https://cw.fel.cvut.cz/b251/courses/b4m36ds2/start

Lecture 3

Basic Principles: CAP theorem, Consistency

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Based on the presentation of Martin Svoboda (martin.svoboda@matfyz.cuni.cz)

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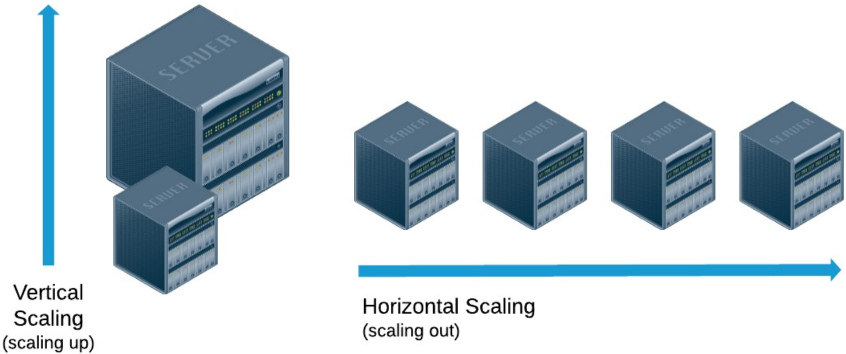
Lecture Outline

Different aspects of **data distribution**

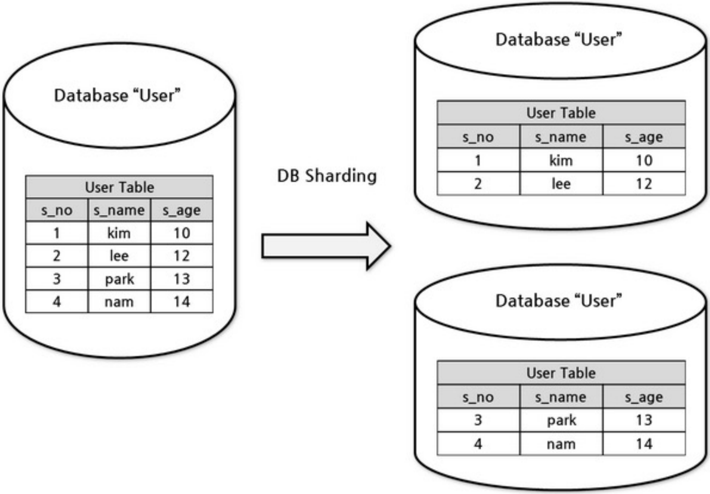
- **Scaling**
  - Vertical vs. horizontal
- **Distribution** models
  - **Sharding**
  - **Replication**: master-slave vs. peer-to-peer architectures
- **CAP** properties
  - **Consistency**, **availability** and partition tolerance
  - ACID vs. **BASE guarantees**
- **Consistency**
  - Read and write quorums

Lecture 2 overview:
Horizontal vs. Vertical Scaling



Source: https://ded9.com/what-is-horizontal-scaling

Lecture 2 overview: Sharding



Source: https://nadermedhatthoughts.medium.com/understand-database-sharding-the-good-and-ugly-868aa1cbc94c

Replication

Replication in distributed systems

Replication refers to maintaining identical copies of data across multiple servers.

The primary **motivations** include:

- **Fault tolerance**:

  System resilience against individual node failures

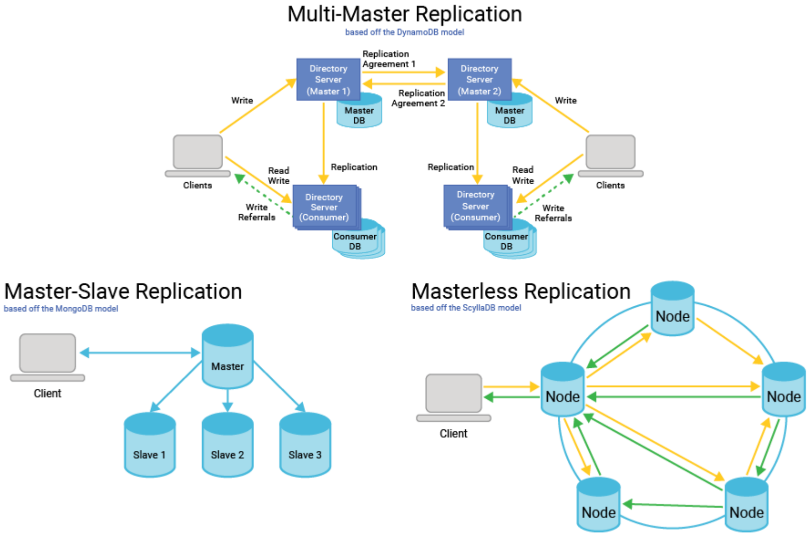
- **High availability**:

  Continued operation during partial system failures

- **Performance optimization**:

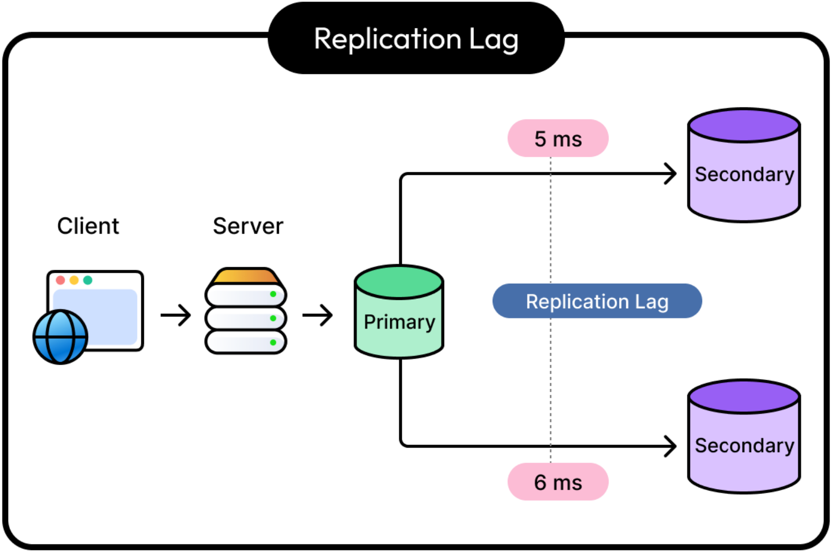
  Reduced latency through geographic proximity

Replication in distributed systems



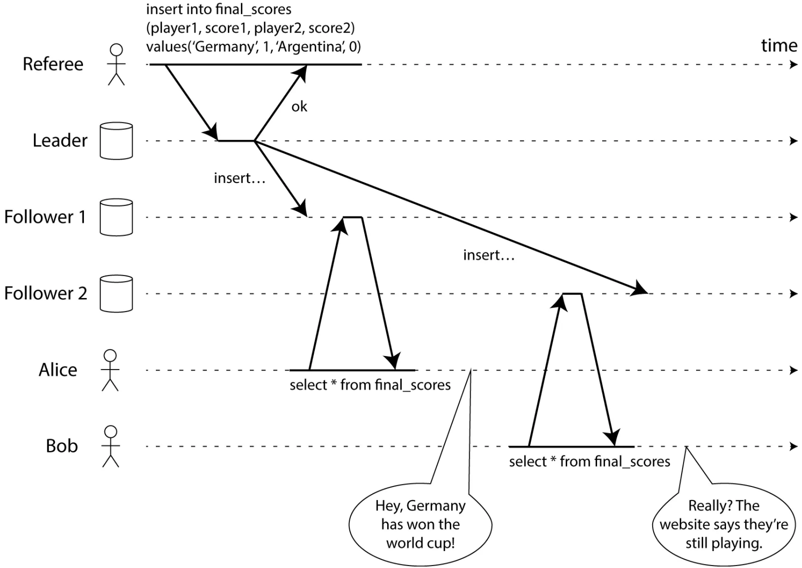
Source: https://www.scylladb.com/glossary/database-replication

Replication Lag



Source: hhttps://blog.bytebytego.com/p/a-guide-to-database-replication-key

Replication Lag



Source: https://tarunjain07.medium.com/cap-theorem-notes-68b04523cbce

Consensus Protocols

Consensus protocols ensure data consistency among replicas. They are essential for making unified decisions about the system's state, especially during failures and network partitions.

Main Protocols:

- Paxos
- Raft
- Viewstamped Replication
- Zookeeper’s Zab Protocol.

Role of Consensus Protocols:

- Ensuring data consistency across replicas.
- Leader or master election within the system.
- Coordinating data updates and managing node failures.

CAP Theorem

CAP Theorem

Assumptions

- Distributed system with **sharding and replication**
- Read and write **operations on a single aggregate** only

CAP properties

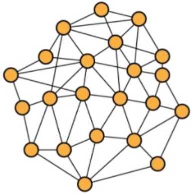
- Properties of a distributed system
- Consistency, Availability, and Partition tolerance **CAP theorem**

> In the presence of a network **partition**, a distributed system can choose either **consistency** or **availability**, but not both.

But, what these properties actually mean?

C : Consistency

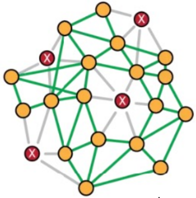
At any given time, all nodes in the network have exactly the same (most recent) value.



= Value: X @ 2018-05-03T08:52:40

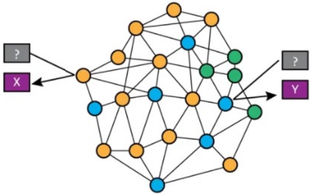
P : Partition tolerance

The network continues to operate, even if an arbitrary number of nodes are failing.



A : Availability

Every request to the network receives a response, though without any guarantee that returned data is the most recent.



= Value: X @ 2018-05-03T08:52:40

= Value: Z @ 2018-05-03T08:32:58

= Value: Y @ 2018-05-03T07:12:12

Source: https://tarunjain07.medium.com/cap-theorem-notes-68b04523cbce

CAP Properties

Property	Formal Definition	Practical Meaning
Consistency	**Linearizability**: Operations appear to execute atomically	All reads return the most recent write
Availability	Every request receives a response (success or failure)	The system always responds, never times out
Partition Tolerance	System continues despite message loss between nodes	Works even when network splits occur

- Hardware failures are inevitable
- Network congestion causes effective partitions
- Slow networks trigger timeouts
- Geographic distribution increases partition probability

CAP Properties: Consistency Details

- **Intuition:** Each read/write on a key is atomic.
- **Formal (linearizability):** There is a single global order of operations; each operation takes effect at an instantaneous point between its call and completion – as if all ran sequentially on one node.
- **Consequence:** After a successful write, any later read of the same key returns the updated value (read-after-write).
- **Replication requirement:** If any replica can serve reads, a write must be replicated to a sufficient set (e.g., a quorum) before acknowledgment to preserve strong consistency.
- **Weaker** consistency models also exist.

CAP Properties

Availability

- **If a node is working, it must respond to user requests**
  - *A bit more formally…*

    Every read or write request successfully received by a non-failing node in the system must result in a response (success or failure), not be silently dropped.

    I.e., their execution must not be rejected

Partition tolerance

- **The system continues to operate even when two or more sets of nodes get isolated**
  - *A bit more formally…*

    The network is allowed to lose arbitrarily many messages sent from one node to another
- I.e. a connection failure must not shut the whole system down

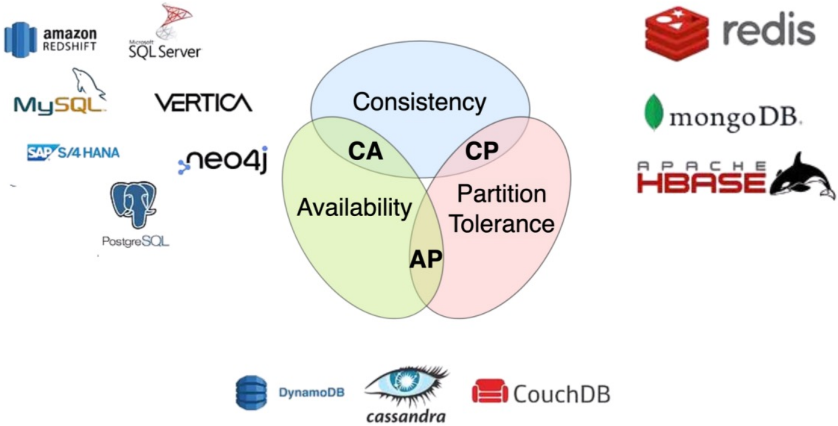
CAP Theorem Proof

- **Proof by contradiction**
  - **Assume all three properties can be satisfied simultaneously**
  - Consider a network partition scenario
- **Partition scenario setup**
  - Network splits into two disjoint sets of nodes: G_1 and G_2
  - No communication possible between G_1 and G_2
- **Write operation on G_1**
  - Client writes to G_1, must be consistent across all replicas
  - G_2 cannot receive this update due to partition
- **Read operation on G_2**
  - If system is available, G_2 must respond to read requests
  - If system is consistent: G_2 must return the updated value

⚡ **Contradiction: G_2 cannot have updated value (violates C) but must respond (requires A)**

$C \land A \land P$ is impossible in distributed systems

CAP Theorem Consequences



Source: https://www.linkedin.com/pulse/cap-theorem-optimizing-database-selection-enhanced-application-kar--ey86f

Consistency Spectrum

- **Strong consistency models**
  - **Linearizability** (strongest for a single operation/key)
  - Transactional models (Serializability / Snapshot Isolation)
  - Sequential consistency
  - Causal consistency
- **Weak consistency models**
  - Session consistency
  - Monotonic read/write consistency
  - **Eventual** consistency (weakest)
- **Consistency vs. Performance trade-off**
  - Stronger consistency → Higher latency
  - Weaker consistency → Better performance
- **Application requirements determine choice**
  - Banking: Strong consistency required
  - Social media: Eventual consistency acceptable
  - Collaborative editing: Causal consistency needed

CAP Theorem Consequences

If **at most two properties** can be guaranteed…

- **CA** = **consistency + availability**
  - Traditional ACID **properties** are easy to achieve
  - Examples: **RDBMS**
  - Any single-node system, but even clusters (at least in theory)
    - However, should the network partition happen, all the nodes must be forced to stop accepting user requests

CA: Consistency + Availability – only possible if **no network partitions occur**
(e.g., traditional RDBMS under normal conditions)

CAP Theorem Consequences

If **at most two properties** can be guaranteed…

- **CP** = **consistency + partition tolerance**
  - Other examples: distributed locking
- **AP** = **availability + partition tolerance**
  - New concept of **BASE properties**
  - Examples: Apache Cassandra, Apache CouchDB.
  - Other examples: web caching, DNS

In real-world environments, network partitions can and do occur. Distributed systems therefore **should be designed to tolerate partitions (P)** and then choose between C and A during a partition. Systems that sacrifice P effectively stop responding when a partition occurs.

CAP Theorem Consequences

Design for partitions in clusters

- Why?
  - Because it is difficult to detect network failures
- Does this mean that only purely CP and AP systems are possible?
  - No…

The real meaning of the CAP theorem:

- *The real world does not need to be just black and white*
- **Partition tolerance** is a must,
  but we can **trade off consistency versus availability**
  - A relaxed consistency can bring a lot of availability.
  - Such trade-offs are not only possible,
    but often work very well in practice

ACID Properties

Traditional **ACID** properties

- **Atomicity**
  - Partial execution of transactions is not allowed (all or nothing)
- **Consistency**
  - Transactions bring the database from one consistent (valid) state to another
- **Isolation**
  - Transactions executed in parallel do not see uncommitted effects of each other
- **Durability**
  - Effects of committed transactions must remain durable

BASE Properties

New concept of **BASE** properties

- Basically Available
  - The system works basically all the time
  - Partial failures can occur, but there are no total system failures
- Soft State
  - The system is in flux (unstable), non-deterministic state
  - Changes occur all the time
- Eventual Consistency
  - Sooner or later the system will be in some consistent state

BASE is just a vague term, no formal definition was provided

- **Proposed to illustrate design philosophies at the opposite ends of the consistency-availability spectrum**

ACID and BASE

ACID

- Choose consistency over availability
- Pessimistic approach
- Implemented by traditional **relational databases**

BASE

- Choose availability over consistency
- Optimistic approach
- Common in **NoSQL databases**
- **Allows levels of scalability that cannot be acquired with ACID**

Historical move:

strong consistency → **eventual consistency**

Current trend in NoSQL:

eventual only → **tunable/stronger** consistency options

Consistency

Consistency

Consistency in general…

- **Consistency is the lack of contradiction** in the database
- However, it has many facets…
  - For example, we only assume atomic operations that constantly manipulate a single aggregate.
    But set operations could also be considered, etc.

Strong consistency is achievable in clusters **with appropriate replication/consensus (e.g., quorum/majority, consensus protocols)**, but **eventual consistency** might often be sufficient.

- A one-minute-old article on a news portal does not matter
- Even when an already unavailable hotel room is booked once again, the situation can still be figured out in the real world
- …

Consistency vs. Latency Trade-offs

- **Strong consistency costs**
  - Synchronous replication to a **quorum/majority** of nodes
  - Latency ≈ latency to the slowest node in the quorum
  - Example: 3 nodes, majority = 2, 100 ms max → ~100 ms latency
- **Weak consistency benefits**
  - Asynchronous replication
  - Latency = latency to a single node
  - Example: 3 nodes, 10ms local → 10ms total latency
- **Real-world measurements**
  - MongoDB: 5ms local read, 50ms strongly consistent read
  - Cassandra: 2ms eventual read, 20ms quorum read
- **Tunable consistency (modern approach)**
  - Applications can choose per-operation
  - Critical operations: strong consistency
  - Non-critical operations: eventual consistency

Consistency

Write consistency (update consistency)

- Problem: **write-write** conflict
  - Two or more write requests on the same aggregate are initiated concurrently
- Context: **peer-to-peer architecture only**
- Issue: lost update
- Solution:
  - **Pessimistic** strategies
    - **Preventing conflicts from occurring**
    - Write locks, …
  - **Optimistic** strategies
    - **Conflicts may occur, but are detected and resolved later on**
    - Version stamps, vector clocks, …

Consistency

Read consistency (replication consistency)

- Problem: **read-write** conflict
  - Write and read requests on the same aggregate are initiated concurrently
- Context: **both master-slave and peer-to-peer architectures**
- Issue: inconsistent read
- When not treated, **inconsistency window** will exist
  - **Propagation of changes to all the replicas takes some time**
  - Until this process is finished, inconsistent reads may happen
  - <u>Even the initiator of the write request may read wrong data!</u>
    - Session consistency / read-your-writes / sticky session

Strong Consistency

How many nodes need to be involved to get strong consistency?

General rule: R + W > N (read and write quorums must intersect)

- **Write quorum**: $W > N/2$

  Idea: a majority write ensures only one write can succeed at a time

  W = number of nodes successfully acknowledged the write

  N = number of nodes involved in replication (replication factor)

- **Read quorum**: choose **R** such that **R + W > N** (e.g., **R > N − W**)

Idea: intersecting quorums ensure reads see the latest committed write

R = number of nodes participating in the read

If the retrieved replicas return different versions, resolve to the **latest committed version** (e.g., via version/timestamp) and then return it.

When a quorum is not attained → the request cannot be handled

Strong Consistency

Examples

Examples for replication factor $N = 3$

- Write quorum $W = 3$ and read quorum $R = 1$
  - All the replicas are always updated
  - $\Rightarrow$ we can read any one of them
- **Write quorum** $W = 2$ **and read quorum** $R = 2$
  - *Typical configuration, reasonable trade-off*

Consequence

- **Quora can be configured to balance read and write workload**
  - The higher the write quorum is required,
    the lower the read quorum can then be required

Bank:
Different Tasks = Different Decisions

Prefer CP semantics

- Account Balance
- Money Transfers
- Loan Approvals
- Transaction Processing
- Credit Limits

Prefer AP semantics

- Transaction History
- Product Recommendations
- Market News
- Branch Locator
- Customer Chat

Online Store: Customer Journey

E-commerce System

Product Browsing
AP
Discovery over accuracy

Shopping Cart
Mixed
Session consistency

Inventory Check
CP
Prevent overselling

Payment Processing
CP
Financial accuracy

Order Confirm
CP
Customer trust

University: Academic vs Administrative

Academic Functions (CP)

- Student Grades
- Course Registration
- Tuition Payments
- Financial Aid
- Transcripts

Campus Services (AP)

- Library Search
- Campus Events
- Dining Menus
- Student Organizations
- News & Updates

University:
Critical Example – Course Registration

Problem: Popular Course with Limited Seats

'Machine Learning 101' - 30 seats, 200 students at 8 AM → Need fair, accurate registration

Solution: CP (Consistency Required): the system may sacrifice availability to avoid overbooking.

Trade-off: System slower during peak times, but zero overbooking

Universal Patterns Across Industries

Function Type	Bank	E-commerce	University	Pattern
Money/Financial	CP	CP	CP	Usually CP
User Identity	CP	Mixed	CP	Usually CP
Limited Resources	—	CP	CP	Usually CP
Content/Search	AP	AP	AP	Usually AP
History/Logs	AP	AP	AP	Usually AP
Recommendations	AP	AP	AP	Usually AP

Function type predicts CP/AP choice across all industries

How to Decide: CP or AP?

1 **Identify Function Type**

Financial? → Usually **CP**
Content? → Usually **AP**
Registration? → Usually **CP**

2 **Analyze Error Impact**

Money lost? → **CP** required
User frustration? → **AP** better
Legal issue? → **CP** required

3 **User Expectations**

Instant response? → **AP**
Accuracy critical? → **CP**
Both needed? → Hybrid

4 **Design Implementation**

CP: Transactions, locks
AP: Caches, replicas
Mixed: Different DBs

Lecture Conclusion

There is a wide range of options influencing…

- **Availability** – when nodes may refuse to handle user requests?
- **Consistency** – what level of consistency is required?
- **Latency** – how long does it take to handle user requests?
- **Durability** – is the committed data written reliably?
- **Resilience** – can the data be recovered in case of failures?

$\Rightarrow$ it's good to know these properties and choose the right trade-off