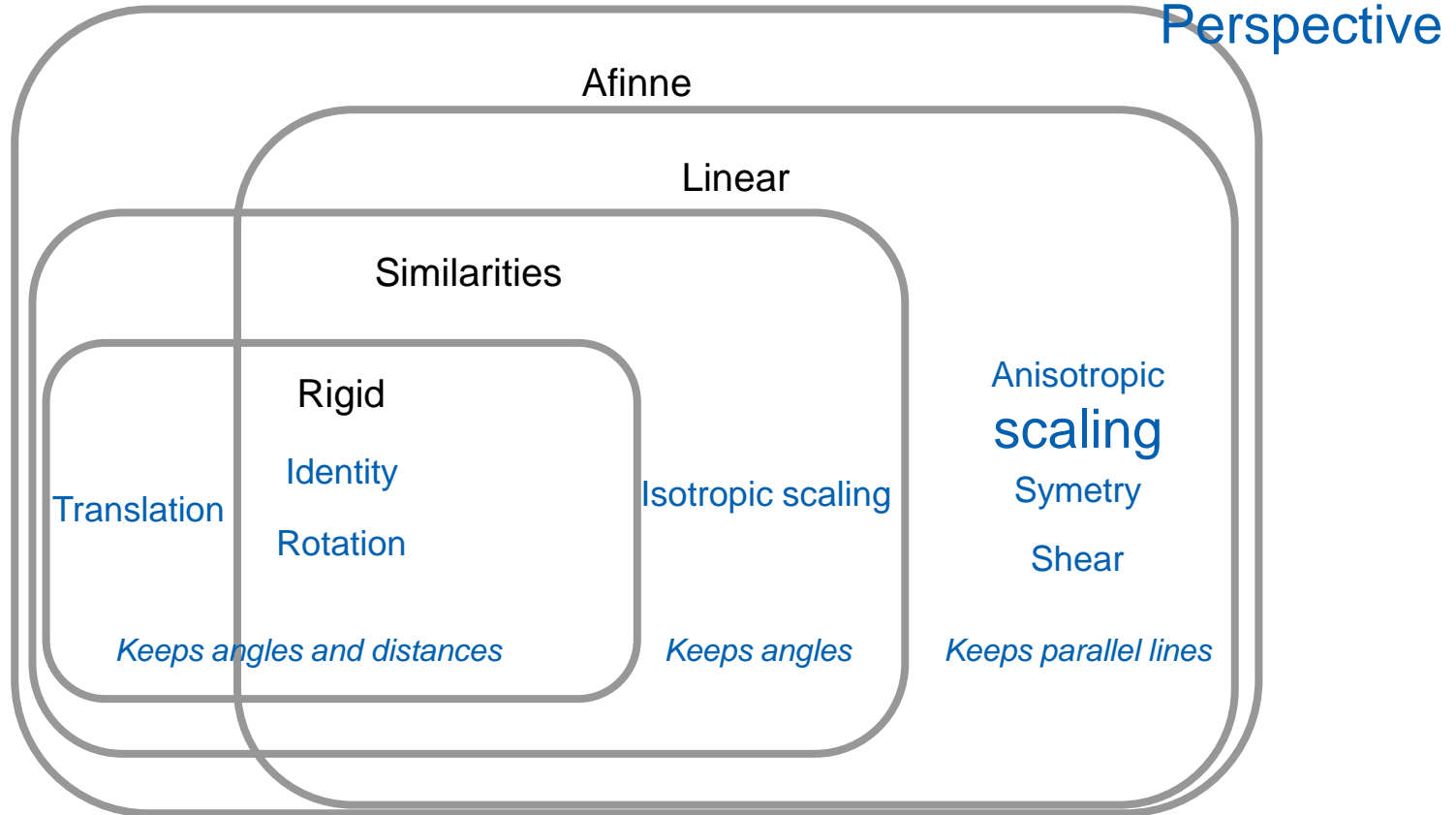
- Matrix 4x4
- General affine transformation + perspective
- Simple concatenation (matrix multiplication)
- Fast application of transformation

# Transformation – Summary

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- Interpolace a skládání rotací pomocí kvaternionů (animace)
- Transformace vektorů pomocí matice (zobrazování)
- Conversions between representations

# Transformations



# Outline

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- Points, Vectors, Transformations      MPG – chapter 21
- Camera and Projection      MPG – chapter 9
- 3D Scene Representation      MPG - chapters 5.11,  
5.12, 5.13, 6-8, 14

# Camera

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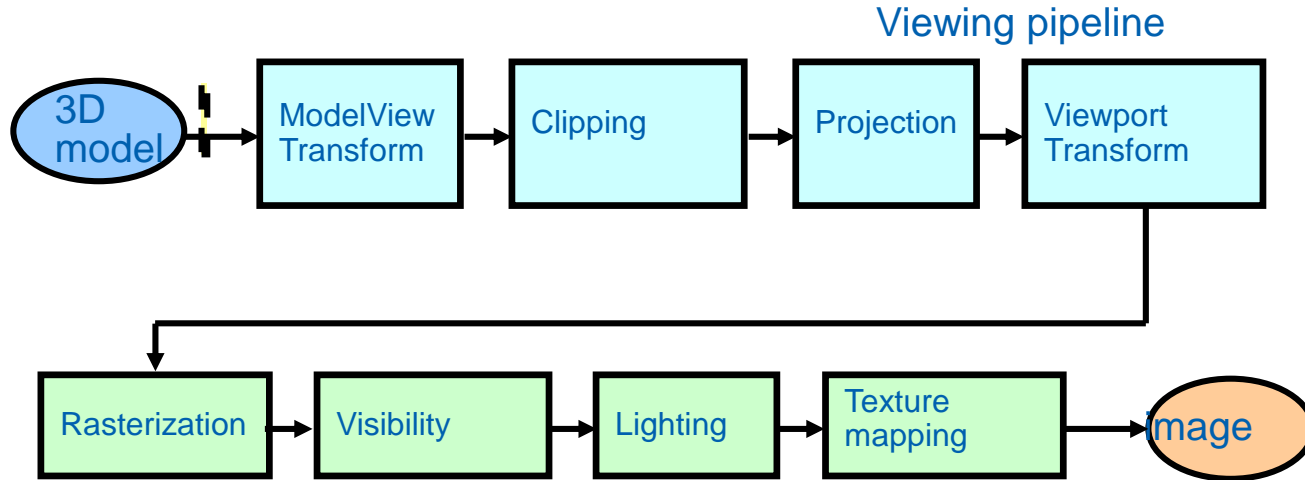
- Idealized camera (pin-hole)
  - Idealized geometric optics
  - Realistic effects as post process
- Camera description
  - Explicit parameters (position, orientation)
  - Node in a scene graph
  - Other parameters – viewing angle, viewport, rendering setup, ...
- Series of transformations
  - Viewing transformation (camera position / orientation)
  - Projection transformation (viewing volume)
  - Viewport transformation (viewport on the screen)
  - Composed with the modeling transformation



# Rendering Pipeline

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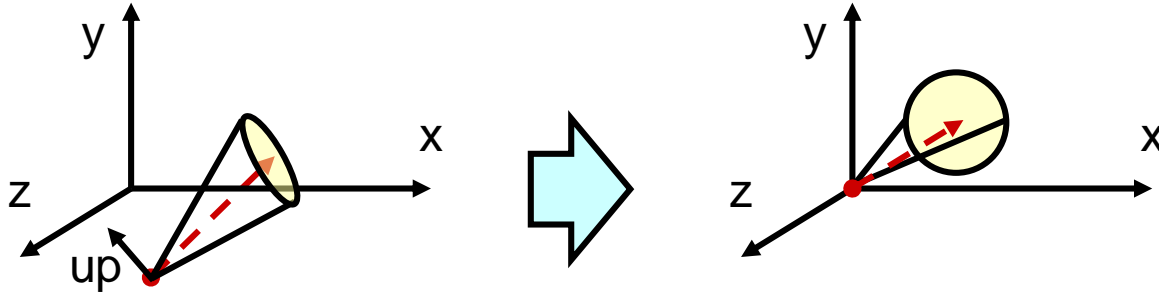
- 1. part – transformations (*viewing pipeline*)
- 2. part – further operations



# View transformation

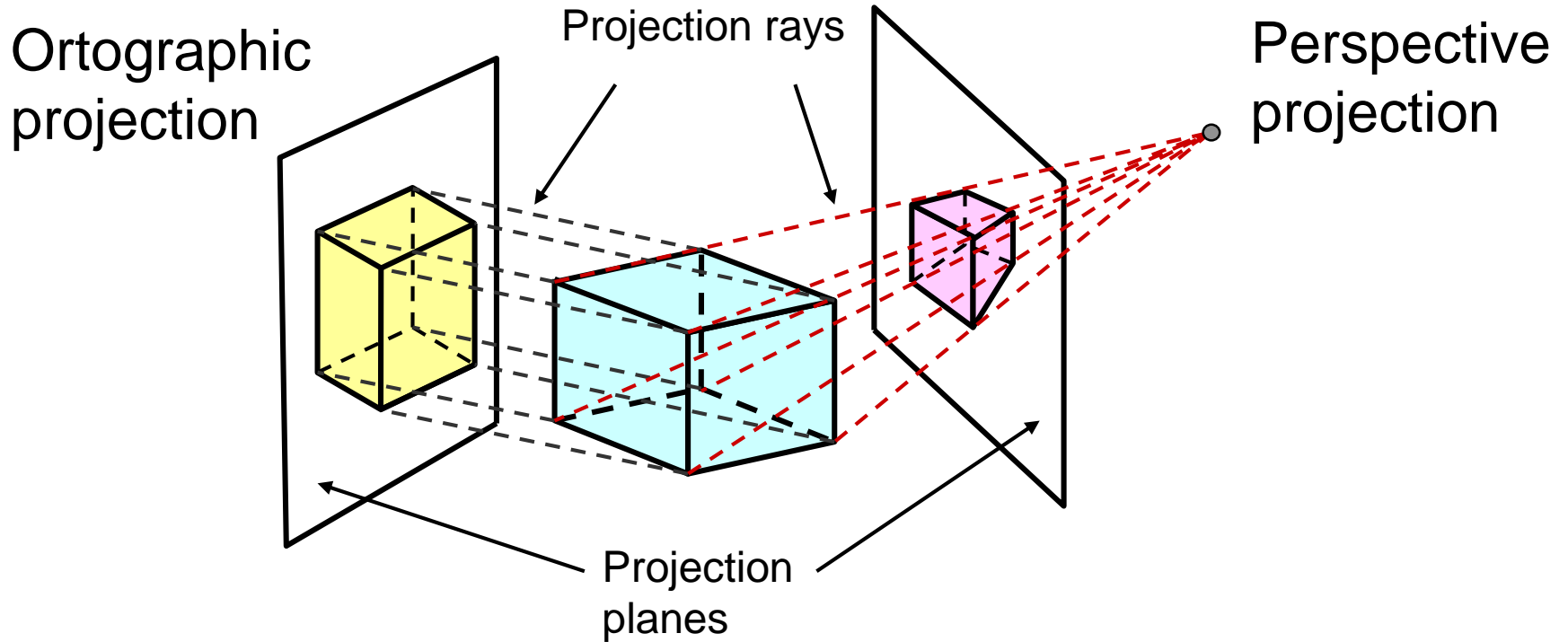
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- Transformation of scene to unified position



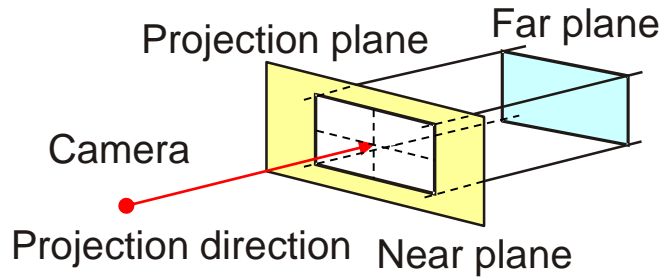
- Camera position** to  $[0,0,0]$  ... translation
- View direction** // with z axis ... rotation
- Up vector** // with y axis ... rotation around z axis
- Camera matrix  $M$ : Viewing transformation =  $M^{-1}$

# Orthographic and perspective projection

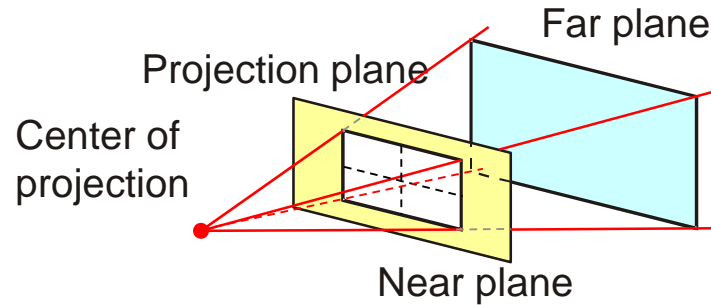


# Camera – projection transformation

- Transformation from space to projection plane
- *Viewing volume / frustum (záběr)*



Orthographic projection  
view volume = cuboid



Perspective projection  
view volume = pyramid frustum

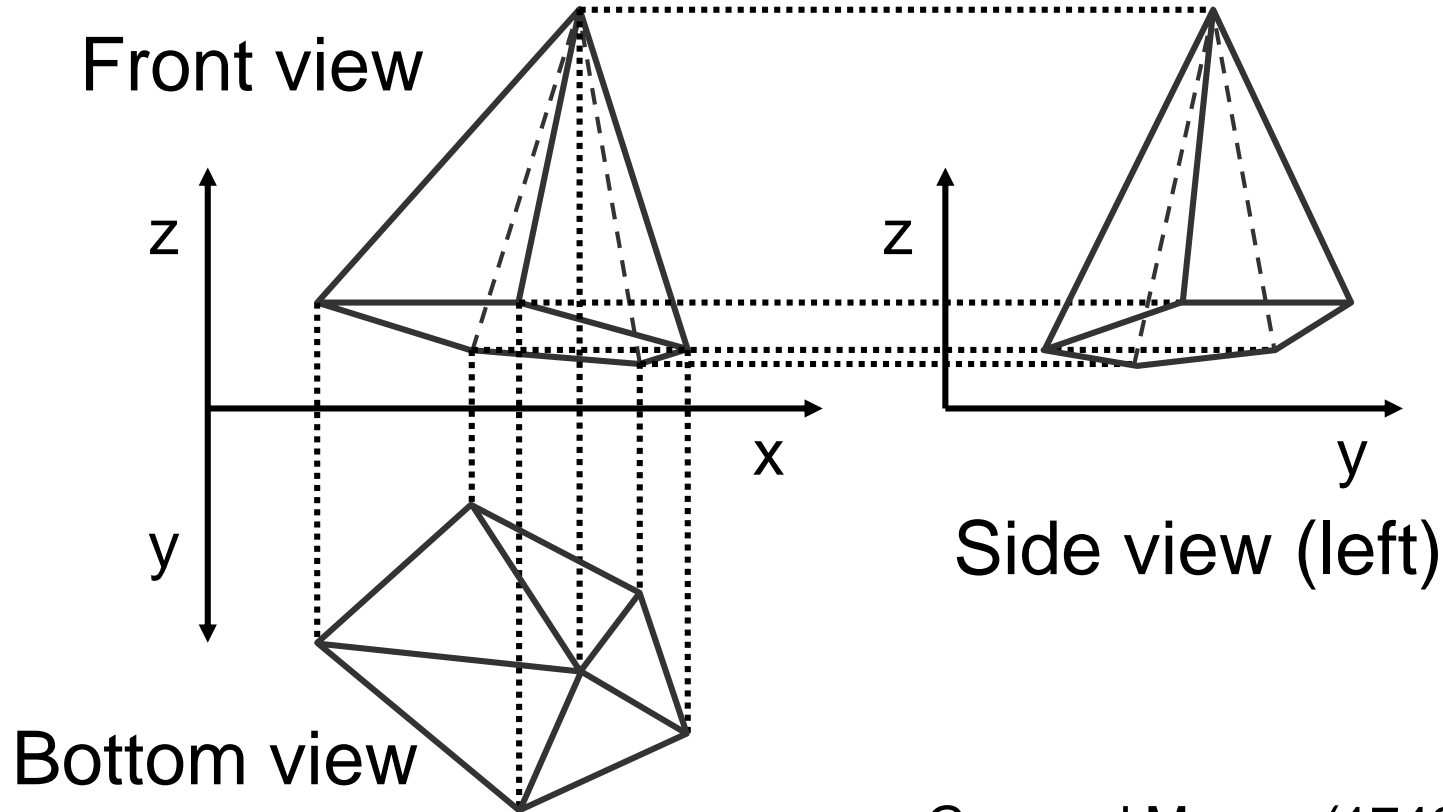
# Orthographic Projection

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- All rays parallel!
- Rays **orthogonal** to projection plane
  - Monge's projection: top, front, side
  - Axonometry (arbitrary projection plane)
- Rays **non-orthogonal** to projection plane (oblique projection)
  - Cavalier projection (the same scale on axes)
  - Cabinet projection (z axis scale = 1/2)

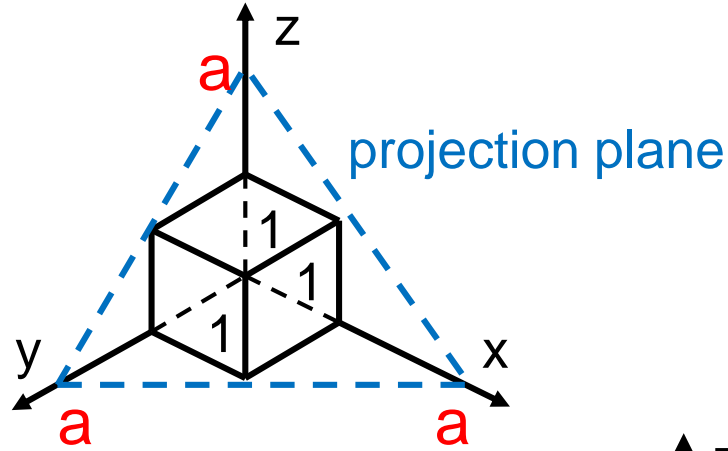
# Monge's projection

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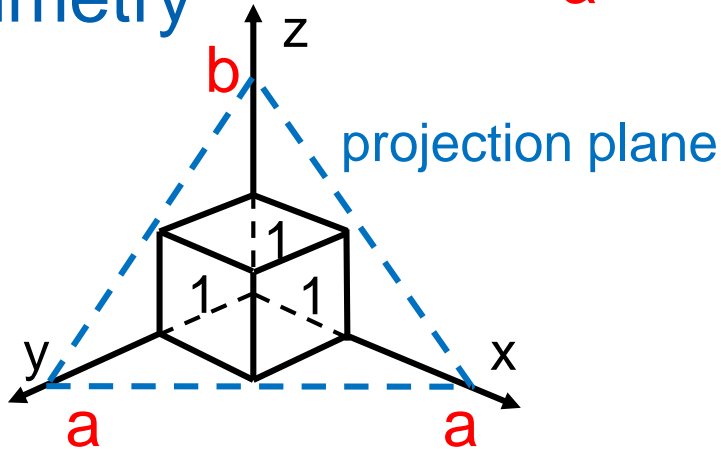


# Axonometry

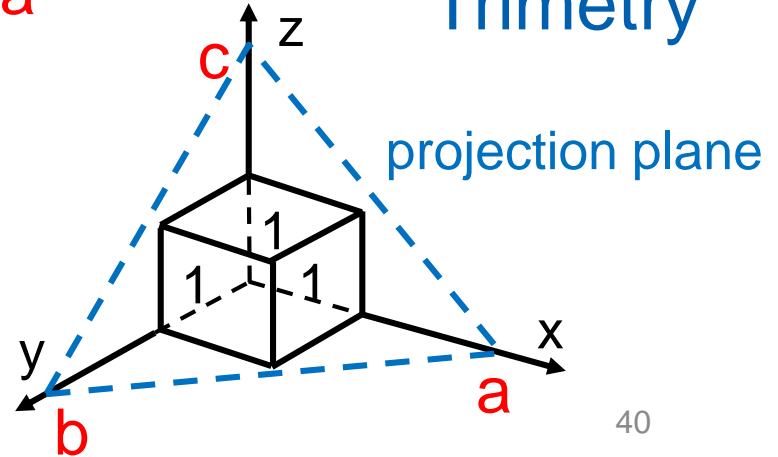
## Isometry



## Dimetry

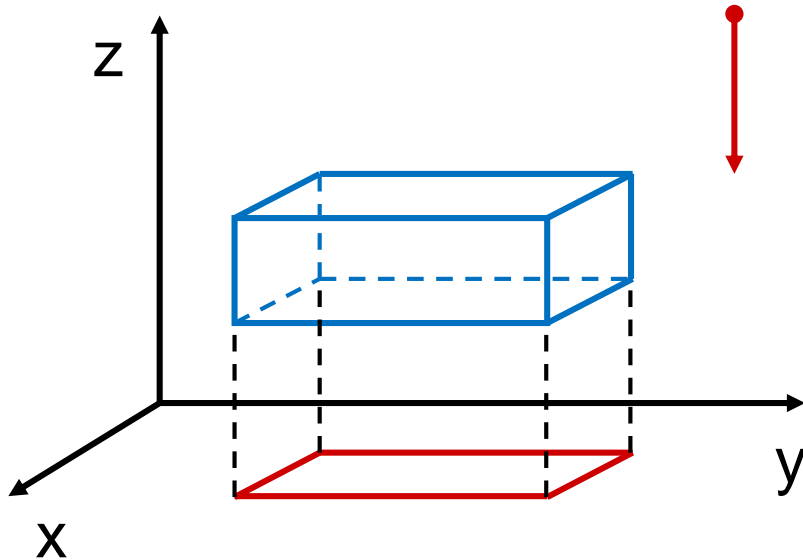


## Trimetry



# Projection: Matrix Form

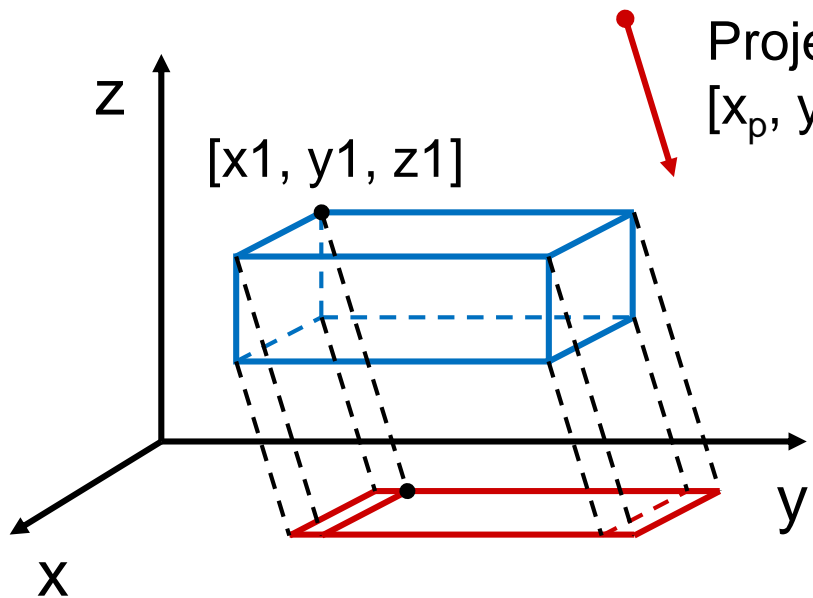
- Align projection direction to  $z$  axis (rotation)
- Projection plane =  $xy$



$$M_{//} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



# Oblique Projection



$$\begin{aligned}x &= x_1 + x_p \cdot t \\y &= y_1 + y_p \cdot t \\z &= z_1 + z_p \cdot t\end{aligned}$$

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$$z = 0 \Rightarrow t = -z_1 / z_p$$

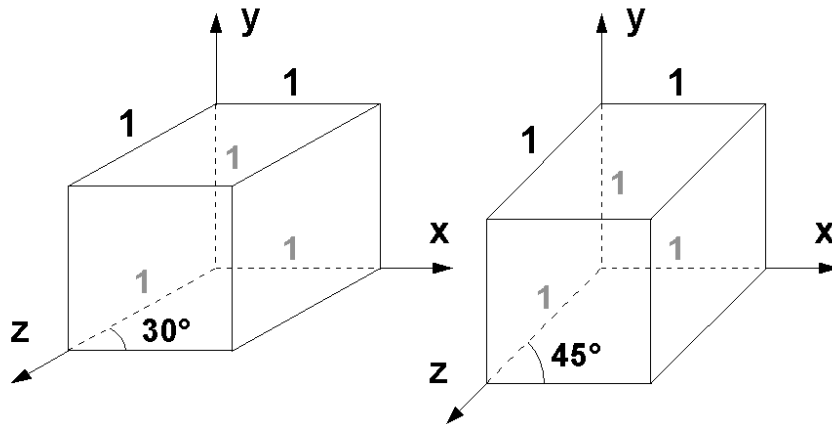
$$M = \begin{bmatrix} 1 & 0 & -\frac{x_p}{z_p} & 0 \\ 0 & 1 & -\frac{y_p}{z_p} & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$M = M_{//} \cdot M_{zk}$$

# Oblique Projection

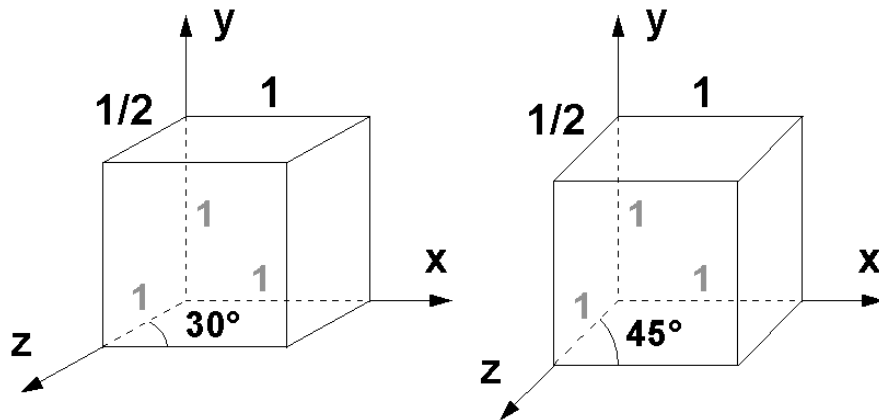
## Cavalier

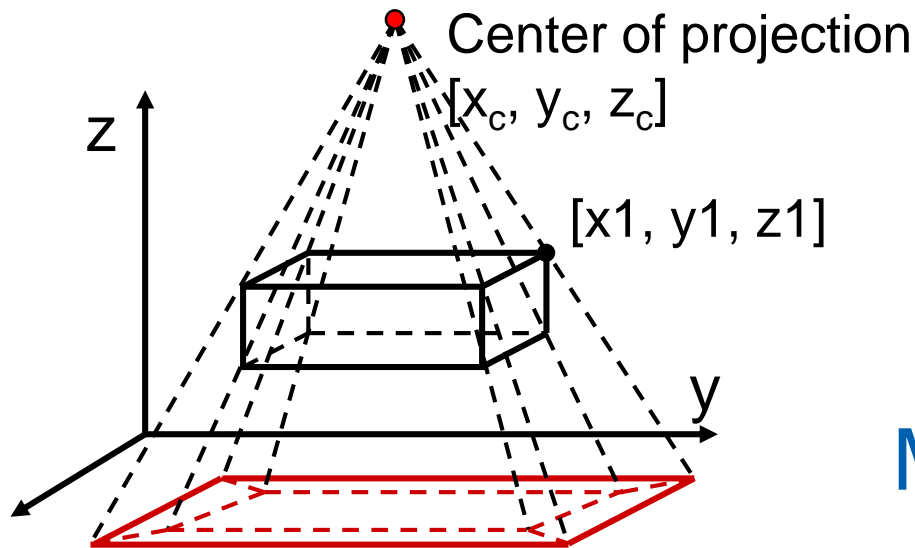
$$M = \begin{bmatrix} 1 & 0 & -\cos \beta & 0 \\ 0 & 1 & -\sin \beta & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



## Cabinet

$$M = \begin{bmatrix} 1 & 0 & \frac{-\cos \beta}{2} & 0 \\ 0 & 1 & \frac{-\sin \beta}{2} & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$





$$\begin{aligned}
 x &= x_c + (x_1 - x_c) \cdot t \\
 y &= y_c + (y_1 - y_c) \cdot t \\
 z &= z_c + (z_1 - z_c) \cdot t
 \end{aligned}$$

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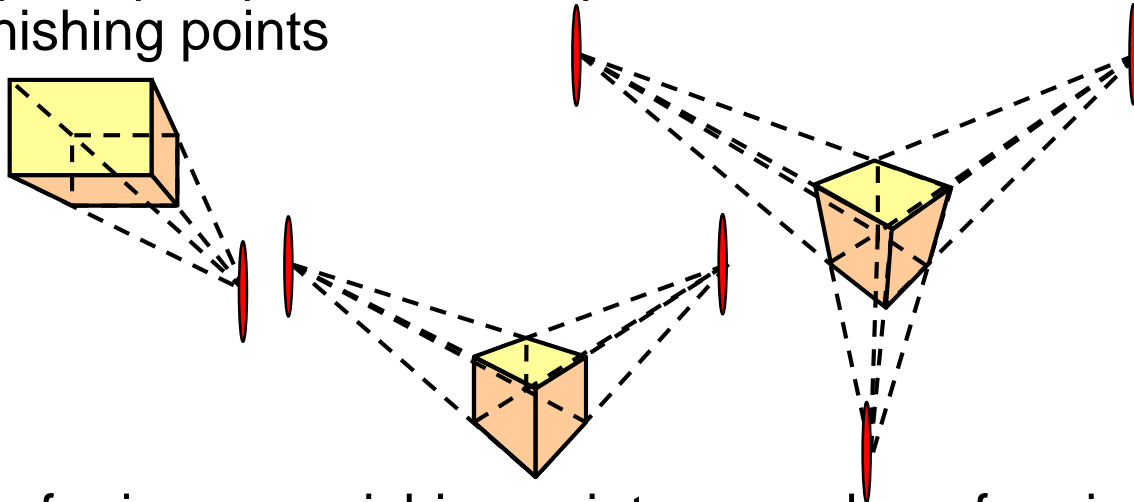

$$z = 0 \Rightarrow t = z_c / (z_c - z_1)$$

$$M = \begin{bmatrix} 1 & 0 & -\frac{x_c}{z_c} & 0 \\ 0 & 1 & -\frac{y_c}{z_c} & 0 \\ 0 & 0 & \frac{z_c}{z_c} & 0 \\ 0 & 0 & -\frac{1}{z_c} & 1 \end{bmatrix}$$

# Vanishing Points (Úběžníky)

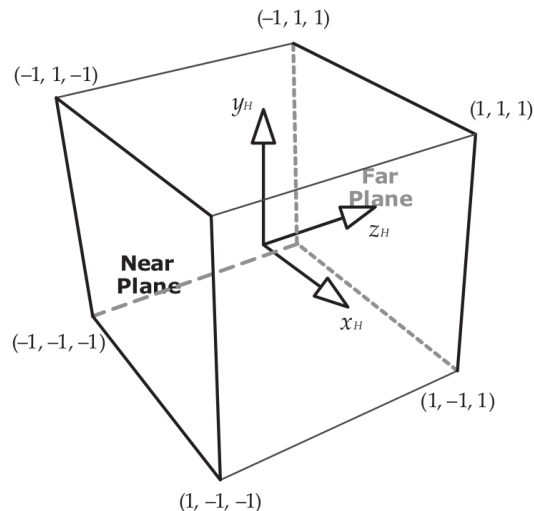
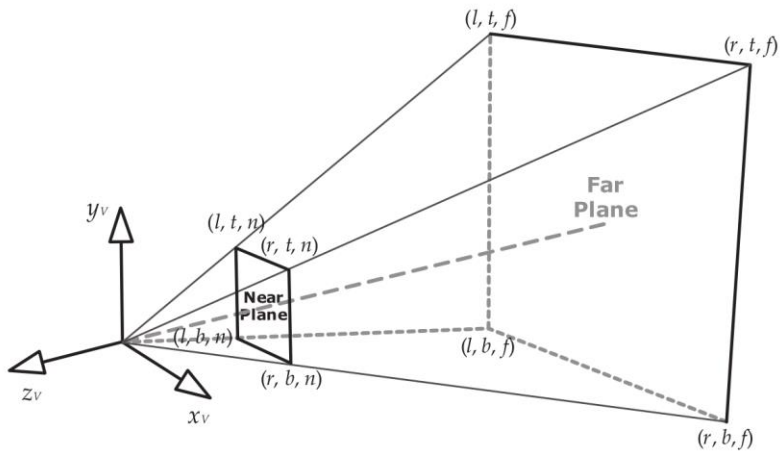
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- Perspective projection does not keep parallelism
- 1-, 2-, 3-point perspective: lines parallel to coordinate axes meet in primary vanishing points



- Number of primary vanishing points = number of projection plane intersections with coordinate axes

# Perspective projection (OpenGL)

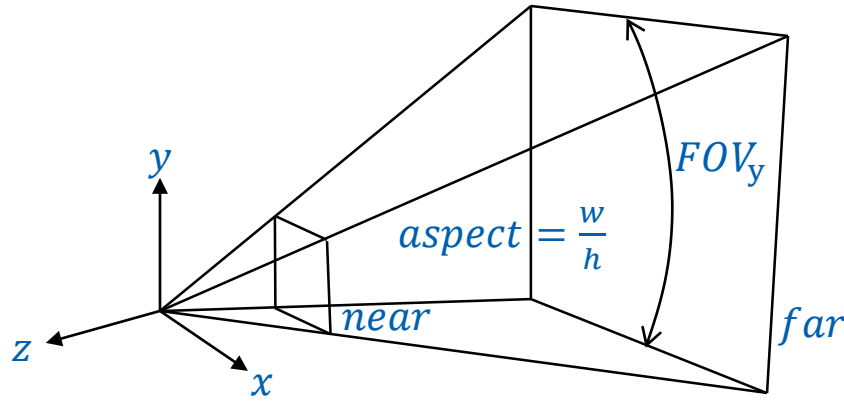


camera / eye space

$$P = \begin{bmatrix} \frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\ 0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\ 0 & 0 & -\frac{f+n}{f-n} & -\frac{2nf}{f-n} \\ 0 & 0 & -1 & 0 \end{bmatrix}$$

NDC / clip space

# Symmetrical Perspective Projection



$$P = \begin{bmatrix} \frac{\cotg \frac{FOV_y}{2}}{aspect} & 0 & 0 & 0 \\ 0 & \cotg \frac{FOV_y}{2} & 0 & 0 \\ 0 & 0 & -\frac{f+n}{f-n} & -\frac{2nf}{f-n} \\ 0 & 0 & -1 & 0 \end{bmatrix}$$

# Camera – viewport transformation

---

- Size and position of the viewport

$$x' = (x_{\text{NDC}} + 1) \frac{W}{2} + X$$

$$y' = (y_{\text{NDC}} + 1) \frac{H}{2} + Y$$

- $x_{\text{NDC}}$  and  $y_{\text{NDC}}$  result of previous transf. (range -1..1)

# Coordinate systems overview

---

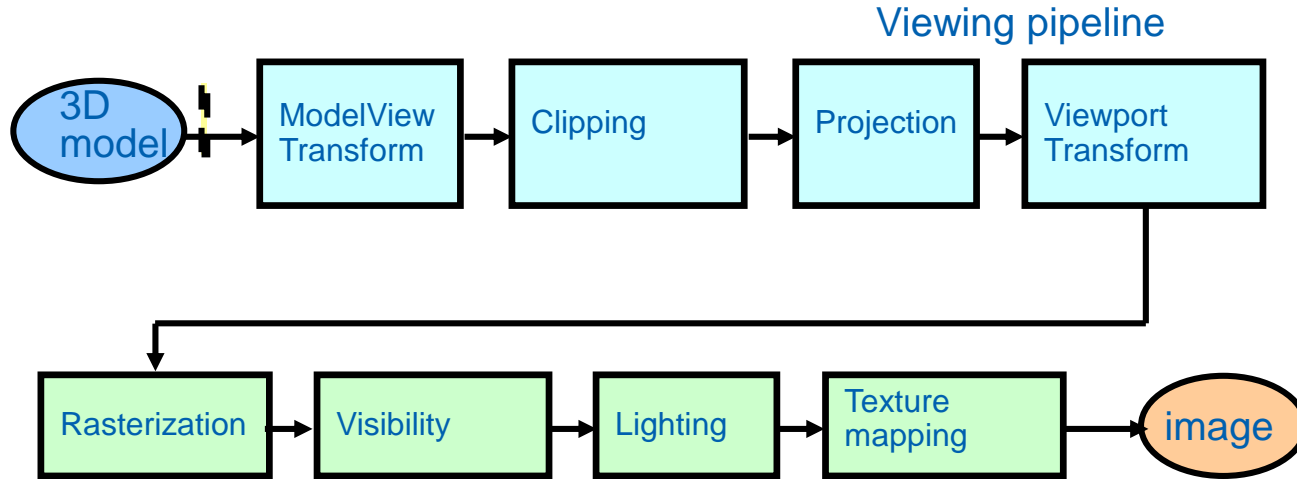
- Object / Modeling / Local coordinates
  - Relative to object origin
- World coordinates
  - Global scene coordinates
- Camera / Eye / View coordinates
  - Camera in the origin, looks along  $-z$
- Clip coordinates
  - After multiplication by projection matrix
- Normalized device coordinates
  - Cuboid after perspective division  $[-1,-1,-1] - [1,1,1]$
- Screen / Window coordinates
  - $x, y$  pixel position,  $z$  in  $0..1$  range



# Rendering Pipeline

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- 1. part – transformations (*viewing pipeline*)
- 2. part – further operations



# Outline

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- Points, Vectors, Transformations MPG – chapter 21
- Camera and Projection MPG – chapter 9
- 3D Scene Representation MPG - chapters  
5.11, 5.12, 5.13, 6-8, 14

# Introduction to 3D geometry

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- Scene = mathematical model of *the world* in computer
  - Rendering
  - Animation
  - Colisions
  - ...
- Geometry (3D models)
- Materials
- Lights
- Camera
- ...



# 3D Models

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- Boundary representation (B-rep)
- Volumetric representation
- Constructive solid geometry (CSG)
- Implicit surfaces
- Point clouds
- ...

# Polygonal Mesh

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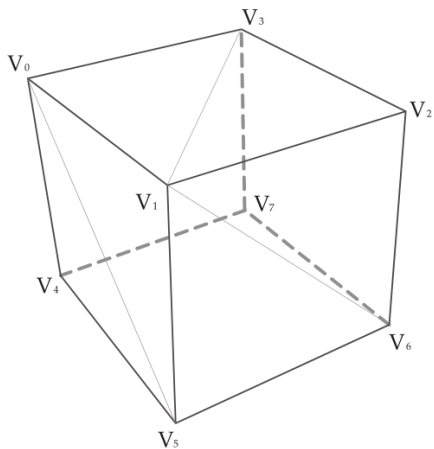
- Classical boundary representation
- Describes object surface (vertices, edges, faces)
- List of polygons defining object boundary (surface)
  - Better convex polygons
  - Even better just triangles (triangulation)
- Different representations
  - Sequence of vertices (separator)
  - Vertex array + index array
  - ...

# Triangle Mesh

---

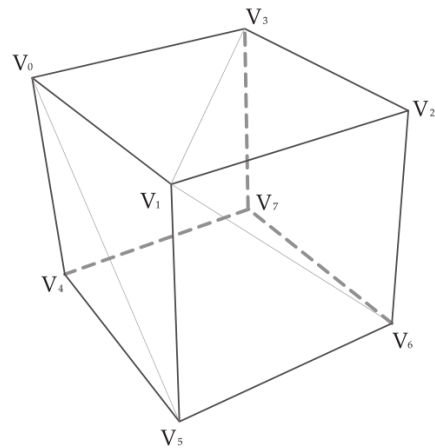
- Just triangles
  - HW friendly !
  - Simplified rendering, clipping, collisions, ...
- Mathematics of a triangle
  - In visibility / ray intersection lecture...

# Triangle Mesh



V <sub>0</sub>	V <sub>1</sub>	V <sub>3</sub>	V <sub>1</sub>	V <sub>2</sub>	V <sub>3</sub>	V <sub>0</sub>	V <sub>5</sub>	V <sub>1</sub>	...	V <sub>5</sub>	V <sub>7</sub>	V <sub>6</sub>
----------------	----------------	----------------	----------------	----------------	----------------	----------------	----------------	----------------	-----	----------------	----------------	----------------

triangle list



Vertices 

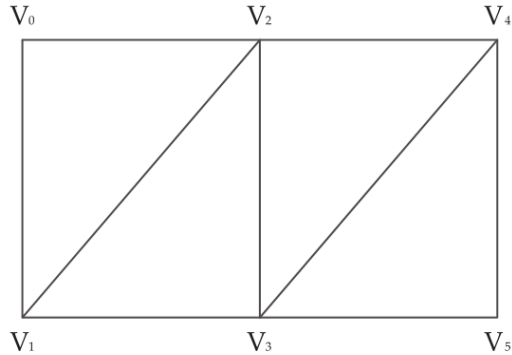
V <sub>0</sub>	V <sub>1</sub>	V <sub>2</sub>	V <sub>3</sub>	V <sub>4</sub>	V <sub>5</sub>	V <sub>6</sub>	V <sub>7</sub>
----------------	----------------	----------------	----------------	----------------	----------------	----------------	----------------

Indices 

0	1	3	1	2	3	0	5	1	...	5	7	6
---	---	---	---	---	---	---	---	---	-----	---	---	---

indexed triangle list

# Triangle Mesh – Compact Representation



Vertices 

V <sub>0</sub>	V <sub>1</sub>	V <sub>2</sub>	V <sub>3</sub>	V <sub>4</sub>	V <sub>5</sub>
----------------	----------------	----------------	----------------	----------------	----------------

Interpreted as triangles: 

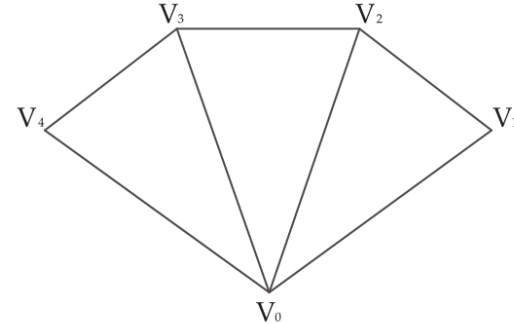
0	1	2
---	---	---

1	3	2
---	---	---

2	3	4
---	---	---

3	5	4
---	---	---

triangle strip



Vertices 

V <sub>0</sub>	V <sub>1</sub>	V <sub>2</sub>	V <sub>3</sub>	V <sub>4</sub>
----------------	----------------	----------------	----------------	----------------

Interpreted as triangles: 

0	1	2
---	---	---

0	2	3
---	---	---

0	3	4
---	---	---

triangle fan

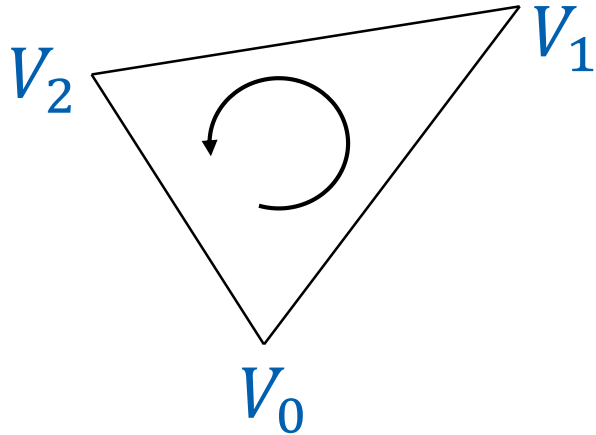
No indices – saves memory!



# Triangle Mesh – Winding Order

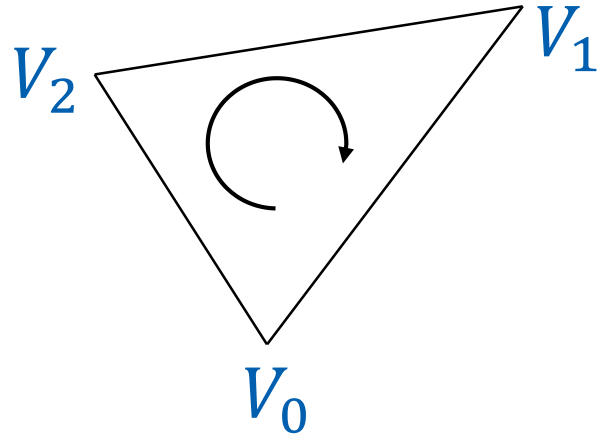
---

- Defining front and back faces



$V_0V_1V_2$

CCW (counter clock wise)



$V_0V_2V_1$

CW (clock wise)

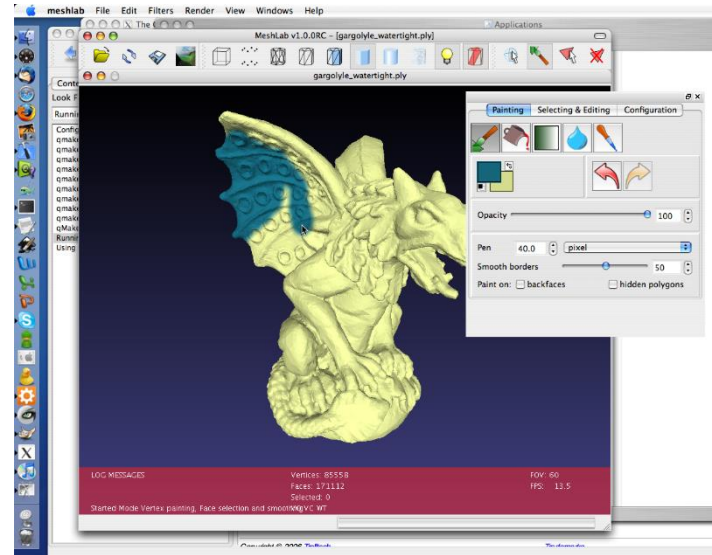
# Storing Other Information

---

- Vertices
  - Position, normal, texture coordinates, color, ...
- Edges
  - sharp, auxiliary
- Faces
  - normal, material
- Solids
  - material, texture

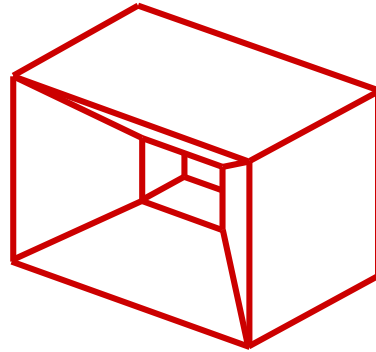
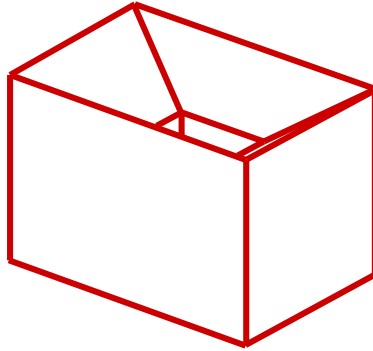
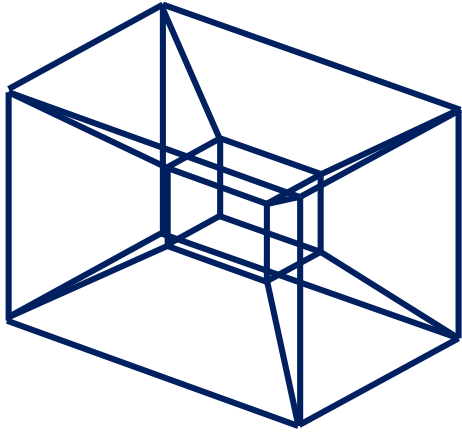
# Triangle Mesh

- Modeling
  - Maya, 3DS Max, Blender, Cinema
- Editing / Optimization
  - MeshLab
  - NvTriStrip
  - ...



# Wireframe Model

---

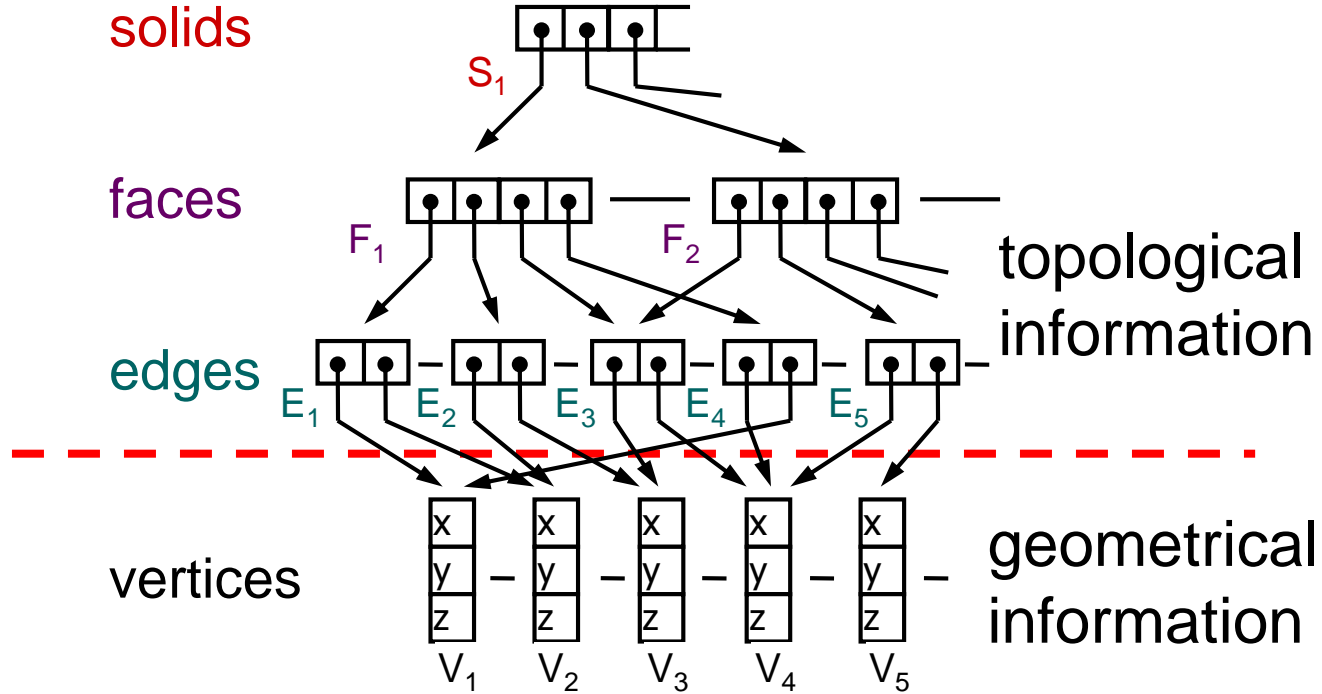


Ambiguous interpretation

But very useful  
for debugging!

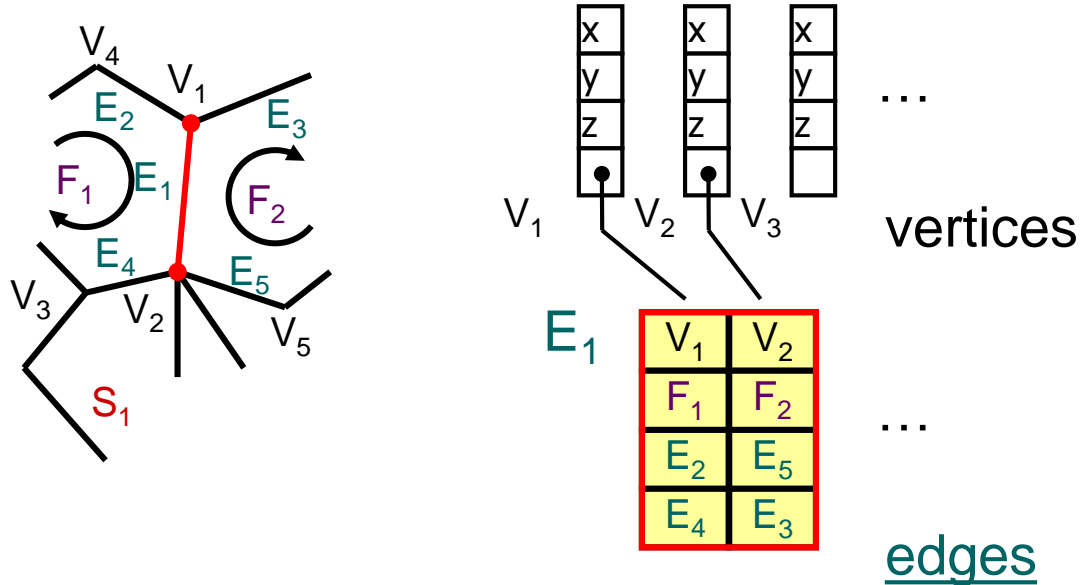
# Mesh Graph

## Hierarchical representation



# Winged-Edge

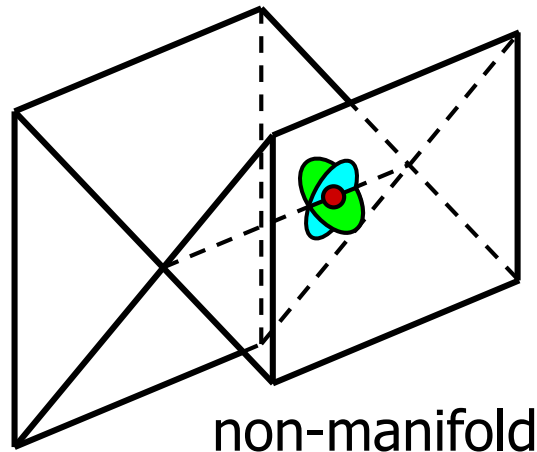
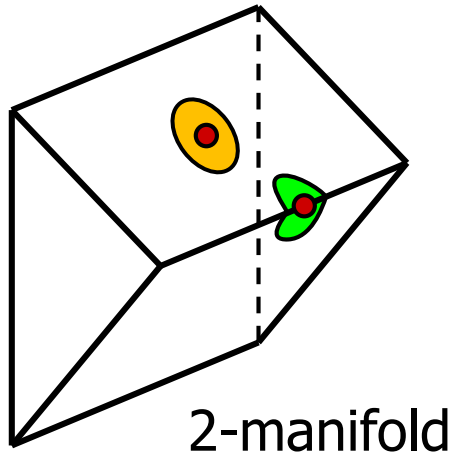
- Information about the neighborhood
- Useful for editing & maintaining consistency



# Model Unambiguity

---

- Manifold (rozvinutelný)
- 2-manifold: for every surface point there is a neighborhood topologically equivalent with plane
- Important for manufacturing, CAD/CAM

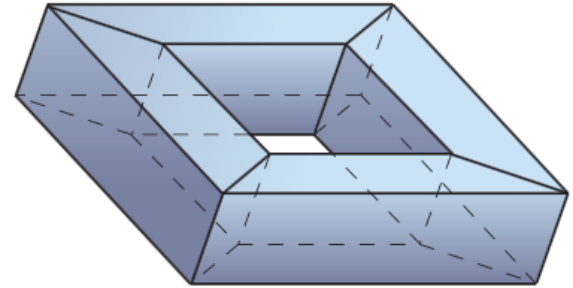


# Euler-Poincare Formula for Manifolds

---

$$V - E + F - R = 2(S - H)$$

- V #vertices
- E #edges
- F #faces
- R #rings (holes in faces)
- H #holes (holes through object)
- S #shells (separate objects)



$$V=16$$

$$E=32$$

$$F=16$$

$$R=0$$

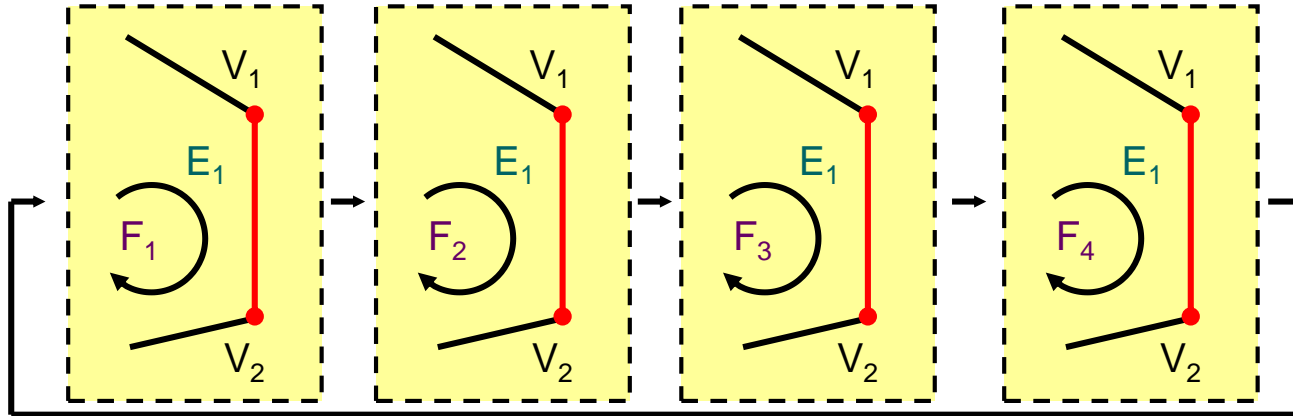
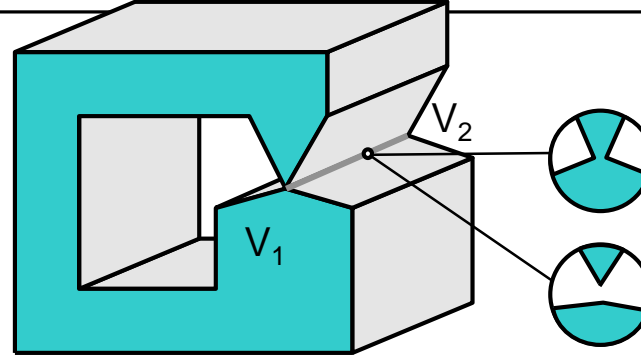
$$H=1$$

$$S=1$$



# Representing non-manifolds

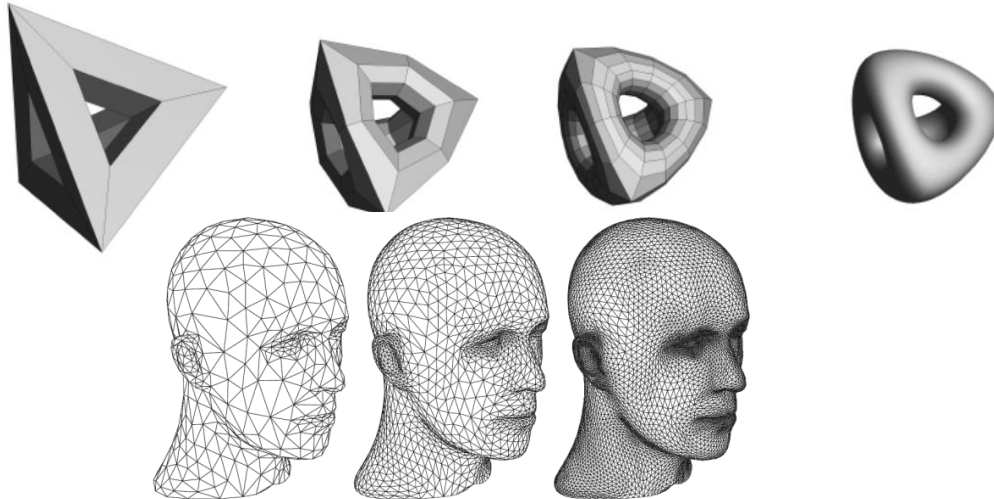
- Winged half-edge



# Subdivision Surfaces

---

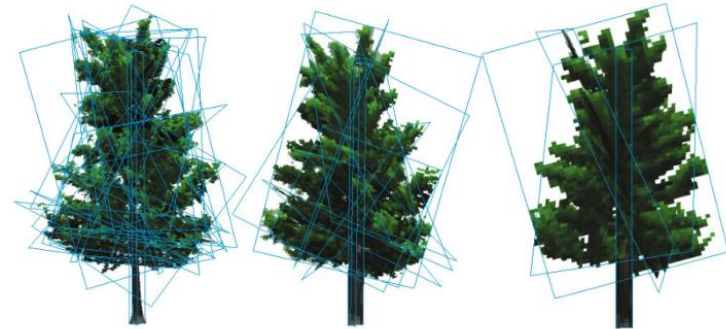
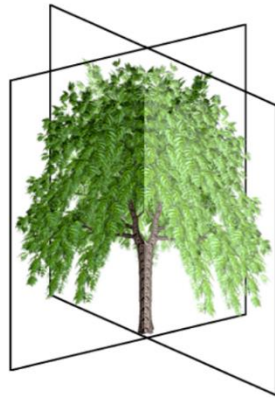
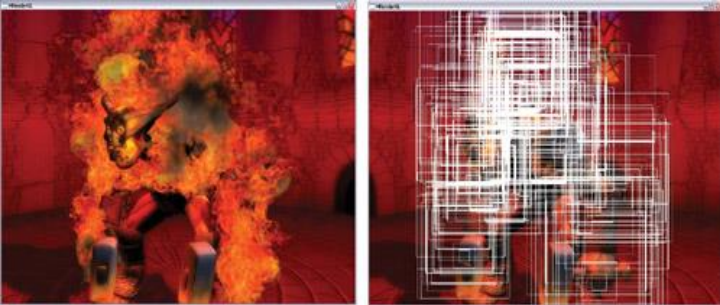
- Progressively subdivide coarse mesh
- Different subdivision schemes
  - Loop, Catmull-Clark, Doo-Sabin
  - HW support: hull+tessellation shaders



# Sprites, Billboards

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- Replacing geometry with images – sprites / billboards/ impostors
- Billboard: oriented sprite
  - towards a camera or based on object features ...



# Other B-reps

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- Parametric surfaces
  - Bezier surface, Coons surface, NURBS
- Height fields
  - Regular / irregular
  - Terrains
- Depth impostors
- LODs

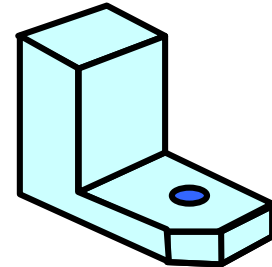
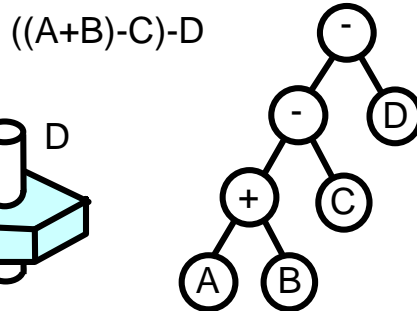
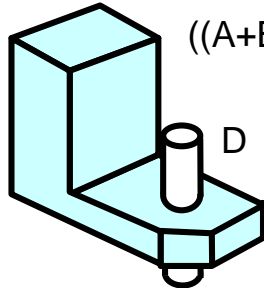
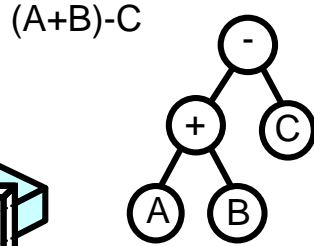
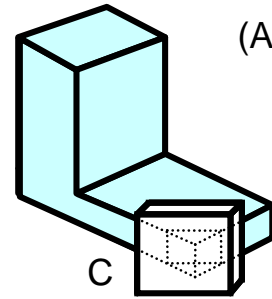
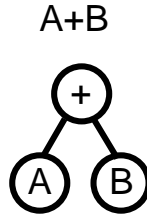
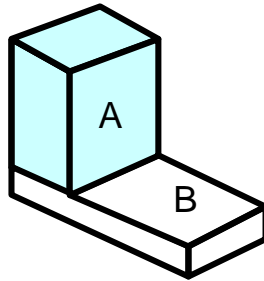
# B-rep: Summary

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- Easy (GPU) rendering
- Complicated operations on solids
  - No explicit information on what is the interior

# CSG Tree

- Leaves: geometric primitives
- Inner nodes: set operations, transformations
- Root = model



# CSG Tree - Properties

---

- Easy „point in solid“ test
- Modeling resembles manufacturing
  - Popular for 3D printing!
- Memory compact (primitives defined analytically)
- More complex rendering

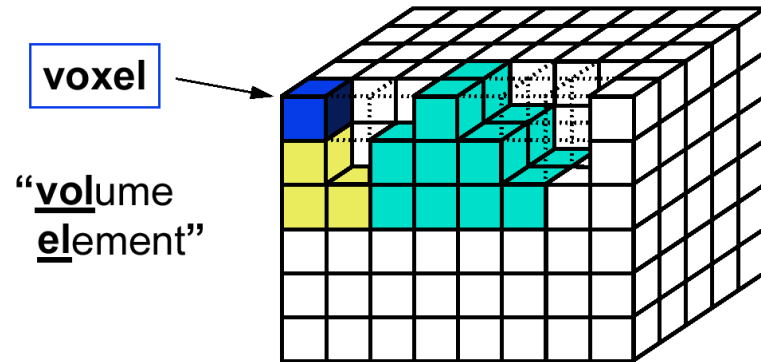


DP: Markéta Karaffová 2016

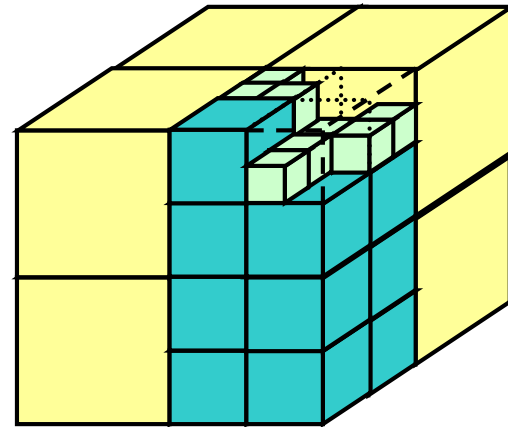
# Volumetric representation

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3D grid (regular structure)



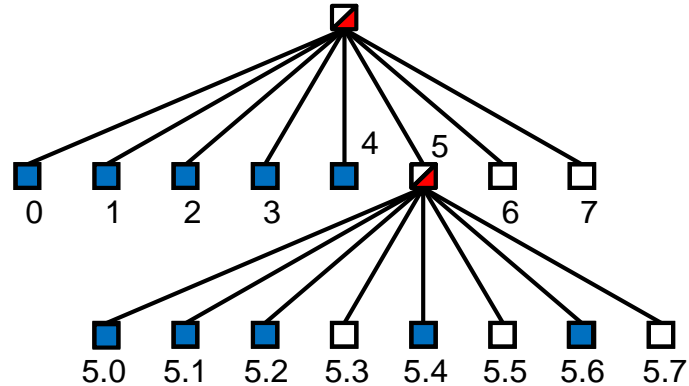
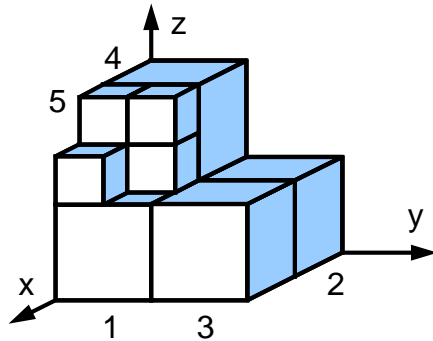
Octree (hierarchical structure)





# Octree Encoding

- 3 cell states
  - F (full), V (void, empty), M (mixed)
- Encoding example
  - MFFFFFFMFFFVFVFVVV



# Volumetric rep.- Properties

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- Easy „point in solid“ test
- More difficult rendering (ray casting)



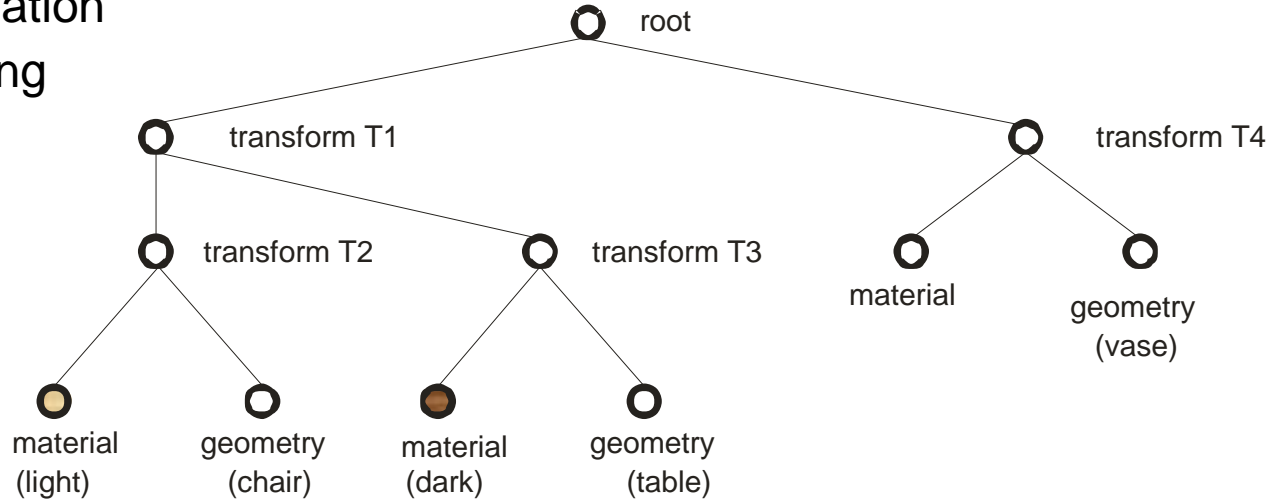
Source: Ikits et al. GPU Gems 2



DP: M. Benatsky 2011

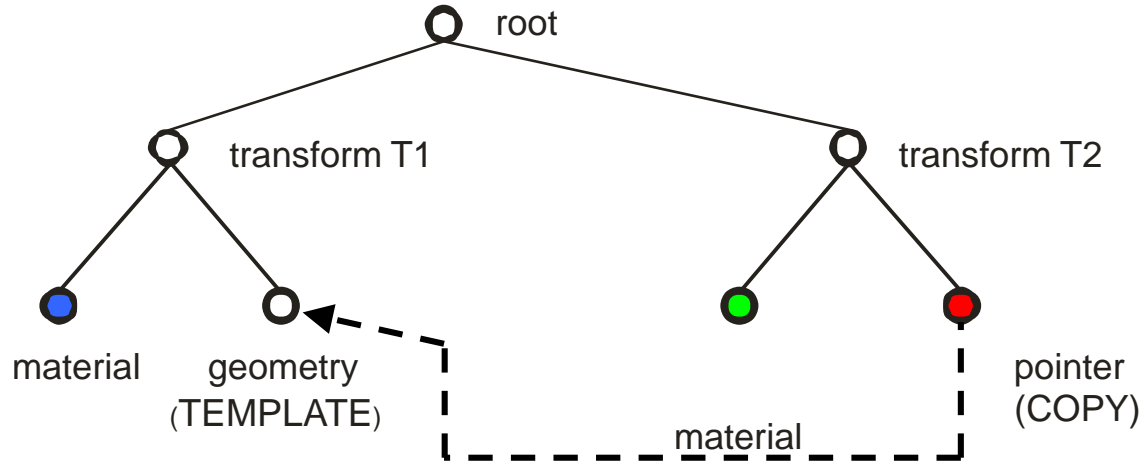
# Scene Graph

- Logical / Semantical grouping
  - Transformation composition
  - Naming
  - Activation / deactivation
  - Partial spatial sorting



# Scene graph - Instancing

- One Template / Many copies



- Saving memory, propagating changes
- Not a tree anymore: DAG!
  - Implications for a renderer



**DCGI**

**KATEDRA POČÍTAČOVÉ GRAFIKY A INTERAKCE**

**Questions?**