

1 Tutorial

1.1 Syntax

$$\begin{aligned} Expr ::= & Num \mid \\ & \Delta Expr \mid \\ & Expr \odot Expr, \end{aligned} \tag{1}$$

where Num is a predefined set of integer numbers (a.k.a. \mathbb{Z}).

1.2 Small-Step Operational Semantics

Convention: $e, e', e_1, e_2, \dots \in Expr$ and $n, n', n_1, n_2, \dots \in Num$.

$$\frac{}{\Delta n \Rightarrow -n} \tag{2}$$

$$\frac{}{n \odot n' \Rightarrow n + n'} \tag{3}$$

$$\frac{e \Rightarrow e'}{\Delta e \Rightarrow \Delta e'} \tag{4}$$

$$\frac{e_1 \Rightarrow e'}{e_1 \odot e_2 \Rightarrow e' \odot e_2} \tag{5}$$

$$\frac{e_2 \Rightarrow e'}{e_1 \odot e_2 \Rightarrow e_1 \odot e'} \tag{6}$$

1.3 Big-Step Operational Semantics

$$\frac{}{n \Longrightarrow n} \tag{7}$$

$$\frac{e \Longrightarrow n}{\Delta e \Longrightarrow -n} \tag{8}$$

$$\frac{e \Longrightarrow n \quad e' \Longrightarrow n'}{e \odot e' \Longrightarrow n + n'} \tag{9}$$

Please note: $\Rightarrow \in Expr \times Expr$, $\Longrightarrow \in Expr \times Num$