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Lecture 07

B4M36UIR - Artificial Intelligence in Robotics

Overview of the Lecture

- Part 1 Improved Sampling-based Motion Planning
 - Improved Sampling-based Motion Planners
- Part 2 Multi-Goal Path and Motion Planning
 - Multi-Goal Path Planning
 - Multi-Goal Motion Planning
 - Multi-Goal Planning in Robotic Missions

Part I

Part 1 - Improved Sampling-based Motion **Planning**

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Improved Sampling-based Motion Planners

Improved Sampling-based Motion Planners

- Although Asymptotically optimal sampling-based motion planners such RRT* or RRG may provide high-quality or even optimal solutions of complex problem, their performance in simple, e.g., 2D scenarios, is relatively poor In a comparison to the previous approaches
- They are computationally demanding and performance can be improved similarly as RRT, e.g.,
 - Goal biasing, supporting sampling in narrow passages, multi-tree growns (Bidirectional RRT)
- The general idea of improvements is based on informing the sampling process
- Many modifications of the algorithms exists, selected representative modifications are
 - Informed RRT*
 - Batch Informed Trees (BIT*)
 - Regionally Accelerated BIT* (RABIT*)

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Informed RRT*

Improved Sampling-based Motion Planner

- Focused RRT* search to increase the convergence rate
- Use Euclidean distance as an admissible
- Ellipsoidal informed subset the current best solution *c*_{best}

$$\textit{X}_{\hat{f}} = \{\mathbf{x} \in \textit{X} | ||\textit{x}_{\textit{start}} - \mathbf{x}||_2 + ||\mathbf{x} - \mathbf{x}_{\textit{goal}}||_2 \leq c_{\textit{best}} \}$$



- Having a feasible solution
- Sampling inside the ellipse

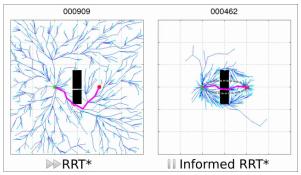


Gammell, J. B., Srinivasa, S. S., Barfoot, T. D. (2014): Informed RRT*: Optimal Sampling-based Path Planning Focused via Direct Sampling of an Admissible Ellipsoidal Heuristic. IROS.

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Informed RRT* - Demo

Improved Sampling-based Motion Planners



https://www.youtube.com/watch?v=d7dX5MvDYTc

Gammell, J. B., Srinivasa, S. S., Barfoot, T. D. (2014): Informed RRT*: Optimal Sampling-based Path Planning Focused via Direct Sampling of an Admissible

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Improved Sampling-based Motion Planners

Batch Informed Trees (BIT*)

- Combining RGG (Random Geometric Graph) with the heuristic in incremental graph search technique, e.g., Lifelong Planning A* (LPA*)
 - The properties of the RGG are used in the RRG and RRT*
- Batches of samples a new batch starts with denser implicit RGG
- The search tree is updated using LPA* like incremental search to reuse existing information

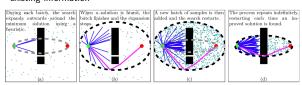
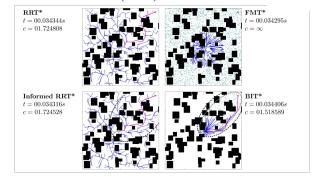


Fig. 3. An illustration of the informed search procedure used by BIT*. The start and goal states are shown as green and rod, respectively. The current solution is highlighted in magenta. The subproblem that contains any better solutions is shown as a black dashed line, while the progress of the current both its shown as a gery dashed line. Fig. (a) shows the government part of the first batch of samples, and ob) shows the first search ending when a miner carder chain given a major search of the first batch of samples, and chain green and the second batch of samples, Fig. (c) shows the search restarting on a denser graph while (d) shows the second search ending when an improved solution is found. An animated literation is savailable in the attached video.

Gammell, J. B., Srinivasa, S. S., Barfoot, T. D. (2015): Batch Informed Trees (BIT*): Sampling-based optimal planning via the heuristically guided search of implicit ran dom geometric graphs. ICRA.

Batch Informed Trees (BIT*) - Demo

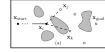


Gammell, J. B., Srinivasa, S. S., Barfoot, T. D. (2015); Batch Informed Trees (BIT*); Sampling-based optimal planning via the heuristically guided search of implicit ranImproved Sampling-based Motion Planners

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Regionally Accelerated BIT* (RABIT*)

- Use local optimizer with the BIT* to improve the convergence speed
- Local search Covariant Hamiltonian Optimization for Motion Planning (CHOMP) is utilized to connect edges in the search graphs using local information about the obstacles







Choudhury, S., Gammell, J. D., Barfoot, T. D., Srinivasa, S. S., Scherer, S. (2016): Regionally Accelerated Batch Informed Trees (RABIT*): A Framework to Integrate Local Information into Optimal Path Planning. ICRA.

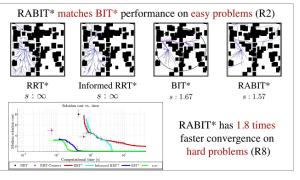
B4M36UIR - Lecture 07: Multi-Goal Planning Jan Faigl, 2017 Jan Faigl, 2017 B4M36UIR - Lecture 07: Multi-Goal Planning Jan Faigl, 2017 B4M36UIR - Lecture 07: Multi-Goal Planning RRT* [7]

Part II

Part 2 – Multi-Goal Path and Motion

Planning

Regionally Accelerated BIT* (RABIT*) - Demo



https://www.voutube.com/watch?v=mgg-DW36iSo

Choudhury S. Gammell, I. D. Barfoot, T. D. Sriniyasa, S. S. Scherer, S. (2016). Local Information into Optimal Path Planning. ICRA.

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To perform measurements such as scan the environment or

Having a set of locations (goals) to be visited, determine the

cost-efficient path to visit them and return to a starting location.

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Overview of Improved Algorithm

Optimal motion planning is an active research field

Offline

Offline

Rigid Body

Point

UAV Car-like

Car-like

Robotic Arm

Local bia

Uniform

Uniform

Intelligent

Noreen, I., Khan, A., Habib, Z. (2016): Optimal path planning using RRT* base approaches: a survey and future directions. IJACSA.

Goal biased

Greedy + Euclidea

lan Faigl, 2017 Multi-Goal Path Planning B4M36UIR - Lecture 07: Multi-Goal Planning

Multi-Goal Path Planning

Motivation

Multi-Goal Path Planning

Locations where a robotic arm performs some task

Locations where a mobile robot has to be navigated

Multi-Goal Planning in Robotic Missions

Multi-Goal Path Planning

Informed RRT* [34] Holonomic

12. DT-RRT [39]

13. RRT*i[3]

17. PRRT* [48]

Solutions of the TSP

- Efficient heuristics from the Operational Research have been proposed
- LKH K. Helsgaun efficient implementation of the Lin-Kernighan heuristic (1998) http://www.akira.ruc.dk/~keld/research/LKH/
- Concorde Solver with several heuristics and also optimal solver

http://www.math.uwaterloo.ca/tsp/concorde.html



Problem Berlin52 from the

TSPLIB

Beside the heuristic and approximations algorithms (such as Christofides 3/2-approximation algorithm), other (..soft-computing") approaches have been proposed, e.g., based on genetic algorithms, and memetic approaches, ant colony optimization (ACO), and neural networks.

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Multi-Goal Motion Planning

Traveling Salesman Problem (TSP)

Given a set of cities and the distances between each pair of cities, what is the shortest possible route that visits each city exactly once and returns to the origin city.

- The TSP can be formulated for a graph G(V, E), where V denotes a set of locations (cities) and E represents edges connecting two cities with the associated travel cost c (distance), i.e., for each $v_i, v_i \in V$ there is an edge $e_{ii} \in E$, $e_{ii} = (v_i, v_i)$ with the cost c_{ii} .
- If the associated cost of the edge (v_i, v_i) is the Euclidean distance $c_{ii} = |(v_i, v_i)|$, the problem is called the **Euclidean TSP** (ETSP). In our case, $v \in V$ represents a point in \mathbb{R}^2 and solution of the ETSP
- It is known, the TSP is NP-hard (its decision variant) and several algorithms can be found in literature.

William J. Cook (2012) - In Pursuit of the Traveling Salesman: Mathematics at the Limits of Computation

Alatartsev et al. (2015) - Robotic Task Sequencing Problem: A Survey

Multi-Goal Path Planning

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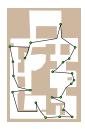
Multi-Goal Motion Planning

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Multi-Goal Path Planning (MTP) Problem

Given a map of the environment W, mobile robot R, and a set of locations, what is the shortest possible collision free path that visits each location exactly once and returns to the origin location.

- MTP problem is de facto the TSP with the cost associated to the edges as the length of the shortest path connecting the locations
- For *n* locations, we need to compute up to n^2 shortest paths (solve n^2 motion planning problems)
- The paths can be found as the shortest path in a graph (roadmap), from which the G(V, E)for the TSP can be constructed



Visibility graph as the roadmap for a point robot provides a straight forward solution, but such a shortest path may not be necessarily feasible for more complex robots

Multi-Goal Motion Planning

- In the previous cases, we consider existing roadmap or relatively "simple" collision free (shortest) paths in the polygonal domain
- However, determination of the collision-free path in a high dimensional configuration space (C-space) can be a challenging problem itself
- Therefore, we can generalize the MTP to multi-goal motion planning (MGMP) considering motion (trajectory) planners in C-space.
- An example of MGMP can be

Plan a cost efficient trajectory for hexapod walking robot to visit a set of target locations.



Problem Statement - MGMP Problem

- The working environment $\mathcal{W} \subset \mathbb{R}^3$ is represented as a set of obstacles $\mathcal{O} \subset \mathcal{W}$ and the robot configuration space \mathcal{C} describes all possible configurations of the robot in ${\mathcal W}$
- For $q \in \mathcal{C}$, the robot body $\mathcal{A}(q)$ at q is collision free if $\mathcal{A}(q) \cap \mathcal{O} = \emptyset$ and all collision free configurations are denoted as \mathcal{C}_{free}
- Set of *n* goal locations is $\mathcal{G} = (g_1, \dots, g_n)$, $g_i \in \mathcal{C}_{free}$
- lacksquare Collision free path from q_{start} to q_{goal} is $\kappa:[0,1] o \mathcal{C}_{free}$ with $\kappa(0) = q_{start}$ and $d(\kappa(1), q_{end}) < \epsilon$, for an admissible distance ϵ
- Multi-goal path τ is admissible if $\tau:[0,1]\to \mathcal{C}_{free},\ \tau(0)=\tau(1)$ and there are n points such that $0 \le t_1 \le t_2 \le \ldots \le t_n$, $d(\tau(t_i), v_i) < \epsilon$, and $\bigcup_{1 < i < n} v_i = \mathcal{G}$
- The problem is to find path τ^* for a cost function c such that $c(\tau^*) = \min\{c(\tau) \mid \tau \text{ is admissible multi-goal path}\}\$

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■ It is a combinatorial optimization problem to determine the se-

■ It allows to solve (or improve performance of) more complex prob-

■ Inspection planning - Find the shortest tour to see (inspect) the

■ Data collection planning – Determine a cost efficient path to col-

■ Robotic exploration - Create a map of unknown environment as

MGMP – Examples of Solutions

- Determination of all paths connecting any two locations $g_i, g_i \in \mathcal{G}$ is usually very computationally demanding
- Several approaches can be found in literature, e.g.,
 - Considering Euclidean distance as approximation in solution of the TSP as the Minimum Spanning Tree (MST) – Edges in the MST are iteratively refined using optimal motion planner until all edges represent a feasible solution

Saha, M., Roughgarden, T., Latombe, J.-C., Sánchez-Ante, G. (2006): Planning Tours of Robotic Arms among Partitioned Goals. IJRR.

- Synergistic Combination of Layers of Planning (SyCLoP) A combination of route and trajectory planning
 - Plaku, E., Kavraki, L.E., Vardi, M.Y. (2010): Motion Planning With Dynamics by a Synergistic Combination of Layers of Planning. T-RO.
- Steering RRG roadmap expansion by unsupervised learning for the TSP







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Multi-Goal Planning in Robotic Missions

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Multi-Goal Planning in Robotic Missions

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Multi-Goal Planning in Robotic Missions

Inspection Planning - Decoupled Approach

1. Determine sensing locations such that the whole environment would be inspected (seen) by visiting them

A solution of the Art Gallery Problem

- 2. Create a roadmap connecting the sensing location E.g., using visibility graph or randomized sampling based approaches
- 3. Find the inspection path visiting all the sensing locations as a solution of the multi-goal path planning

De facto solution of the TSP

Inspection planning is also called coverage path planning in literature.

Example – Inspection Planning with AUV

■ Determine shortest inspection path for Autonomous Underwater Vehicle (AUV) to inspect a propeller of the vessel







Three-dimensional coverage planning for an underwater inspection robot Brendan Englot and Franz S. Hover

International Journal of Robotic Research, 32(9-10):1048-1073, 2013.

If we do not prescribe a discrete set of sensing locations, we can formulate the problem as the Watchman route problem









Approximate Solution of the Multiple Watchman Routes Problem with Restricted Visibility Range

IEEE Transactions on Neural Networks, 21(10):1668-1679, 2010.

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Multi-Goal Planning in Robotic Missions

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Self-Organizing Maps based Solution of the TSP

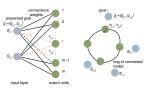
Kohonen's type of unsupervised two-layered neural network

- Neurons' weights represent nodes $\mathcal{N} = \{\nu_1, \dots, \nu_m\}$) in a plane.
- Nodes are organized into a ring.
- Sensing locations $S = \{s_1, \dots s_n\}$ are presented to the network in a random order.
- Nodes compete to be winner according to their distance to the presented goal s

$$\nu^* = \operatorname{argmin}_{\nu \in \mathcal{N}} |\mathcal{D}(\nu, s)|$$

■ The winner and its neighbouring nodes are adapted (moved) towards the city according to the neighbouring function

$$F(\sigma,d) = \left\{ egin{array}{ll} {
m e}^{-rac{d^2}{\sigma^2}} & {
m for} \ d < m/n_f, \ 0 & {
m otherwise}, \end{array}
ight.$$



- Best matching unit ν to the presented prototype s is determined according to distance function $|\mathcal{D}(\nu, s)|$
- For the Euclidean TSP. \mathcal{D} is the Euclidean
- However, for problems with obstacles, the multi-goal path planning, \mathcal{D} should correspond to the length of the shortest, collision free path.

SOM for the Multi-Goal Path Planning

Unsupervised learning procedure

Algorithm 1: SOM-based MTP solver

 $\mathcal{N} \leftarrow \text{initialization}(\nu_1, \dots, \nu_m);$ repeat error \leftarrow 0: foreach $g \in \Pi(S)$ do **selectWinner** argmin $_{\nu \in \mathcal{N}} |S(g, \nu)|$; $adapt(S(g, \nu), \mu f(\sigma, l)|S(g, \nu)|);$ $error \leftarrow \max\{error, |S(g, \nu^*)|\};$ $\sigma \leftarrow (1 - \alpha) \cdot \sigma$:



■ For multi-goal path planning – the selectWinner and adapt procedures are based on the solution of the path planning problem



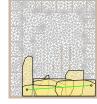
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until *error* $< \delta$;

An Application of Self-Organizing Map in the non-Euclidean Traveling Salesman

Jan Faigl, Miroslav Kulich, Vojtěch Vonásek and Libor Přeučil Neurocomputing, 74(5):671-679, 2011. B4M36UIR - Lecture 07: Multi-Goal Planning





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Multi-Goal Path Planning in Robotic Missions

■ It builds on a simple path and trajectory planning

lect data from the sensor stations (locations)

quence to visit the given locations

quickly as possible

Multi-goal path planning

Inspection Planning Motivations (examples)

- Periodically visit particular locations of the environment to check, e.g., for intruders, and return to the starting locations
- Based on available plans, provide a guideline how to search a building to find possible victims as quickly as possible (search and rescue scenario)

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Inspection Planning - "Continuous Sensing"

Given a map of the environment \mathcal{W} determine the shortest, closed, and collision-free path, from which the whole environment is covered by an omnidirectional sensor with the radius ρ .

adapt the network towards uncovered parts of ${\cal W}$ lacksquare Convex cover set of ${\mathcal W}$ created on top of a triangular mesh

- Incident convex polygons with a straight line segment are found by walking in a triangular mesh technique

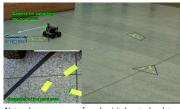
from the current ring (solution represented by the neurons) and

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Multi-Goal Path Planning with Goal Areas

■ It may be sufficient to visit a goal region instead of the particular point location

E.g., to take a sample measurement at each goal



Not only a sequence of goals visit has to be determined, but also an appropriate sensing location for each goal need to be found.

The problem with goal regions can be considered as a variant of the Traveling Salesman Problem with Neighborhoods (TSPN).

Traveling Salesman Problem with Neighborhoods

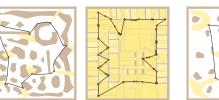
Given a set of n regions (neighbourhoods), what is the shortest closed path that visits each region.

■ The problem is NP-hard and APX-hard, it cannot be approximated to within factor $2 - \epsilon$, where $\epsilon > 0$

Safra and Schwartz (2006) - Computational Complexity

- Approximate algorithms exists for particular problem variants
 - E.g., Disjoint unit disk neighborhoods
- Flexibility of SOM for the TSP allows generalizing the unsupervised learning procedure to address the TSPN
- TSPN provides a suitable problem formulation for planning various inspection and data collection missions

SOM-based Solution of the Traveling Salesman Problem with Neighborhoods (TSPN)



Polygonal Goals Convex Cover Set n=9, T=0.32 s n=106. T=5.1 s

n=5, T=0.1 s

Visiting Convex Regions in a Polygonal Map, Jan Faigl, Vojěch Vonásek and Libor Přeučil Robotics and Autonomous Systems, 61(10):1070-1083, 2013.

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Example – TSPN for Inspection Planning with UAV

- Determine a cost-efficient trajectory from which a given set of target regions is covered
- For each target region a subspace $S \subset \mathbb{R}^3$ from which the target can be covered is determined S represents the neighbourhood
- The PRM motion planning algorithm is utilized to construct a motion planning roadmap (a graph)
- SOM based solution of the TSP with a graph input is generalized to the TSPN







Janoušek and Faigl, (2013) - ICRA

Example - TSPN for Planning with Localization Uncertainty

- Selection of waypoints from the neighborhood of each location
- P3AT ground mobile robot in an outdoor environment











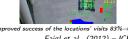
Real overall error at the goals decreased from 0.89 m \rightarrow 0.58 m (about 35%)

Decrease localization error at the target locations (indoor)









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Faigl et al., (2012) - ICRA

Summary of the Lecture

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- Improved sampling-based motion planners
- - Multi-Goal Motion Planning (MGMP) problem
- Multi-goal planning in robotic missions

Topics Discussed

- Multi-goal planning
 - Robotic variant of the Traveling Salesman Problem (TSP)
 - Multi-Goal Path Planning (MTP) problem

 - Traveling Salesman Problem with Neighborhoods (TSPN)
 - Inspection planning
- Next: Data collection planning

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