Expressive Description Logics

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Our plan

From \mathcal{ALC} to OWL(2)-DL

Final Remarks

From ALC to OWL(2)-DL



Extending $\dots \mathcal{ALC} \dots$

- We have introduced \mathcal{ALC} , together with a decision procedure. Its expressiveness is higher than propositional calculus, still it is insufficient for many practical applications.
- ullet Let's take a look, how to extend \mathcal{ALC} while preserving decidability.

Extending ... ALC ... (2)

 ${\cal N}$ (Number restructions) are used for restricting the number of successors in the given role for the given concept.

syntax (concept)	sema	ntics
$(\geq nR)$	$\left\{ a \right $	$\Big \{b\mid (a,b)\in R^{\mathcal{I}}\}\Big \geq n$
$(\leq nR)$	('	$\Big \{b\mid (a,b)\in R^{\mathcal{I}}\}\Big \leq n$
(= nR)	$\left\{ a\right $	$\Big \{b\mid (a,b)\in R^{\mathcal{I}}\}\Big =n$

- Concept $Woman \sqcap (\leq 3 hasChild)$ denotes women who have at most 3 children.
- What denotes the axiom $Car \sqsubseteq (\geq 4 \text{ hasWheel})$?
- ... and $Bicycle \equiv (= 2 hasWheel)$?



Extending ... ALC ... (3)

Q (Qualified number restrictions) are used for restricting the number of successors of the given type in the given role for the given concept.

syntax (concept)	semantics
(≥ n R C)	$\left\{ a \middle \left \left\{ b \mid (a,b) \in R^{\mathcal{I}} \wedge b^{\mathcal{I}} \in C^{\mathcal{I}} \right\} \right \geq n \right\}$
$(\leq nRC)$	$\left\{ a \middle \left \left\{ b \mid (a,b) \in R^{\mathcal{I}} \wedge b^{\mathcal{I}} \in C^{\mathcal{I}} \right\} \right \leq n \right\}$
(= n R C)	$\left\{ a \middle \left \left\{ b \mid (a,b) \in R^{\mathcal{I}} \wedge b^{\mathcal{I}} \in C^{\mathcal{I}} \right\} \right = n \right\}$

- Concept Woman \sqcap (\geq 3 hasChild Man) denotes women who have at least 3 sons.
- What denotes the axiom $Car \sqsubseteq (\geq 4 \text{ hasPart Wheel})$?
- ullet Which qualified number restrictions can be expressed in \mathcal{ALC} ? $\overline{\mbox{\tiny aboratory}}$

Extending ... ALC ... (4)

O (Nominals) can be used for naming a concept elements explicitely.

syntax (concept)	semantics
$\{a_1,\ldots,a_n\}$	$\{a_1^{\mathcal{I}},\ldots,a_n^{\mathcal{I}}\}$

- Concept {MALE, FEMALE} denotes a gender concept that must be interpreted with at most two elements. Why at most ?
- Continent ≡
 {EUROPE, ASIA, AMERICA, AUSTRALIA, AFRICA, ANTARCTICA}
 ?



$$\dots \mathcal{ALC} \dots (5)$$

 ${\cal I}$ (Inverse roles) are used for defining role inversion.

$$\begin{array}{ccc} \text{syntax (role)} & \text{semantics} \\ R^- & (R^{\mathcal{I}})^{-1} \end{array}$$

- Role maDite denotes the relationship maRodice.
- What denotes axiom $Person \sqsubseteq (= 2 hasChild^-)$?
- What denotes axiom $Person \sqsubseteq \exists hasChild \cdot \neg \exists hasChild \cdot \neg ?$



Extending ... ALC ... (6)

trans (Role transitivity axiom) denotes that a role is transitive.

Attention – it is not a transitive closure operator.

syntax (axiom)	semantics
trans(R)	$R^{\mathcal{I}}$ is transitive

- Role isPartOf can be defined as transitive, while role hasParent is not. What about roles hasPart, hasPart⁻, hasGrandFather⁻?
- What is a transitive closure of a relationship? What is the difference between a transitive closure of hasDirectBoss^I and hasBoss^I.



Extending ... ALC ...(7)

 ${\cal H}$ (Role hierarchy) serves for expressing role hierarchies (taxonomies) – similarly to concept hierarchies.

syntax (axiom)	semantics
$R \sqsubseteq S$	$R^{\mathcal{I}} \subseteq S^{\mathcal{I}}$

- Role hasMother can be defined as a special case of the role hasParent.
- What is the difference between a concept hierarchy
 Mother

 □ Parent and role hierarchy hasMother
 □ hasParent.



Extending ... ALC ... (8)

 ${\cal R}$ (role extensions) serve for defining expressive role constructs, like role chains, role disjunctions, etc.

syntax	semantics
$R \circ S \sqsubseteq P$	$R^{\mathcal{I}} \circ S^{\mathcal{I}} \sqsubseteq P^{\mathcal{I}}$
Dis(R,R)	$R^{\mathcal{I}}\cap \mathcal{S}^{\mathcal{I}}=\emptyset$
$\exists R \cdot \textit{Self}$	$\{a (a,a)\in R^{\mathcal{I}}\}$

- How would you define the role hasUncle by means of hasSibling and hasParent?
- how to express that R is transitive, using a role chain?
- Whom does the following concept denote Person □ ∃likes · Self ?



Extending ... ALC ... – OWL-DL a OWL2-DL

- From the previously introduced extensions, two prominent decidable supersets of \mathcal{ALC} can be constructed:
 - \mathcal{SHOIN} is a description logics that backs OWL-DL.
 - SROIQ is a description logics that backs OWL2-DL.
 - Both OWL-DL and OWL2-DL are semantic web languages they extend the corresponding description logics by:
 - syntactic sugar axioms NegativeObjectPropertyAssertion, AllDisjoint, etc.
 - extralogical constructs imports, annotations data types XSD datatypes are used



Extending ALC – Reasoning

- What is the impact of the extensions to the automated reasoning procedure? The introduced tableau algorithm for ALC has to be adjusted as follows:
 - additional inference rules reflecting the semantics of newly added constructs $(\mathcal{O}, \mathcal{N}, \mathcal{Q})$
 - definition of *R-neighbourhood* of a node in a completion graph. R-neighbourhood notion generalizes simple tests of two nodes being connected with an edge, e.g. in \exists -rule. $(\mathcal{H}, \mathcal{R}, \mathcal{I})$
 - new conditions for direct clash detection
 - more strict blocking conditions (blocking over graph structures).
- ullet This results in significant computation blowup from EXPTIME (\mathcal{ALC}) to
 - NEXPTIME for \mathcal{SHOIN}
 - N2EXPTIME for SROIQ

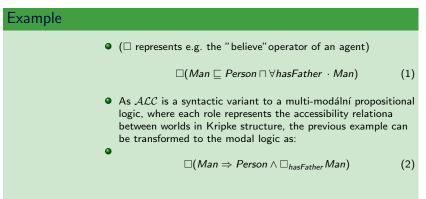


Final Remarks



Other extensions

Modal Logic introduces *modal operators* – possibility/necessity, used in multiagent systems.



Vague Knowledge - fuzzy, probabilistic and possibilistic extensions (see [HPS05]).

Data Types (\mathcal{D}) allow integrating a data domain (numbers, strings), e.g. $Person \sqcap \exists hasAge \cdot 23$ represents the concept describing "23-years old persons".

DL Tools and Reasoners

- RacerPro (http://www.racer-systems.com) is a commercial LISP-based system for OWL-DL and SWRL (also available in client/server version).
 - Pellet (http://www.mindswap.org) is an open-source Java OWL2-DL engine.
 - Jena http://jena.sourceforge.net/ is an open-source Java framework and API for OWL and RDF(S).
- FaCT++ http://owl.man.ac.uk/factplusplus/ is a DL reasoner for \mathcal{SHOIQ} written in C++.
- and other ... KAON2, FOWL, Kris

