# Data collection planning - TSP(N), PC-TSP(N), and OP(N))

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Lecture 08

B4M36UIR - Artificial Intelligence in Robotics

### Overview of the Lecture

- Part 1 Data Collection Planning
  - Data Collection Planning Motivational Problem
  - Traveling Salesman Problem (TSP)
  - Traveling Salesman Problem with Neighborhoods (TSPN)
  - Generalized Traveling Salesman Problem (GTSP)
  - Noon-Bean Transformation
  - Orienteering Problem (OP)
  - Orienteering Problem with Neighborhoods (OPN)

Part I

Part 1 – Data Collection Planning

Motivation Autonomous Data Collection

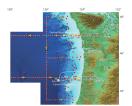
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■ Having a set of sensors (sampling stations), we aim to determine a cost-efficient path to retrieve data autonomous underwater vehicles (AUVs) from the individual sensors



■ The planning problem is a variant of the Traveling Salesman Problem



### Two practical aspects of the data collection can be identified

- 1. Data from particular sensors may be of different importance
- 2. Data from the sensor can be retrieved using wireless communication

These two aspects (of general applicability) can be considered in the Prize-Collecting Traveling Salesman Problem (PC-TSP) and Orienteering Problem (OP) and their extensions with neighborhoods

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Prize-Collecting Traveling Salesman Problem with Neighborhoods (PC-TSPN)

- Let *n* sensors be located in  $\mathbb{R}^2$  at the locations  $S = \{s_1, \dots, s_n\}$
- **Each** sensor has associated penalty  $\xi(s_i) > 0$  characterizing additional cost if the data are not retrieved from si
- $\blacksquare$  Let the data collecting vehicle operates in  $\mathbb{R}^2$  with the motion cost  $c(p_1, p_2)$  for all pairs of points  $p_1, p_2 \in \mathbb{R}^2$
- The data from  $s_i$  can be retrieved within  $\delta$  distance from  $s_i$

PC-TSPN – Optimization Criterion

The PC-TSPN is a problem to

- Determine a set of unique locations  $P = \{p_1, \dots, p_k\}, k < n$  $p_i \in \mathbb{R}^2$ , at which data readings are performed
- Find a cost efficient tour T visiting P such that the total cost C(T) of T is minimal

$$C(T) = \sum_{(p_{l_i}, p_{l_{i+1}}) \in T} c(p_{l_i}, p_{l_{i+1}}) + \sum_{s \in S \setminus S_T} \xi(s), \tag{1}$$

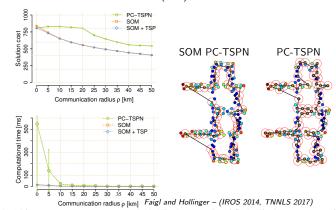
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where  $S_T \subseteq S$  are sensors such that for each  $s_i \in S_T$  there is  $p_l$  on  $T = (p_{l_1}, \dots, p_{l_{k-1}}, p_{l_k})$  and  $p_{l_i} \in P$  for which  $|(s_i, p_{l_i})| \leq \delta$ .

- PC-TSPN includes other variants of the TSP
  - for  $\delta = 0$  it is the PC-TSP
  - for  $\xi(s_i) = 0$  and  $\delta \ge 0$  it is the TSPN
  - for  $\xi(s_i) = 0$  and  $\delta = 0$  it is the ordinary TSP

PC-TSPN – Example of Solution

Ocean Observatories Initiative (OOI) scenario



# Traveling Salesman Problem (TSP)

- Let S be a set of n sensor locations  $S = \{s_1, \ldots, s_n\}, s_i \in \mathbb{R}^2$  and  $c(s_i, s_i)$ is a cost of travel from  $s_i$  to  $s_i$
- Traveling Salesman Problem (TSP) is a problem to determine a closed tour visiting each  $s \in S$  such that the total tour length is minimal, i.e.,
  - determine a sequence of visits  $\Sigma = (\sigma_1, \dots, \sigma_n)$  such that

minimize 
$$_{\Sigma}$$
  $L = \left(\sum_{i=1}^{n-1} c(s_{\sigma_i}, s_{\sigma_{i+1}})\right) + c(s_{\sigma_n}, s_{\sigma_1})$  (2) subject to  $\Sigma = (\sigma_1, \dots, \sigma_n), 1 \le \sigma_i \le n, \sigma_i \ne \sigma_j \text{ for } i \ne j$ 

- The TSP can be considered on a graph G(V, E) where the set of vertices V represents sensor locations S and E are edges connecting the nodes with the cost  $c(s_i, s_i)$
- For simplicity we can consider  $c(s_i, s_j)$  to be Euclidean distance; otherwise, it is a solution of the path planning problem Fuclidean TSP
- If  $c(s_i, s_i) \neq c(s_i, s_i)$  it is the **Asymmetric TSP**
- The TSP is known to be NP-hard unless P=NP

### Existing solvers to the TSP

- Exact solutions
  - Branch and Bound, Integer Linear Programming (ILP)

E.g., Concorde solver - http://www.tsp.gatech.edu/concorde.html

- Approximation algorithms
  - Minimum Spanning Tree (MST) heuristic with  $L \leq 2L_{opt}$
  - Christofides's algorithm with  $L \leq \frac{3/2}{L_{opt}}$
- Heuristic algorithms
  - Constructive heuristic Nearest Neighborhood (NN) algorithm
  - 2-Opt local search algorithm proposed by Croes 1958
  - Lin-Kernighan (LK) heuristic

- Soft-Computing techniques, e.g.,
  - Variable Neighborhood Search (VNS)
  - Evolutionary approaches
  - Unsupervised learning

# MST-based Approximation Algorithm to the TSP

### ■ Minimum Spanning Tree Heuristic

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- 1. Compute the MST (denoted T) of the input graph G
- 2. Construct a graph H by doubling every edge of T
- 3. Shortcut repeated occurrences of a vertex in the tour



■ For the triangle inequality, the length of such a tour *L* is

Unsupervised Learning based Solution of the TSP

$$L \leq 2L_{optimal}$$
,

where  $L_{optimal}$  is the cost of the optimal solution of the TSP

■ Sensor locations  $S = \{s_1, \ldots, s_n\}$ ,  $s_1 \in \mathbb{R}^2$ ; Neurons  $\mathcal{N} = (\nu_1, \ldots, \nu_m)$ ,  $\nu_i \in \mathbb{R}^2$ , m = 2.5n

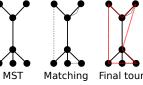
1.  $\mathcal{N} \leftarrow \text{init ring of neurons as a small ring around some } s_i \in \mathcal{S}$ , e.g., a circle with radius 0.5

■ Learning gain  $\sigma$ ; epoch counter i; gain decreasing rate  $\alpha = 0.1$ ; learning rate  $\mu = 0.6$ 

# Christofides's Algorithm to the TSP

### ■ Christofides's algorithm

- 1. Compute the MST of the input graph G
- 2. Compute the minimal matching on the odd-degree vertices 3. Shortcut a traversal of the re-
- sulting Eulerian graph



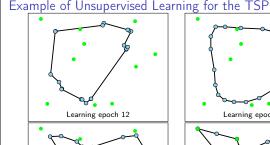
For the triangle inequality, the length of such a tour L is

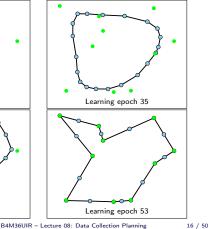
$$L \leq \frac{3}{2}L_{optimal},$$

where  $L_{optimal}$  is the cost of the optimal solution of the TSP

Length of the MST is  $< L_{optimal}$ 

Sum of lengths of the edges in the matching  $\leq \frac{1}{2}L_{optimal}$ 





E.g., using evolutionary techniques or unsupervised learning

# $\nu \leftarrow \nu + \mu f(\sigma, d)(s - \nu)$

$$f(\sigma, d) = \begin{cases} e^{-\sigma^2} & \text{for } d < 0.2a \\ 0 & \text{otherwise,} \end{cases}$$

- 4.3  $I \leftarrow I \cup \{\nu^*\}$ // inhibit the winner 5.  $\sigma \leftarrow (1-\alpha)\sigma$ ;  $i \leftarrow i+1$ ;
- 6. If (termination condition is not satisfied) Goto Step 3; Otherwise retrieve solution

4. foreach  $s \in \Pi(S)$  (a permutation of S)

4.1  $\nu^* \leftarrow \operatorname{argmin}_{\nu \in \mathcal{N} \setminus I} ||(\nu, s)||$ 

4.2 foreach  $\nu$  in d neighborhood of  $\nu^*$ 

2.  $i \leftarrow 0$ ;  $\sigma \leftarrow 12.41n + 0.06$ ;

■ Maximal number of learning epochs i ≤  $i_{max}$ , e.g.,  $i_{max} = 120$ Winner neurons are negligibly close to sen-

Termination condition can be

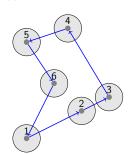
sor locations, e.g., less than 0.001

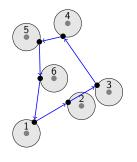
Somhom, S., Modares, A., Enkawa, T. (1999): Competition-based neural network for the mul ective. Computers & Operations Research.

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# Traveling Salesman Problem with Neighborhoods (TSPN)

- Euclidean TSPN with disk shaped  $\delta$ -neighborhoods
- Sequence of visits to the regions with particular locations of the visit





## Approaches to the TSPN

Learning epoch 42

TSPN

- A direct solution of the TSPN approximation algorithms and heuristics
- Decoupled approach
  - 1. Determine sequence of visits  $\Sigma$  independently on the locations PE.g., as the TSP for centroids of the regions R
  - 2. For the sequence  $\Sigma$  determine the locations P to minimize the total tour length, e.g.,
    - Touring polygon problem (TPP)
    - Sampling possible locations and use a forward search for finding the best locations
    - Continuous optimization such as hill-climbing E.g., Local Iterative Optimization (LIO), Váña & Faigl (IROS 2015)
- Sampling-based approaches

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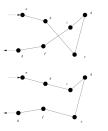
- For each region, sample possible locations of visits into a discrete set of locations for each region
- The problem can be then formulated as the Generalized Traveling Salesman Problem (GTSP)
- **E**uclidean TSPN with, e.g., disk-shaped  $\delta$  neighborhoods
  - lacktriangle Simplified variant with regions as disks with radius  $\delta$  remote sensing with the  $\delta$  communication range

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# 2-Opt Heuristic

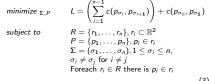
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- 1. Use a construction heuristic to create an initial route
  - NN algorithm, cheapest insertion, farther insertion
- 2. Repeat until no improvement is made
  - 2.1 Determine swapping that can shorten the tour (i, j) for  $1 \le i \le n$  and  $i + 1 \le j \le n$ 
    - route[0] to route[i-1]
    - route[i] to route[j] in reverse order
    - route[i] to route[end]
    - Determine length of the route
    - Update the current route if length is shorter than the existing solution



# Traveling Salesman Problem with Neighborhoods (TSPN)

- Instead visiting a particular location  $s \in S$ ,  $s \in \mathbb{R}^2$  we can request to visit, e.g., a region  $r \subset \mathbb{R}^2$  to save travel cost, i.e., visit regions  $R = \{r_1, \dots, r_n\}$
- The TSP becomes the TSP with Neighborhoods (TSPN) where it is necessary, in addition to the determination of the order of visits  $\Sigma$ , determine suitable locations  $P = \{p_1, \dots, p_n\}$ ,  $p_i \in r_i$ , of visits to R
- The problem is a combination of combinatorial optimization to determine  $\Sigma$  with continuous optimization to determine P





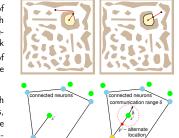
In general, TSPN is APX-hard, and cannot be approximated to within a factor  $2 - \epsilon$ .  $\epsilon > 0$ . unless P = NP.

Safra, S., Schwartz, O. (2006)

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Motivation	TCD	TSDN	CTCD	Near Pean Transformation	OB	OBN

# Unsupervised Learning for the TSPN

- In the unsupervised learning for the TSP, we can sample suitable sensing locations during winner selection
- We can use the centroid of the region for the shortest path computation from  $\nu$  to the region r presented to the network
- Then, an intersection point of the path with the region can be used as an alternate location
- For the Euclidean TSPN with disk-shaped  $\delta$  neighborhoods, we can compute the alternate location directly from the Euclidean distance



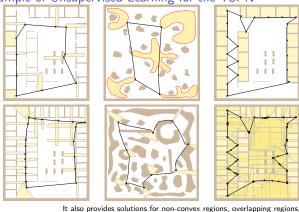
Faigl, J. et al. (2013): Visiting convex regions in a polygonal map. Robotics and Autonomous Systems.

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//clear inhibited neurons

Sampling-based Decoupled Solution of the TSPN

# Example of Unsupervised Learning for the TSPN



and coverage problems.

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# Solving the TSPN as the TPP - Iterative Refinement ■ Let the sequence of *n* polygon regions be $R = (r_1, ..., r_n)$

- 1. Sampling the polygons into a discrete set of points and determine all shortest paths between each sampled points in the sequence of the regions visits 2. Initialization: Construct an initial touring polygons path us-
- ing a sampled point of each region Let the path be defined by  $P = (p_1, p_2, ..., p_n)$ , where  $p_i \in r_i$  and L(P) be the length of the shortest path induced by P
- 3. Refinement: For  $i = 1, 2, \ldots, n$ 
  - Find  $p_i^*$  ∈  $r_i$  minimizing the length of the path  $d(p_{i-1}, p_i^*) + d(p_i^*, p_{i+1})$ , where  $d(p_k, p_l)$  is the path length from  $p_k$  to  $p_l$ ,  $p_0 = p_n$ , and  $p_{n+1} = p_1$ If the total length of the current path over point p\* is
  - shorter than over  $p_i$ , replace the point  $p_i$  by  $p_i^*$
- 4. Compute path length Lnew using the refined points
- 5. Termination condition: If  $L_{new} L < \epsilon$  Stop the refinement. Otherwise  $L \leftarrow L_{new}$  and go to Step 3
- 6. Final path construction: use the last points and construct the path using the shortest paths among obstacles between two consecutive points lan Faigl, 2017





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Trying each of the k possible starting locations

■ Sample each neighborhood with, e.g., k = 6 samples

the centroids of the regions

for  $nk^2$  edges in the sequence

■ Determine sequence of visits, e.g., by a solution of the ETSP for

■ Finding the shortest tour takes in a forward search graph  $O(nk^3)$ 

Transformation of the GTSP to the Asymmetric TSP

■ The Generalized TSP can be transformed into the Asymmetric

TSP that can be then solved, e.g., by LKH or exactly using

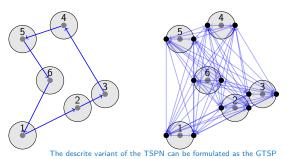
Concorde with further transformation of the problem to the TSP

A transformation of the GTSP to the ATSP has been proposed by

Noon and Bean in 1993, and it is called as the Noon-Bean

# Sampling-based Solution of the TSPN

- For an unknown sequence of the visits to the regions, there are  $\mathcal{O}(n^2k^2)$  possible edges
- Finding the shortest path is NP-hard, we need to determine the sequence of visits, which is the solution of the TSP

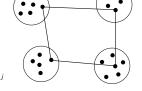


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# Generalized Traveling Salesman Problem (GTSP)

- For sampled neighborhoods into discrete sets of locations, we can formulate the problem as the Generalized Traveling Salesman Problem (GTSP)
- For a set of n sets  $S = \{S_1, \dots, S_n\}$ , each with particular set of locations (nodes)  $S_i = \{s_1^i, \dots, s_{n_i}^i\}$
- The problem is to determine the shortest tour visiting each set  $S_i$ , i.e., determining the order  $\Sigma$  of visits to S and a particular locations  $s^i \in S_i$  for each  $S_i \in S$

 $\Sigma = (\sigma_1, \dots, \sigma_n), 1 \le \sigma_i \le n, \sigma_i \ne \sigma_j \text{ for } i \ne j$   $s^{\sigma_i} \in S_{\sigma_i}, S_{\sigma_i} = \{s_1^{\sigma_i}, \dots, s_{n\sigma_i}^{\sigma_i}\}, S_{\sigma_i} \in S$ 



In addition to exact, e.g., ILP-based, solution, a heuristic algorithm **GLNS** is available (besides other heuristics)

Smith, S. L., Imeson, F. (2017), GLNS: An effective large neighborhood search heuristic the Generalized Traveling Salesman Problem. Computers and Operations Research.

Implementation in Julia - https://ece.uwaterloo.ca/~s12smith/GLNS

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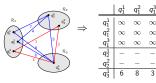
Noon, C.E., Bean, J.C. (1993), An efficient transformation of the ge problem. INFOR: Information Systems and Operational Research.

# Noon-Bean transformation – Matrix Notation

Ben-Arieg, et al. (2003), Transfo

Transformation

■ 1. Create a zero-length cycle in each set; and 2. for each edge  $(q_i^m, q_i^n)$  create an edge  $(q_i^m, q_i^{n-1})$  with a value increased by sufficiently large M



ations of generalized ATSP into ATSP. Operations Res

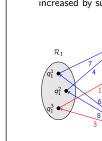
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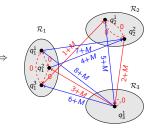
### Original GATSP Transformed ATSP



# Example – Noon-Bean transformation (GATSP to ATSP)

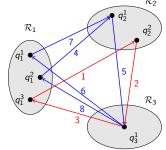
- 1. Create a zero-length cycle in each set and set all other arcs to  $\infty$ To ensure all vertices of the cluster are visited before leaving the cluster
- 2. For each edge  $(q_i^m, q_i^n)$  create an edge  $(q_i^m, q_i^{n-1})$  with a value increased by sufficiently large M





# Noon-Bean Transformation

- Noon-Bean transformation to transfer GTSP to ATSP
- Modify weight of the edges (arcs) such that the optimal ATSP tour visits all vertices of the same cluster before moving to the next cluster
  - Adding a large a constant M to the weights of arcs connecting the clusters, e.g., a sum of the n heaviest edges
  - Ensure visiting all vertices of the cluster in prescribed order, i.e., creating zero-length cycles within each cluster
- The transformed ATSP can be further transformed to the TSP For each vertex of the ATSP created 3 ver
  - tices in the TSP, i.e., it increases the size of



Noon, C.E., Bean, J.C. (1993), An efficient transformation of the generalized traveling salesman . INFOR: Information Systems and Operational Research

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# Noon-Bean Transformation – Summary

### ■ It transforms the GATSP into the ATSP which can be further

- Solved by existing solvers, e.g., the Lin-Kernighan heuristic algorithm (LKH) http://www.akira.ruc.dk/~keld/research/LKH
- the ATSP can be further transformed into the TSP and solve it
- optimaly, e.g., by the Concorde solver,  $t_{\text{http://www.tsp.gatech.edu/concorde.html}}$
- It runs in  $\mathcal{O}(k^2n^2)$  time and uses  $\mathcal{O}(k^2n^2)$  memory, where n is the number of sets (regions) each with up to k samples
- The transformed ATSP problem contains kn vertices

Noon, C.E., Bean, J.C. (1993), An efficient transformation of the generalized traveling salesman

# The Orienteering Problem (OP)

- The problem is to collect as many rewards as possible within the given travel budget  $(T_{max})$ , which is especially suitable for robotic vehicles such as multi-rotor Unmanned Aerial Vehicles (UAVs)
- The starting and termination locations are prescribed and can be different The solution may not be a closed tour as in the TSP



Travel budget  $T_{max} = 50$ , Collected rewards R = 190

Collected rewards R = 270

■ Travel Salesman Problem (TSP) in determining the shortest tour

The Orienteering Problem (OP) combines two NP-hard problems: ■ Knapsack problem in determining the most valuable locations  $S_{\nu} \subseteq S$ 

below  $T_{max}$ 

Orienteering Problem - Specification ■ Let the given set of n sensors be located in  $\mathbb{R}^2$ 

with the locations  $S = \{s_1, \dots, s_n\}, s_i \in \mathbb{R}^2$ 

**Each** sensor  $s_i$  has an associated score  $\zeta_i$  char-

The vehicle is operating in  $\mathbb{R}^2$ , and the travel

 $\blacksquare$  We aim to determine a subset of k locations

OP Benchmarks – Example of Solutions

 $S_k \subseteq S$  that maximizes the sum of the collected

rewards while the travel cost to visit them is

Starting and final locations are prescribed

cost is the Euclidean distance

acterizing the reward if data from si are col-

# Orienteering Problem – Optimization Criterion

- Let  $\Sigma = (\sigma_1, \dots, \sigma_k)$  be a permutation of k sensor labels,  $1 \le \sigma_i \le$ *n* and  $\sigma_i \neq \sigma_i$  for  $i \neq i$
- $\Sigma$  defines a tour  $T = (s_{\sigma_1}, \dots, s_{\sigma_k})$  visiting the selected sensors  $S_k$
- Let the start and end points of the tour be  $\sigma_1 = 1$  and  $\sigma_k = n$
- The Orienteering problem (OP) is to determine the number of sensors k, the subset of sensors  $S_k$ , and their sequence  $\Sigma$  such that

maximize
$$_{k,S_k,\Sigma}$$
  $R = \sum_{i=1}^k \zeta_{\sigma_i}$  subject to  $\sum_{i=2}^k |(s_{\sigma_{i-1}},s_{\sigma_i})| \leq T_{\max}$  and  $s_{\sigma_1} = s_1, s_{\sigma_k} = s_n.$  (4)

The OP combines the problem of determining the most valuable locations  $S_k$  with finding the shortest tour T visiting the locations  $S_k$ . It is NP-hard, since for  $s_1 = s_n$ and particular  $S_k$  it becomes the TSP.

# Existing Heuristic Approaches for the OP

■ The Orienteering Problem has been addressed by several approaches, e.g.,

4-phase heuristic algorithm proposed in [3] Results for the method proposed by Pillai in [2] Heuristic algorithm proposed in [1] Guided local search algorithm proposed in [4]

[1] I.-M. Chao, B. L. Golden, and E. A. Wasil. A fast and effective heuristic for the orienteering problem. European Journal of Operational Research, 88(3):475-489, 1996.

The traveling salesman subset-tour problem with one additional constraint Ph.D. thesis, The University of Tennessee, Knoxville, TN, 1992.

- [3] R. Ramesh and K. M. Brown An efficient four-phase heuristic for the generalized orienteering problem Computers & Operations Research, 18(2):151-165, 1991
- [4] P. Vansteenwegen, W. Souffriau, G. V. Berghe, and D. V. Oudheusden. A guided local search metaheuristic for the team orienteering problem. European Journal of Operational Research, 196(1):118-127, 2009

Tmax=95, R=1395





# Unsupervised Learning for the OP 1/2

- A solution of the OP is similar to the solution of the PC-TSP and TSP
- We need to satisfy the limited travel budget  $T_{max}$ , which needs the final tour over the sensing locations
- During the unsupervised learning, the winners are associated with the particular sensing locations, which can be utilized to determine the tour as a solution of the OP represented by the network:



Learning epoch 7 Learning epoch 55 Learning epoch 87 Final solution

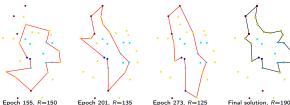
■ This is utilized in the conditional adaptation of the network towards the sensing location and the adaptation is performed only if the tour represented by the network after the adaptation would satisfy  $T_{max}$ 

# Unsupervised Learning for the OP 2/2

- The winner selection for  $s' \in S$  is conditioned according to  $T_{max}$ 
  - The network is adapted only if the tour  $T_{win}$  represented by the current winners would be shorter or equal than  $T_{max}$

$$\mathcal{L}(T_{win}) - |(s_{\nu_n}, s_{\nu_n})| + |(s_{\nu_n}, s')| + |(s', s_{\nu_n})| \le T_{max}$$

■ The unsupervised learning performs a *stochastic search* steered by the rewards and the length of the tour to be below  $T_{max}$ 



# Comparison with Existing Algorithms for the OP

- Standard benchmark problems for the Orienteering Problem represent various scenarios with several values of  $T_{max}$
- The results (rewards) found by different OP approaches presented as the average ratios (and standard deviations) to the best-known solution

Instances of the Tsiligirides problems

Problem Set	RB	PL	CGW	Unsupervised Learning
Set 1, $5 \le T_{max} \le 85$	0.99/0.01	1.00/0.01	1.00/0.01	1.00/0.01
Set 2, $15 \le T_{max} \le 45$	1.00/0.02	0.99/0.02	0.99/0.02	0.99/0.02
Set 3, $15 \leq T_{max} \leq 110$	1.00/0.00	1.00/0.00	1.00/0.00	1.00/0.00

Diamond-shaped (Set 64) and Square-shaped (Set 66) test problems

Problem Set	RB <sup>†</sup>	PL	CGW	Unsupervised Learning	
Set 64, $5 \le T_{max} \le 80$	0.97/0.02	1.00/0.01	0.99/0.01	0.97/0.03 0.97/0.02	
Set 66, $15 \le T_{max} \le 130$	0.97/0.02	1.00/0.01	0.99/0.04	0.97/0	

Required computational time is up to units of seconds, but for small problems tens

Epoch 201, R=135

# Orienteering Problem with Neighborhoods

■ Similarly to the TSP with Neighborhoods and PC-TSPN we can formulate the Orienteering Problem with Neighborhoods.





 $T_{max}$ =60,  $\delta$ =1.5, R=1600

 $T_{max}$ =45,  $\delta$ =1.5, R=1344

# Orienteering Problem with Neighborhoods

- Data collection using wireless data transfer allows to reliably retrieve data within some communication radius  $\delta$ 
  - lacksquare Disk-shaped  $\delta$ -neighborhood
- We need to determine the most suitable locations  $P_k$  such that



Introduced by Best, Faigl, Fitch (IROS 2016, SMC 2016, IJCNN 2017)

■ More rewards can be collected than for the OP formulation with the same travel budget  $T_{max}$ 

■ The location p' for retrieving data from s' is determined as the alternate goal location during the conditioned winner selection

Generalization of the Unsupervised Learning to the

# OPN

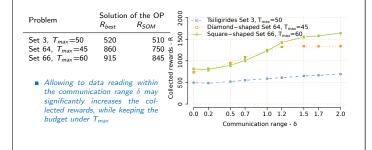
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# Influence of the $\delta$ -Sensing Distance

 Influence of increasing communication range to the sum of the collected rewards



# OP with Neighborhoods (OPN) – Example of Solutions

lacksquare Diamond-shaped problem Set 64 – SOM solutions for  $T_{max}$  and  $\delta$ 

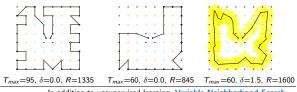






 $T_{max}$ =80,  $\delta$ =0.0, R=1278  $T_{max}$ =45,  $\delta$ =0.0, R=756

ullet Square-shaped problem Set 66 – SOM solutions for  $T_{max}$  and  $\delta$ 



In addition to unsupervised learning, Variable Neighborhood Search (VNS) for the OP has been generalized to the OPN B4M36UIR - Lecture 08: Data Collection Planning

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### Jan Faigl, 2017 Topics Discusse

# Topics Discussed

- Data Collection Planning motivational problem and solution
  - Prize-Collecting Traveling Salesman Problem with Neighborhoods (PC-TSPN)

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- Traveling Salesman Problem (TSP)
  - Approximation and heuristic approaches
- Traveling Salesman Problem with Neighborhoods (TSPN)
  - Sampling-based and decoupled approaches
  - Unsupervised learning
- Generalized Traveling Salesman Problem (GTSP)
  - Heuristic and transformation (GTSP→ATSP) approaches
- Orienteering problem (OP)
  - Heuristic and unsupervised learning based approaches
- Orienteering problem with Neighborhoods (OPN)
  - Unsupervised learning based approach
- Next: Data-collection planning with curvature-constrained vehicles

 $T_{max} = 50, R = 270$ 

Orienteering Problem with Neighborhoods

connected neuron

■ The same idea of the alternate location as in the TSPN

connected neuron communication range  $\delta$ alternate location

Summary of the Lecture

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