

Algorithm Configuration (Parameter Tuning) Problem

The objective of the parameter configuration (parameter tuning) problem is to find the parameter configuration $\theta \in \Theta$ resulting in the best performance of \mathcal{A} on distribution \mathcal{D} .

There are many ways of measuring an algorithm's performance, denoted as $c(\mathcal{A}, \theta, I, s)$ – i.e. the cost of a single run of algorithm \mathcal{A} with parameter configuration θ on an instance I , using seed s in case of randomized algorithm. For example, we might be interested in

- minimizing computational resources consumed by the given algorithm (such as runtime, memory or communication bandwidth), or
- approximation error, or
- the improvement achieved over an instance-specific reference cost,
- maximizing the quality of the solution found.

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The behaviour of the algorithms can vary significantly between multiple runs on different instances or when randomized algorithms are run repeatedly with fixed parameters on a single problem instance.

Therefore, the goal must be to choose parameter settings that minimize some statistic, $c(\theta)$, of the algorithm's cost distribution, $CD(\mathcal{A}, \theta, \mathcal{D})$, over instances and, in case of randomized algorithms, a distribution over random seeds. For example, we might aim to minimize mean runtime or median solution cost.

The $CD(\mathcal{A}, \theta, \mathcal{D})$ is typically unknown, so we can only acquire approximations of their statistics, $c(\theta)$, based on a limited number of samples (i.e. the cost of single executions of $\mathcal{A}(\theta)$) – let's denote an approximation of $c(\theta)$ based on N samples by $\hat{c}_N(\theta)$.

- For deterministic algorithms, the algorithm \mathcal{A} is run on $N \leq M$ instances (M is the size of the finite training set of instances).
- For randomized, algorithms, we can run multiple runs with different seeds if $M < N$.

