## Instructions for seminars from Numerical Analysis: Least squares approximation

Continue work with the Maple document aproximE.mw. You can choose the approximated function, approximating functions and their number, the number and distribution of nodes. You should be able to solve the simpest tasks without a program. Before trying to solve the second task for assessment, you should pay attention to the following topics:

## A. Error of the method

Approximate function  $f_1(t) = \ln t$  at interval (0, 1; 10) and observe the dependence of the error of the method

- 1. on the number of nodes (e.g., for the approximation by a polynomial of degree at most 5);
- 2. on the degree of the approximating polynomial for a fixed number of nodes, e.g., 20;
- 3. on the approximating functions used, e.g.,  $\varphi_1(t) = 1/(t+r)^s$ ,  $\varphi_2(t) = \exp(-t/T)$ , etc.; observe also the values of the coefficients of the components of the solution.

## **B.** Round-off errors

Repeat the approximation from A2 for function  $f_2(t) = \ln(t-p)$  at interval  $\langle p+0,1; p+10 \rangle$ , where p is a big constant, e.g.,  $10^4$ . (The error of the method remains the same.)