Robotic Information Garthering -Exploration of Unknown Environment

Jan Faigl

Overview of the Lecture

Robotic Information Garthering - Exploration of Unknown Environment	Part 1 – Robotic Information Gathering - Robotic Exploration		
	 Robotic Information Gathering 		
Jan Faigl	Debatic Evaluation		
Department of Computer Science	 Robotic Exploration 		
Faculty of Electrical Engineering Czech Technical University in Prague	 TSP-based Robotic Exploration 		
Lecture 05	 Robotic Information Gathering 		
B4M36UIR – Artificial Intelligence in Robotics			
Jan Faigl, 2017 B4M36UIR – Lecture 05: Robotic Exploration 1 ,	/ 37 Jan Faigl, 2017 B4M36UIR – Lecture 05: Robotic Exploration 2 / 37		
Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gather	ing Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering		
	Robotic Information Gathering		
	Create a model of phenomena by autonomous mobile robots per- forming measurements in a dynamic unknown environment.		
Part I			

Part 1 – Robotic Exploration

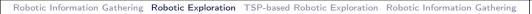


Robotic Exploration of Unknown Environment Challenges in Robotic Information Gathering Robotic exploration is a fundamental problem of robotic information gathering Where to take new measurements? The problem is: To improve the phenomena model How to efficiently utilize a group of mo-What locations visit first? Learning bile robots to autonomously create a adaptivity On-line decision-making map of an unknown environment **Robotic Information** How to efficiently utilize more Gathering Performance indicators vs constraints robots? Sensina Planning Time, energy, map quality vs robots, communication To divide the task between the robots Performance in a real mission depends on uncertainty uncertaintv the on-line decision-making How to navigate robots to the selected locations? It includes the problems of: Improve Localization vs Model Map building and localization Determination of the navigational waypoints Where to go next? Path planning and navigation to the waypoints How to address all these aspects altogether to find a cost Coordination of the actions (multi-robot team) efficient solution using in-situ decisions? Courtesy of M. Kulich Jan Faigl, 2017 B4M36UIR - Lecture 05: Robotic Exploration 6 / 37 Jan Faigl, 2017 B4M36UIR - Lecture 05: Robotic Exploration 7 / 37 Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering Robotic Information Gathering Environment Representation – Mapping and Occupancy Grid Mobile Robot Exploration Create a map of the environment The robot uses its sensors to build a map of the environment Frontier-based approach The robot should be localized to integrate new sensor measurements into a globally consistent map Yamauchi (1997) Occupancy grid map SLAM – Simultaneous Localization and Mapping Moravec and Elfes (1985) The robot uses the map being built to localize itself The map is primarily to help to localize the robot Laser scanner sensor The map is a "side product" of SLAM Next-best-view approach Grid map – discretized world representation Select the next robot goal A cell is occupied (an obstacle) or free Occupancy grid map Performance metric: Each cell is a binary random variable modeling Time to create the map of the whole environment the occupancy of the cell search and rescue mission

Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering

9 / 37 Jan Faigl, 2017

Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering



Occupancy Grid

Assumptions

- The area of a cell is either completely free or occupied
- Cells (random variables) are indepedent of each other
- The state is static
- A cell is a binary random variable modeling the occupancy of the cell
 - Cell m_i is occupied $p(m_i) = 1$
 - Cell m_i is not occupied $p(m_i) = 0$
 - Unknown $p(m_i) = 0.5$
- Probability distribution of the map *m*

$$p(m) = \prod_i p(m_i)$$

• Estimation of map from sensor data $z_{1:t}$ and robot poses $x_{1:t}$

 $p(m|z_{1:t}, x_{1:t}) = \prod_i p(m_i|z_{1:t}, x_{1:t})$

Binary Bayes filter - Bayes rule and Markov process assumption

 Jan Faigl, 2017
 B4M36UIR – Lecture 05: Robotic Exploration
 11 / 37
 Jan Faigl, 201

 Robotic Information Gathering
 Robotic Exploration
 TSP-based Robotic Exploration
 Robotic Information Gathering
 Robotic Information Gathering
 Robotic Information

Binary Bayes Filter 2/2

Probability a cell is occupied

$$p(m_i|z_{1:t}, x_{1:t}) = \frac{p(m_i|z_t, x_t)p(z_t|x_t)p(m_i|z_{1:t-1}, x_{1:t-1})}{p(m_i)p(z_t|z_{1:t-1}, x_{1:t})}$$

Probability a cell is not occupied

 $p(\neg m_i | z_{1:t}, x_{1:t}) = \frac{p(\neg m_i | z_t, x_t) p(z_t | x_t) p(\neg m_i | z_{1:t-1}, x_{1:t-1})}{p(\neg m_i) p(z_t | z_{1:t-1}, x_{1:t})}$

Ratio of the probabilities

$$\frac{p(m_i|z_{1:t}, x_{1:t})}{p(\neg m_i|z_{1:t}, x_{1:t})} = \frac{p(m_i|z_t, x_t)p(m_i|z_{1:t-1}, x_{1:t-1})p(\neg m_i)}{p(\neg m_i|z_t, x_t)p(\neg m_i|z_{1:t-1}, x_{1:t-1})p(m_i)}$$

= $\frac{p(m_i|z_t, x_t)}{1 - p(m_i|z_t, x_t)} \frac{p(m_i, z_{1:t-1}, x_{1:t-1})}{1 - p(m_i|z_{1:t-1}, x_{1:t-1})} \frac{1 - p(m_i)}{p(m_i)}$
sensor model z_t , recursive term, prior

B4M36UIR - Lecture 05: Robotic Exploration

Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering

Binary Bayes Filter 1/2

free space

occupied space

p(m) = 0

 $p(m_i)=1$

- Sensor data $z_{1:t}$ and robot poses $x_{1:t}$
- Binary random variables are indepedent and states are static

$$p(m_{i}|z_{1:t}, x_{1:t}) = \frac{p(z_{t}|m_{i}, z_{1:t-1}, x_{1:t})p(m_{i}|z_{1:t-1}, x_{1:t})}{p(z_{t}|z_{1:t-1}, x_{1:t})}$$

$$\frac{p(z_{t}|m_{i}, x_{t})p(m_{i}|z_{1:t-1}, x_{1:t-1})}{p(z_{t}|z_{1:t-1}, x_{1:t-1})}$$

$$p(z_{t}|m_{i}, x_{t}) = \frac{p(m_{i}, z_{t}, x_{t})p(z_{t}, x_{t})}{p(m_{i}|x_{t})}$$

$$p(m_{i}, z_{1:t}, x_{1:t}) = \frac{p(m_{i}|z_{t}, x_{t})p(z_{t}|x_{t})p(m_{i}|z_{1:t-1}, x_{1:t-1})}{p(m_{i}|x_{t})p(z_{t}|z_{1:t-1}, x_{1:t-1})}$$

$$\frac{p(m_{i}|z_{t}, x_{t})p(z_{t}|x_{t})p(m_{i}|z_{1:t-1}, x_{1:t-1})}{p(m_{i}|x_{t})p(z_{t}|z_{1:t-1}, x_{1:t-1})}$$

$$P(m_{i}|x_{t})p(z_{t}|z_{1:t-1}, x_{1:t-1}) = \frac{p(m_{i}|z_{t}, x_{t})p(z_{t}|x_{t})p(m_{i}|z_{1:t-1}, x_{1:t-1})}{p(m_{i}|p(z_{t}|z_{1:t-1}, x_{1:t-1})}$$

$$P(m_{i}|z_{t}, x_{t})p(z_{t}|z_{1:t-1}, x_{1:t-1}) = \frac{p(m_{i}|z_{t}, x_{t})p(z_{t}|z_{1:t-1}, x_{1:t-1})}{p(m_{i})p(z_{t}|z_{1:t-1}, x_{1:t-1})}$$

$$P(m_{i}|z_{t}, x_{t})p(z_{t}|z_{1:t-1}, x_{1:t-1}) = \frac{p(m_{i}|z_{t}, x_{t})p(z_{t}|z_{1:t-1}, x_{1:t-1})}{p(m_{i})p(z_{t}|z_{1:t-1}, x_{1:t-1})}$$

Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering

Logs Odds Notation

Log odds ratio is defined as

$$l(x) = \log \frac{p(x)}{1 - p(x)}$$

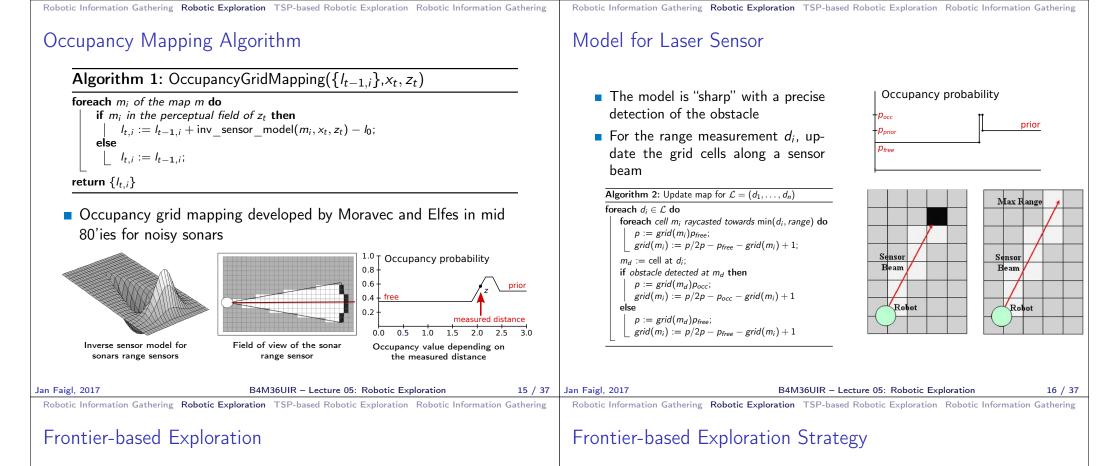
• and the probability p(x) is

$$p(x) = 1 - \frac{1}{1 - e^{I(x)}}$$

• The product modeling the cell m_i based on $z_{1:t}$ and $x_{1:t}$

$$I(m_i|z_{1:t}, x_{1:t}) = I(m_i|z_t, x_t) + I(m_i, |z_{1:t-1}, x_{1:t-1}) - I(m_i)$$

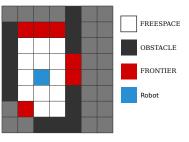
inverse sensor model recursive term prior



■ The basic idea of the frontier based exploration is navigation of the mobile robot towards unknown regions

Yamauchi (1997)

- **Frontier** a border of the known and unknown regions of the environment
- Based on the probability of individual cells in the occupancy grid, cells are classified into:
 - FREESPACE $p(m_i) < 0.5$
 - OBSTACLE $p(m_i) > 0.5$
 - UNKNOWN $p(m_i) = 0.5$
- Frontier cell is a FREESPACE cell that is incident with an UNKNOWN cell
- Frontier cells as the navigation waypoints have to be reachable, e.g., after obstacle growing



Use grid-based path planning

Jan Faigl, 2017

B4M36UIR - Lecture 05: Robotic Exploration

B4M36UIR - Lecture 05: Robotic Exploration

Update occupancy *map* using new sensor data and Bayes rule;

 $\mathcal{M} :=$ Grow obstacle according to the dimension of the robot;

f := Select the closest frontier from \mathcal{F} , e.g. using shortest path;

path := Plan a path from the current robot position to f;

Navigate robot towards f along *path* (for a while);

 $\mathcal{M} :=$ Created grid map from *map* using thresholding;

Algorithm 3: Frontier-based Exploration

while there are some reachable frontiers do

 $\mathcal{F} :=$ Determine frontier cells from \mathcal{M} :

 $\mathcal{F} :=$ Filter out unreachable frontiers from \mathcal{F} :

map := init(robot, scan);

Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering	Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering
Multi-Robot Exploration – Map Marge	Multi-Robot Exploration – Overview
• The individual maps can be merged in a similar way as integration of new sensor measurements $P(occ_{x,y}) = \frac{odds_{x,y}}{1 + odds_{x,y}},\\ odds_{x,y} = \prod_{i=1}^{n} odds_{x,y}^{i},\\ odds_{x,y}^{i} = \frac{P(occ_{x,y}^{i})}{1 - P(occ_{x,y}^{i})}.$	 We need to assign navigation waypoint to each robot, which can be formulated as the task-allocation problem Exploration can be considered as an iterative procedure Initialize the occupancy grid Occ M ← create_navigation_grid(Occ) cells of M have values {treespace, obstacle, unknown} F ← detect_frontiers(M) Goal candidates G ← generate(F) Assign next goals to each robot r ∈ R, ((r₁, g_{r₁}),, (r_m, g_{r_m})) = assign(R, G, M) Create a plan P_i for each pair (r_i, g_{r₁}) consisting of simple operations Perform each plan up to s_{max} operations At each step, update Occ using new sensor measurements If G == 0 exploration finished, otherwise go to Step 2
Jan Faigl, 2017 B4M36UIR – Lecture 05: Robotic Exploration 19 / 37	Jan Faigl, 2017 B4M36UIR – Lecture 05: Robotic Exploration 20 / 37
Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering Exploration Procedure – Decision-Making Parts	Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering Improvements of the basic Frontier-based Exploration
 Initialize – set plans for <i>m</i> robots, <i>P</i> = (<i>P</i>₁,,<i>P_m</i>), <i>P_i</i> = Ø. Repeat Navigate robots using the plans <i>P</i>; Collect new measurements; Update the navigation map <i>M</i>; Until replanning condition is met. Determine goal candidates <i>G</i> from <i>M</i>. If <i>G</i> > 0 assign goals to the robots (⟨r₁, g_{r1}⟩,,⟨r_m, g_{rm}⟩)=assign(<i>R</i>, <i>G</i>, <i>M</i>), <i>r_i</i> ∈ <i>R</i>, <i>g_{ri}</i> ∈ <i>G</i>; Plan paths to the assigned goals <i>P</i> = plan(⟨r₁, g_{r1}⟩,,⟨r_m, g_{rm}⟩,<i>M</i>); Go to Step 2. 	 Several improvements have been proposed in the literature Introducing utility as a computation of expected covered area from a frontier Conzález-Baños, Latombe (2002) Map segmentation for identification of rooms and exploration of the whole room by a single robot Holz, Basilico, Amigoni, Behnke (2010) Consider longer planning horizon (as a solution of the Traveling Salesman Problem (TSP)) Zlot, Stentz (2006), Kulich, Faigl (2011,2012) Representatives of free edges Faigl, Kulich (2015) Faigl

All reachable parts of the environment are explored.

B4M36UIR - Lecture 05: Robotic Exploration

Multi-Robot Exploration Strategy

- A set of *m* robots at positions R = $\{r_1, r_2, \ldots, r_m\}$
- At time t, let a set of n goal candidates be $\boldsymbol{G}(t) = \{g_1, \ldots, g_n\}$ I.e. frontiers



■ The exploration strategy (at the planning step *t*):

Select a goal $g \in G(t)$ for each robot $r \in \mathbf{R}$ that will minimize the required time to explore the environment.

The problem is formulated as the task-allocation problem

 $(\langle r_1, g_{r_1} \rangle, \ldots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}(t), \mathcal{M}),$

where \mathcal{M} is the current map

Jan Faigl, 2017	B4M36UIR – Lecture 05: Robotic Exploration	24 / 37	Jan Faigl, 2017	B4M36UIR – Lecture 05: Robotic Exploration	25 / 37
Robotic Information Cat	thering Robotic Exploration TSP-based Robotic Exploration Robotic Information	Gathering	Robotic Information	n Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information	Gathering

Multi-Robot Exploration – Problem Definition

Evaluate all goals using the robot-goal distance

Using frontier representatives improves the per-

Solve the associated traveling salesman problem (TSP)

■ Greedy goal selection – the closest one

A length of the path from the robot position to the

A problem of creating a grid map of the unknown environment by a set of *m* robots $\mathbf{R} = \{r_1, r_2, ..., r_m\}$.

Kulich, M., Faigl, J. Přeučil, L. (2011): On Distance Utility in the Exploration Task. ICRA.

Exploration is an iterative procedure:

1. Collect new sensor measurements

Distance Cost Variants

formance a bit

TSP distance cost

Simple robot-goal distance

goal candidate

Consider visitations of all goals

Use frontier representatives

A length of the tour visiting all goals

e.g., expected coverage (utility)

• the TSP distance cost improves performance

about 10-30% without any further heuristics,

2. Determinate a set of goal candidates

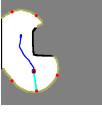
$$\boldsymbol{G}(t) = \{g_1, g_2, \ldots, g_n\}$$

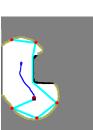
e.g., frontiers

3. At time step t, select next goal for each robot as the task-allocation problem

> $(\langle r_1, g_{r_1} \rangle, \ldots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}(t), \mathcal{M}(t))$ using the distance cost function

- 4. Navigate robots towards goal
- 5. If $|\mathbf{G}(t)| > 0$ go to Step 1; otherwise terminate





Goal Assignment Strategies – Task Allocation Algorithms

1. Greedy Assignment

Yamauchi B, Robotics and Autonomous Systems 29, 1999

Randomized greedy selection of the closest goal candidate

2. Iterative Assignment

Werger B, Mataric M, Distributed Autonomous Robotic Systems 4, 2001

- Centralized variant of the broadcast of local eligibility algorithm (BLE)
- 3. Hungarian Assignment
 - Optimal solution of the task-allocation problem for assignment of *n* goals and *m* robots in $O(n^3)$

Stachniss C, C implementation of the Hungarian method, 2004

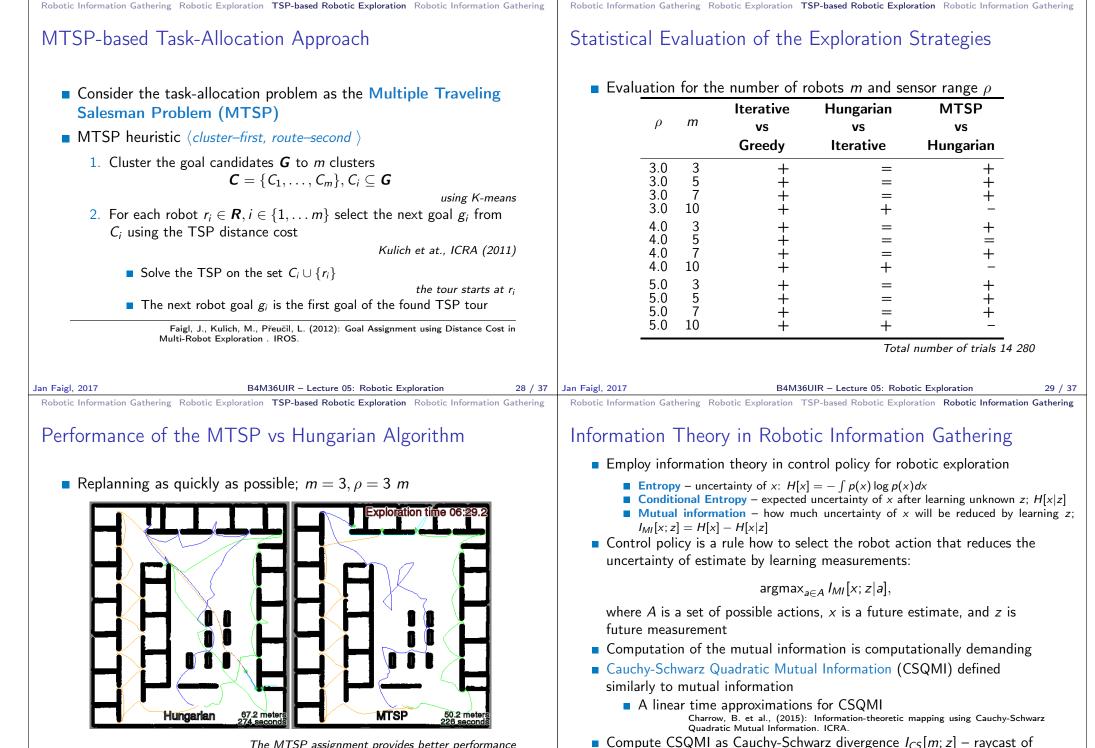
4. Multiple Traveling Salesman Problem – MTSP Assignment

cluster-first, route-second, the TSP distance cost

Faigl et al. 2012

Jan Faigl, 2017

B4M36UIR - Lecture 05: Robotic Exploration



The MTSP assignment provides better performance

the sensor beam and determine distribution over the range returns

Example of Autonomous Exploration using CSQMI



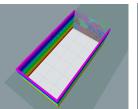


Ground vehicle

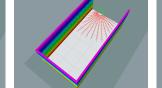
Aerial vehicle

Planning with trajectory optimization – determine trajectory maximizing I_{CS} Charrow, B. et al., (2015): Information-Theoretic Planning with Trajectory Optimization for Dense 3D Mapping. RSS.

Jan Faigl, 2017	B4M36UIR – Lecture 05: Robotic Exploration	33 / 37	Jan Faigl, 2017	B4M36UIR – Lecture 05: Robotic Exploration	34 / 37
Robotic Information Gathering	Robotic Exploration TSP-based Robotic Exploration Robotic Information	ation Gathering	Topics Discussed		
Robotic Informa	ation Gathering				
 Robotic information planning 	ation gathering can be considered as the informative problem to a determine trajectory \mathcal{P}^* such that	e mo -			
\mathcal{P}^{i}	${}^*=\operatorname{argmax}_{\mathcal{P}\in\Psi} I(\mathcal{P}), ext{ such that } c(\mathcal{P})\leq B, ext{ where }$				
\blacksquare $I(\mathcal{P})$ is the	pace of all possible robot trajectories, e information gathered along the trajectory ${\cal P}$ e cost of ${\cal P}$ and B is the allowed budget			Summary of the Lecture	
-	pace of all possible trajectories demanding problem	tacles			
combinatorial c _{Usua}	roblem can solved by optimization techniques <i>Ily scale poorly with the size of the problem</i> from a continuous domain	2000 End			
Sampling-bas finding maxim	sed motion planning techniques can employe ally informative trajectories tme, G. (2014): Sampling-based robotic information gathering algorithm				



Actions



Detect and cluster frontiers Sampled poses to cover a cluster Paths to the sampled poses

Select an action (a path) that maximizes the rate of Cauchy-Schwarz Quadratic Mutual Information

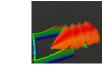






Actions are shortest path to cover the frontiers







Topics Discussed

Jan Faigl, 2017

Topics Discussed

- Robotic information gathering
- Robotic exploration of unknown environment
- Occupancy grid map
- Frontier based exploration
- Exploration procedure and decision-making
- **TSP-based distance cost in frontier-based exploration**
- Multi-robot exploration and task-allocation
- Mutual information and informative path planning informative and motivational

Next: Randomized sampling-based motion planning methods

B4M36UIR - Lecture 05: Robotic Exploration

37 / 37