# Robotic Information Garthering - Exploration of Unknown Environment

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Lecture 05

B4M36UIR - Artificial Intelligence in Robotics

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Robotic Information Gathering Robotic Exploration TSP-based Robotic Exploration Robotic Information Gathering

Part I

Part 1 - Robotic Exploration

#### Overview of the Lecture

- Part 1 Robotic Information Gathering Robotic Exploration
  - Robotic Information Gathering
  - Robotic Exploration
  - TSP-based Robotic Exploration
  - Robotic Information Gathering

## Robotic Information Gathering

Create a model of phenomena by autonomous mobile robots performing measurements in a dynamic unknown environment.

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## Challenges in Robotic Information Gathering

■ Where to take new measurements?

To improve the phenomena model

■ What locations visit first?

On-line decision-making

■ How to efficiently utilize more robots?

To divide the task between the robots

■ How to navigate robots to the selected locations?

Improve Localization vs Model

Learning adaptivity **Robotic Information** Gathering Planning uncertainty

How to address all these aspects altogether to find a cost efficient solution using in-situ decisions?

Robotic Exploration of Unknown Environment

## Robotic exploration is a fundamental problem of robotic information gathering

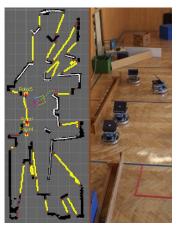
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■ The problem is:

How to efficiently utilize a group of mobile robots to autonomously create a map of an unknown environment

- Performance indicators vs constraints Time, energy, map quality vs robots, communication
- Performance in a real mission depends on the on-line decision-making
- It includes the problems of:
  - Map building and localization
  - Determination of the navigational waypoints

- Path planning and navigation to the waypoints
- Coordination of the actions (multi-robot team)



Courtesy of M. Kulich

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## Mobile Robot Exploration

- Create a map of the environment
- Frontier-based approach

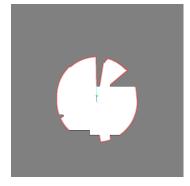
Yamauchi (1997)

Occupancy grid

Moravec and Elfes (1985)

- Laser scanner sensor
- Next-best-view approach

Select the next robot goal



#### Performance metric:

Time to create the map of the whole environment

search and rescue mission

## Environment Representation – Mapping and Occupancy Grid

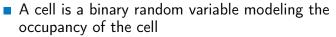
- The robot uses its sensors to build a map of the environment
- The robot should be localized to integrate new sensor measurements into a globally consistent map
- SLAM Simultaneous Localization and Mapping
  - The robot uses the map being built to localize itself
  - The map is primarily to help to localize the robot
  - The map is a "side product" of SLAM
- Grid map discretized world representation
  - A cell is occupied (an obstacle) or free
- Occupancy grid map
  - Each cell is a binary random variable modeling the occupancy of the cell



## Occupancy Grid

#### Assumptions

- The area of a cell is either completely free or occupied
- Cells (random variables) are indepedent of each other
- The state is static



- Cell  $m_i$  is occupied  $p(m_i) = 1$
- Cell  $m_i$  is not occupied  $p(m_i) = 0$
- Unknown  $p(m_i) = 0.5$
- Probability distribution of the map m

$$p(m) = \Pi_i p(m_i)$$

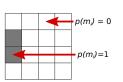
**E**stimation of map from sensor data  $z_{1+t}$  and robot poses  $x_{1+t}$ 

$$p(m|z_{1:t},x_{1:t}) = \prod_{i} p(m_i|z_{1:t},x_{1:t})$$

Binary Bayes filter - Bayes rule and Markov process assumption

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free space occupied space



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## Binary Bayes Filter 2/2

Probability a cell is occupied

$$p(m_i|z_{1:t},x_{1:t}) = \frac{p(m_i|z_t,x_t)p(z_t|x_t)p(m_i|z_{1:t-1},x_{1:t-1})}{p(m_i)p(z_t|z_{1:t-1},x_{1:t})}$$

Probability a cell is not occupied

$$p(\neg m_i|z_{1:t},x_{1:t}) = \frac{p(\neg m_i|z_t,x_t)p(z_t|x_t)p(\neg m_i|z_{1:t-1},x_{1:t-1})}{p(\neg m_i)p(z_t|z_{1:t-1},x_{1:t})}$$

Ratio of the probabilities

$$\frac{p(m_i|z_{1:t},x_{1:t})}{p(\neg m_i|z_{1:t},x_{1:t})} = \frac{p(m_i|z_t,x_t)p(m_i|z_{1:t-1},x_{1:t-1})p(\neg m_i)}{p(\neg m_i|z_t,x_t)p(\neg m_i|z_{1:t-1},x_{1:t-1})p(m_i)} \\
= \frac{p(m_i|z_t,x_t)}{1-p(m_i|z_t,x_t)} \frac{p(m_i,z_{1:t-1},x_{1:t-1})}{1-p(m_i|z_{1:t-1},x_{1:t-1})} \frac{1-p(m_i)}{p(m_i)}$$

sensor model z+ recursive term prior

Binary Bayes Filter 1/2

- Sensor data  $z_{1:t}$  and robot poses  $x_{1:t}$
- Binary random variables are indepedent and states are static

$$\begin{array}{ccc}
\rho(m_i|z_{1:t},x_{1:t}) & \stackrel{\mathsf{Bayes\ rule}}{=} & \frac{p(z_t|m_i,z_{1:t-1},x_{1:t})p(m_i|z_{1:t-1},x_{1:t})}{p(z_t|z_{1:t-1},x_{1:t})} \\
& \stackrel{\mathsf{Markov}}{=} & \frac{p(z_t|m_i,z_t)p(m_i|z_{1:t-1},x_{1:t})}{p(z_t|z_{1:t-1},x_{1:t})}
\end{array}$$

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$$\frac{p(z_t|m_i,x_t)}{p(m_i,z_{1:t},x_{1:t})} \stackrel{=}{=} \frac{\frac{p(m_i,z_t,x_t)p(z_t,x_t)}{p(m_i|x_t)}}{\frac{p(m_i|z_t,x_t)p(z_t|x_t)p(m_i|z_{1:t-1},x_{1:t-1})}{p(m_i|x_t)p(z_t|z_{1:t-1},x_{1:t})}}{\frac{p(m_i|z_t,x_t)p(z_t|x_t)p(m_i|z_{1:t-1},x_{1:t-1})}{p(m_i)p(z_t|z_{1:t-1},x_{1:t})}}$$

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## Logs Odds Notation

Log odds ratio is defined as

$$I(x) = \log \frac{p(x)}{1 - p(x)}$$

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 $\blacksquare$  and the probability p(x) is

$$p(x) = 1 - \frac{1}{1 - e^{I(x)}}$$

■ The product modeling the cell  $m_i$  based on  $z_{1:t}$  and  $x_{1:t}$ 

$$I(m_i|z_{1:t},x_{1:t}) = \underbrace{I(m_i|z_t,x_t)}_{\text{inverse sensor model}} + \underbrace{I(m_i,|z_{1:t-1},x_{1:t-1})}_{\text{recursive term}} - \underbrace{I(m_i)}_{\text{prior}}$$

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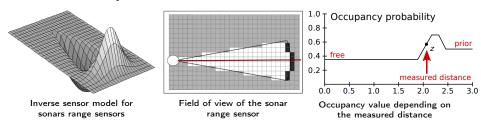
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## Algorithm 1: OccupancyGridMapping $(\{l_{t-1,i}\},x_t,z_t)$

return  $\{I_{t,i}\}$ 

 Occupancy grid mapping developed by Moravec and Elfes in mid 80'ies for noisy sonars



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Frontier-based Exploration

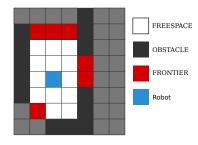
■ The basic idea of the **frontier** based exploration is navigation of the mobile robot towards unknown regions

Yamauchi (1997)

■ Frontier – a border of the known and unknown regions of the environment

Based on the probability of individual cells in the occupancy grid, cells are classified into:

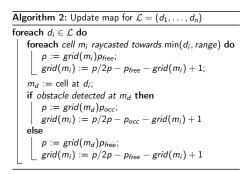
- FREESPACE  $-p(m_i) < 0.5$
- OBSTACLE  $p(m_i) > 0.5$
- UNKNOWN  $-p(m_i) = 0.5$
- Frontier cell is a FREESPACE cell that is incident with an UNKNOWN cell
- Frontier cells as the navigation waypoints have to be reachable, e.g., after obstacle growing

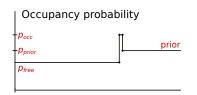


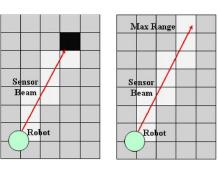
Use grid-based path planning

#### Model for Laser Sensor

- The model is "sharp" with a precise detection of the obstacle
- For the range measurement  $d_i$ , update the grid cells along a sensor beam







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## Frontier-based Exploration Strategy

#### Algorithm 3: Frontier-based Exploration

map := init(robot, scan);

while there are some reachable frontiers do

Update occupancy map using new sensor data and Bayes rule;

 $\mathcal{M} :=$ Created grid map from *map* using thresholding;

 $\mathcal{M} :=$ Grow obstacle according to the dimension of the robot;

 $\mathcal{F} := \text{Determine frontier cells from } \mathcal{M}$ :

 $\mathcal{F} := \text{Filter out unreachable frontiers from } \mathcal{F};$ 

f :=Select the closest frontier from  $\mathcal{F}$ , e.g. using shortest path;

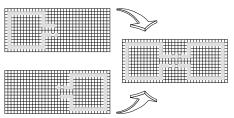
path := Plan a path from the current robot position to <math>f;

Navigate robot towards f along path (for a while);

## Multi-Robot Exploration – Map Marge

■ The individual maps can be merged in a similar way as integration of new sensor measurements

$$\begin{split} P(occ_{x,y}) &= \frac{odds_{x,y}}{1 + odds_{x,y}}, \\ odds_{x,y} &= \prod_{i=1}^{n} odds_{x,y}^{i}, \\ odds_{x,y}^{i} &= \frac{P(occ_{x,y}^{i})}{1 - P(occ_{x,y}^{i})}. \end{split}$$



 $P(occ_{x,y}^i)$  is the probability that grid cell on the global coordinate is occupied in the map of the

We need the same global reference frame (localization).

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## Exploration Procedure – Decision-Making Parts

- 1. Initialize set plans for m robots,  $\mathcal{P} = (P_1, \dots, P_m), P_i = \emptyset$ .
- 2. Repeat
- 2.1 Navigate robots using the plans  $\mathcal{P}$ ;
- 2.2 Collect new measurements:
- 2.3 Update the navigation map  $\mathcal{M}$ ; Until replanning condition is met.
- 3. Determine goal candidates G from M.
- 4. If  $|\mathbf{G}| > 0$  assign goals to the robots
  - $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}, \mathcal{M}),$  $r_i \in \boldsymbol{R}, g_{r_i} \in \boldsymbol{G}$ ;
  - Plan paths to the assigned goals  $\mathcal{P} = \mathsf{plan}(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle, \mathcal{M});$
  - Go to Step 2.
- 5. Stop all robots or navigate them to the depot

All reachable parts of the environment are explored.

Multi-Robot Exploration – Overview

- We need to assign navigation waypoint to each robot, which can be formulated as the task-allocation problem
- Exploration can be considered as an iterative procedure
  - 1. Initialize the occupancy grid Occ
  - 2.  $\mathcal{M} \leftarrow \text{create navigation grid}(Occ)$ cells of M have values {freespace, obstacle, unknown}
  - 3.  $\mathbf{F} \leftarrow \text{detect frontiers}(\mathcal{M})$
  - 4. Goal candidates  $\mathbf{G} \leftarrow \text{generate}(\mathbf{F})$
  - 5. Assign next goals to each robot  $r \in R$ ,  $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}, \mathcal{M})$
  - 6. Create a plan  $P_i$  for each pair  $\langle r_i, g_{r_i} \rangle$ consisting of simple operations
  - 7. Perform each plan up to  $s_{max}$  operations At each step, update Occ using new sensor measurements
  - 8. If |G| == 0 exploration finished, otherwise go to Step 2



- There are several parts of the exploration procedure where important decisions are made regarding the exploration performance, e.g.
- How to determined goal candidates from the the frontiers?
- How to plan a paths and assign the goals to the robots?
- How to navigate the robots towards the goal?
- When to replan?
- etc.

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## Improvements of the basic Frontier-based Exploration

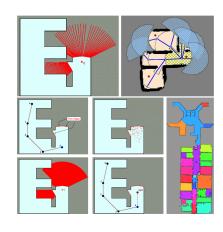
Several improvements have been proposed in the literature

- Introducing utility as a computation of expected covered area from a frontier
  - González-Baños, Latombe (2002)
- Map segmentation for identification of rooms and exploration of the whole room by a single robot Holz, Basilico, Amigoni, Behnke (2010)
- Consider longer planning horizon (as a solution of the Traveling Salesman Problem (TSP)) Zlot, Stentz (2006), Kulich, Faigl (2011,2012)
- Representatives of free edges

Faigl, Kulich (2015)

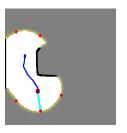






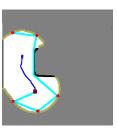
## ■ Simple robot-goal distance

- Evaluate all goals using the robot–goal distance A length of the path from the robot position to the goal candidate
- Greedy goal selection the closest one
- Using frontier representatives improves the performance a bit



#### ■ TSP distance cost

- Consider visitations of all goals Solve the associated traveling salesman problem (TSP)
- A length of the tour visiting all goals
- Use frontier representatives
- the TSP distance cost improves performance about 10-30% without any further heuristics, e.g., expected coverage (utility)



Kulich, M., Faigl, J. Přeučil, L. (2011): On Distance Utility in the Exploration Task. ICRA.

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## Multi-Robot Exploration – Problem Definition

A problem of creating a grid map of the unknown environment by a set of *m* robots  $R = \{r_1, r_2, ..., r_m\}.$ 

Exploration is an iterative procedure:

- 1. Collect new sensor measurements
- 2. Determinate a set of goal candidates

$$\boldsymbol{G}(t) = \{g_1, g_2, \ldots, g_n\}$$

e.g., frontiers

3. At time step t, select next goal for each robot as the task-allocation problem



$$(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}(t), \mathcal{M}(t))$$
using the distance cost function

- 4. Navigate robots towards goal
- 5. If  $|\boldsymbol{G}(t)| > 0$  go to Step 1; otherwise terminate

## Multi-Robot Exploration Strategy

- lacksquare A set of m robots at positions R =  $\{r_1, r_2, \ldots, r_m\}$
- $\blacksquare$  At time t, let a set of n goal candidates be  $G(t) = \{g_1, \ldots, g_n\}$



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■ The exploration strategy (at the planning step t):

Select a goal  $g \in G(t)$  for each robot  $r \in R$  that will minimize the required time to explore the environment.

The problem is formulated as the task-allocation problem

$$(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}(t), \mathcal{M}),$$

where  $\mathcal{M}$  is the current map

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## Goal Assignment Strategies – Task Allocation Algorithms

#### 1. Greedy Assignment

Yamauchi B, Robotics and Autonomous Systems 29, 1999

Randomized greedy selection of the closest goal candidate

#### 2. Iterative Assignment

Werger B, Mataric M, Distributed Autonomous Robotic Systems 4, 2001

 Centralized variant of the broadcast of local eligibility algorithm (BLE)

#### 3. Hungarian Assignment

 Optimal solution of the task-allocation problem for assignment of n goals and m robots in  $O(n^3)$ 

Stachniss C, C implementation of the Hungarian method, 2004

#### 4. Multiple Traveling Salesman Problem - MTSP Assignment

■ ⟨cluster-first, route-second⟩, the TSP distance cost

Faigl et al. 2012

## MTSP-based Task-Allocation Approach

- Consider the task-allocation problem as the Multiple Traveling Salesman Problem (MTSP)
- MTSP heuristic ⟨cluster-first, route-second⟩
  - 1. Cluster the goal candidates  ${\it G}$  to m clusters

$$\mathbf{C} = \{C_1, \ldots, C_m\}, C_i \subseteq \mathbf{G}$$

using K-means

2. For each robot  $r_i \in \mathbf{R}, i \in \{1, \dots m\}$  select the next goal  $g_i$  from  $C_i$  using the TSP distance cost

Kulich et at., ICRA (2011)

■ Solve the TSP on the set  $C_i \cup \{r_i\}$ 

the tour starts at  $r_i$ 

■ The next robot goal  $g_i$  is the first goal of the found TSP tour

Faigl, J., Kulich, M., Přeučil, L. (2012): Goal Assignment using Distance Cost in Multi-Robot Exploration . IROS.

## Statistical Evaluation of the Exploration Strategies

**E** Evaluation for the number of robots m and sensor range  $\rho$ 

ρ	m	Iterative vs Greedy	Hungarian vs Iterative	MTSP vs Hungarian
3.0	3	+	=	+ + + -
3.0	5	+	=	
3.0	7	+	=	
3.0	10	+	+	
4.0	3	+	=	+
4.0	5	+	=	=
4.0	7	+	=	+
4.0	10	+	+	-
5.0	3	+	=	+
5.0	5	+	=	+
5.0	7	+	=	+
5.0	10	+	+	-

Total number of trials 14 280

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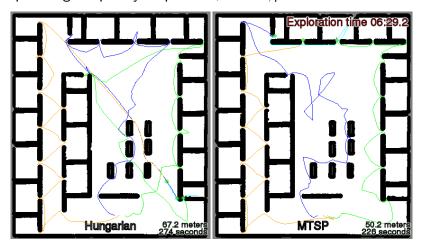
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## Performance of the MTSP vs Hungarian Algorithm

■ Replanning as quickly as possible; m = 3,  $\rho = 3$  m



The MTSP assignment provides better performance

## Information Theory in Robotic Information Gathering

- Employ information theory in control policy for robotic exploration
  - **Entropy** uncertainty of x:  $H[x] = -\int p(x) \log p(x) dx$
  - **Conditional Entropy** expected uncertainty of x after learning unknown z; H[x|z]
  - Mutual information how much uncertainty of x will be reduced by learning z;  $I_{MI}[x;z] = H[x] H[x|z]$
- Control policy is a rule how to select the robot action that reduces the uncertainty of estimate by learning measurements:

$$\operatorname{argmax}_{a \in A} I_{MI}[x; z|a],$$

where A is a set of possible actions, x is a future estimate, and z is future measurement

- Computation of the mutual information is computationally demanding
- Cauchy-Schwarz Quadratic Mutual Information (CSQMI) defined similarly to mutual information
  - A linear time approximations for CSQMI

    Charrow, B. et al., (2015): Information-theoretic mapping using Cauchy-Schwarz

    Quadratic Mutual Information. ICRA.
- Compute CSQMI as Cauchy-Schwarz divergence  $I_{CS}[m; z]$  raycast of the sensor beam and determine distribution over the range returns

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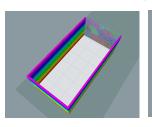
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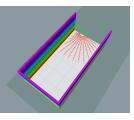
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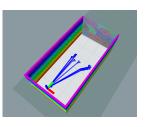
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#### Actions

Actions are shortest path to cover the frontiers







Detect and cluster frontiers 
Sampled poses to cover a cluster 
Paths to the sampled poses

■ Select an action (a path) that maximizes the rate of Cauchy-Schwarz Quadratic Mutual Information









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Topics Discussed

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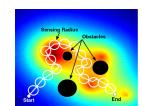
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## Robotic Information Gathering

Robotic information gathering can be considered as the informative motion planning problem to a determine trajectory  $\mathcal{P}^*$  such that

 $\mathcal{P}^* = \operatorname{argmax}_{\mathcal{P} \in \mathcal{W}} I(\mathcal{P})$ , such that  $c(\mathcal{P}) \leq B$ , where

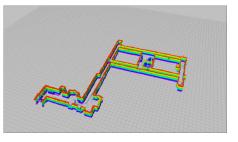
- $\blacksquare$   $\Psi$  is the space of all possible robot trajectories,
- $\blacksquare$   $I(\mathcal{P})$  is the information gathered along the trajectory  $\mathcal{P}$
- $c(\mathcal{P})$  is the cost of  $\mathcal{P}$  and B is the allowed budget
- Searching the space of all possible trajectories is complex and demanding problem
- A discretized problem can solved by combinatorial optimization techniques Usually scale poorly with the size of the problem



- A trajectory is from a continuous domain
- Sampling-based motion planning techniques can employed for finding maximally informative trajectories

Hollinger, G., Sukhatme, G. (2014): Sampling-based robotic information gathering algorithms. IJRR.

## Example of Autonomous Exploration using CSQMI





Ground vehicle

Aerial vehicle

Planning with trajectory optimization – determine trajectory maximizing  $I_{CS}$ Charrow, B. et al., (2015): Information-Theoretic Planning with Trajectory Optimization for Dense 3D Mapping. RSS.

Summary of the Lecture

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## Topics Discussed

- Robotic information gathering
- Robotic exploration of unknown environment
- Occupancy grid map
- Frontier based exploration
- Exploration procedure and decision-making
- TSP-based distance cost in frontier-based exploration
- Multi-robot exploration and task-allocation
- Mutual information and informative path planning

informative and motivational

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■ Next: Randomized sampling-based motion planning methods

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