Robotic Information Gathering - Exploration of Unknown Environment

Jan Faigl

Department of Computer Science Faculty of Electrical Engineering Czech Technical University in Prague

Lecture 04

B4M36UIR - Artificial Intelligence in Robotics



tions?

Overview of the Lecture

Challenges in Robotic Information Gathering

How to address all these aspects altogether to find a cost-efficient solution

using in-situ decisions?

■ Part 1 - Robotic Information Gathering - Robotic Exploration

• Robotic Information Gathering and Robotic Exploration

Environment Representation

Frontier Based Exploration

Exploration and Search

Where to take new measurements?

How to efficiently utilize more robots?

How to navigate robots to the selected loca-

■ What locations visit first?

Information Theoretic Approaches

Robotic Information Gathering

Create a model of phenomena by autonomous mobile robots performing measurements in a dynamic unknown environment.















Learning

adaptivity

Robotic Information

Gathering

Planning

uncertainty

tonomously?

decision-making

information gathering.

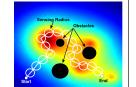
Informative Motion Planning

 Robotic information gathering can be considered as the informative path planning problem to a determine trajectory \mathcal{P}^* such that

 $\mathcal{P}^* = \operatorname{argmax}_{\mathcal{P} \in \Psi} I(\mathcal{P})$, such that $c(\mathcal{P}) \leq B$, where

- Ψ is the space of all possible robot trajectories,
- $I(\mathcal{P})$ is the information gathered along the trajectory \mathcal{P} ,
- c(P) is the cost of P and B is the allowed budget.
- Searching the space of all possible trajectories is complex and demanding problem.
- A discretized problem can be solved by combinatorial optimization techniques. Usually scale poorly with the size of the problem
- A trajectory is from a continuous domain.
- Sampling-based path/motion planning techniques can be employed for finding maximally informative trajectories.

Hollinger, G., Sukhatme, G. (2014): Sampling-based robotic information gathering algorithms. IJRR.



- robotic information gathering mission.
- about the studied phenomenon.
- considering a limited travel budget.
- Collect data and update the phenomenon model.
- Search for the next locations to improve the model.
- Optimal sampling design to Determine locations to be visited w.r.t. the mission objective.
- Trajectory planning Path/motion planning to find optimal paths/trajectories.
- Multi-goal path/motion planning for an optimal sequence of visits to the locations.
- Solutions have to respect, e.g., kinematic and kinodynamic constraints, collision-free paths. In general, the problem is very challenging, and therefore, we consider the most important and relevant constraints, i.e., we address the problem under particular assumptions

Robotic information gathering aims to determine an optimal solution to collect the most relevant

data (measurements) in a cost-efficient way.

Robotic Information Gathering and Multi-Goal Planning

Part I

Part 1 – Robotic Exploration

- It builds on a simple path and trajectory planning point-to-point planning.
- It may consist of determining locations to be visited and a combinatorial optimization problem to determine
- It can be considered a general problem for various tasks and missions, including online decisionmaking.
 - Informative path/motion planning and persistent monitoring.
 - Robotic exploration create a map of the environment as quickly as possible.

and determining a plan according to the particular assumptions and constraints; a plan that is then executed by the robots.

- Inspection planning Find a shortest tour to inspect the given environment.
- Surveillance planning Find the shortest (a cost-efficient) tour to periodically monitor/capture the given objects/regions of interest
- Data collection planning Determine a cost-efficient path to collect data from the sensor stations (locations).
- In both cases, multi-goal path planning allows solving (or improving the performance) of the particular missions.

Robotic Exploration of Unknown Environment

Persistent Monitoring of Spatiotemporal Phenomena

Persistent environment monitoring is an example of the

To improve the phenomena model.

To divide the task between the robots/

Improve Localization vs Model.

On-line decision-making.

- It stands to determine suitable locations to collect data
- Determine a cost-efficient path to visit the locations, e.g.,

- Robotic information gathering is challenging problem.





- It includes multiple challenges:
 - Map building and localization;

Performance indicators vs. constraints.

■ Indicators - time, energy, map quality.

■ Constraints - no. of robots, communication

Performance in a real mission depends on the on-line

- Determination of the navigational waypoints;
- Path planning and navigation to the waypoints;
- Coordination of the actions (multi-robot team).

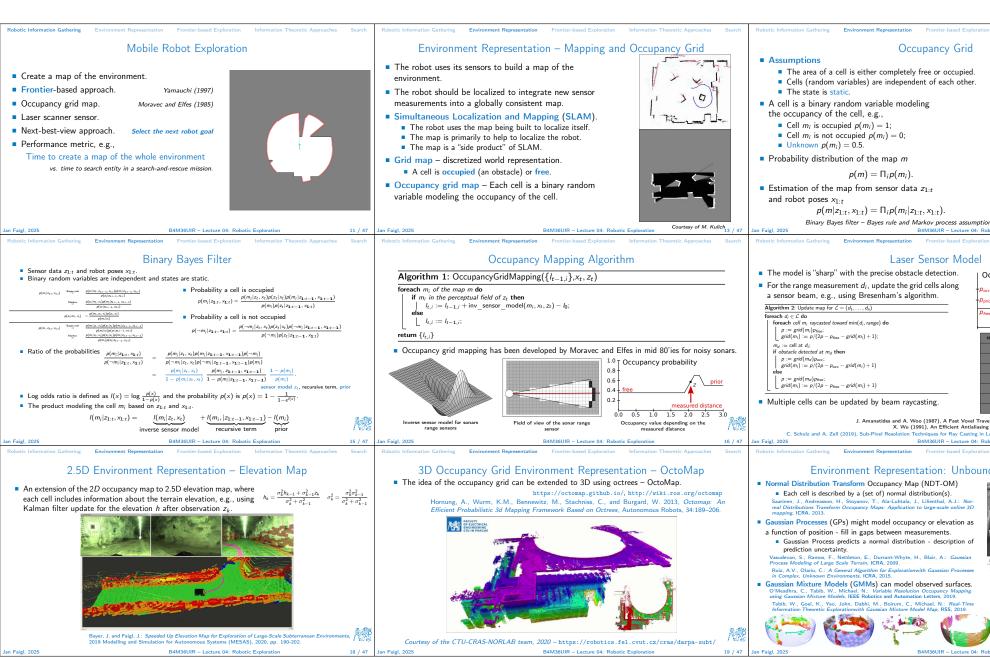
Robotic exploration is a fundamental problem of robotic

How to efficiently utilize a group of mobile robots

to create a map of an unknown environment au-



Courtesy of M. Kulich



Occupancy Grid

- The area of a cell is either completely free or occupied.
- Cells (random variables) are independent of each other.

$$p(m|z_{1:t},x_{1:t}) = \prod_i p(m_i|z_{1:t},x_{1:t}).$$

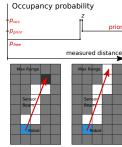
free space

occupied space

Laser Sensor Model

- a sensor beam, e.g., using Bresenham's algorithm.





J. Amanatides and A. Woo (1987), A Fast Voxel Traversal Algorithm for Ray Tracing, Eurographics.

X. Wu (1991), An Efficient Antialiasing Technique, SIGGRAPH Computer Graphics.

Techniques for Ray Casting in Low-Resolution Occupancy Grid Mans. ECMF

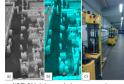
Environment Representation: Unbound by Resolution

Each cell is described by a (set of) normal distribution(s).

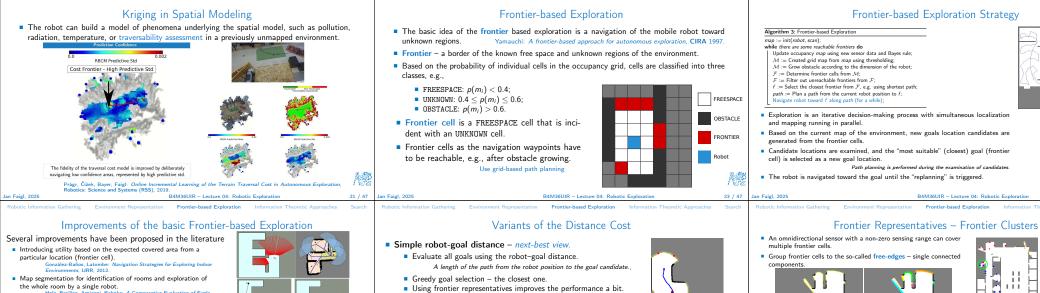
Saarinen, J., Andreasson, H., Stoyanov, T., Ala-Luhtala, J., Lilienthal, A.J.: No mal Distributions Transform Occupancy Maps: Application to large-scale online 3

Gaussian Process predicts a normal distribution - description of

Gaussian Mixture Models (GMMs) can model observed surfaces.







Consider visitations of all goals.

■ TSP distance cost - Non-myopic next-best view.

Solve the associated traveling salesman problem (TSP). A length of the tour visiting all goals.

- Use frontier representatives to avoid large instances of the TSP.
- the TSP distance cost improves performance about 10-30% with-
- out further heuristics, e.g., expected coverage (utility).

Kulich, M., Faigl, J., Přeučil, L.: On Distance Utility in the Exploration Task, ICRA, 2011









covered by the sensor range D; determine the number of subclusters n, and use k-means clustering

$$n_r=1+\left\lfloor\frac{f}{1.8D}+0.5\right\rfloor.$$
 Faiel, J., Kulich, M., and Přeučil, L.: Goal assignment using distance cost in

It reduces the number of goal candidates and yields navigation

toward middle locations of the free-edges

Multi-robot Exploration – Overview of Centralized Strategy

- We need to assign navigation waypoint to each robot that can be formulated as the task-allocation problem
- Multi-robot exploration as an iterative procedure.
- 1. Initialize the occupancy grid Occ.
- 2. $\mathcal{M} \leftarrow \text{create}_{\text{navigation}_{\text{grid}}}(\textit{Occ})$.
- cells of M have values {freespace, obstacle, unknown}
- F ← detect frontiers(M).
- Goal candidates G ← generate(F)
- 5. Assign next goals to each robot $r \in R$. $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(R, G, M).$
- 6. Create a plan P_i for each pair $\langle r_i, g_{r_i} \rangle$.
- 7. Perform each plan up to smax operations
- 8. If |G| == 0 exploration finished, otherwise go to Step 2.



 Several parts of the exploration procedure are important regarding decisionmaking and achieved performance.

- How to determine goal candidates from the the frontiers?
- How to plan a paths and assign the goals to the robots?
- · How to navigate the robots toward the goal?
- When to replan?

Exploration Procedure – Decision-Making Parts

- 1. Initialize set of plans for m robots, $\mathcal{P} = (P_1, \dots, P_m), P_i = \emptyset$.
- 2. Repeat
- 2.1 Navigate robots using the plans P:
- 2.2 Collect new measurements:
- 2.3 Update the navigation map M;
- Until replanning condition is met.
- 3. Determine goal candidates G from M.
- 4. If $|\mathbf{G}| > 0$ assign goals to the robots
 - $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle)$ = assign $(\mathbf{R}, \mathbf{G}, \mathcal{M})$ $r_i \in \mathbf{R}, g_r \in \mathbf{G};$
 - Plan paths to the assigned goals
 - $\mathcal{P} = \mathsf{plan}(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle, \mathcal{M});$
- Go to Step 2.
- 5. Stop all robots or navigate them to the depot. All reachable parts of the environment are explored.





cation based on its (limited) information about other robots.

distributed task allocation.

Consider a longer planning horizon as a solution to the Traveling

Representatives of free edges - Frontier cells are formed into

by following the closest frontier.

can be viewed as the task allocation problem.

Zlot, Stentz (2006), Kulich, Faigl (2011, 2012).

to autonomously create a model of a priory unknown environment.

Kulich, Faigl (2011, 2013)

Multi-robot Exploration

• Multi-robot exploration is a problem to efficiently utilize a group of (mobile) robots

Uncoordinated approach – Each robot independently explores the environment, e.g.,

■ Centralized approaches – a central authority assigns the goals, and the goal assignment

Decentralized approaches – Each robot selects its own goal and solves the task allo-

but it is generally not mandatory for "true" decentralized approaches.

Considering communication between the exploring units, we can further establish

Existing communication between the exploring units can improve the performance

Various strategies have been proposed, such as greedy assignment, Hungarian

assignment, and multiple traveling salesman problem assignments.

Salesman Problem (TSP)



1. Cluster the goal candidates G to m clusters (using k-means)

■ Solve the TSP on the set $C_i \cup \{r_i\}$ – the tour starts at r_i . ■ The next robot goal gi is the first goal of the found TSP tour.

■ The exploration performance depends on the whole solution, albeit

Locally optimal Hungarian algorithm might not necessarily provide

A solution of the particular sub-task (i.e., goal candidate selec-

tion) might have side effects that are exhibited during the missions

Vector Field Histogram (VFH) slows down the robot close to

 A side effect of the representatives of free edges is that goal candidates are "in the middle of free-edges" and the robot is

navigated toward them, which results in faster motion because

It is all related to simplifications we made to solve the challenging

Borenstein, J. and Koren, Y.: The vector field histogram-fast obstacle avoidance for mobile robots. IEEE Transactions on Robotics. 1991.

better solutions than for example the MTSP-based approach.

we can have "best" possible solutions of each part.

- depending on the utilized navigation technique.

the obstacles

■ m-TSP heuristic ⟨cluster-first, route-second⟩

MTSP-based Task-Allocation Approach

 $\boldsymbol{C} = \{C_1, \ldots, C_m\}, C_i \subseteq \boldsymbol{G}.$

2. For each robot $r_i \in \mathbf{R}, i \in \{1, \dots m\}$ select the next goal g_i from C_i using the TSP

Faigl, J., Kulich, M., Přeučil, L.: Goal Assignment using Distance Cost in Multi-Robot Exploration, IROS 2012.

Influence of Decision-Making - Exploration Strategy

Task-allocation problem as the Multiple Traveling Salesman Problem (MTSP).

Performance of the MTSP vs Hungarian Algorithm

Goal Assignment Strategies - Task Allocation Algorithms

■ Exploration strategy can be formulated as the task-allocation problem

$$(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}(t), \mathcal{M}),$$

where \mathcal{M} is the current map.

1. Greedy Assignment

Randomized greedy selection of the closest goal candidate.

Yamauchi B., Robotics and Autonomous Systems 29, 1999.

2. Iterative Assignment

• Centralized variant of the broadcast of local eligibility algorithm (BLE).

Werger, B., Mataric, M., Distributed Autonomous Robotic Systems 4, 2001

3. Hungarian Assignment

 \blacksquare Optimal solution of the task-allocation problem for assignment of n goals and m robots in $O(n^3)$. For n < m: use Iterative assignment or dummy tasks; For n > m: add dummy robots with costly assignments.

Stachniss, C., C implementation of the Hungarian method, 2004

4. Multiple Traveling Salesman Problem - MTSP Assignment

(cluster-first, route-second), the TSP distance cost.

Faigl, et al. 2012

Kulich et al., ICRA (2011)

MinPos: Decentralized Exporation Strategy

- The robot solves the task allocation based on its (limited) information about other robots.
- **Assumption**: the distance cost matrix C between robots \mathcal{R} and frontiers \mathcal{F} are known to all robots In practice, it requires the robots to share the map of the whole environment, which might not be feasible, and therefore, approximations can be employed.
- Each robot ranks each frontier using the relative distance of the robots to the frontier cell (goal candidate).
- The robot is assigned the goal with the minimum rank.



Gready assignment of goal candidates (frontiers Simonin O Charnillet E : MinPos: A Novel En Faigl. J., Simonin, O., Charpillet, F.: Comparison of Task-Allocation Algorithms in F. me FIIMAS 2014

autonomous exploration.

Computing Mutual Information in Exploration

- Sensor placement approach with raycasting of the sensor beam and determination of the distribution over the range returns.
- Precise computing of the mutual information is usually not computationally feasible given the size of the action set and the uncertainty of action results.
- We can assume that observation removes all uncertainty from observed areas

$$I_{MI}[x;z] = H[x] - H[x|z] \approx H[x].$$

- Then, we can decrease the computational requirements by using simplified approach where the action is selected to maximize the entropy over the sensed regions in the current map.
- We are maximizing mutual information in the sensor placement problem of observing the region with maximum entropy

$$\operatorname{argmax}_{a \in A} \sum_{x \in P(a)} H[p(x)],$$

where R(a) represents the region sensed by the action a.

Computational cost can be decreased using Cauchy-Schwarz Quadratic Mutual Information

(CSQMI) defined similarly to mutual information. Can be evaluated analytically for occupancy grid mapping.







Information Theory in Robotic Information Gathering

Replanning as quickly as possible; $m=3, \rho=3$ m - The MTSP assignment p

- Frontier-based exploration assumes perfect knowledge about the robot states and the utility function depends only on the map.
- We can avoid such assumption by defining the control policy as a rule how to select the robot action that reduces the uncertainty of estimate by learning measurements:

$$\operatorname{argmax}_{a \in A} I_{MI}[x; z|a],$$

where A is a set of possible actions, x is a future estimate, and z is future measurement

■ Mutual information – how much uncertainty of x will be reduced by learning z

$$I_{MI}[x;z] = H[x] - H[x|z],$$

where H[x] is the current entropy, and H[x|z] is future/predicted entropy.

- Conditional Entropy H[x|z] is the expected uncertainty of x after learning unknown z (collecting new measurements).
- Entropy uncertainty of x: $H[x] = -\int p(x) \log p(x) dx$.

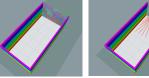


Example of Autonomous Exploration using CSQMI

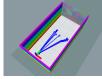
Actions

Actions are shortest paths to cover the frontiers

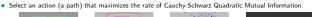
it is relatively far from the obstacles.







Paths to the sampled pose











Ground vehicle

Charrow, B., Kahn, G., Patil, S., Liu, S., Goldberg, K., Abbeel, P., Michael, N., Kumar, V.: Information Mapping. Robotics: Science and Systems (RSS), 2015



Aerial vehicle



In exploration scenarios, where we search for some phenomenon, such as searching for

 $x_t = \operatorname{argmax}_{x \in D} \mu_{t-1}(x) + \beta_t^{\frac{1}{2}} \sigma_{t-1}(x).$

Exploration of the current model vs. exploration of unknown parts of the environment.

a source of radiation or heat, we search for the modeled function's extrema.

The search strategy needs to balance exploitation and exploration.

It addresses the search as a multi-armed bandit problem.

• The GP-UCB policy to chose the next sampling point x_t is

■ Gaussian Process Upper Confidence Bound

Mutual Information in Kriging

- The GP regressors provide an inbuilt representation of uncertainty their prediction is a normal distribution.
 - The differential entropy of a normal distribution is

$$H(\mathcal{N}(\mu, \sigma^2)) = \frac{1}{2} \log(2\pi e \sigma^2),$$

i.e., it is a function of its variance σ^2 .

- We can employ greedy approach sample at the highest prediction variance.
- Example: Building communication maps
- A pairwise problem select locations of two robots to sample the communication signal strength.

Quattrini Li, A., Penumarthi, P.K., Banfi, J., Basilico, N., O'Kane, J.M., Rekleitis, I., Nelakuditi, S., Amigoni, F.: Multi-robot online sensing strategies for the construction of communication maps, Autonomous Robots 44:299—319, 2020.





Wenhao, L., Sycara, K.: Adaptive S of Gaussian Processes, ICRA, 2018.

Exploration with Position Uncertainty

- A reliable localization is needed to map the environment reliably; thus, we might need to consider both the occupancy and localization mutual information:
 - $I = \gamma I_{occupancy} + (1 \gamma) I_{localization}.$ The localization uncertainty can be based on the entropy

$$\frac{1}{2} \log [(2\pi e)^n det P]$$

where P is the covariance of location of the robot and localization landmarks.

- Summing Shannon's entropy of the map and the differential entropy of the pose leads to scaling issues.
 The explorer may stricly prefer to improve either its map or localization that can achieved by adjusting γ
 - We can use the notion of Rényi's entropy

on of Rényi's entropy
$$H_{\alpha}\left[P(\mathbf{x})\right] = \frac{1}{1-\alpha}\log_2(\sum p_i^{\alpha})$$

where for $\alpha \to 1$ its becomes Shannon's entropy.

The utility function of taking an action a is the difference

$$\operatorname{argmax}_{a} \sum_{x \in R(a)} H^{\mathsf{Shannon}} \left[P(x) \right] - H^{\mathsf{R\acute{e}nyi}}_{1 + \frac{1}{\delta(a)}} \left[P(x) \right]$$

where $\delta(a)$ is related to predicted position uncertainty given the action a. Carrillo, H., Dames, P., Kumar, V., Castellanos, J.A.: Autonomous rob based on Reny's general theory of entropy, Autonomous Robots, 2018

Search in Unknown Environments

- A variant of exploration is a search to find objects of interest in an unknown environment
- In search-and-rescue missions, the performance indicator is the time to find the objects and report their position.
- The map is used for navigation, localization of artifacts, and decision-making where to search



Summary of the Lecture

Topics Discussed

- Robotic information gathering informative path planning
- Robotic exploration of unknown environment
 - Occupancy grid map

Topics Discussed

- Frontier based exploration
- Exploration procedure and decision-making
- TSP-based distance cost in frontier-based exploration
- Multi-robot exploration and task-allocation
- Mutual information and informative path planning

Motivation for the semestral project

Next: Invited lecture on a topic topic to be announced; then, Multi-goal planning



