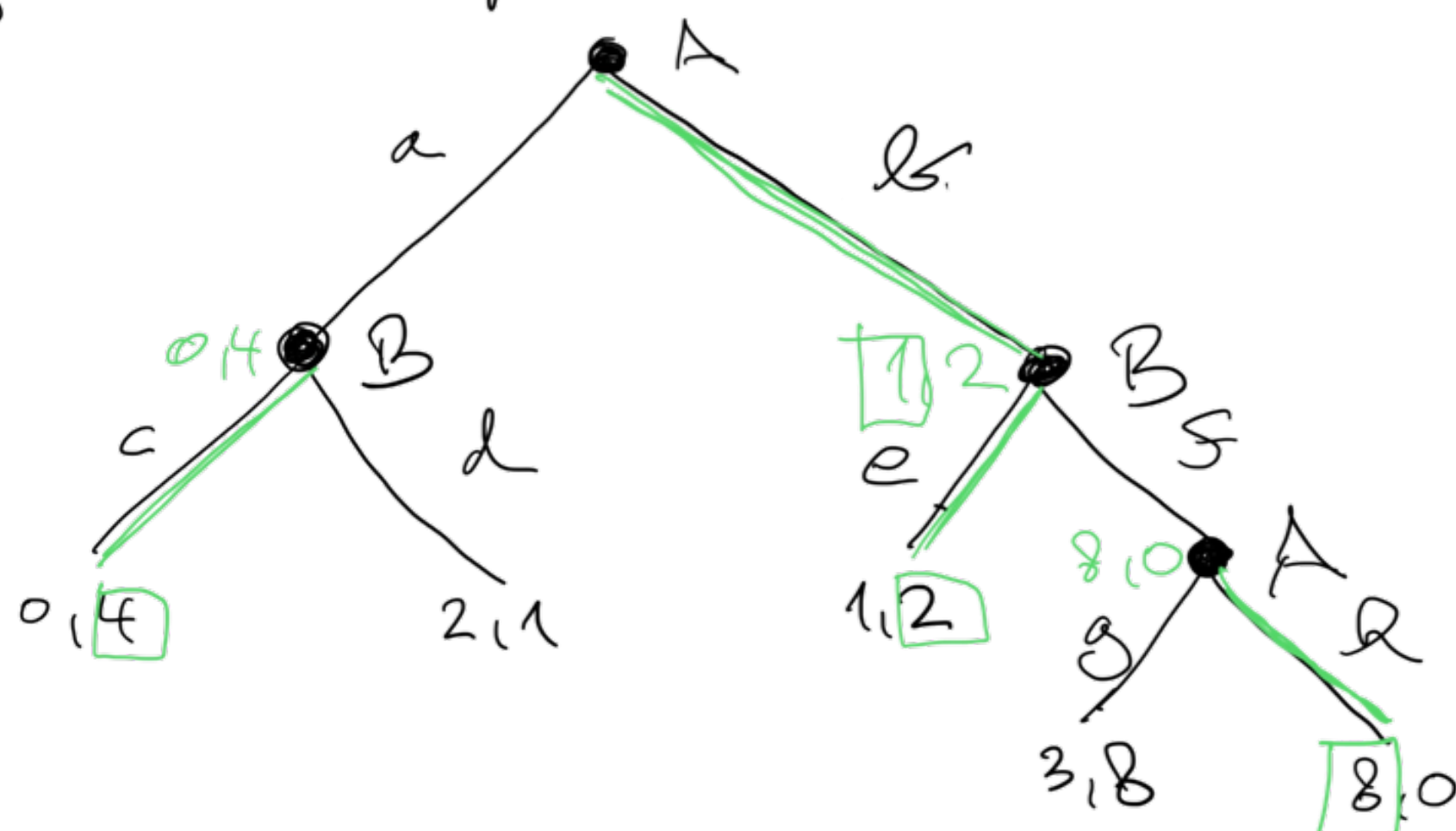


① A game with perfect information



	ce	cf	de	df
ag	0, 4	0, 4	2, 1	2, 1
ah	0, 4	0, 4	2, 1	2, 1
bg	1, 2	3, 8	1, 2	3, 8
bh	1, 2	8, 0	1, 2	8, 0

NE

No strictly dominated strategy.

② Iterative elimination and weak dominance

	x	y	z
a	10, 0	5, 1	4, -2
b	10, 1	5, 0	1, -1

Order 1: Eliminate b, then
x and z $\Rightarrow$ (9, 4)

Order 2: Eliminate z. There
are no order dominated
strategies.

③ Truthful bidding in
2nd price auction

Claim: Strategy v_i weakly dominates
any other strategy b_i for
any player i .

Proof:

First, assume that $b_i < v_i$,
that is, player i is underbidding.

We distinguish 3 cases:

(i) $\bar{b}_i < b_i$

$$\Downarrow$$

$$u_i(v_i, b_{-i}) = u_i(b_i, b_{-i}) = v_i - \bar{b}_i$$

(ii) $\bar{b}_i = b_i$

$$u_i(v_i, b_{-i}) = v_i - b_i$$

$$u_i(b_i, b_{-i}) = \frac{v_i - b_i}{k}, \quad k \geq 2$$

(iii) $\bar{b}_i > b_i$

$$u_i(v_i, b_{-i}) \geq 0$$

$$u_i(b_i, b_{-i}) = 0$$

We proceed analogously when $b_i > v_i$.

It is instructive to draw the
dependence of the function
 $u_i(v_i, b_{-i})$ on b_{-i} . Note
that the function depends only
on $\bar{b}_i$, so we may write

$$u_i(v_i, \bar{b}_i) := u_i(v_i, b_{-i}).$$

We get:

