# Data collection planning - TSP(N), PC-TSP(N), and OP(N))

### Jan Faigl

Department of Computer Science Faculty of Electrical Engineering Czech Technical University in Prague

## Lecture 08

### **B4M36UIR – Artificial Intelligence in Robotics**

# Overview of the Lecture

- Part 1 Data Collection Planning
  - Data Collection Planning Motivational Problem
  - Traveling Salesman Problem (TSP)
  - Traveling Salesman Problem with Neighborhoods (TSPN)
  - Generalized Traveling Salesman Problem (GTSP)
  - Noon-Bean Transformation
  - Orienteering Problem (OP)
  - Orienteering Problem with Neighborhoods (OPN)

Jan Faigl, 2017	B4M36UIR – Lecture 08: Data Collection Planning	1 / 50	Jan Faigl, 2017 B4M36UIR – Lecture 08: Data Collection Planning 2 / 50
Motivation	TSP TSPN GTSP Noon-Bean Transformation	OP OPN	Motivation TSP TSPN GTSP Noon-Bean Transformation OP OPN Autonomous Data Collection
	Part I Part 1 – Data Collection Planning		<ul> <li>Having a set of sensors (sampling stations), we aim to determine a cost-efficient path to retrieve data by autonomous underwater vehicles (AUVs) from the individual sensors <i>E.g., Sampling stations on the ocean floor</i></li> <li>The planning problem is a variant of the Traveling Salesman Problem</li> </ul>
			<ul> <li>Two practical aspects of the data collection can be identified</li> <li>1. Data from particular sensors may be of different importance</li> <li>2. Data from the sensor can be retrieved using wireless communication</li> <li>These two aspects (of general applicability) can be considered in the Prize-Collecting Traveling Salesman Problem (PC-TSP) and Orienteering Problem (OP) and their extensions with neighborhoods</li> </ul>
Jan Faigl, 2017	B4M36UIR – Lecture 08: Data Collection Planning	3 / 50	Jan Faigl, 2017 B4M36UIR – Lecture 08: Data Collection Planning 5 / 50







18 / 50 Jan Faigl, 2017

Motivation TSP TSPN GTSP Noon-Bean Transformation OP OPN	Motivation TSP <b>TSPN</b> GTSP Noon-Bean Transformation OP OPN			
Approaches to the TSPN	Unsupervised Learning for the TSPN			
<ul> <li>A direct solution of the TSPN – approximation algorithms and heuristics         <ul> <li>E.g., using evolutionary techniques or unsupervised learning</li> </ul> </li> <li>Decoupled approach         <ul> <li>Determine sequence of visits Σ independently on the locations P E.g., as the TSP for centroids of the regions R</li> <li>For the sequence Σ determine the locations P to minimize the total tour length, e.g.,             <ul> <li>Touring polygon problem (TPP)</li> <li>Sampling possible locations and use a forward search for finding the best locations</li> </ul> </li> </ul> </li> </ul>	<ul> <li>In the unsupervised learning for the TSP, we can sample suitable sensing locations during winner selection</li> <li>We can use the centroid of the region for the shortest path computation from ν to the region r presented to the network.</li> <li>Then, an intersection point of the path with the region can be used as an alternate location.</li> <li>For the Euclidean TSPN with disk-shaped δ neighborhoods, we can compute the alternate location directly from the Euclidean distance.</li> <li>Faigl, J. et al. (2013): Visiting convex regions in a polygonal map. Robotics and Autonomous Systems.</li> </ul>			
<ul> <li>Continuous optimization such as hill-climbing</li></ul>				
Jan Faigl, 2017     B4M36UIR – Lecture 08: Data Collection Planning     20 / 50	Jan Faigl, 2017         B4M36UIR – Lecture 08: Data Collection Planning         21 / 5			
Motivation TSP TSPN GTSP Noon-Bean Transformation OP OPN Example of Unsupervised Learning for the TSPN U U U U U U U U U U U U U U U U U U U	Motivation TSP TSPN GTSP Noon-Bean Transformation OP OPN <b>Solving the TSPN as the TPP – Iterative Refinement</b> • Let the sequence of <i>n</i> polygon regions be $R = (r_1,, r_n)$ Li, F., Klette, R.: Approximate algorithms for touring a sequence of polygons. 2008 1. Sampling the polygons into a discrete set of points and de- termine all shortest paths between each sampled points in the sequence of the regions visits $E.g.$ , using visibility graph 2. Initialization: Construct an initial touring polygons path us- ing a sampled point of each region Let the path be defined by $P = (p_1, p_2,, p_n)$ , where $p_i \in$ $r_i$ and $L(P)$ be the length of the shortest path induced by $P$			
Image: the second se	<ul> <li>3. Refinement: For i = 1,2,, n</li> <li>Find p<sub>i</sub><sup>*</sup> ∈ r<sub>i</sub> minimizing the length of the path d(p<sub>i-1</sub>, p<sub>i</sub><sup>*</sup>) + d(p<sub>i</sub><sup>*</sup>, p<sub>i+1</sub>), where d(p<sub>k</sub>, p<sub>l</sub>) is the path length from p<sub>k</sub> to p<sub>l</sub>, p<sub>0</sub> = p<sub>n</sub>, and p<sub>n+1</sub> = p<sub>1</sub></li> <li>If the total length of the current path over point p<sub>i</sub><sup>*</sup> is shorter than over p<sub>i</sub>, replace the point p<sub>i</sub> by p<sub>i</sub><sup>*</sup></li> <li>Compute path length L<sub>new</sub> using the refined points</li> <li>Termination condition: If L<sub>new</sub> - L &lt; ε Stop the refinement. Otherwise L ← L<sub>new</sub> and go to Step 3</li> <li>Final path construction: use the last points and construct the path using the shortest paths among obstacles between</li> </ul>			

Jan Faigl, 2017

B4M36UIR – Lecture 08: Data Collection Planning

22 / 50 Jan Faigl, 2017

B4M36UIR - Lecture 08: Data Collection Planning



 In addition to exact, e.g., ILP-based, solution, a heuristic algorithm GLNS is available (besides other heuristics)

Smith, S. L., Imeson, F. (2017), GLNS: An effective large neighborhood search heuristic for the Generalized Traveling Salesman Problem. Computers and Operations Research. Implementation in Julia - https://ece.uwaterloo.ca/~sl2smith/GLNS

### Jan Faigl, 2017

27 / 50 Jan Faigl, 2017

Transformation

Letters

Noon, C.E., Bean, J.C. (1993), An efficient transformation of the generalized traveling salesman

Ben-Arieg, et al. (2003), Transformations of generalized ATSP into ATSP. Operations Research

problem. INFOR: Information Systems and Operational Research.



Jan Faigl, 2017

B4M36UIR - Lecture 08: Data Collection Planning



37 / 50

Jan Faigl, 2017

Jan Faigl, 2017

B4M36UIR - Lecture 08: Data Collection Planning



- The winner selection for  $s' \in S$  is conditioned according to  $T_{max}$ 
  - The network is adapted only if the tour  $T_{win}$  represented by the current winners would be shorter or equal than  $T_{max}$

$$\mathcal{L}({\mathit{T}_{{\mathit{win}}}}) - |({\mathit{s}_{{\nu _p}}},{\mathit{s}_{{\nu _n}}})| + |({\mathit{s}_{{\nu _p}}},{\mathit{s}'})| + |({\mathit{s}'},{\mathit{s}_{{
u _n}}})| \le {\mathit{T}_{{\mathit{max}}}}$$

The unsupervised learning performs a stochastic search steered by the rewards and the length of the tour to be below T<sub>max</sub>



- Standard benchmark problems for the Orienteering Problem represent various scenarios with several values of T<sub>max</sub>
- The results (rewards) found by different OP approaches presented as the average ratios (and standard deviations) to the best-known solution

### Instances of the Tsiligirides problems

Problem Set	RB	PL	CGW	Unsupervised Learning
Set 1, $5 \le T_{max} \le 85$ Set 2, $15 \le T_{max} \le 45$ Set 3, $15 \le T_{max} \le 110$	0.99/0.01	1.00/0.01	1.00/0.01	1.00/0.01
	1.00/0.02	0.99/0.02	0.99/0.02	0.99/0.02
	1.00/0.00	1.00/0.00	1.00/0.00	1.00/0.00

### Diamond-shaped (Set 64) and Square-shaped (Set 66) test problems

Problem Set	RB <sup>†</sup>	PL	CGW	Unsupervised Learning
Set 64, $5 \le T_{max} \le 80$	0.97/0.02	1.00/0.01	0.99/0.01	0.97/0.03
Set 66, $15 \le T_{max} \le 130$	0.97/0.02	1.00/0.01	0.99/0.04	0.97/0.02

Required computational time is up to units of seconds, but for small problems tens or hundreds of milliseconds.

Jan Faigl, 2017



