Grid and Graph based Path Planning Methods

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Lecture 04

B4M36UIR - Artificial Intelligence in Robotics

Overview of the Lecture

- Part 1 Grid and Graph based Path Planning Methods
 - Grid-based Planning
 - DT for Path Planning
 - Graph Search Algorithms
 - D* Lite

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Grid-based Planning

DT for Path Planning

Graph Search Algorithms

D* Lite

Grid-based Planning

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Part I

Part 1 – Grid and Graph based Path Planning Methods

Grid-based Planning

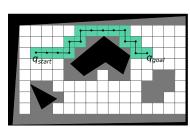
- A subdivision of C_{free} into smaller cells
- Grow obstacles can be simplified by growing borders by a diameter of the robot
- Construction of the planning graph G = (V, E) for V as a set of cells and E as the neighbor-relations
 - 4-neighbors and 8-neighbors





A grid map can be constructed from the so-called occupancy grid maps

E.g., using thresholding







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Grid-based Environment Representations

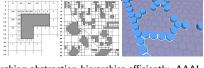
- Hiearchical planning
 - Coarse resolution and re-planning on finer resolution

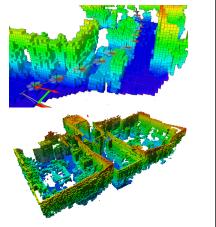
Holte, R. C. et al. (1996): Hierarchical A *: searching abstraction hierarchies efficiently. AAAI

- Octree can be used for the map representation
- In addition to squared (or rectangular) grid a hexagonal grid can be used
- 3D grid maps octomap

https://octomap.github.io

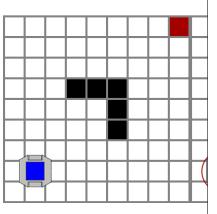
- Memory grows with the size of the environment
- Due to limited resolution it may fail in narrow passages of $\mathcal{C}_{\textit{free}}$





Example of Simple Grid-based Planning

- Wave-front propagation using path simplication
- Initial map with a robot and goal
- Obstacle growing
- Wave-front propagation "flood fill"
- Find a path using a navigation function
- Path simplification
 - "Ray-shooting" technique combined with Bresenham's line algorithm
 - The path is a sequence of "key" cells for avoiding obstacles



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Grid-based Planning

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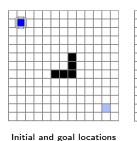
DT for Path Planning

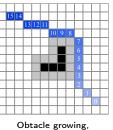
Graph Search Algorithms

D* Lite

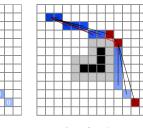
Path Simplification

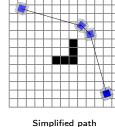
- The initial path is found in a grid using 4-neighborhood
- The rayshoot cast a line into a grid and possible collisions of the robot with obstacles are checked
- The "farthest" cells without collisions are used as "turn" points
- The final path is a sequence of straight line segments





wave-front propagation





Ray-shooting Simplified

Bresenham's Line Algorithm

- Filling a grid by a line with avoding float numbers
- A line from (x_0, y_0) to (x_1, y_1) is given by $y = \frac{y_1 y_0}{x_1 x_0}(x x_0) + y_0$

```
CoordsVector& bresenham(const Coords& pt1, const 26
                                                              int twoDy = 2 * dy;
           Coords& pt2, CoordsVector& line)
                                                              int twoDyTwoDx = twoDy - 2 * dx; //2*Dy - 2*Dx
                                                              int e = twoDy - dx; //2*Dy - Dx
        // The pt2 point is not added into line
                                                              int y = y0;
        int x0 = pt1.c; int y0 = pt1.r;
                                                              int xDraw, yDraw;
        int x1 = pt2.c; int y1 = pt2.r;
                                                              for (int x = x0; x != x1; x += xstep) {
                                                                 if (steep) {
        int dx = x1 - x0;
                                                      33
                                                                    xDraw = y;
        int dy = y1 - y0;
                                                                    yDraw = x;
        int steep = (abs(dy) >= abs(dx));
                                                                 } else {
10
                                                      36
                                                      37
11
           SWAP(x0, y0);
                                                                    yDraw = y;
12
           SWAP(x1, y1);
13
           dx = x1 - x0; // recompute Dx, Dy
                                                                 p.c = xDraw;
14
                                                                 p.r = yDraw;
           dy = y1 - y0;
15
                                                                 line.push_back(p); // add to the line
16
        int xstep = 1;
17
                                                                     e += twoDyTwoDx; //E += 2*Dy - 2*Dx
18
           xstep = -1;
19
                                                                 } else {
20
                                                                     e += twoDy; //E += 2*Dy
        int ystep = 1;
22
        if (dy < 0) {
                                                      48
23
                                                      49
           ystep = -1;
                                                              return line;
                                                      50
24
25
```

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Distance Transform based Path Planning

- For a given goal location and grid map compute a navigational function using wave-front algorithm, i.e., a kind of potential field
 - The value of the goal cell is set to 0 and all other free cells are set to some very high value
 - For each free cell compute a number of cells towards the goal cell
 - It uses 8-neighbors and distance is the Euclidean distance of the centers of two cells, i.e., EV=1 for orthogonal cells or $EV = \sqrt{2}$ for diagonal cells
 - The values are iteratively computed until the values are changed
 - The value of the cell c is computed as

$$cost(c) = \min_{i=1}^{8} \left(cost(c_i) + EV_{c_i,c} \right),$$

where c_i is one of the neighboring cells from 8-neighborhood of the cell c

- The algorithm provides a cost map of the path distance from any free cell to the goal cell
- The path is then used following the gradient of the cell cost

Jarvis, R. (2004): Distance Transform Based Visibility Measures for Covert Path Planning in Known but Dynamic Environments

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Grid-based Planning

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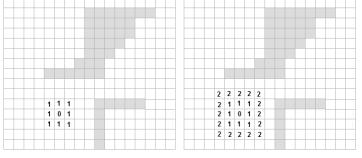
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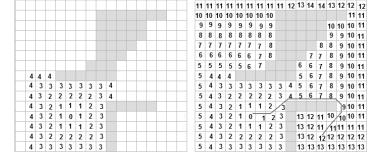
Distance Transform Path Planning

Algorithm 1: Distance Transform for Path Planning

```
for y:=0 to yMax+1 do
    for x:=0 to xMax+1 do
         if goal [x,y] then
             cell [x,y] := 0;
             cell [x,y]:=xMax*y Max;
repeat
    for y:=2 to yMax do
         for x:=2 to xMax do
              if not blocked [x,y] then
                  cell [x,y]:= min (cell[x-1,y]+1, cell[x-1,y-1]+\sqrt{2},cell[x,y-1]+1, cell[x+1,y-1]+\sqrt{2},cell [x,y]);
    for y:=yMax-1downto 1 do
         for x:=xMax-1 downto 1 do
              if not blocked [x,y] then
                   cell[x,y]:=min(cell[x+1,y]+1,cell[x+1,y+1]+\sqrt{2},cell[x,y+1]+1,cell[x-1,y+1]+\sqrt{2},cell[x,y]);
until no change;
```

Example – Distance Transform based Path Planning





Graph Search Algorithms

Distance Transform based Path Planning - Impl. 1/2

```
Grid& DT::compute(Grid& grid) const
                                                                         for (int c = W - 2; c > 0; c--) {
                                                          36
                                                          37
                                                                           if (map[r][c] != FREESPACE) {
          static const double DIAGONAL = sqrt(2);
          static const double ORTOGONAL = 1;
                                                          38
                                                                               continue;
           const int H = map.H;
                                                          39
                                                                           } //obstacle detected
          const int W = map.W;
                                                          40
                                                                            double t[4];
          assert(grid.H == H and grid.W == W, "size");
                                                          41
                                                                            t[1] = grid[r + 1][c] + ORTOGONAL;
                                                          42
                                                                            t[0] = grid[r + 1][c + 1] + DIAGONAL
          bool anyChange = true;
          int counter = 0;
                                                          43
                                                                            t[3] = grid[r][c + 1] + ORTOGONAL;
  10
          while (anyChange) {
                                                          44
                                                                            t[2] = grid[r + 1][c - 1] + DIAGONAL
  11
             anyChange = false;
                                                                            double pom = grid[r][c];
             for (int r = 1; r < H - 1; r++) {
                                                          46
                                                                            bool s = false;
  13
                                                          47
                for (int c = 1; c < W - 1; c++) {
                                                                            for (int i = 0; i < 4; i++) {
                    if (map[r][c] != FREESPACE) {
                                                          48
                                                                               if (pom > t[i]) {
  15
                       continue;
                                                                                  pom = t[i];
  16
                    } //obstacle detected
                                                                                  s = true;
                    double t[4];
  17
                    t[0] = grid[r - 1][c - 1] + DIAGONAL;
  19
                    t[1] = grid[r - 1][c] + ORTOGONAL;
                                                                            if (s) {
  20
                    t[2] = grid[r - 1][c + 1] + DIAGONAL; 54
                                                                               anyChange = true;
  21
                    t[3] = grid[r][c - 1] + ORTOGONAL;
                                                          55
                                                                               grid[r][c] = pom;
                    double pom = grid[r][c];
  22
                                                          56
  23
                    for (int i = 0; i < 4; i++) {</pre>
                                                          57
  24
                       if (pom > t[i]) {
                                                          58
  25
                          pom = t[i];
                                                          59
                                                                      counter++:
  26
                          anyChange = true;
                                                          60
                                                                   } //end while any change
  27
                                                          61
                                                                   return grid;
  28
                                                          62
  29
                    if (anyChange) {
  30
                       grid[r][c] = pom;
  31
  32
  33
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```

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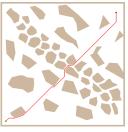
Distance Transform based Path Planning – Impl. 2/2

■ The path is retrived by following the minimal value towards the goal using min8Point()

```
Coords& min8Point(const Grid& grid, Coords& p)
                                                              CoordsVector& DT::findPath(const Coords& start,
 2
                                                                    const Coords& goal, CoordsVector& path)
        double min = std::numeric_limits<double>::max(); 23
        const int H = grid.H;
                                                                 static const double DIAGONAL = sqrt(2);
        const int W = grid.W;
                                                                 static const double ORTOGONAL = 1:
                                                                 const int W = map.W;
        for (int r = p.r - 1; r \le p.r + 1; r++) {
                                                                 Grid grid(H, W, H*W); // H*W max grid value
                                                         29
                                                                 grid[goal.r][goal.c] = 0;
           if (r < 0 or r >= H) { continue; }
10
           for (int c = p.c - 1; c <= p.c + 1; c++) {
                                                        30
                                                                 compute(grid);
11
              if (c < 0 or c >= W) { continue; }
                                                         31
12
              if (min > grid[r][c]) {
                                                                 if (grid[start.r][start.c] >= H*W) {
13
                 min = grid[r][c];
                                                                    WARN("Path has not been found");
14
                                                                } else {
                 t.r = r; t.c = c;
15
                                                                    Coords pt = start;
16
                                                                    while (pt.r != goal.r or pt.c != goal.c) {
17
                                                                       path.push_back(pt);
                                                                       min8Point(grid, pt);
                                                         39
20
                                                                    path.push_back(goal);
                                                         41
                                                         42
                                                                 return path;
```

DT Example











 $\delta = 30$ cm. L = 42.8 m

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Graph Search Algorithms

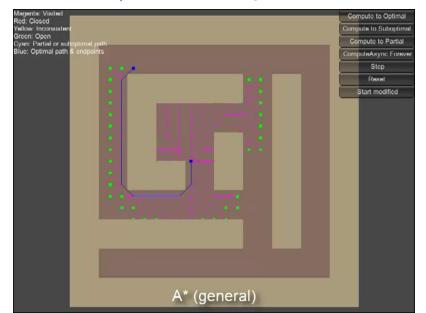
- The grid can be considered as a graph and the path can be found using graph search algorithms
- The search algorithms working on a graph are of general use, e.g.
 - Breadth-first search (BSD)
 - Depth first search (DFS)
 - Dijsktra's algorithm,
 - A* algorithm and its variants
- There can be grid based speedups techniques, e.g.,
 - Jump Search Algorithm (JPS) and JPS+
- There are many search algorithm for on-line search, incremental search and with any-time and real-time properties, e.g.,
 - Lifelong Planning A* (LPA*)

Koenig, S., Likhachev, M. and Furcy, D. (2004): Lifelong Planning A*. AlJ.

E-Graphs – Experience graphs

Phillips, M. et al. (2012): E-Graphs: Bootstrapping Planning with Experience Graphs. RSS.

Examples of Graph/Grid Search Algorithms



https://www.youtube.com/watch?v=X5a149nSE9s

Dijkstra's Algorithm

■ Dijsktra's algorithm determines paths as iterative update of the cost of the shortest path to the particular nodes

Let start with the initial cell (node) with the cost set to 0 and update all successors

- Select the node
 - with a path from the initial node
 - and has a lower cost
- Repeat until there is a reachable node
 - I.e., a node with a path from the initial node ■ has a cost and parent (green nodes).

The cost of nodes can only decrease (edge cost is positive). Therefore, for a node with the currently lowest cost, there cannot be a shorter path from the initial node.

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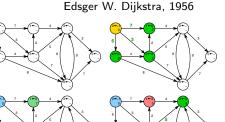
Grid-based Planning

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Graph Search Algorithms

1: After the expansion, the shortest path to the 2: There is not shorter path to the node 2 over the

Example (cont.)



3: After the expansion, there is a new path to the node 5 Jan Faigl, 2017

node 2 is over the node 3

4: The path does not improve for further

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D* Lite

Dijkstra's Algorithm – Impl.

```
1 dij->nodes[dij->start_node].cost = 0; // init
   void *pq = pq_alloc(dij->num_nodes); // set priority queue
   int cur_label;
   pq_push(pq, dij->start_node, 0);
   while ( !pq_is_empty(pq) && pq_pop(pq, &cur_label)) {
       node_t *cur = &(dij->nodes[cur_label]); // remember the current node
       for (int i = 0; i < cur->edge_count; ++i) { // all edges of cur
          edge_t *edge = &(dij->graph->edges[cur->edge_start + i]);
          node_t *to = &(dij->nodes[edge->to]);
          const int cost = cur->cost + edge->cost;
10
          if (to->cost == -1) { // node to has not been visited
11
12
             to->cost = cost:
             to->parent = cur_label;
13
             pq_push(pq, edge->to, cost); // put node to the queue
14
         } else if (cost < to->cost) { // node already in the queue
15
16
             to->cost = cost; // test if the cost can be reduced
             to->parent = cur_label; // update the parent node
17
             pq_update(pq, edge->to, cost); // update the priority queue
18
19
       } // loop for all edges of the cur node
      // priority queue empty
   pq_free(pq); // release memory
```

A* Algorithm

Grid-based Planning

- A* uses a user-defined h-values (heuristic) to focus the search Peter Hart, Nils Nilsson, and Bertram Raphael, 1968
 - Prefer expansion of the node n with the lowest value

DT for Path Planning

$$f(n) = g(n) + h(n),$$

where g(n) is the cost (path length) from the start to n and h(n)is the estimated cost from n to the goal

- h-values approximate the goal distance from particular nodes
- Admissibility condition heuristic always underestimate the remaining cost to reach the goal
 - Let $h^*(n)$ be the true cost of the optimal path from n to the goal
 - Then h(n) is admissible if for all n: $h(n) \le h^*(n)$
 - E.g., Euclidean distance is admissible
 - A straight line will always be the shortest path
- Dijkstra's algorithm h(n) = 0

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A* Implementation Notes

- The most costly operations of A* are
 - Insert and lookup an element in the closed list
 - Insert element and get minimal element (according to f() value) from the open list
- The closed list can be efficiently implemented as a hash set
- The open list is usually implemented as a priority queue, e.g.,
 - Fibonacii heap, binomial heap, k-level bucket
 - **binary heap** is usually sufficient (O(logn))
- Forward A*
 - 1. Create a search tree and initiate it with the start location
 - 2. Select generated but not yet expanded state s with the smallest f-value, f(s) = g(s) + h(s)
 - 3. Stop if s is the goal
 - 4. Expand the state s
 - 5. Goto Step 2

Similar to Dijsktra's algorithm but it used f(s) with heuristic h(s) instead of pure g(s)

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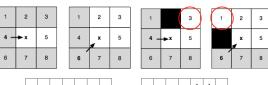
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Jump Point Search Algorithm for Grid-based Path Planning

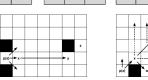
■ Jump Point Search (JPS) algorithm is based on a macro operator that identifies and selectively expands only certain nodes (jump points)

Harabor, D. and Grastien, A. (2011): Online Graph Pruning for Pathfinding on Grid Maps. AAAI.

 Natural neighbors after neighbor prunning with forced neighbors because of obstacle



■ Intermediate nodes on a path connecting two jump points are never expanded



■ No preprocessing and no memory overheads while it speeds up A*

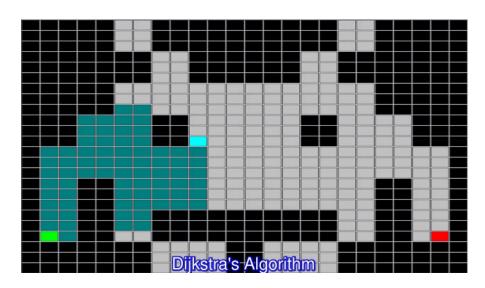
https://harablog.wordpress.com/2011/09/07/jump-point-search/

■ JPS+ – optimized preprocessed version of JPS with goal bounding

https://github.com/SteveRabin/JPSPlusWithGoalBounding

http://www.gdcvault.com/play/1022094/JPS-Over-100x-Faster-than

Dijsktra's vs A* vs Jump Point Search (JPS)



https://www.youtube.com/watch?v=ROG4Ud081LY

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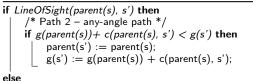
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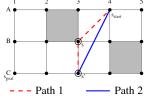
Theta* - Any-Angle Path Planning Algorithm

- Any-angle path planning algorithms simplify the path during the search
- Theta* is an extension of A* with LineOfSight()

Nash, A., Daniel, K, Koenig, S. and Felner, A. (2007): Theta*: Any-Angle Path

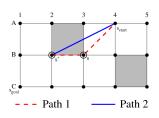
Algorithm 2: Theta* Any-Angle Planning





/* Path 1 - A* path */ if g(s) + c(s,s') < g(s') then parent(s') := s;g(s') := g(s) + c(s,s');

■ Path 2: considers path from start to parent(s) and from parent(s) to s' if s' has line-of-sight to parent(s)

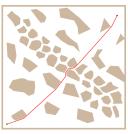


http://aigamedev.com/open/tutorials/theta-star-any-angle-paths/

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Theta* Any-Angle Path Planning Examples

■ Example of found paths by the Theta* algorithm for the same problems as for the DT-based examples on Slide 16





Both algorithms implemented in C++



$$\delta=$$
 30 cm, $L=$ 40.3 m

The same path planning problems solved by DT (without path smoothing) have $L_{\delta=10}=27.2$ m and $L_{\delta=30}=42.8$ m, while DT seems to be faster

■ Lazy Theta* – reduces the number of line-of-sight checks

Nash, A., Koenig, S. and Tovey, C. (2010): Lazy Theta*: Any-Angle Path Planning and Path Length Analysis in 3D. AAAI.

http://aigamedev.com/open/tutorial/lazy-theta-star/

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Real-Time Adaptive A* (RTAA*)

- Execute A* with limited lookahead
- Learns better informed heuristic from the experience, initially h(s), e.g., Euclidean distance
- Look-ahead defines trade-off between optimality and computational cost
 - astar(lookahead)

A* expansion as far as "lookahead" nodes and it terminates with the state s'

while $(s_{curr} \notin GOAL)$ do astar(lookahead); if s' = FAILURE then return FAILURE; for all $s \in CLOSED$ do H(s) := g(s') + h(s') - g(s);execute(plan); // perform one step

return SUCCESS:

s' is the last state expanded during the previous A* search

A* Variants - Online Search

- The state space (map) may not be known exactly in advance
 - Environment can dynamically change
 - True travel costs are experienced during the path execution
- Repeated A* searches can be computationally demanding
- Incremental heuristic search
 - Repeated planning of the path from the current state to the goal
 - Planning under the **free-space** assumption
 - Reuse information from the previous searches (closed list entries):
 - Focused Dynamic A* (D*) h^* is based on traversability, it has been used, e.g., for the Mars rover "Opportunity"

Stentz, A. (1995): The Focussed D* Algorithm for Real-Time Replanning. IJCAI.

■ D* Lite - similar to D*

Koenig, S. and Likhachev, M. (2005): Fast Replanning for Navigation in Unknown Terrain. T-RO

Real-Time Heuristic Search

- Repeated planning with limited look-ahead suboptimal but fast
 - Learning Real-Time A* (LRTA*)

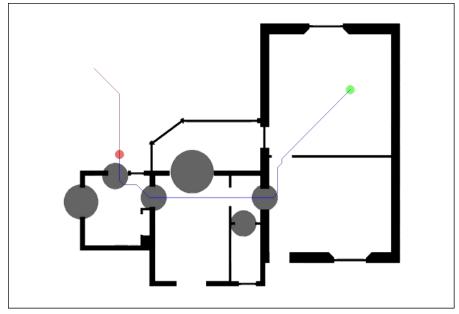
Korf, E. (1990): Real-time heuristic search. JAI

Real-Time Adaptive A* (RTAA*)

Koenig, S. and Likhachev, M. (2006): Real-time adaptive A*. AAMAS.

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D* Lite - Demo



https://www.youtube.com/watch?v=X5a149nSE9s

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D* Lite Overview

■ It is similar to D*, but it is based on Lifelong Planning A*

Koenig, S. and Likhachev, M. (2002): D* Lite. AAAI.

- It searches from the goal node to the start node, i.e., g-values estimate the goal distance
- Store pending nodes in a priority queue
- Process nodes in order of increasing objective function value
- Incrementally repair solution paths when changes occur
- Maintains two estimates of costs per node
 - g the objective function value based on what we know
 - rhs one-step lookahead of the objective function value based on what we know
- **■** Consistency
 - Consistent g = rhs
 - Inconsistent $g \neq rhs$
- Inconsistent nodes are stored in the priority queue (open list) for processing

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Grid-based Planning

DT for Path Planning

Graph Search Algorithms

D* Lite

Graph Search Algorithms

D* Lite

D* Lite Algorithm

■ Main – repeat until the robot reaches the goal $(or g(s_{start}) = \infty \text{ there is no path})$

```
Initialize():
ComputeShortestPath();
while (s_{start} \neq s_{goal}) do
    s_{start} = \operatorname{argmin}_{s' \in Succ(s_{start})}(c(s_{start}, s') + g(s'));
Move to s_{start};
Scan the graph for changed edge costs;
if any edge cost changed perform then
    foreach directed edges (u, v) with changed edge costs do
          Update the edge cost c(u, v);
         UpdateVertex(u);
    foreach s \in U do
         U.Update(s, CalculateKey(s));
     ComputeShortestPath();
```

Procedure Initialize

```
U = 0:
foreach s \in S do
     rhs(s) := g(s) := \infty;
rhs(s_{goal}) := 0;
U.Insert(s_{goal}, CalculateKey(s_{goal}));
```

D* Lite: Cost Estimates

■ rhs of the node u is computed based on g of its successors in the graph and the transition costs of the edge to those successors

$$rhs(u) = \min_{s' \in Succ(u)} (g(s') + c(u, s'))$$

■ The key/priority of a node s in the open list is the minimum of g(s) and rhs(s) plus a focusing heuristic h

$$[\min(g(s), rhs(s)) + h(s_{start}, s); \min(g(s), rhs(s))]$$

- The first term is used as the primary key
- The second term is used as the secondary key for tie-breaking

Grid-based Planning

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DT for Path Planning

D* Lite Algorithm - ComputeShortestPath()

```
Procedure ComputeShortestPath
while U.TopKey() < CalculateKey(s_{start}) OR rhs(s_{start}) \neq g(s_{start}) do
    u := U.Pop();
    if g(u) > rhs(u) then
         g(u) := rhs(u);
         foreach s \in Pred(u) do UpdateVertex(s);
         g(u) := \infty:
         foreach s \in Pred(u) \cup \{u\} do UpdateVertex(s);
```

Procedure UpdateVertex

```
if u \neq s_{goal} then rhs(u) := \min_{s' \in Succ(u)} (c(u, s') + g(s'));
if u \in U then U.Remove(u);
if g(u) \neq rhs(u) then U.Insert(u, CalculateKey(u));
```

Procedure CalculateKey

return $[\min(g(s), rhs(s)) + h(s_{start}, s); \min(g(s), rhs(s))]$

| Grid-based Planning | DT for Path Planning | Graph Search Algorithms | D* Lite | | | |
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