Often, finding performance-optimizing **parameter configurations of heuristic algorithms requires considerable effort**. In many cases, this task is performed **manually in an ad-hoc way**.

Automating this task is of high practical relevance in several contexts:

- Development of complex algorithms setting the parameters of a heuristic algorithm is a highly labour-intensive task, and indeed can consume a large fraction of overall development time. The use of automated algorithm configuration methods can lead to significant time savings and potentially achieve better results than manual, ad-hoc methods.
- Empirical studies, evaluations, and comparisons of algorithms a central question in comparing heuristic algorithms is whether one algorithm outperforms another because it is fundamentally superior, or because its developers more successfully optimized its parameters. Automatic algorithm configuration methods can mitigate this problem of unfair comparisons and thus facilitate more meaningful comparative studies.
- Practical use of algorithms the ability of complex heuristic algorithms to solve large and hard problem instances often depends critically on the use of suitable parameter settings. End users often have little or no knowledge about the impact of an algorithm's parameter settings on its performance, and thus simply use default settings. Automatic algorithm configuration methods can be used to improve performance in a principled and convenient way.

Algorithm Configuration (Parameter Tuning) Problem

Let \mathcal{A} denote an algorithm, whose parameters are to be optimized for a probability distribution of problem instances, \mathcal{D} .

 ${\mathcal D}$ may be given

- implicitly, as through a random instance generator or a distribution over such generators, or
- as the uniform distribution over a finite sample of problem instances.

With each of the algorithm parameters, $p_1 \dots p_k$, a domain of possible values is associated and the parameter configuration space, Θ , is the cross-product of these domains (or a subset thereof).

• We assume that all parameter domains are finite sets.

This assumption can be met by discretizing all numerical parameters to a finite number of values.

 While parameters may be ordered, we do not exploit such ordering relations are finite and categorical.

The elements of Θ are called parameter configurations, θ_i , and $\mathcal{A}(\theta)$ denotes algorithm \mathcal{A} with parameter configuration $\theta \in \Theta$.

The objective of the parameter configuration (parameter tuning) problem is to find the parameter configuration $\theta \in \Theta$ resulting in the best performance of \mathcal{A} on distribution \mathcal{D} .

There are many ways of measuring an algorithm's performance, denoted as $c(\mathcal{A}, \theta, I, s)$ – i.e. the cost of a single run of algorithm \mathcal{A} with parameter configuration θ on an instance I, using seed s in case of randomized algorithm. For example, we might be interested in

- minimizing computational resources consumed by the given algorithm (such as runtime, memory or communication bandwidth), or
- approximation error, or
- the improvement achieved over an instance-specific reference cost,
- maximizing the quality of the solution found.

The behaviour of the algorithms can vary significantly between multiple runs on different instances or when randomized algorithms are run repeatedly with fixed parameters on a single problem instance.

Therefore, the goal must be to choose parameter settings that minimize some statistic, $c(\theta)$, of the algorithm's cost distribution, $CD(\mathcal{A}, \theta, \mathcal{D})$, over instances and, in case of randomized algorithms, a distribution over random seeds. For example, we might aim to minimize mean runtime or median solution cost.

The $CD(\mathcal{A}, \theta, \mathcal{D})$ is typically unknown, so we can only acquire approximations of their statistics, $c(\theta)$, based on a limited number of samples (i.e. the cost of single executions of $\mathcal{A}(\theta)$) – let's denote an approximation of $c(\theta)$ based on N samples by $\hat{c}_N(\theta)$.

- For deterministic algorithms, the algorithm \mathcal{A} is run on $N \leq M$ instances (M is the size of the finite training set of instances).
- For randomized, algorithms, we can run multiple runs with different seeds if M < N.

Algorithm Configuration (Parameter Tuning) Scenario



Manually-executed local search in parameter configuration space

- 1. begin with some initial parameter configuration;
- experiment with modifications to single parameter values at a time, accepting new configurations whenever they result in improved performance (iterative first improvement procedure);
- 3. repeat step 2 until no single-parameter change yields an improvement.

This procedure stops as soon as it reaches a local optimum (a parameter configuration that cannot be improved by modifying a single parameter value) – straightforward remedy is to employ **iterated local search** that builds a chain of local optima by iterating through a main loop consisting of:

- 1. a solution perturbation to escape from local optima,
- 2. a subsidiary local search procedure and
- 3. an acceptance criterion to decide whether to keep or reject a newly obtained candidate solution.

 $\mathsf{ParamILS}(\theta_0, r, p_{restart}, s)$

1. uses a combination of default and random settings for initialization,

- $heta_0$ is the initial parameter configuration, and
- r is the number of randomly chosen configurations for initialization,
- 2. uses a one-exchange neighborhood (one parameter is modified in each search step),
- 3. employs iterative first improvement as a subsidiary local search procedure,
- 4. uses a fixed number, s, of random moves for perturbation,
- 5. always accepts better or equally-good parameter configurations,
- 6. re-initializes the search at random with probability $p_{restart}$.

Basic variant, BasicILS(N), uses procedure $better(\theta_1, \theta_2)$ that compares two cost approximations $\widehat{c}_N(\theta_1)$ and $\widehat{c}_N(\theta_2)$ based on exactly N samples from the respective cost distributions $CD(\mathcal{A}, \theta_1, \mathcal{D})$ and $CD(\mathcal{A}, \theta_2, \mathcal{D})$ – the same N instances are used for all configurations θ_i .

ParamILS(N): Algorithm

Input : Initial configuration $\theta_0 \in \Theta$, algorithm parameters r, $p_{restart}$, and s. **Output** : Best parameter configuration θ found. **1** for i = 1, ..., r do $\theta \leftarrow \text{random } \theta \in \Theta;$ 2 if better(θ , θ_0) then $\theta_0 \leftarrow \theta$; 3 4 $\theta_{ils} \leftarrow IterativeFirstImprovement(\theta_0);$ 5 while not TerminationCriterion() do $\theta \leftarrow \theta_{ils}$; 6 *// ===== Perturbation* for $i = 1, \ldots, s$ do $\theta \leftarrow$ random $\theta' \in Nbh(\theta)$; 7 // ===== Basic local search $\theta \leftarrow IterativeFirstImprovement(\theta);$ 8 *// ===== AcceptanceCriterion* if better(θ , θ_{ils}) then $\theta_{ils} \leftarrow \theta$; 9 with probability $p_{restart}$ do $\theta_{ils} \leftarrow$ random $\theta \in \Theta$; 10 11 return overall best θ_{inc} found; **12 Procedure** *IterativeFirstImprovement* (θ) 13 repeat $\theta' \leftarrow \theta$: 14 foreach $\theta'' \in Nbh(\theta')$ in randomized order do 15 if better(θ'', θ') then $\theta \leftarrow \theta''$; break; 16 17 until $\theta' = \theta$: 18 return θ :

Procedure $better_N(\theta_1, \theta_2)$ simply compares estimates $\hat{c}_N(\theta_1)$ and $\hat{c}_N(\theta_2)$ based on the same N instances using the same random seeds.

• It updates the best-so-far solution, θ_{inc} .

	Input	: Parameter configuration θ_1 , parameter configuration θ_2
	Output	: True if θ_1 does better than or equal to θ_2 on the first N instances; false otherwise
	Side Effect	: Adds runs to the global caches of performed algorithm runs \mathbf{R}_{θ_1} and \mathbf{R}_{θ_2} ; potentially
		updates the incumbent θ_{inc}
1	$\hat{c}_N(\boldsymbol{\theta}_2) \leftarrow \boldsymbol{a}$	$bbjective(\boldsymbol{ heta}_2,N)$
2	$\hat{c}_N(\boldsymbol{\theta}_1) \leftarrow \boldsymbol{a}$	$bbjective(\boldsymbol{ heta}_1,N)$
3	return $\hat{c}_N(\boldsymbol{\theta})$	$(oldsymbol{ heta}_1) \leq \hat{c}_N(oldsymbol{ heta}_2)$

There are two main problems associated with the use of a fixed number of N training samples.

1. Over-confidence – the cost estimated for the best training configuration, θ^*_{train} , underestimates the cost of the same configuration on the test set (i.e. previously unseen samples). $\widehat{c}_N(\theta^*_{train}) = \min\{\widehat{c}_N(\theta_1), \ldots, \widehat{c}_N(\theta_n)\}$ is a biased estimator of $c(\theta^*)$, where $\theta^* \in \arg \min_{\theta_i} \{c(\theta_1), \ldots, c(\theta_n)\}$.

It was shown that $E[\min\{\widehat{c}_N(\theta_1),\ldots,\widehat{c}_N(\theta_n)\}] \leq E[c(\theta^*)]$ with equality only holding in pathological cases.

This effect increases with the number of configurations evaluated and the variance of the cost distributions, and it decreases as N is increased.

2. **Over-tuning** – the situation where additional tuning actually impairs test performance.

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The question is how to choose the optimal number of training instances, N?

- \bullet Using too small N leads to good training performance, but poor generalization to previously unseen test benchmarks.
- On the other hand, we cannot evaluate every parameter configuration on an enormous training set - if we did, search progress would be unreasonably slow.

FocusedILS

ParamILS avoid the problems with over-confidence and over-tuning by adaptively varying the number of training samples considered from one parameter configuration to another in order to focus samples on promising configurations.

• $N(\theta)$ denotes the number of runs available to estimate the cost statistic $c(\theta)$.

The question is how to compare two parameter configurations θ_1 and θ_2 for which $N(\theta_1) \leq N(\theta_2)$?

• What if we computed the empirical statistics based on the available number of runs for each configuration?

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Domination: Configuration θ_1 dominates θ_2 when at least as many runs have been conducted on θ_1 as on θ_2 , and the performance of $\mathcal{A}(\theta)$ on the first $N(\theta_1)$ runs is at least as good as that of $\mathcal{A}(\theta_2)$ on all of its runs.

 θ_1 dominates θ_2 if and only if $N(\theta_1) \ge N(\theta_2)$ and $\widehat{c}_{N(\theta_2)}(\theta_1) \le \widehat{c}_{N(\theta_2)}(\theta_2)$.

ParamILS version, called FocusedILS, encodes a comparison strategy based on the domination in procedure $better_{Foc}(\theta_1, \theta_2)$.

Procedure $better_{Foc}(\Theta_1, \Theta_2)$

- 1. first it acquires one additional run for the configuration i having smaller $N(\theta_i)$, or one run for both configurations if $N(\theta_1) = N(\theta_2)$;
- 2. then, it continues performing runs in this way until one configuration dominates the other. It returns true if θ_1 dominates θ_2 , and false otherwise.

It keeps track of the total number, B, of configurations evaluated since the last improving step.

- Whenever $better_{Foc}(\Theta_1, \Theta_2)$ returns true, B extra runs are performed for θ_1 and B is reset to 0.
- This way it is ensured that many runs are performed with good configurations ⇒ the error made in every comparison of two configurations θ₁ and θ₂ decreases on expectation.
 A theoretical analysis of the resulting algorithm proves its convergence to the globally optimal

A theoretical analysis of the resulting algorithm proves its convergence to the globally optimal parameter configuration.

: Parameter configuration θ_1 , parameter configuration θ_2 Input : True if θ_1 dominates θ_2 , false otherwise Output Side Effect: Adds runs to the global caches of performed algorithm runs \mathbf{R}_{θ_1} and \mathbf{R}_{θ_2} ; updates the global counter B of bonus runs, and potentially the incumbent θ_{inc} 1 $B \leftarrow B + 1$ 2 if $N(\theta_1) < N(\theta_2)$ then $\begin{array}{c|c} \mathbf{3} & \boldsymbol{\theta}_{min} \leftarrow \boldsymbol{\theta}_1; \boldsymbol{\theta}_{max} \leftarrow \boldsymbol{\theta}_2 \\ \mathbf{4} & \quad \text{if } N(\boldsymbol{\theta}_1) = N(\boldsymbol{\theta}_2) \text{ then } B \leftarrow B+1 \end{array}$ 5 else $\theta_{min} \leftarrow \theta_2; \theta_{max} \leftarrow \theta_1$ 6 repeat 7 $i \leftarrow N(\boldsymbol{\theta}_{min}) + 1$ 8 $\hat{c}_i(\boldsymbol{\theta}_{max}) \leftarrow objective(\boldsymbol{\theta}_{max}, i) // If N(\boldsymbol{\theta}_{min}) = N(\boldsymbol{\theta}_{max}), adds a new run to \mathbf{R}_{\boldsymbol{\theta}_{max}}.$ 9 $\hat{c}_i(\boldsymbol{\theta}_{min}) \leftarrow objective(\boldsymbol{\theta}_{min}, i) \parallel Adds a new run to \mathbf{R}_{\boldsymbol{\theta}_{min}}.$ 10 until dominates(θ_1, θ_2) or dominates(θ_2, θ_1) 11 if dominates(θ_1, θ_2) then // ==== Perform B bonus runs. $\hat{c}_{N(\theta_1)+B}(\theta_1) \leftarrow objective(\theta_1, N(\theta_1)+B) \parallel Adds B \text{ new runs to } \mathbf{R}_{\theta_1}.$ 12 $B \leftarrow 0$ 13 return true 14 15 else return false 16 **Procedure** dominates(θ_1, θ_2) 17 if $N(\theta_1) < N(\theta_2)$ then return false 18 return $objective(\theta_1, N(\theta_2)) < objective(\theta_2, N(\theta_2))$

Often, the search for a performance-optimizing parameter setting spends a lot of time with evaluating a parameter configuration that is much worse than other, previously-seen configurations.

Ex.: Let's assume a case where parameter configuration θ_1 takes a total of 10 seconds to solve N = 100 instances (i.e. it has a mean time runtime of 0.1 seconds per instance), and another parameter configuration θ_2 takes 100 seconds to solve the first of these instances.

Clearly, when comparing the mean runtimes of θ_1 and θ_2 based on this set of instances, it is not necessary to run θ_2 on remaining 99 instances. Instead, we can terminate the first run of θ_2 after $10 + \epsilon$ seconds, which is a lower bound on θ_2 's mean runtime of $0.1 + \epsilon/100$. this lower bound exceeds the mean runtime of θ_1 , so we can already be sure that θ_2 cannot do better than θ_1 .

Question is how to determine the cutoff time for each run of the target algorithm, A, in an automated way?

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Question is how to determine the cutoff time for each run of the target algorithm, A, in an automated way?

Adaptive capping is based on the idea of avoiding unnecessary runs of the algorithm \mathcal{A} by developing bounds on the performance measure to be optimized.

- **Trajectory-preserving capping** provably does not change *BasicILS*'s trajectory, but can lead to large computational savings.
- **Aggressive capping** potentially yielding even better performance.

Trajectory-Preserving Capping (for the case of optimizing the mean of non-negative cost function) – implements bounded evaluation of a parameter configuration θ , procedure $objective(\theta, bound)$, based on N runs so that

- it sequentially performs runs for θ and after each run computes a lower bound on $\widehat{c}_N(\theta)$ based on $i \leq N$ runs performed so far;
- once the lower bound exceeds the bound passed as an argument, the remaining runs for θ_2 are skipped.

Procedure $better_N(\theta_1, \theta_2)$ is modified as follows

$$\begin{array}{ll} 1 & bound \leftarrow \infty \\ 2 & \widehat{c}_N(\theta_2) \leftarrow objective(\theta_2, N, bound) \\ 3 & bound \leftarrow \widehat{c}_N(\theta_2) \\ 4 & \widehat{c}_N(\theta_1) \leftarrow objective(\theta_1, N, bound) \\ 5 & \operatorname{return} \widehat{c}_N(\theta_1) \leq \widehat{c}_N(\theta_2) \end{array}$$

Aggressive Capping – bounds the evaluation of any configuration by the performance of the best-so-far (incumbent) configuration, θ_{inc} , multiplied by a factor **bound multiplier**, bm.

When two configurations \(\theta_1\) and \(\theta_2\) are compared and the evaluations both are terminated preemptively, the configuration having solved more instances within the allowed time is considered the better one.

Ties are broken to favor moving to a new parameter configuration.

• For $bm = \infty$, this reduces to trajectory-preserving but no savings strategy.

bm = 1 means that once we know the evaluated configuration θ is worse than the θ_{inc} , its evaluation is terminated (recommended setting is bm = 2).

Frank Hutter, Holger H. Hoos, Kevin Leyton-Brown, and Thomas Stützle: ParamILS: An Automatic Algorithm Configuration Framework. In *Journal of Artificial Intelligence Research* (JAIR), volume 36, pp. 267-306, October 2009.

Other papers and SW available at http://www.cs.ubc.ca/labs/beta/Projects/ParamILS/