

# Coevolution

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## Coevolution and its basic types

What is “coevolution”?

Types of coevolution

1-population competitive coevolution

2-population competitive coevolution

N-population cooperative coevolution

1-population cooperative coevolution

Problems in coevolution

# Coevolution and its basic types

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## Coevolution in EAs:

- ✓ The fitness of individuals in a population
  - ✗ is not given by the characteristics of the individual (only), but
  - ✗ is *affected by the presence of other individuals in the population.*
- ✓ It is closer to the biological evolution than ordinary EAs are.

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## Coevolution can help in:

- ✓ dealing with increasing difficulty of the problem
- ✓ providing diversity in the system
- ✓ producing not just high-quality, but also robust solutions
- ✓ solving complex or high-dimensional problems by breaking them into nearly decomposable parts

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By relation type:

- ✓ cooperative (synergic, compositional)
- ✓ competitive (antagonistic, test-based)

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By relation type:

- ✓ cooperative (synergic, compositional)
- ✓ competitive (antagonistic, test-based)

By the entities playing role in the relation:

- ✓ 1-population
  - ✗ intra-population
  - ✗ individuals from the same population cooperate or compete
- ✓ N-population
  - ✗ inter-population
  - ✗ individuals from distinct populations cooperate or compete



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**Example:** The goal is to evolve a game playing strategy

✓ successful against diverse opponents!!!

How would you proceed in an ordinary EA?

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**Solution:** Intra-population competitive coevolution

- ✓ by playing several games against other strategies in the population.
- ✓ All individuals of the same type.
- ✓ In the beginning, all are probably quite bad, but some of them are a bit better.
- ✓ The fitness (the number of games won) may not rise as expected since your opponents improve with you.

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- ✓ able to sort any sequence of numbers
- ✓ correctly and quickly.

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  - ✗ sorting algorithms
  - ✗ test cases (sequences to sort)

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  - ✗ test cases (sequences to sort)
- ✓ Fitness evaluation:
  - ✗ Algorithm: by its ability to sort. How many sequences is it able to sort correctly? How quickly?
  - ✗ Test case: by its difficulty for the current sorting algorithms. How many algorithms did not sort it?
- ✓ Predator-prey relationship

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- ✓ a goalie, back, midfielder, and forward
- ✓ so that they form a good team together.

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- ✓ Theoretically possible, but the space is too large.
- ✓ May result in a team of players which wouldn't perform well if substituted to another team.

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Cooperation:

- ✓ symbiotic relationship
- ✓ good performance of the team  $\Rightarrow$  high contribution to fitness of all members

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Example: **Niching** methods for

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- ✓ fitness sharing
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- ✓ diversity preservation
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Examples of niching methods:

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Principle:

- ✓ better individuals similar to others already in population are thrown away in favour of worse, but diverse individuals
- ✓ the selection process is affected by the presence of other individual in the neighborhood

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**Problems in coevolution**

Fitness in coevolution  
“Fitness” in  
competitions

Problems with fitness  
assessment: 1-pop.  
competitive coevolution  
2 competitive  
populations (illustration)

Problems with fitness  
assessment: 2-pop.  
competitive coevolution

Problems with fitness  
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Summary

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Some important classifications of fitness

- ✓ by its time-dependence:
  - ✗ **static**: does not change with time
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Ideally, external fitness

- ✓ should be **static**, **deterministic** and **absolute**
- ✓ can easily be used as internal fitness

External fitness in coevolution:

- ✓ impossible (hard) to define
- ✓ often, it is **relative**, but measured with a carefully chosen, large enough set of other individuals (**static**) sufficiently many times (almost **deterministic**)

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Internal fitness in coevolution:

- ✓ **relative**: affected by other individuals
- ✓ **dynamic**: affected by evolving individuals (needs re-evaluation)
- ✓ **stochastic**: usually evaluated against a smaller number of individuals

# “Fitness” in competitions



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Football league:

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- ✓ all teams play against all others
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## Golf players:

- ✓ tournaments have different prize money to distribute to tournament winners
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The same holds for fitness assessment in coevolution!

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## Cycles, etc.

- ✓ What if A beats B, B beats C, but C beats A?

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- ✓ What if A beats B, but B beats far more individuals than A?
- ✓ The quality assessment depends on what we really want:

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assessment: N-pop.  
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Summary

## Cycles, etc.

- ✓ What if A beats B, B beats C, but C beats A?
- ✓ What if A beats B, but B beats far more individuals than A?
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  - ✗ A player that wins by the most total points on average?
- ✓ Often, other tests are executed.
- ✓ But, do you want to spend your fitness budget
  - ✗ on evaluating current individuals more precisely, or
  - ✗ on searching further?

## 2 competitive populations (illustration)

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Lotka-Volterra model (Predator-prey population dynamics):

$$\frac{dx}{dt} = \alpha x - \beta xy$$

$$\frac{dy}{dt} = -\gamma y + \delta xy$$

where  $x$  is the number of prey (rabbits) and  $y$  is the number of predators (wolves).

Assumptions:

1. The prey population has always food enough.
2. The predators eat only the prey.
3. The rate of change of population is proportional to its size.
4. The environment is static.

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Meaning:

- ✓ The change of the prey population ( $dx/dt$ ) is composed of
  - ✗ increase due to the newly born individuals (proportional to the population size,  $\alpha x$ ) and
  - ✗ decrease caused by the predation (which is proportional to the rate of predator-prey meetings,  $\beta xy$ ).
- ✓ The change of the predator population ( $dy/dt$ ) is composed of
  - ✗ decrease due to natural death (proportional to the population size,  $\gamma y$ ) and
  - ✗ increase allowed by the food supply (proportional to the rate of predator-prey meetings,  $\delta xy$ ).

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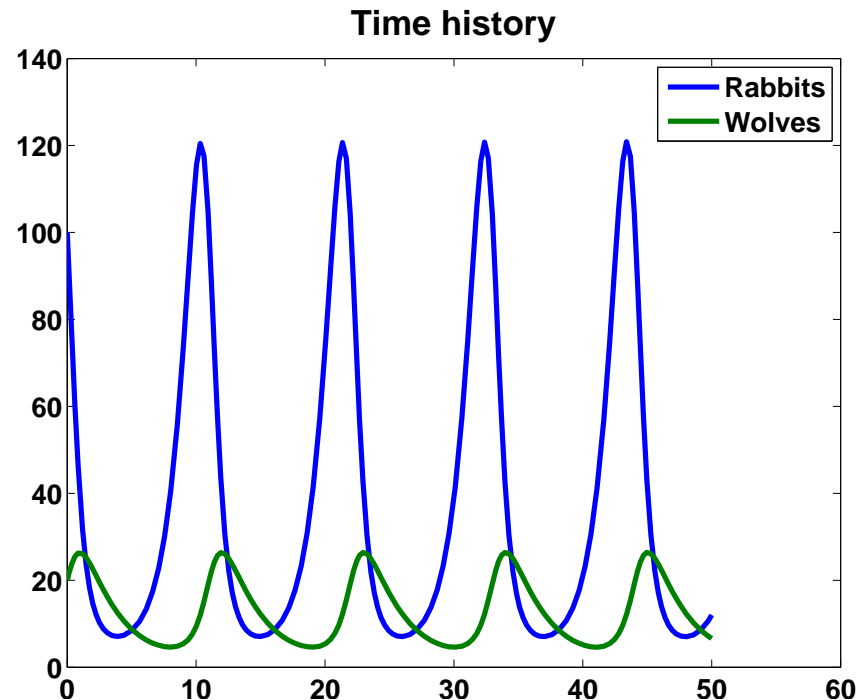
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## Arms races

- ✓ one population learns a trick and forces the second population to learn a new trick to beat the first one...
- ✓ one population may evolve faster than the other:

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  - ✗ external fitness in both populations drops until the gradient re-emerges
- ✓ not exactly what was shown by Lotka-Volterra, but similar
- ✓ Solution:
  - ✗ detect such situation (but how?)
  - ✗ delay the evolution of the better population until the worse one catches up

## Hijacking

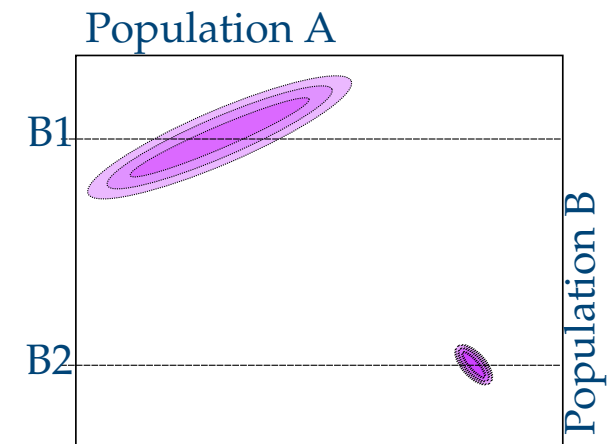
- ✓ a really good forward takes over one population, any team will play well thanks to him
- ✓ members of all other populations have almost the same fitness  $\Rightarrow$  uniform random selection
- ✓ Solution: apply some form of *credit assignment*

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## Relative overgeneralization

- ✓ when evaluated by average score, worse (but more robust) individual B1 will have higher score than better (but volatile) B2
- ✓ use maximum score (more tests needed)
- ✓ but again, the choice depends on what we want — a player able to get the highest score, or a player that would compare well with the most other opponents?



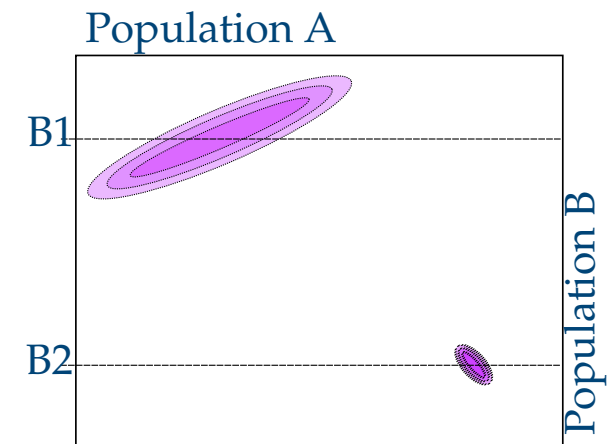
# Problems with fitness assessment: N-pop. cooperative coevolution

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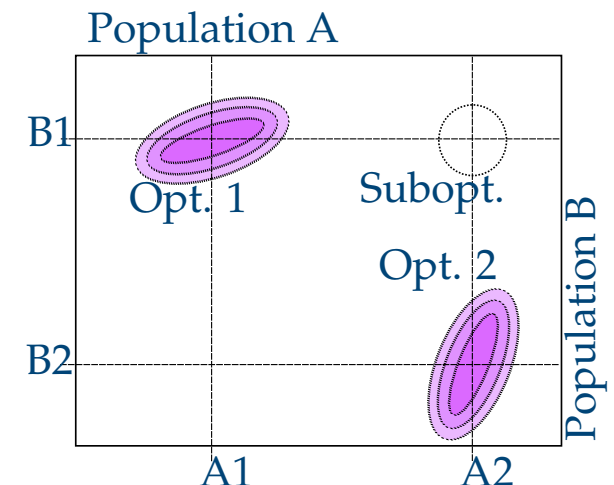
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## Miscoordination

- ✓ when the team components are not independent
- ✓ Pop. A evolved A2 (but not A1), pop. B evolved B1 (but not B2)
- ✓ Neither A2 nor B1 survives



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## Coevolution

- ✓ can be cooperative or competitive (or both)
- ✓ can take place in 1 population or in more populations
- ✓ fitness is not fixed during evolution
- ✓ introduces new unexpected dynamics to the system (new issues to be solved)

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## Appropriate when

- ✓ no explicit fitness function can be formed
- ✓ there are too many fitness cases
- ✓ the problem is modularizable (divide and conquer)