Robotic Information Garthering -**Exploration of Unknown Environment**

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Lecture 05

B4M36UIR - Artificial Intelligence in Robotics

Overview of the Lecture

- Part 1 Robotic Information Gathering Robotic Exploration
 - Robotic Information Gathering
 - Robotic Exploration
 - TSP-based Robotic Exploration
 - Robotic Information Gathering

Part I

Part 1 – Robotic Exploration

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Robotic exploration is a fundamental problem of robotic information gathering

Robotic Exploration of Unknown Environment

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Robotic Information Gathering

Create a model of phenomena by autonomous mobile robots performing measurements in a dynamic unknown environment.











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Challenges in Robotic Information Gathering

Where to take new measurements?

To improve the phenomena model

■ What locations visit first? On-line decision-making

■ How to efficiently utilize more robots?

To divide the task between the robots

■ How to navigate robots to the selected locations?

into a globally consistent map

■ SLAM – Simultaneous Localization and Mapping

■ The robot uses the map being built to localize itself

■ The map is primarily to help to localize the robot

■ Each cell is a binary random variable modeling

Improve Localization vs Model

Learning adaptivity Robotic Information

Gathering Sensing Planning

the on-line decision-making

It includes the problems of:

- Map building and localization
- Determination of the navigational waypoints

How to efficiently utilize a group of mo-

bile robots to autonomously create a map of an unknown environment

Performance in a real mission depends on

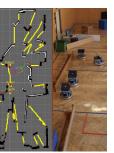
Performance indicators vs constraints

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Path planning and navigation to the waypoints

Time, energy, map quality vs robots, communication

Coordination of the actions (multi-robot team)



Courtesv of M. Kulich

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free space

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■ The robot should be localized to integrate new sensor measurements

■ The robot uses its sensors to build a map of the environment

How to address all these aspects altogether to find a cost

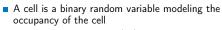
efficient solution using in-situ decisions?

Occupancy Grid

■ The problem is:

Assumptions

- The area of a cell is either completely free or occupied
- Cells (random variables) are indepedent of each other
- The state is static



- Cell m_i is occupied $p(m_i) = 1$
- Cell m_i is not occupied $p(m_i) = 0$
- Unknown $p(m_i) = 0.5$
- Probability distribution of the map m



Estimation of map from sensor data $z_{1:t}$ and robot poses $x_{1:t}$

$$p(m|z_{1:t}, x_{1:t}) = \prod_i p(m_i|z_{1:t}, x_{1:t})$$

Binary Bayes filter - Bayes rule and Markov process assumption

Mobile Robot Exploration

- Create a map of the environment
- Frontier-based approach

Yamauchi (1997)

- Occupancy grid map
 - Moravec and Elfes (1985)
- Laser scanner sensor
- Next-best-view approach
 - Select the next robot goal



Performance metric:

Time to create the map of the whole environment

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search and rescue mission

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Occupancy grid map

the occupancy of the cell

■ The map is a "side product" of SLAM

■ Grid map – discretized world representation

A cell is occupied (an obstacle) or free

Binary Bayes Filter 1/2

- Sensor data $z_{1:t}$ and robot poses $x_{1:t}$
- Binary random variables are indepedent and states are static

$$\begin{array}{cccc} \rho(m_{i}|z_{1:t},x_{1:t}) & \stackrel{\mathsf{Bayes \, rule}}{=} & \frac{\rho(z_{t}|m_{i},z_{1:t-1},x_{1:t})\rho(m_{i}|z_{1:t-1},x_{1:t})}{\rho(z_{t}|z_{1:t-1},x_{1:t})} \\ & \stackrel{\mathsf{Markov}}{=} & \frac{\rho(z_{t}|m_{i},x_{t})\rho(m_{i}|z_{1:t-1},x_{1:t})}{\rho(z_{t}|z_{1:t-1},x_{1:t})} \\ & \rho(z_{t}|m_{i},x_{t}) & = \frac{\rho(m_{i},z_{t},x_{t})\rho(z_{t},x_{t})}{\rho(m_{i}|x_{t})} \\ \hline \rho(m_{i},z_{1:t},x_{1:t}) & \stackrel{\mathsf{Bayes \, rule}}{=} & \frac{\rho(m_{i}|z_{t},x_{t})\rho(z_{t}|x_{t})\rho(m_{i}|z_{1:t-1},x_{1:t-1})}{\rho(m_{i}|x_{t})\rho(z_{t}|z_{1:t-1},x_{1:t-1})} \\ & \stackrel{\mathsf{Markov}}{=} & \frac{\rho(m_{i}|z_{t},x_{t})\rho(z_{t}|x_{t})\rho(m_{i}|z_{1:t-1},x_{1:t-1})}{\rho(m_{i})\rho(z_{t}|z_{1:t-1},x_{1:t})} \end{array}$$

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Binary Bayes Filter 2/2

Probability a cell is occupied

Probability a cell is not occupied

Ratio of the probabilities

Model for Laser Sensor

foreach $d \in \mathcal{L}$ do

 $m_d := \text{cell at } d_i$; if obstacle detected at mu then

 $p := grid(m_i)p_{free};$

 $p := grid(m_d)p_{occ}$;

 $p := grid(m_d)p_{Grad}$

■ The model is "sharp" with a precise

For the range measurement d_i, up-

Algorithm 2: Update map for $\mathcal{L} = (d_1, \dots, d_n)$

 $grid(m_i) := p/2p - p_{free} - grid(m_i) + 1;$

 $grid(m_i) := p/2p - p_{occ} - grid(m_i) + 1$

 $grid(m_i) := p/2p - p_{free} - grid(m_i) + 1$

date the grid cells along a sensor

detection of the obstacle

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Occupancy probability

 $\frac{p(m_i|z_t,x_t)}{1-p(m_i|z_t,x_t)} \frac{p(m_i,z_{1:t-1},x_{1:t-1})}{1-p(m_i|z_{1:t-1},x_{1:t-1})} \frac{1-p(m_i)}{p(m_i)}$

 $p(m_i|z_{1:t},x_{1:t}) = \frac{p(m_i|z_t,x_t)p(z_t|x_t)p(m_i|z_{1:t-1},x_{1:t-1})}{p(m_i)p(z_t|z_{1:t-1},x_{1:t})}$

 $p(\neg m_i|z_{1:t}, x_{1:t}) = \frac{p(\neg m_i|z_t, x_t)p(z_t|x_t)p(\neg m_i|z_{1:t-1}, x_{1:t-1})}{p(\neg m_i)p(z_t|z_{1:t-1}, x_{1:t})}$

 $\frac{p(m_i|z_{1:t},x_{1:t})}{p(\neg m_i|z_{1:t},x_{1:t})} = \frac{p(m_i|z_t,x_t)p(m_i|z_{1:t-1},x_{1:t-1})p(\neg m_i)}{p(\neg m_i|z_t,x_t)p(\neg m_i|z_{1:t-1},x_{1:t-1})p(m_i)}$

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Occupancy Mapping Algorithm

Algorithm 1: OccupancyGridMapping($\{l_{t-1,i}\}, x_t, z_t$)

foreach m; of the map m do if m_i in the perceptual field of z_t then $I_{t,i} := I_{t-1,i} + \text{inv_sensor_model}(m_i, x_t, z_t) - I_0;$ return $\{I_{t,i}\}$

Frontier-based Exploration Strategy

map := init(robot, scan);

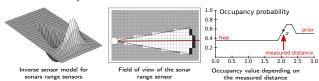
Algorithm 3: Frontier-based Exploration

while there are some reachable frontiers do

 $\mathcal{F} := \text{Determine frontier cells from } \mathcal{M}$:

 $\mathcal{F} := \text{Filter out unreachable frontiers from } \mathcal{F}$;

Occupancy grid mapping developed by Moravec and Elfes in mid 80'ies for noisy sonars



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Update occupancy map using new sensor data and Bayes rule;

 $\mathcal{M} :=$ Grow obstacle according to the dimension of the robot:

f :=Select the closest frontier from \mathcal{F} , e.g. using shortest path;

path := Plan a path from the current robot position to f;

Navigate robot towards f along path (for a while);

 $\mathcal{M} :=$ Created grid map from *map* using thresholding;

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Robot

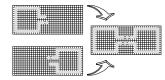
points have to be reachable, e.g., after obstacle growing



Multi-Robot Exploration – Map Marge

of new sensor measurements

$$\begin{split} P(occ_{x,y}) &= \frac{odds_{x,y}}{1 + odds_{x,y}} \\ odds_{x,y} &= \prod_{i=1}^{n} odds_{x,y}^{i}, \\ odds_{x,y}^{i} &= \frac{P(occ_{x,y}^{i})}{1 - P(occ_{x,y}^{i})} \end{split}$$



 $P(occ_{x,y}^i)$ is the probability that grid cell on the global coordinate is occupied in the map of the

We need the same global reference frame (localization).

Logs Odds Notation

■ Log odds ratio is defined as

$$I(x) = \log \frac{p(x)}{1 - p(x)}$$

 \blacksquare and the probability p(x) is

$$p(x) = 1 - \frac{1}{1 - e^{I(x)}}$$

■ The product modeling the cell m_i based on $z_{1:t}$ and $x_{1:t}$

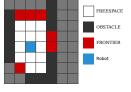
$$I(m_i|z_{1:t},x_{1:t}) = \underbrace{I(m_i|z_t,x_t)}_{\text{inverse sensor model}} + \underbrace{I(m_i,|z_{1:t-1},x_{1:t-1})}_{\text{recursive term}} - \underbrace{I(m_i)}_{\text{prior}}$$

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Frontier-based Exploration

- The basic idea of the frontier based exploration is navigation of the mobile robot towards unknown regions Yamauchi (1997)
- Frontier a border of the known and unknown regions of the environment
- Based on the probability of individual cells in the occupancy grid, cells are classified into:
 - FREESPACE $-p(m_i) < 0.5$ ■ OBSTACLE $-p(m_i) > 0.5$

 - UNKNOWN $-p(m_i) = 0.5$
- Frontier cell is a FREESPACE cell that is incident with an UNKNOWN cell
- Frontier cells as the navigation way-



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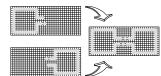
■ The individual maps can be merged in a similar way as integration

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$$P(occ_{x,y}) = \frac{odds_{x,y}}{1 + odds_{x,y}}$$

$$odds_{x,y} = \prod_{i=1}^{n} odds_{x,y}^{i},$$

$$odds_{x,y}^{i} = \frac{P(occ_{x,y}^{i})}{1 - P(occ_{x,y}^{i})}$$



Multi-Robot Exploration – Overview

- We need to assign navigation waypoint to each robot, which can be formulated as the task-allocation problem
- Exploration can be considered as an iterative procedure
 - 1. Initialize the occupancy grid Occ
 - 2. M ← create navigation grid(Occ) cells of M have values {freespace, obstacle, unknown}
 - 3. **F** ← detect frontiers(M)
 - Goal candidates G ← generate(F)
 - 5. Assign next goals to each robot $r \in R$, $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}, \mathcal{M})$
 - **6.** Create a plan P_i for each pair $\langle r_i, g_n \rangle$
 - 7. Perform each plan up to s_{max} operations
 - At each step, update Occ using new sensor measured 8. If |G| == 0 exploration finished, otherwise go to
- exploration where important decisions are made regarding the exploration performance,
- How to determined goal candidates from the the frontiers?
- How to plan a paths and assign the goals to the robots?
- How to navigate the robots
- towards the goal? ■ When to replan?
- etc.

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Exploration Procedure – Decision-Making Parts

- 1. Initialize set plans for *m* robots, $\mathcal{P} = (P_1, \dots, P_m), P_i = \emptyset$.
- 2. Repeat
- 2.1 Navigate robots using the plans \mathcal{P} ;
- 2.2 Collect new measurements;
- 2.3 Update the navigation map \mathcal{M} ; Until replanning condition is met.
- 3. Determine goal candidates G from M.
- 4. If $|\mathbf{G}| > 0$ assign goals to the robots
 - $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}, \mathcal{M}),$ $r_i \in \mathbf{R}, g_{r_i} \in \mathbf{G};$
 - Plan paths to the assigned goals $\mathcal{P} = \mathsf{plan}(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle, \mathcal{M});$

Multi-Robot Exploration Strategy

 \blacksquare A set of m robots at positions R =

At time t, let a set of n goal candidates be

■ The exploration strategy (at the planning step t):

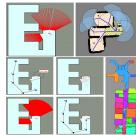
Go to Step 2.

 $\{r_1, r_2, \ldots, r_m\}$

 $\boldsymbol{G}(t) = \{g_1, \dots, g_n\}$

5. Stop all robots or navigate them to the depot

All reachable parts of the environment are explored



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Multi-Robot Exploration – Problem Definition

A problem of creating a grid map of the unknown environment by a set of m robots $\mathbf{R} = \{r_1, r_2, \dots, r_m\}$.

Exploration is an iterative procedure:

- 1. Collect new sensor measurements
- 2. Determinate a set of goal candidates

$$\boldsymbol{G}(t) = \{g_1, g_2, \dots, g_n\}$$

e.g., frontiers

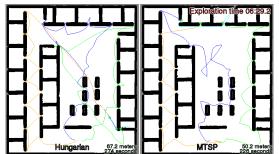
3. At time step t, select next goal for each robot as the task-allocation problem

$$(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}(t), \mathcal{M}(t))$$
using the distance cost function

- 4. Navigate robots towards goal
- 5. If |G(t)| > 0 go to Step 1; otherwise terminate

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The MTSP assignment provides better performance

Improvements of the basic Frontier-based Exploration

Several improvements have been proposed in the literature

 Introducing utility as a computation of expected covered area from a frontier

González-Baños, Latombe (2002)

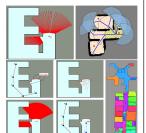
- Map segmentation for identification of rooms and exploration of the whole room by a single robot Holz, Basilico, Amigoni, Behnke (2010)
- Consider longer planning horizon (as a solution of the Traveling Salesman Problem (TSP)) Zlot, Stentz (2006), Kulich, Faigl (2011, 2012)

Representatives of free edges

Faigl, Kulich (2015)







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Select a goal $g \in G(t)$ for each robot $r \in R$ that will

minimize the required time to explore the environment.

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Goal Assignment Strategies - Task Allocation Algorithms

1. Greedy Assignment

(BLE)

n goals and m robots in $O(n^3)$

where M is the current map

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The problem is formulated as the task-allocation problem

 $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}(t), \mathcal{M}),$

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MTSP-based Task-Allocation Approach

- Consider the task-allocation problem as the Multiple Traveling Salesman Problem (MTSP)
- MTSP heuristic ⟨cluster-first, route-second⟩

1. Cluster the goal candidates G to m clusters

 $\boldsymbol{C} = \{C_1, \ldots, C_m\}, C_i \subseteq \boldsymbol{G}$

using K-means

2. For each robot $r_i \in \mathbf{R}, i \in \{1, \dots m\}$ select the next goal g_i from Ci using the TSP distance cost Kulich et at., ICRA (2011)

■ Solve the TSP on the set $C_i \cup \{r_i\}$

the tour starts at r

■ The next robot goal gi is the first goal of the found TSP tour

Faigl, J., Kulich, M., Přeučil, L. (2012): Goal Assignment using Distance Cost in

Statistical Evaluation of the Exploration Strategies

E Evaluation for the number of robots m and sensor range ρ

ρ	m	Iterative vs	Hungarian vs	MTSP vs
		Greedy	Iterative	Hungarian
3.0	3	+	=	+
3.0 3.0 3.0 3.0	3 5	+	=	+
3.0	. 7	+	=	+
	10	+	+	_
4.0	3 5	+	=	+
4.0	5	+	=	=
	/	+	=	+
4.0	10	+	+	_
5.0	3 5	+	=	+
5.0 5.0 5.0	5	+	=	+
5.0	10	+	= +	+

Total number of trials 14 280

Distance Cost Variants

■ TSP distance cost

- Simple robot-goal distance ■ Evaluate all goals using the robot-goal distance A length of the path from the robot position to the goal candidate
 - Greedy goal selection the closest one

Consider visitations of all goals

Use frontier representatives

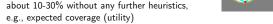
A length of the tour visiting all goals

■ the TSP distance cost improves performance

 Using frontier representatives improves the performance a bit

Solve the associated traveling salesman problem (TSP)





Kulich, M., Faigl, J, Přeučil, L. (2011): On Distance Utility in the Exploration Task. ICRA.

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Yamauchi B. Robotics and Autonomous Systems 29, 1999

Randomized greedy selection of the closest goal candidate

2. Iterative Assignment

Werger B, Mataric M, Distributed Autonomous Robotic Systems 4, 2001

■ Centralized variant of the broadcast of local eligibility algorithm

3. Hungarian Assignment

Optimal solution of the task-allocation problem for assignment of

Stachniss C, C implementation of the Hungarian method, 2004

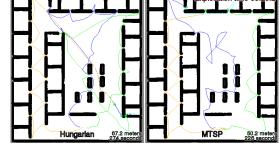
4. Multiple Traveling Salesman Problem - MTSP Assignment

(cluster-first, route-second), the TSP distance cost

Faigl et al. 2012

Performance of the MTSP vs Hungarian Algorithm

■ Replanning as quickly as possible; $m = 3, \rho = 3$ m



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Information Theory in Robotic Information Gathering

■ Employ information theory in control policy for robotic exploration

- **Entropy** uncertainty of x: $H[x] = -\int p(x) \log p(x) dx$
- **Conditional Entropy** expected uncertainty of x after learning unknown z; H[x|z]
- Mutual information how much uncertainty of x will be reduced by learning z; $I_{MI}[x;z] = H[x] - H[x|z]$
- Control policy is a rule how to select the robot action that reduces the uncertainty of estimate by learning measurements:

$$\operatorname{argmax}_{a \in A} I_{MI}[x; z|a],$$

where A is a set of possible actions, x is a future estimate, and z is future measurement

- Computation of the mutual information is computationally demanding
- Cauchy-Schwarz Quadratic Mutual Information (CSQMI) defined similarly to mutual information
 - A linear time approximations for CSQMI

Charrow, B. et al., (2015): Information-theoretic mapping using Cauchy-Schwarz Quadratic Mutual Information. ICRA.

■ Compute CSQMI as Cauchy-Schwarz divergence $I_{CS}[m; z]$ – raycast of the sensor beam and determine distribution over the range returns

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Actions are shortest path to cover the frontiers





Detect and cluster frontiers. Sampled poses to cover a cluster. Paths to the sampled pose

Select an action (a path) that maximizes the rate of Cauchy-Schwarz Quadratic Mutual Information



Actions





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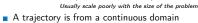
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Robotic Information Gathering

■ Robotic information gathering can be considered as the informative motion planning problem to a determine trajectory \mathcal{P}^* such that

$$\mathcal{P}^* = \operatorname{argmax}_{\mathcal{P} \in \Psi} I(\mathcal{P}), \text{ such that } c(\mathcal{P}) \leq B, \text{ where }$$

- Ψ is the space of all possible robot trajectories,
- \blacksquare $I(\mathcal{P})$ is the information gathered along the trajectory \mathcal{P}
- $\mathbf{c}(\mathcal{P})$ is the cost of \mathcal{P} and \mathcal{B} is the allowed budget
- Searching the space of all possible trajectories is complex and demanding problem
- A discretized problem can solved by combinatorial optimization techniques





Sampling-based motion planning techniques can employed for finding maximally informative trajectories

Hollinger, G., Sukhatme, G. (2014): Sampling-based robotic information gathering algorithms. IJRR

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Summary of the Lecture

Topics Discussed

Topics Discussed

■ Robotic information gathering

Ground vehicle

- Robotic exploration of unknown environment
- Occupancy grid map
- Frontier based exploration
- Exploration procedure and decision-making
- TSP-based distance cost in frontier-based exploration

Example of Autonomous Exploration using CSQMI

■ Planning with trajectory optimization – determine trajectory maximizing I_{CS}

Charrow, B. et al., (2015): Information-Theoretic Planning with Trajectory Optimization for Dense 3D Mapping. RSS.

- Multi-robot exploration and task-allocation
- Mutual information and informative path planning informative and motivational

Aerial vehicle

■ Next: Randomized sampling-based motion planning methods

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