

Neuroinformatics — lab exercises manual

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Abstract

This is supportive text for labs of Neuroinformatics course at Czech Technical University in Prague, Faculty of Electrical Engineering. Exercises for each task are provided in Matlab language.

We further recommend the book [3], which is nice and easy to read. A good summary is provided by [1]. Particular topics are covered by [2], [4] Some advanced material is covered by [2], [4].

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0 Mathematical apparatus

We will introduce numerical apparatus, which will be applied during activity modelling of neurons.

0.1 Numerical solution of differential equations

As in other fields dealing with dynamic systems, we will use differential equations throughout this course. Due to the fact that their exact analytical solution can often be difficult or even impossible to obtain, we introduce the approximate numerical solutions in this exercise.

Euler's method

Let's consider the first order differential equation

$$\frac{\delta x}{\delta t} = f(x, t), \quad (0.1)$$

Euler's first order method consist of discretization $\frac{\delta x}{\delta t} = \frac{\Delta x}{\Delta t}$. Lets' take:

$$\begin{aligned} \Delta x &= x(t + \Delta t) - x(t) = x(t_2) - x(t) \\ \Delta t &= t_2 - t, \end{aligned}$$

then we can express eq (0.1) as

$$\frac{\Delta x}{\Delta t} = f(x(t), t)$$

finally

$$x(t + \Delta t) = x(t) + \Delta t f(x(t), t)$$

We can approximate the solution by taking into account the slope of the line at that point. However, if the slope is dependent on t , this will lead to a very rough approximation. In this case, we can refine the solution by other parameters of the Taylor series according to the formula:

$$x(t + \Delta t) = x(t) + \Delta t \frac{\delta x}{\delta t} + \frac{1}{2} (\Delta t)^2 \frac{\delta^2 x}{\delta t^2} + O, \quad (0.2)$$

where O represents all members of the higher orders. Therefore, the second order model is extended by the curvature (2nd order derivative). This approximation should be closer to the analytical solutions.

Runge-Kutta method

In more sophisticated methods, we can additionally refine the solution by estimation not in the point x or $x + \Delta x$, but in the middle of this interval - the so-called „*midpoint method*“. The resulting value should be more representative and lead to a more accurate estimate. Moreover, if we do not have analytical expression of parameters of the Taylor expansion of higher orders, we can again estimate parameters of high orders using numerical methods.

The actual Runge-Kutta method for numerical integration is the 4th order, which combines estimation in the middle of the interval with a numerical estimate of higher order. It can therefore approximate solution of arbitrary functions. This leads to a higher computational cost, but - as we shall see - leads to very accurate estimates of the solution. Runge-Kutta method is implemented in Matlab function `ode45()`.

Exercise 0.1 Our task is numerical approximation of the following differential equation

$$\frac{dx}{dt} = t - x + 1, \quad (0.3)$$

initial conditions: $x(0) = 1$ using Euler's method (1 and 2 order) and Runge-Kutta methods.

The analytical solution of this equation has the form $x = t + e^{-t}$ ¹. Solve the equation in the interval (0, 5), choose $\Delta t = 0.02$.

¹You can check e.g. at <http://www.wolframalpha.com/>, question: „solve differential equation x '= ... “

Task 0.1 (2 b) Plot the solution $x(t) = f(t)$ for $t = 0, \dots, 2s$ using Euler's method of first and second order ² (X_{Euler}) and plot into graph along with the analytical solution.

Task 0.2 (1 b) Solve the task using Runge-Kutta x_{Runge} and add the solution to the same graph.

Hints: in the function `ode45`, the first parameter is a callback function, which describes the equation to be solved. In this case the callback can be easily defined using so called *function handle* and *anonymous function*³ as `ode_func = @(t,x,flag) 1-x+t;`

Task 0.3 (1.5 b) Plot the dependence of relative error of each numerical method and compare it to the analytical solution. For example (for Euler's method) $(x_{Euler} - x_{exact})/x_{Euler} = f(\Delta t)$

Task 0.4 (1.5 b) Plot absolute error of each numerical method as a function of the size of the integration step $\Delta t \in (0.001, 1)s$ in time $t = 1s$.

²when solving the second order Euler method you can proceed in two ways. 1) Derivating analytic function $f(x, t)$.
2) estimate value of $f'(x, t)$ using the slope $f(x, t)$ between points t and $t + Deltat$

³see for example. http://www.mathworks.com/help/matlab/matlab_prog/creating-a-function-handle.html

1 Neuron models

In this block, we will describe properties of the action potential and behavior of individual neurons. We will implement several membrane and neuron models of differing level of complexity and investigate how the simplifying assumptions affect the resulting action potentials or spike-trains.

1.1 Model of membrane and synapse: simplest case

Considering that the action potentials propagate as changes in electrical potential on the cell membrane, it seems natural to model the membrane as an equivalent electrical circuit. The simplest model that we introduce in this exercise works with single type of ion channels only - the leakage chloride channels (always open) - and consists of an RC circuit and a voltage power source, representing the membrane resting potential (*Nernst potential*). As we shall see, its response to the input excitation represents only a part of the true membrane behavior and is far away from the the real action potential but we can still find it useful in understanding the basic concept and properties of the membrane itself.

Exercise 1.1 (RC model) Model memrabe behavior using RC model - see figure 1. Input membrane current I_{stim} is a rectangular pulse signal $10pA$ lasting $20ms$. It is necessary to convert the stimulation current I_{stim} to current density to be compatible with I_{Cl} and I_C . This can be done easily by dividing the input current by membrane area A^4 . The electrode is stimulating and at the same time recording the membrane current (expressed in cm^2). Hence $I'_{stim} = I_{stim}/A \approx 10^{-11} \cdot 10^6 \approx 10^{-5}$. The membrane parameters are the following:

- capacity: $C_m = 1 \mu F/cm^2$,
- conductance: $g_{Cl} = 0.3 ms/cm^2$,
- time constant : $\tau = C_m/g_{Cl}$,
- membrane surface : $A \approx 1 \cdot 10^{-6} cm^2$
- Nernst potential of Cl: $V_{Cl} = -68 mV$,
- initial conditions: $V(0) = -68 mV$, $I_{Cl}(0) = 0 \mu A/cm^2$, $I_C(0) = 0 \mu A/cm^2$.

Task 1.1 (4 b) Plot dependence $V(t)(= \phi_{in} - \phi_{out})$, $I_{Cl}(t)$, $I_C(t)$ for these time interval $(0, 40)ms$, $\Delta t = 0.01ms$

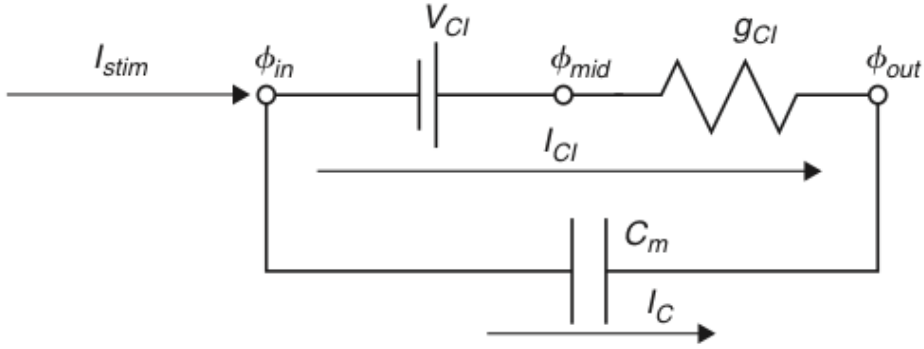


Figure 1: Membrane model with Cl leakage channel

Hence

$$I_C(t) = C_m \frac{dV}{dt}(t) \tag{1.1}$$

$$I_C(t) = \frac{I_{stim}(t)}{A} - I_{Cl}(t) \quad \rightarrow I_{stim} = A \cdot I_C(t) + A \cdot I_{Cl}(t) \tag{1.2}$$

$$I_{Cl}(t) = g_{Cl}(V(t) - V_{Cl}) \tag{1.3}$$

⁴ I_{Cl} and I_C are in fact current densities and it would be more appropriate to use ρ instead of I . However, we will stick to the terminology used in [3] and use I .

We can express the time constant of the RC circuit as

$$\tau = \frac{C_m}{g_{Cl}} \quad (1.4)$$

Combining the above equations we get

$$C_m \frac{dV}{dt} = \frac{I_{stim}(t)}{A} - g_{Cl}(V(t) - V_{Cl}) \quad (1.5)$$

Or expressed using time constant τ from 1.4 we get

$$\tau \frac{dV}{dt} = V_{Cl} - V(t) + \frac{I_{stim}(t)}{Ag_{Cl}} \quad (1.6)$$

Euler's method (forward)

$$\tau \frac{V(j) - V(j-1)}{\Delta t} = V_{Cl} - V(j-1) + \frac{I_{stim}(j-1)}{Ag_{Cl}} \quad (1.7)$$

$$V(j) = V(j-1) + \frac{\Delta t}{\tau} [V_{Cl} - V(j-1) + \frac{I_{stim}(j-1)}{Ag_{Cl}}] \quad (1.8)$$

Exercise 1.2 (EPSP model) The task is analysis of a model depicted in figure 2. This model incorporates so called „excitatory postsynaptic potential“ (EPSP) simulating behavior of membrane dendrite of the postsynaptic neuron after receiving excitation. Synapse is modeled by variable conductance g_{syn} . In other words: the model contains additional channels, whose conductance is neurotransmitter-controlled and further voltage and time-dependent (literally in the moment of receiving neurotransmitter the channels are opening, hence their conductance is increasing - see result of eq (1.9)) with time constant $\tau_{syn} = 1 \text{ mS}$. The parameters are the same like in the previous case. Stimulation current $I_{stim} = 0$, $V_{syn} = 10 \text{ mV}$. In time $t = 1 \text{ ms}$ the neurotransmitter is released, hence $g_{syn}(1 + \delta) = 1$. Initial conditions $V(1) = 0$, $I_{syn} = 0$, $g_{syn}(1) = 0$, $g_L = 1$.

$$\tau_{syn} \frac{dg_{syn}(t)}{dt} = -g_{syn}(t) + \delta(t - t_{pre} - t_{delay}) \quad (1.9)$$

Task 1.2 (1 b) Plot dependence $V(t)$, $I_{Cl}(t)$, $I_C(t)$, $I_{syn}(t)$. Explain trends and compare them with the previous task 1.1.

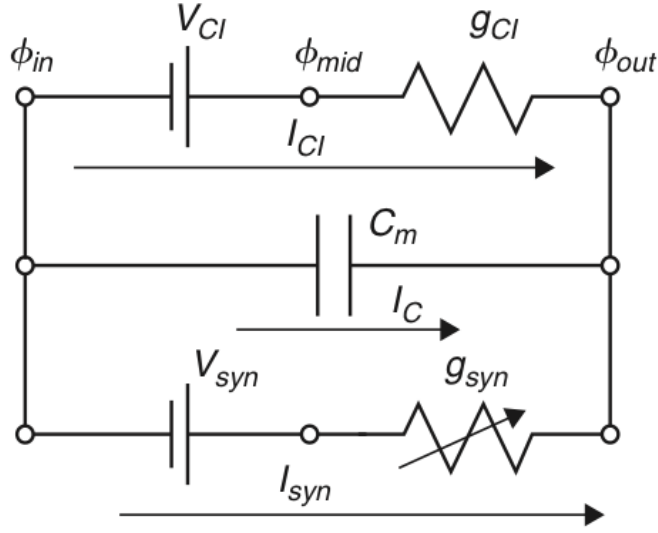


Figure 2: EPSP: Synapse model with leakage Cl channel

1.2 Membrane and synapse modelling 2: Hodgkin-Huxley

Exercise 1.3 (Hodgkin-Huxley) The main aim of this exercise is analysis of the Hodgkin-Huxley(HH) model depicted in Figure 3. Compared to the previous models, HH incorporates ion channels whose conductivity is dependent on both time and voltage: the Na^+ a K^+ channels. The model is based on the following set of equations:

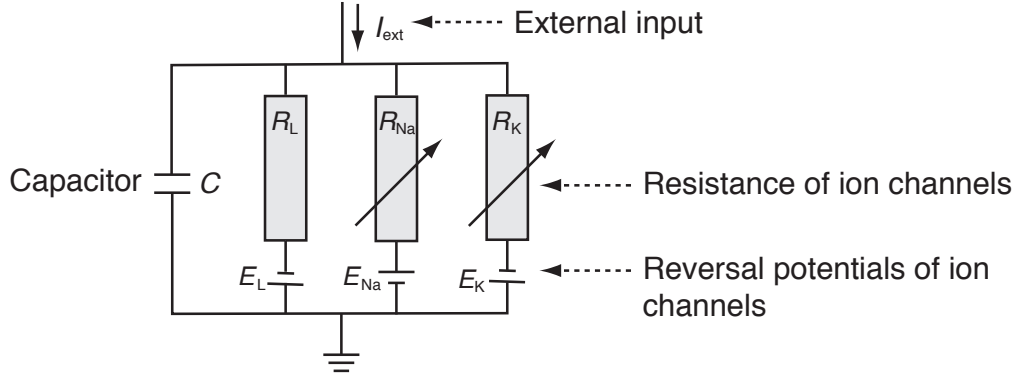


Figure 3: Hodgkin-Huxley model. Each branch represents resting potential and resistivity of a particular channel: E_L, R_L – always open channels („Leakage channels“), E_{Na}, R_{Na} – voltage-controlled sodium channels, E_K, R_K – voltage-controlled calcium channels.

Current through ion channels can be described by Ohm's law:

$$I_{ion} = \hat{g}_{ion}(V - E_{ion}) \quad \left(= (V - E_{ion}) / \hat{R}_{ion} \right), \quad (1.10)$$

where \hat{g}_{ion} is the maximum conductance of ion channel

Next, we introduce auxiliary variables dependent on voltage and time $n(V, t)$, $m(V, t)$, $h(V, t)$, resulting in the following conductances:

$$\hat{g}_K(V, t) = g_K n^4 \quad (1.11)$$

$$g_{\hat{N}a}(V, t) = g_{Na} m^3 h \quad (1.12)$$

Combining eq.1.12-1.10 we get

$$C \frac{dV}{dt} = -g_K n^4 (V - E_K) - g_{Na} m^3 h (V - E_{Na}) - g_L (V - E_L) + I_{ext}(t) \quad (1.13)$$

Next, we define time constants

$$\tau_n(V) \frac{dn}{dt} = -[n - n_0(V)] \quad (1.14)$$

$$\tau_m(V) \frac{dm}{dt} = -[m - m_0(V)] \quad (1.15)$$

$$\tau_h(V) \frac{dh}{dt} = -[h - h_0(V)] \quad (1.16)$$

For each variable we get

$$\frac{dx}{dt} = -\frac{1}{\tau_x(V)} [x - x_0(V)], \quad x \in \{n, m, h\} \quad (1.17)$$

and after substituting Euler's numerical integration we get

$$x(t + \Delta t) = \left(1 - \frac{\Delta t}{\tau_x}\right) x(t) + \frac{\Delta t}{\tau_x} x_0. \quad (1.18)$$

Under the initial conditions:

$$x(0) = \frac{\alpha}{\alpha + \beta}, \quad \tau_x = \alpha\beta, \quad x \in \{n, m, h\} \quad (1.19)$$

$$\alpha_n = \frac{10 - V}{100 \left(e^{\frac{10-V}{10}} - 1\right)}, \quad \beta_n = 0.125e^{-\frac{V}{80}} \quad (1.20)$$

$$\alpha_m = \frac{25 - V}{10 \left(e^{\frac{25-V}{10}} - 1\right)}, \quad \beta_m = 4e^{-\frac{V}{8}} \quad (1.21)$$

$$\alpha_h = 0.07e^{\frac{V}{20}}, \quad \beta_h = \frac{1}{e^{\frac{30-V}{10}} + 1} \quad (1.22)$$

Task 1.3 (0 b) Download model implementation file `cv3_HH.m` from course website. Visualize time output of the model (membrane voltage V), which is stimulated by constant current $I_{ext} = 30 \mu A/cm^2$ (default settings). The simulation starts at time $-30ms$ to get steady system. Plot output for time $0 - 100ms$.

Task 1.4 (1 b) Expand the visualization by adding time trend of conductance g for each channel type (describe different time series using `legend`)

Task 1.5 (2 b) Visualize dependence of firing frequency on external constant current I_{ext} - so called *activation or transfer function*. Set the input current I_{ext} in the range $0 - 15 \mu A/cm^2$. To obtain the result, compute the firing frequency after reaching the steady state (hint: use `fce diff`, `find alt`, `findpeaks`). What shape does the activation function resemble? For which values of the current I_{ext} will the shape of the activation function change significantly (discuss the result)?

Task 1.6 (2 b) Adding noise to the input current will change behaviour of the model. Visualize the membrane voltage V and activation function as a response to input current with added noise. Use $I_{ext} = 30 \mu A/cm^2$ and white noise (`randn`) with standard deviation 60 and zero mean. For plotting activation function use $I_{ext} = \langle 0, 15 \rangle \mu A/cm^2$, noise with standard deviation 30. How did the resulting output change? Try out for different noise levels.

Task 1.7 (1 b) Plot ISI histogram for the input current $I_{ext} = 30 \mu A/cm^2$ and noise with standard deviation 60. Compare to the case with zero noise and discuss the results.

1.3 Spike train modelling

We showed in the previous tasks, how does noise on the input affect temporal and frequency characteristics of a neuron. Noise signal on neuron input is much more realistic than constant current - mainly due to the fact that neuron input is formed by a summary signal from many synapses of pre-synaptic neurons, connected to its dendrites. In this section, we will simulate such signal and use it as input to a neuron model.

You have learned in the lectures, that interspike intervals (ISI) of typical cortical neurons exhibit log-normal distribution. Before we start modelling spiketrains, let us verify this on a model.

Exercise 1.4 (LIF neuron model and Poisson spiketrain) The complex models from previous exercises, such as Hodgkin-Huxley, are able to model the action potential shape based on physiological modelling of ion channels' behavior. If we want to model more complex neural networks, even simpler models (such as Wilson model) are overly complex for such application. When modelling neural networks, the accurate shape of action potential is not as important (we will see it can be simply modelled using α functions) as the spike timing. For these purposes, the *Leaky integrate and fire* neuron is often used. The basics of this model includes simple integrator, which is reset to resting potential when a preset threshold is exceeded.

Task 1.8 (1 b) Download LIF model from the course website - `cv4_lif.m`. Show model output for constant input current (default setting). Plot output voltage, along with spike times (= reset times) over time. Compute firing rate and display an ISI histogram.

Task 1.9 (2 b) Modify previous task by applying input noise with mean 12 and standard deviation 100, instead of constant current (function `randn`). Simulate for times in the range $0 - 10^5$ and integration step $dt = 0.01$. Set bin number to 60 when computing histograms. Convert histograms to probability density function estimates ($\sum pdf = 1$).

Task 1.10 (2 b) Fit lognormal distribution to the data from the previous task. The lognormal distribution is given by:

$$pdf^{lognormal}(x; \mu, \sigma) = \frac{1}{x\sigma\sqrt{2\pi}} e^{-\frac{(\log(x)-\mu)^2}{2\sigma^2}} \quad (1.23)$$

One possible solution would be to fit the analytical pdf to ISI histogram from the previous task. This, however, would be completely wrong, as one point in the histogram does not mean one, but many data points (think about this for a while!).

Thus, we will use the function `lognfit`, which estimates lognormal distribution parameters using maximum likelihood estimates. Based on these estimates, calculate the lognormal pdf and display along with the histogram. (You will probably have to adjust the bin number to get a good representation)

2 Real data analysis, modelling of neuronal populations

In this block, we will analyze real μEEG (*micro-EEG*) data, recorded from brains of Parkinson's disease patients. We will compare the data to our simulations from the previous block and we will analyze correlation with other biosignal - the electrooculogram (EOG).

Further on in this section, we will simulate more complicated network of artificial neurons and (so called *spiking network*) and analyze its behavior under varying conditions.

2.1 Spiketrain modelling II

Exercise 2.1 (Lognorm spiketrain) We showed in the last exercise how does LIF neuron model respond to a noisy input. In this task, we will show that a more representative signal, produced as a combination of presynaptic potentials, really resembles gaussian noise in many ways.

You know from the lectures, that the *Poisson spiketrain*, - a spiketrain where the number of events per unit time follows poisson distribution - has exponential distribution of interspike intervals (ISIs). Further, the physiological constraints prevent neurons from firing earlier than after the *refractory period* - a fact we have to incorporate in our implementation.

In this example, we will generate a set of spiketrains using exponential distribution, taking refractory period into account, and mix them to create an artificial *muEEG* signal.

Task 2.1 (1 b) Generate 100 000 ISI intervals from the exponential distribution with mean $E[X] = 50ms$ (hint: use `expnrnd` function). Display ISI histogram.

Remove all ISI values lower than the refractory period of 1ms. Display ISI histogram and compare to the one before refractory period filtering. How many spikes were removed? Compute mean firing rate and coefficient of variation before and after filtering and compare.

Convert the resulting ISI intervals to a spiketrain (logical vector with ones at spike positions hint: `cumsum`). Use time step of $dt = 0.1ms$. Check for errors by plotting the result

Task 2.2 (2 b) To convert binary spiketrain to time course, we will use convolution with α -function, which will play the role of a post-synaptic spike template.

Generate time course of the α -function according to:

$$I(t) = c \cdot t \cdot e^{-\frac{t}{t_{peak}}} \quad (2.1)$$

$$c = \frac{g_{peak}}{t_{peak}} e^{-1} \quad (2.2)$$

where $g_{peak} = 0.5$, $t_{peak} = 1ms$. Compute the function values for times in the interval $t \in \langle 0, 30 \rangle$, the time step should be again $dt = 0.1ms$. Plot the output. After assessing the result, you may reduce the time range if appropriate.

Convolve the alpha function with Poisson spiketrain from the previous task (`conv`). Check the result again by plotting.

Task 2.3 (2 b) Divide the time course from previous task into 1000 signals of the same length (`reshape`). In this task, we will simulate mixing of presynaptic potentials (represented by the simulated neurons), at dendrites. The resulting summary signal will be given by a linear combination of the individual spiketrains. Coefficients will be given by weights w , which will be modelled as random from exponential distribution with $\lambda = 1$.

In order to have better control of the amplitude of the resulting signal, we will normalize the weights so that their sum equals a constant k . Set the value $k = 100$.

Combine the 1000 spiketrains into one signal, using a linear combination with weights w . You can represent the linear combination as matrix multiplication (elegant + much faster in Matlab).

Compare the resulting signal to gaussian noise (time and distribution). What are the key differences?

Task 2.4 (1 b) Apply the signal from previous task to the input of LIF neuron from Exercise and observe the output. What changes do you observe when you change the normalizing constant $k = 150$. What does the ISI histogram look like, now? Investigate and comment behavior of the LIF neurin.

2.1.1 Artificial and real signal - comparison

We have now generated artificial signal as a combination of Poisson spiketrains, convoluted with alpha function. In these tasks, we will compare the simulated signal to real μEEG , recorded from basal ganglia of a Parkinson's disease patient during deep brain surgery. We will show, that this simple method of data generation is not far from reality.

Task 2.5 (1 b) Use artificial signal generated in the previous task. It is a time course with sampling rate $f_s = 10kHz$. Download μEEG data from the course website. The .mat file contains variable `realmEEG` with 1s recording of activity around Thalamus ($f_s = 24kHz$). Display both signals in parallel plots (with correct time coordinates). Investigate both signals.

Task 2.6 (1 b) The real signal, used in the previous task, was an extracellular recording. Conversely, the signal we generated was a simulation of EPSP signal (that is why we used the alpha function)! In this task, we will generate artificial extracellular signal in a similar way. Use real spike shapes, downloaded from the course website instead of the alpha function. There are 5 spike shapes in the data sample - use random spike shape and random amplitude for each simulated neuron. In your simulation, use same sampling frequency as in the real signal, i.e. $f_s = 24kHz$. Generate the composite signal and compare it to the real microelectrode recording.

Task 2.7 (2 b) From visual comparison of time courses of real and simulated data, we get a rough idea of how similar these two signals are. Your next task is to try out some quantitative comparisons. Choose and implement appropriate methods of signal comparison. You can use e.g.: frequency spectrum, amplitude distribution etc.

2.2 Real data processing: Spike sorting

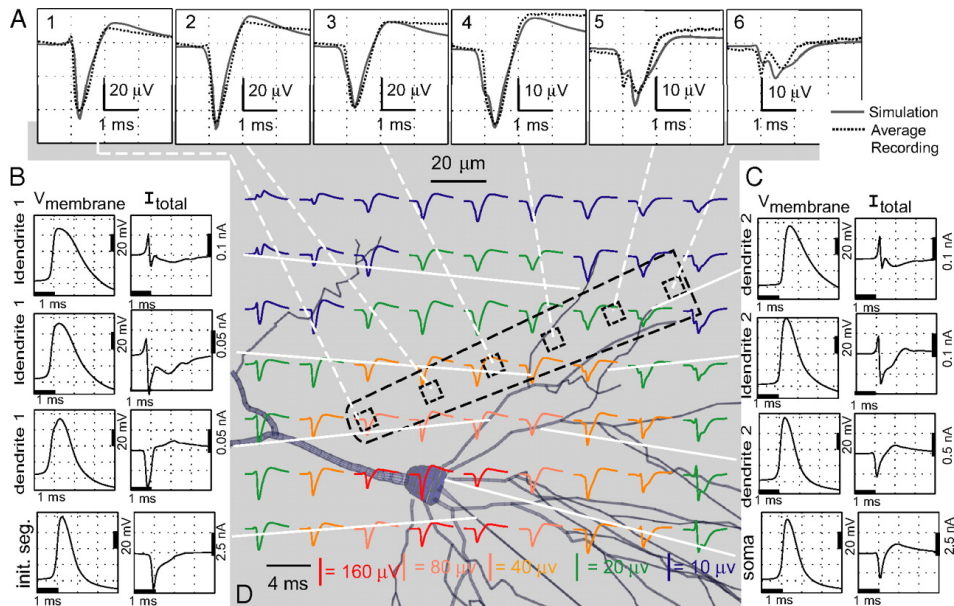
Exercise 2.2 (Spike sorting) In this exercise we will focus on spike detection and spike sorting (i.e.) in real μ EEG data.

Spikes and background noise

The real μ EEG data we will use in this exercise were recorded using microelectrodes placed in the brain of patients suffering from Parkinson's disease, specifically in the area of the thalamus. As we know, the recorded signal consists of activity of a large number of neurons in the vicinity of the electrodes - this is source of a background noise⁵ - from which we can get an approximate idea of the activity of the population in the area. However, we are usually interested in neurons in the vicinity of the electrode - here we can recognize individual action potentials of individual neurons and thus accurately analyze their activity. The recorded AP's (*spikes*) from near neurons have higher amplitude and we are usually able to distinguish them from the background - this procedure is called *spike detection*. Then, to assign individual spikes to different neurons we need a method called *spike sorting*, which usually uses unsupervised learning techniques based on the spike shape.

Spike sorting

Suppose we have a μ EEG signal with detected spikes. Our goal is to classify spikes to individual neurons. Due to the spatial arrangement of different neurons relative to the electrode (plus possibly their individual characteristics) the shapes of recorded spikes originating in different neurons differ. This can be used to sort spikes on the basis of their shape. Given that the correct solution is unknown and we can not know (the number of neurons in the vicinity of the electrode can not be detected by the available imaging techniques, as well as correct assignment of individual spikes to the neurons), we need to use unsupervised learning methods, namely clustering. Regarding the choice of features describing the shape of individual spikes, we have a great range of options, including amplitude, duration, as well as various transformations - such as wavelet, fourier and many more.



Dependence of AP's shape on location to electrodes. ⁶

In this task we will use for spike detection a method designed by R.Q. Quiroga that is available from WaveClus toolbox⁷. The method detects each AP based on amplitude thresholding. The threshold is determined by the number of standard deviation. Furthermore, signal is filtered by band-pass filter in range 300 – 3000 Hz. You can download a script `cv7_amp_detect.m`.

⁵Frequently the noise carries the majority of the signal energy

⁷source code is available here http://www.vis.caltech.edu/~rodri/Wave_clus/Wave_clus_home.htm. Those who are interested can find more information here, specially in „Introduction“)

Task 2.8 (1 b) Download `cv7_spikesorting_data` and load it into the MATLAB. Sampling frequency is again $fs = 24kHz$. Plot the data and roughly estimate the spikes position. How long is record (in seconds)?

Download a script for spike detection `cv7_amp_detect.m`. Launch the script using microelectrode data and plot the time series along with spikes detected with the threshold used for detection (output variable is `index` and threshold is `thr`). .

Task 2.9 (1 b) Variable `spikes` returns spikes detected in rows sorted by max value. Plot a few first spikes and estimate the number of neurons. Design at least one feature that will be used for spikesorting. Set manually threshold and sort the spikes according your feature. Plot the average spike for each group.

Task 2.10 (3 b) Now just imagine the task when we need to sort the signal without manually setting of the threshold. Suggest and calculate at least one more feature. Plot the spikes in feature space and color them based on your sorting from the previous task. Was your threshold calculated well?

Cluster your features by k-means algorithm (function `kmeans` from Statistics Toolbox). Estimate the number of clusters and show results in feature space. Next, show all signals and average signal for each cluster.

Analyse clustering results. Do you consider your features as sufficient? Is there any possible improvement?

2.3 Analysis of real data: Eye movements

Exercise 2.3 (Eye movements) In this exercise, we will show how to analyze reaction of single neuron to a stimulus. The data comes from experiments, where we evaluate connection between eye movements and neuronal activity in human Basal ganglia. If the activity of given neuron correlates with eye movements, we should see a change in its firing pattern when eye movements are present. The data come from ten repetitions of the following experiment: The subject is looking at a PC screen, which is black at the beginning. At given time, a white cross appears and the task of the subject to focus at it. Electrooculogram (EOG) is recorded throughout the experiment using electrodes placed near subject's eyes, as well as micro EEG activity in the area of basal ganglia. Once the experiment is over, the data goes through spike detection and spike sorting and neurons, correlating with EOG are identified.

Task 2.11 (2 b) Download exercise data from the course website. Data contain recording of activity from single neuron in ten repetitions of the same experiments + corresponding EOG. The variable `firingTimes` contains spike times of given neuron, relative to the time of stimulus (cross appears). Variables `eogTimes` and `eogVals` specify corresponding EOG signal for each repetition.

Note: plotting of EOG and corresponding spike times can be done as follows:

```
plot(eogTimes{1},eogVals{1});  
hold on;  
stem(firingTimes{1},ones(size(firingTimes{1})))
```

Plot firing of the neuron in time, aligned with the stimulus (time 0). What can we say about the activity? How many times did the neuron fire during all repetitions before and after the stimulus?

Task 2.12 (3 b) Use an appropriate way to aggregate activity over all repetitions. (e.g. number of spikes in time windows, instantaneous firing rate, etc.). How does the activity change right after the stimulus? Is there some trend even before the stimulus? How long does it take for the activity to drop and how long to return to original level? Be creative!

3 Information coding and transfer in the brain

In this block, we will model some of the processes taking part in transferring and storing information in the brain. We will go through the basics of cognitive modeling and we will try out the so-called *Self-organizing maps*.