# Nuclear imaging PET. SPECT

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#### Resources

- http://www.bic.mni.mcgill.ca/~louis/seminars/399-650/pet.html
- http://ocw.mit.edu/NR/rdonlyres/Nuclear-Engineering/ 22-01Introduction-to-Ionizing-RadiationFall2003/ 60AA5867-88AE-49C7-9478-2F4661B4EBBE/0/pet\_spect.pdf
- http: //www.pet.mc.duke.edu/rsna04/turk-petspectphysicsRSNA2005.pdf
- http://www.nuclear.kth.se/courses/medphys/5A1414/TOFPET1.pdf
- http://www.fmri.org,
- A. Webb: Introduction to Biomedical Imaging
- ▶ images by: Wikipedia, NIH, Moazemi et al., Rager et al., Virginia Commonwealth University...

#### Principles of nuclear imaging

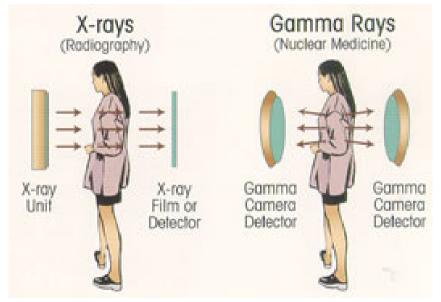
Radioactivity

Gamma camera

**SPECT** 

PET

Conclusions



- ► X-ray and CT
  - transmission imaging, external source

- ► PET, SPECT
  - emission imaging, source internal to body

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  - ► Anatomic imaging (shape, fracture)

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  - ► Functional imaging (metabolism, perfusion), tracer concentration

#### ► X-ray and CT

- transmission imaging, external source
- Anatomic imaging (shape, fracture)
- X-rays

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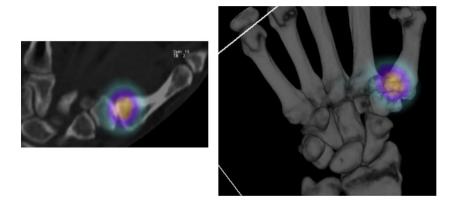
- emission imaging, source internal to body
- Functional imaging (metabolism, perfusion), tracer concentration
- $ightharpoonup \gamma$  rays

#### X-ray and CT

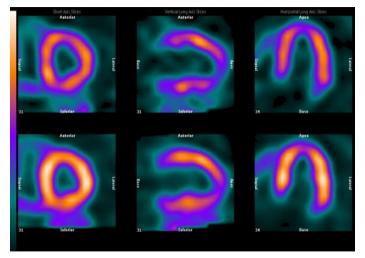
- transmission imaging, external source
- Anatomic imaging (shape, fracture)
- X-rays
- ► Good resolution, < 1 mm

#### ► PET, SPECT

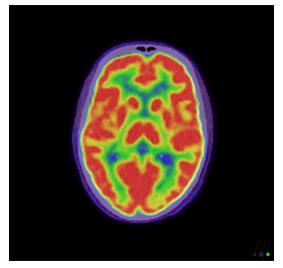
- emission imaging, source internal to body
- Functional imaging (metabolism, perfusion), tracer concentration
- $ightharpoonup \gamma$  rays
- ► Lower resolution,  $5 \sim 20 \, \text{mm}$



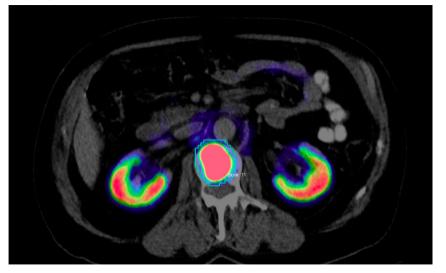
 $Hand,\ osteoarthritis,\ CT+SPECT$ 



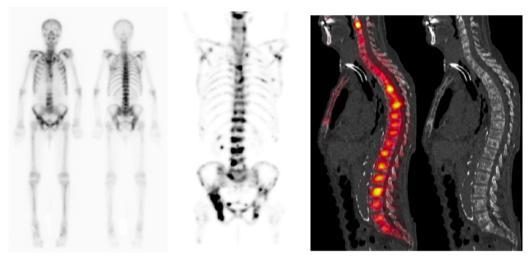
Heart, myocardial perfusion, PET



Brain, FDG PET, metabolism



Renal (kidney) PET+CT, Ga-PSMA contrast agent.



 ${\sf Metastases,\ SPECT+CT,\ MIP}$ 

#### Principles of nuclear imaging

#### Radioactivity

#### Radioactive decay

Radionuclide production Cyklotron Radiopharmaceuticals

#### Gamma camera

**SPECT** 

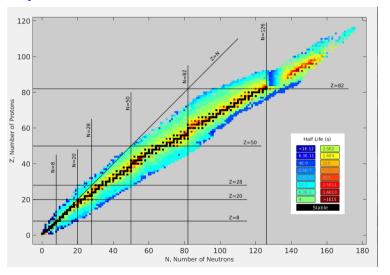
**PET** 

#### Conclusions

#### Radioactivity

- ▶ element = same number of protons
- ▶ isotope/nuclide = same number of protons and neutrons
- $\blacktriangleright$  excess of neutrons/protons  $\rightarrow$  instability  $\rightarrow$  radioactive decay chain  $\rightarrow$  stable isotope

### Valley of stability



Isotopes with Z slightly smaller than N are stable.

### Radioactive decay modes

Unstable parent nucleus  $\longrightarrow$  Daughter nucleus + particles (energy)

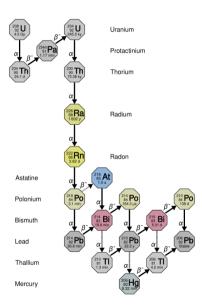
- ightharpoonup Alpha decay  $(\alpha)$
- ightharpoonup Beta decay ( $\beta$ )
- ▶ Positron decay  $(\beta^+)$
- Isomeric transition
- Electron capture
- ▶ Proton emission, neutron emission, . . .

#### Alpha decay

- ▶ Spontaneous emission of  $\alpha$  particles
  - ≥ 2 protons + 2 neutrons, <sup>4</sup><sub>2</sub>He, charged
  - energy 4  $\sim$  8 MeV, speed 0.05c
  - $\blacktriangleright$  strong interaction, low penetration (cm in air,  $\mu$ m in tissue), easy shielding
  - important biological effects (relative biological effectiveness 20), DNA damage
  - no use in imaging, used in therapy
- ▶ happens in heavy nuclei (radium, polonium, uranium, thorium, radon, ...) and Be
- lacktriangle excess energy released as  $\gamma$  (electromagnetic) rays (photons)

$$\begin{array}{c} \overset{A}{Z}\mathsf{X} \stackrel{\alpha}{\longrightarrow} \overset{A-4}{Z-2}\mathsf{Y} + \overset{4}{\underbrace{\mathsf{He}}} \\ \underbrace{\overset{226}{88}\mathsf{Ra}} \stackrel{\alpha}{\longrightarrow} \underbrace{\overset{222}{86}\mathsf{Rn}} + \underbrace{\overset{4}{\underbrace{\mathsf{He}}}} \\ \overset{radium}{\operatorname{radion}} \stackrel{\alpha}{\longrightarrow} \underbrace{\overset{218}{84}\mathsf{Po}} \stackrel{\alpha}{\longrightarrow} \dots \xrightarrow{\overset{206}{82}} \mathsf{Pb} \end{array}$$

# Decay chain



### Beta decay

- $\triangleright$   $\beta$  particles = electrons e<sup>-</sup>
- ► Neutron conversion

$$n \stackrel{\beta}{\longrightarrow} p + e^- + \bar{\nu}_e$$

 $\bar{\nu}_e$  — electron antineutrino

$$_{Z}^{A}X \xrightarrow{\beta} _{Z+1}^{A}Y + e^{-} + \bar{\nu_{e}}$$

- For neutron-rich (N > Z) isotopes
- ightharpoonup e $^-$  ejected with high energy (eta rays), continuous spectrum
- remaining energy =  $\bar{\nu_e}$ , nucleus recoil
- $lackbox{ excited state nucleus} \longrightarrow \gamma \text{ rays}$

### Beta decay

#### Examples

#### Isomeric transition

Excited state nucleus  $\longrightarrow \gamma$  rays

Metastable **Technetium**  $^{99m}_{43}$ Tc

$$^{98}_{42}\text{Mo} \longrightarrow ^{99}_{42}\text{Mo}$$
 neutron bombardment

$$^{99}_{42} ext{Mo} \stackrel{eta}{\longrightarrow} ^{99m}_{43} ext{Tc} + ext{e}^- + ar{
u_e} \qquad ext{half-life 2.7 days}$$

$$^{99m}_{43}$$
Tc  $\stackrel{\gamma}{\longrightarrow} ^{99}_{43}$ Tc

half-life 6 h

#### Isomeric transition

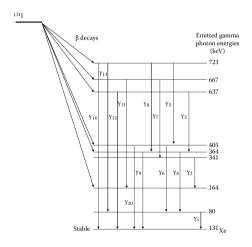
Excited state nucleus  $\longrightarrow \gamma$  rays

Metastable **Technetium**  $^{99m}_{43}$ Tc

- most commonly used medical radioisotope
- $ightharpoonup \gamma$  (photon) energy 140 keV

# Multiple decay processes

#### lodine



### Positron decay

 $\beta^+$  decay

- $\triangleright \beta^+$  particles = positrons e<sup>+</sup>
- Proton conversion

$$p \xrightarrow{\beta^+} n + e^+ + \nu_e$$

 $\nu_e$  — electron neutrino

$$_{Z}^{A}X \xrightarrow{\beta^{+}} _{Z-1}^{A}Y + e^{+} + \nu_{e}$$

For proton-rich (N < Z) isotopes

### Positron decay

 $\beta^+$  decay

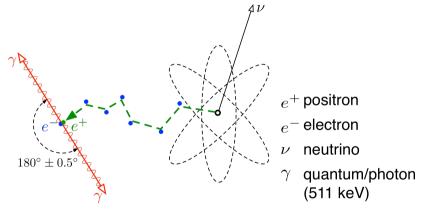
#### Examples

$$\begin{array}{c} ^{23}_{12} \text{Mg} \stackrel{\beta^+}{\longrightarrow} ^{23}_{11} \text{Na} + \text{e}^+ + \nu_e & \quad \text{half-life 11 s} \\ ^{68}_{31} \text{Ga} \stackrel{\beta^+}{\longrightarrow} ^{68}_{30} \text{Zn} + \text{e}^+ + \nu_e & \quad \text{half-life 68 min} \end{array}$$

### Positron decay

 $\beta^+$  decay

▶ Positron  $e^+$  is **annihilated**:  $e^+ + e^+ \longrightarrow \gamma + \gamma$ 



- two photons with energy 511 keV
- lacktriangle Parent/daughter nuclide energy difference  $\gtrsim 1\,\mathrm{MeV}$

#### Electron capture

Proton absorbs inner electron

$$p + e^{-} \xrightarrow{EC} n + \nu_{e}$$

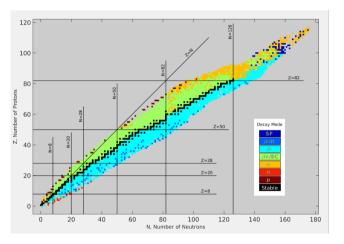
$${}_{Z}^{A}X + e^{-} \xrightarrow{EC} {}_{Z-1}^{A}Y + \nu_{e}$$

Example:

$$\underbrace{\begin{array}{ccc}
51\\24\\\text{Cr}
\end{array}} + e^{-} \xrightarrow{\text{EC}} \underbrace{\begin{array}{c}
51\\23\\\text{Vanadium}
\end{array}} + \nu_{e}$$

- Neutrino carries all energy (characteristic spectrum)
- ► Can occurr for smaller energy differences
- ightharpoonup Excited state nucleus  $\longrightarrow \gamma$  rays

### Decay mode chart



black: stable, light blue:  $\beta$ , green:  $\beta^+$  or electron capture, orange:  $\alpha$ , dark blue: fission, red: neutron emission, brown: proton emission

### Nuclear imaging methods

#### ▶ SPECT

- $ightharpoonup \gamma$  camera (2D)
- single photon emission computed tomography (3D)
- $ightharpoonup \gamma$  photon emitters

#### ► PET

- positron emission tomography (3D)
- positron emitters

### Ideal radionuclides for SPECT imaging

- Physical half-life long enough to allow preparation
- Physical half-life short enough to minimize long-term effects
- ightharpoonup Pure  $\gamma$  emitter (isomeric transition, electron capture)
- Photon energy high-enough to penetrate tissue
- Photon energy low-enough for efficient shielding and detection

# Single photon emitters

for SPECT nuclear imaging

Nuclide		Half-life	$E_{photon}$ [keV]	
Technetium	<sup>99</sup> <sup><i>m</i></sup> Tc	6 h	140	most used
lodine	123 <sub>53</sub> 1	13 h	159	thyroid imaging
Indium	$_{53}^{111}$ In	$2.8\mathrm{d}$	171, 245	good, expensive
Thallium	<sup>201</sup> TI	3 d	$70 \sim 80$	cardiac perfussion
Gallium	$_{31}^{67}$ Ga	3.25 d	$90 \sim 400$	tumor localization
lodine	<sup>131</sup> <sub>53</sub>	8.1 d	$364\sim606$	radiotherapy

#### Positron emitters

for PET nuclear imaging

Nuclide		Half-life	
Rubidium	<sup>82</sup> <sub>37</sub> Rb	1.3 min	cardiac imaging
Oxygen	<sup>15</sup> 0	2 min	
Nitrogen	$_{7}^{13}N$	10 min	
Carbon	11 <sub>6</sub> C	20.3 min	
Gallium	$_{31}^{68}$ Ga	68 min	tumor localization
Fluorine	<sup>18</sup> <sub>9</sub> F	110 min	most often used, FDG
Copper	<sup>64</sup> Cu	12.7 h	oncology, radiotherapy

Mostly short half-time — need to be produced in-situ.

#### Activity

- Activity A[Bq], 1Bq = 1 desintegration/s,
- ▶ Older unit  $1 \text{ Ci} = 3.7 \cdot 10^{10} \text{ Bq} 1 \text{ g of radium}$

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- ▶ Older unit  $1 \text{ Ci} = 3.7 \cdot 10^{10} \text{ Bq} 1 \text{ g of radium}$
- For N nuclei and a decay constant  $\lambda$

$$A = \lambda N = -\frac{\mathrm{d}N}{\mathrm{d}t}$$

# Exponential decay

► Exponential decay of *N* 

$$N = N_0 \mathrm{e}^{-\lambda t}$$

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Half-life

$$egin{align} \mathcal{T}_{1/2} &= \log 2/\lambda pprox 0.693/\lambda \text{ [s]} \ \mathcal{N} &= \mathcal{N}_0 \left(rac{1}{2}
ight)^{rac{t}{T_{1/2}}} \ \end{aligned}$$

# Exponential decay

Exponential decay of N

$$N = N_0 e^{-\lambda t}$$

► Half-life

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ight)^{rac{t}{T_{1/2}}} \end{aligned}$$

Exponential decay of A

$$A = A_0 e^{-\lambda t}$$
, with  $A_0 = \lambda N_0$ ,  $A = \lambda N$ 

### Effective half-life

- ightharpoonup Physical half-life  $T_p$
- ► Biological half-life T<sub>b</sub>
- ► Effective half-life T<sub>e</sub>

$$\frac{1}{T_e} = \frac{1}{T_p} + \frac{1}{T_b}$$

### Effective half-life

- ightharpoonup Physical half-life  $T_p$
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- ightharpoonup Effective half-life  $T_e$

$$\frac{1}{T_e} = \frac{1}{T_p} + \frac{1}{T_b}$$

Note:  $T_e < T_p$ ,  $T_e < T_b$ 

### **Effective Half-Life**

E.g., for an isotope with a 6-hr half life attached to various carrier molecules with different biological half-lives.

$T_{B}$	T <sub>E</sub>	
1 hr	0.86 h	
6 hr	3 hr	
60 hr	5.5 hr	
600 hr	5.9 hr	
	1 hr 6 hr 60 hr	

### **Effective Half-Life**

#### Assume 106 Bq localized in a tumor site, vary T

Nuclide	Half-life (T)	λ (sec <sup>-1</sup> )	N
1	6 sec	0.115	8.7 x 10 <sup>7</sup>
2	6 min	1.75 x 10 <sup>-3</sup>	5.7 x 10 <sup>9</sup>
3	6 hrs	3.2 x 10 <sup>-5</sup>	3.1 x 10 <sup>11</sup>
4	6 days	1.3 x 10 <sup>-6</sup>	7.7 x 10 <sup>12</sup>
5	6 years	4 x 10 <sup>-9</sup>	2.5 x 10 <sup>15</sup>

### **Effective Half-Life**

Assume 1010 atoms of radionuclide localized in a tumor site, vary T

Nuclide	Half-life (T)	λ (sec-1)	Activity (Bq)
1	6 sec	0.115	1.15 x 10 <sup>9</sup>
2	6 min	1.75 x 10 <sup>-3</sup>	1.7 x 10 <sup>7</sup>
3	6 hrs	3.2 x 10 <sup>-5</sup>	3.2 x 10 <sup>6</sup>
4	6 days	1.3 x 10 <sup>-6</sup>	1.3 x 10 <sup>4</sup>
5	6 years	4 x 10 <sup>-9</sup>	40

#### Principles of nuclear imaging

#### Radioactivity

Radioactive decay

Radionuclide production

Cyklotron

Radiopharmaceuticals

#### Gamma camera

**SPECT** 

**PET** 

Conclusions

### Radionuclide production

- Neutron capture
- Nuclear fission
- ► Radionuclide generator
- ▶ (Poisitive) ion bombardment
  - Linear accelerator
  - Cyclotron

### Neutron capture

Neutron activation/neutron bombardment

- ightharpoonup Nuclear reactor, "thermal" neutrons, low energy  $0.03\sim100\,\mathrm{eV}$
- ightharpoonup Yield depends on neutron flow  $\phi$ , cross section  $\sigma$ , decay constant  $\lambda$ , amount of carrier (source) material
- Chemical/physical purification

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- Chemical/physical purification

$$n + {}^{98}_{42}Mo \longrightarrow {}^{99}_{42}Mo + \gamma$$

with proton emission

$$n + {}^{32}_{16}S \longrightarrow {}^{32}_{15}P + p \qquad \text{half-life 14 days}$$

### Radionuclides produced by neutron capture

#### Radionuclides produced by neutron absorption.

Radionuclide	Production Reaction	Gamma-Ray Energy (keV)	Half-Life	σ (Barn)
<sup>51</sup> Cr	<sup>50</sup> Cr(n, γ) <sup>51</sup> Cr	320	27.7 days	15.8
<sup>59</sup> Fe	$^{58}$ Fe(n, $\gamma$ ) $^{59}$ Fe	1099	44.5 days	1.28
<sup>99</sup> Mo	$^{98}$ Mo(n, $\gamma$ ) $^{99}$ Mo	740	66.02 h	0.13
131 <b>I</b>	$^{130}\text{Te}(n, \gamma)$ $^{131}\text{Te} \rightarrow ^{131}\text{I}$	364	8.04 days	0.29

Source: From Mughabghab et al., 1981.

Mostly used for radiotherapy (except \$\frac{99}{42}\$Mo)

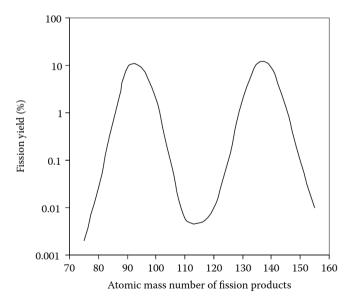
### Nuclear fission

- ► Heavy nuclei (A > 92)  $^{235}_{92}$ U,  $^{237}_{92}$ U,  $^{239}_{94}$ Pu,  $^{232}_{90}$ Th irradiated by neutrons unstable
- Fission example

$$^{235}_{92}$$
U +  $^{1}_{0}$ n  $\longrightarrow ^{99}_{42}$ Mo +  $\overset{133}{\underbrace{50}}$ Sn +  $^{1}_{0}$ n

Chemical/physical purification

# Fission product yield for $^{235}_{92}\mathrm{U}$



# Radionuclides produced by nuclear fission

Isotope	Gamma-Ray Energy (keV)	Half-Life	Fission Yield (%)
<sup>99</sup> Mo	740	66.02 h	6.1
$^{131}\mathrm{I}$	364	8.05 days	2.9
<sup>133</sup> Xe	81	5.27 days	6.5
<sup>137</sup> Cs	662	30 a	5.9

Source: From BRH, 1970.

### Radionuclide generator

- ► Long half-time parent isotope
- ▶ Short half-time daughter isotope,  $\lambda_2 > \lambda_1$

# Radionuclide generator

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- ▶ Short half-time daughter isotope,  $\lambda_2 > \lambda_1$
- ▶ Daughter activity (for  $A_{20} = 0$ )

$$A_2 = \frac{\lambda_1}{\lambda_2 - \lambda_1} A_{10} \left( e^{-\lambda_1 t} - e^{-\lambda_2 t} \right)$$

# Radionuclide generator

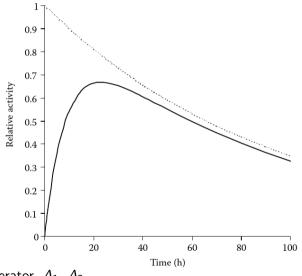
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$$A_2 = \frac{\lambda_1}{\lambda_2 - \lambda_1} A_{10} \left( e^{-\lambda_1 t} - e^{-\lambda_2 t} \right)$$

• After  $\sim 10 T_{1/2}^{(2)}$ , transient equilibrium

$$A_1 = A_{10} e^{-\lambda_1 t}, \qquad A_2 = A_1 \frac{\lambda_1}{\lambda_2 - \lambda_1}$$

### Transient equilibrium

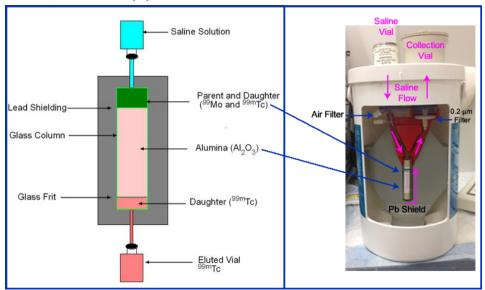


 $^{99}_{42}\mathrm{Mo}/^{99m}_{43}\mathrm{Tc}$  generator,  $A_1,~A_2$ 

### Technetium generator

- 99/42 Mo produced by fission or neutron bombardment, half-life 67 h
- Adsorbed to alumina Al<sub>2</sub>O<sub>3</sub>
- $ightharpoonup {99 \over 42} Mo \stackrel{\beta}{\longrightarrow} {99 \over 43} Tc$  (and 15% to  ${99 \over 43} Tc$ ),
- ► <sup>99m</sup><sub>43</sub>Tc half-life 6 h
- 99m Tc is eluted by physiological saline solution
- $ightharpoonup rac{99m}{43}$ Tc can by chemically manipulated
- ▶ When unused, the ratio  $^{99}_{43}$ Tc/ $^{99m}_{43}$ Tc increases

# Technetium generator (2)



# Radionuclides produced by generators

Parent P	Parent Half-Life	$\begin{array}{c} \textbf{Mode of} \\ \textbf{Decay} \\ \textbf{P} \rightarrow \textbf{D} \end{array}$	Daughter D	Mode of Decay of D	Daughter Half-Life	Daughter γ Energy (keV)
<sup>62</sup> Zn	9.1 h	$\beta^+$	<sup>62</sup> Cu	β+	9.8 min	511
		EC		EC		1173
<sup>68</sup> Ge	280 days	EC	<sup>68</sup> Ga	β+	68 min	511
				EC		1080
$^{81}$ Rb	4.7 h	EC	$^{81}\mathrm{Kr^m}$	IT	13 s	190
$^{82}$ Sr	25 days	EC	$^{82}$ Rb	EC	76 s	777
				β+		511
<sup>99</sup> Mo	66.02 h	$\beta^-$	<sup>99</sup> Tc <sup>m</sup>	IT	6.02 h	140
<sup>113</sup> Sn	115.1 days	EC	$^{113}In^{m}$	IT	1.66 h	392
<sup>195</sup> Hg <sup>m</sup>	40 h	IT	$^{195}Au^{m}$	IT	$30.6\mathrm{s}$	262
		EC				

### Principles of nuclear imaging

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Conclusions

### Proton/ion bombardment

- ► Charged particles: mostly  $p = {}^{1}_{1}H^{+}$ , also  ${}^{2}_{1}D^{+}$ ,  ${}^{3}_{2}He^{2+}$ ,  ${}^{4}_{2}He^{2+}$
- ightharpoonup Accelerated to high energies by a linear accelerator or cyclotron (typical  $E_{p}\sim18\, {
  m MeV})$
- hit target, get absorbed in the nucleus, knock out a neutron
- Typical reactions

$${}^{11}_5B + p \longrightarrow {}^{11}_6C + n$$
  

$${}^{68}_{30}Zn + p \longrightarrow {}^{67}_{31}Ga + 2n$$
  

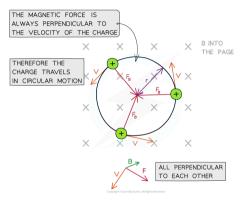
$${}^{18}_8O + p \longrightarrow {}^{18}_9F + n$$

• neutron deficit  $\longrightarrow \beta^+$  emitters (or EC), mostly short-lived

# Radionuclides produced by ion bombardment

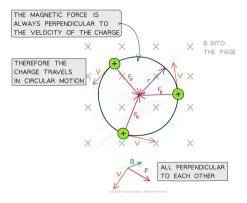
Radionuclide	Principal Gamma-Ray Energy (keV)	Half-Life	Production Reaction
11C	511 (β+)	20.4 min	<sup>14</sup> N(p, α) <sup>11</sup> C
$^{13}N$	511 (β <sup>+</sup> )	9.96 min	$^{13}$ C(p, n) $^{13}$ N
<sup>15</sup> O	511 (β <sup>+</sup> )	2.07 min	$^{15}N(p, n)^{15}O$
$^{18}$ F	511 (β+)	109.7 min	$^{18}O(p, n)^{18}F$
<sup>67</sup> Ga	93, 184, 300	78.3 h	<sup>68</sup> Zn(p, 2n) <sup>67</sup> Ga
<sup>111</sup> In	171, 245	67.9 h	<sup>112</sup> Cd(p, 2n) <sup>111</sup> In
$^{120}\mathrm{I}$	511 (β <sup>+</sup> )	81 min	$^{127}\text{I}(p, 8n)^{120}\text{Xe} \rightarrow ^{120}\text{I}$
<sup>123</sup> I	159	13.2 h	$^{124}\text{Te}(p, 2n)^{123}\text{I}$ $^{127}\text{I}(p, 5n)^{123}\text{Xe} \rightarrow ^{123}\text{I}$
$^{124}\mathrm{I}$	511 (β <sup>+</sup> )	4.2 days	$^{124}\text{Te}(p, n)^{124}\text{I}$
<sup>201</sup> Tl	68-80.3	73 h	$^{203}\text{Tl}(p, 3n)^{201}\text{Pb} \rightarrow ^{201}\text{Tl}$

#### Cyclotron principle



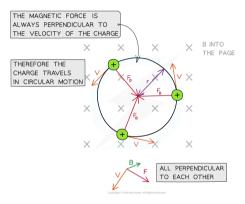
▶ Magnetic (Lorentz) force  $\mathbf{F} = \mathbf{I} \times \mathbf{B} = q\mathbf{v} \times \mathbf{B}$ , perpendicular to  $\mathbf{v}$  and  $\mathbf{B} \longrightarrow$  circular motion

#### Cyclotron principle



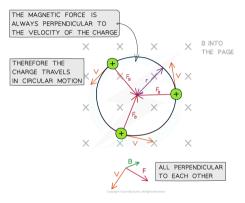
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- ► Centripetal=centrifugal force  $F = mv^2/r$

#### Cyclotron principle



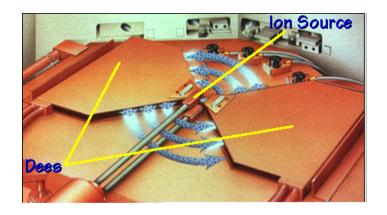
- ▶ Magnetic (Lorentz) force  $\mathbf{F} = \mathbf{I} \times \mathbf{B} = q\mathbf{v} \times \mathbf{B}$ , perpendicular to  $\mathbf{v}$  and  $\mathbf{B} \longrightarrow$  circular motion
- ► Centripetal=centrifugal force  $F = mv^2/r$
- $ightharpoonup r = \frac{mv}{Ba}$ , since  $v \sim r \longrightarrow$  constant f

#### Cyclotron principle



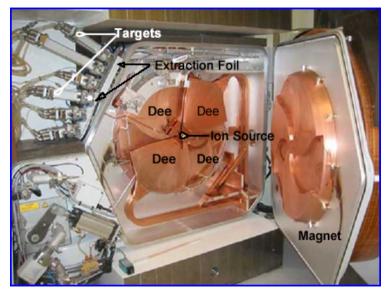
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- ► Centripetal=centrifugal force  $F = mv^2/r$
- $ightharpoonup r = \frac{mv}{Ra}$ , since  $v \sim r \longrightarrow$  constant f
- ▶ Neglecting relativistic mass increase, electrode shape

# Cyclotron

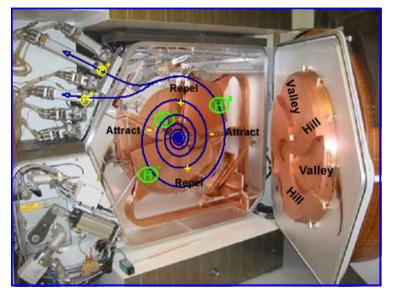


- Vacuum
- ► Ion source (batch), mostly H<sup>-</sup>
- ► Hollow 'D' electrodes, high frequency AC voltage (MHz)
- ► Magnetic field (oriented vertically)

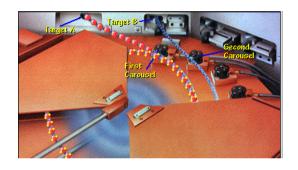
### Real cyclotron



# Real cyclotron

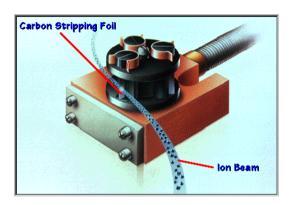


### Carousel



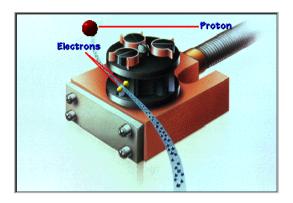
- ightharpoonup after  $\sim$  100s of cycles
- ▶ H<sup>-</sup> ion hits a thin carbon foil
- $lackbox{}\longrightarrow$  looses electrons, converted p  $=\mathrm{H}^+$
- ▶ → opposite curvature
- Only part of the beam is deviated
- Foil lasts  $\sim 100$  hours

### Carousel



- ightharpoonup after  $\sim$  100s of cycles
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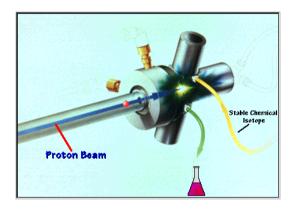
### Carousel



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- ▶ Only part of the beam is deviated
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### Target chamber

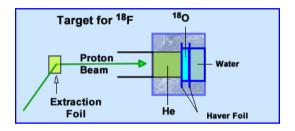
#### Reakční komora



- ► Filled with a stable isotope
- ► Radioactive isotope is created
- ► Shielded, small, easy to change

#### Target chamber

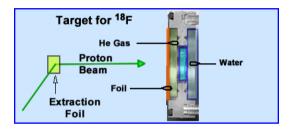
#### Reakční komora



- ▶  $^{18}_{8}$ O rare (0.2%), enrichment needed (distillation, very small  $\Delta T_{boil}$ )
- Cooling needed (by water)
- ► Thin cobalt alloy foils (havar)
- ► Every few hours, <sup>18</sup><sub>9</sub>F can be extracted

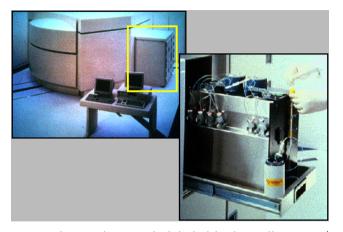
#### Target chamber

Reakční komora



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- $\blacktriangleright$  Every few hours,  $^{18}_9 F$  can be extracted

# Biosynthesizer



- ▶ Radiopharmaceutical radioactively labeled biologically active/compatible chemical compound.
- ▶ Quantitative & qualitative imaging of physiological processes.

#### Principles of nuclear imaging

#### Radioactivity

Radioactive decay Radionuclide production Cyklotron Radiopharmaceuticals

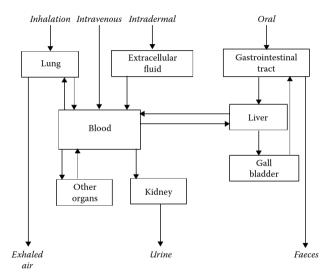
Gamma camera

**SPECT** 

PET

Conclusions

#### Administration, distribution and excretion



Must traverse membranes to get to the targete organ.

## Administration of radiopharmaceuticals

- Mostly physiological (saline) solution
- ► Blood-brain barrier
  - Intravenously administered contrast agent does not get to the brain
  - Contrast agent administered to the cerebro-spinal fluid only gets to the brain and spine.

#### Administration of radiopharmaceuticals

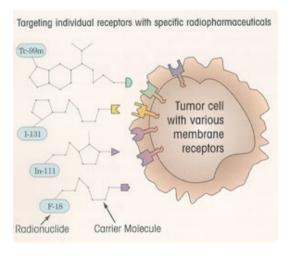
- ► Mostly physiological (saline) solution
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- Other metabolic barriers (blood-ocular, blood-air, ...)

#### Administration of radiopharmaceuticals

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- Other metabolic barriers (blood-ocular, blood-air, ...)
- Imaging afinity and metabolism speed

## Radiopharmaceutical construction

Radionuclide + carrier molecule (+ probe)



Radionuclide	Pharmaceutical	Indication/Use	Typical Administered Activity (MBq)	
<sup>67</sup> Ga	Citrate	Tumour imaging, infection/ inflammation imaging	150ª	
${}^{81}\mathrm{Kr^m}$	Krypton gas	Lung ventilation imaging	6000 <sup>a</sup>	
<sup>99</sup> Tc <sup>m</sup>	Albumin	Cardiac blood-pool imaging, peripheral vascular imaging	800°	
$^{99}\mathrm{Tc^m}$	Colloids, including tin colloid and sulphur colloid	Oesophageal transit and reflux Liver imaging Bone marrow imaging, GI bleeding	40° 80°, 200 (SPECT)° 400°	
99Tcm	DTPA	Lung ventilation imaging (aerosol)	80 <sup>a</sup>	
		Renal imaging/renography	300 <sup>a</sup>	
		Brain imaging (static)	500a, 800 (SPECT)a	
		First-pass blood-flow studies	800a	
<sup>99</sup> Tc <sup>m</sup>	DMSA	Renal imaging (DMSA(III)) Tumour imaging (DMSA(V))	$80^{a}$ $400^{a}$	
<sup>99</sup> Tc <sup>m</sup>	ECD	Brain imaging	500 <sup>a</sup>	
99Tcm	Erythrocytes (normal)	GI bleeding	400a	
		Cardiac blood-pool imaging or peripheral vascular imaging	800 <sup>a</sup>	
99Tcm	Erythrocytes (heat denatured)	Spleen imaging	100 <sup>a</sup>	
99Tcm	Exametazime	Cerebral blood-flow imaging (SPECT)	500a	
99Tcm	Iminodiacetates (IDAs)	Functional biliary system imaging	150a	
<sup>99</sup> Tc <sup>m</sup>	Leucocytes	Infection/inflammation imaging	200 <sup>a</sup>	

Radionuclide		Pharmaceutical	Indication/Use	Administered Activity (MBq)
	99Tcm	Macroaggregated albumin	Lung perfusion imaging	100a, 200 (SPECT)a
	99Tcm	MAG3	Renal imaging/renography First-pass blood-flow imaging	100°a 200°a
	99Tcm	Nanocolloids	Lacrimal drainage Sentinel node or lymph node imaging	4a 20a
	99Tcm	Pertechnetate	Micturating cystogram Thyroid uptake	25 <sup>a</sup> 40 <sup>a</sup>
			Thyroid imaging, salivary gland imaging	80 <sup>a</sup>
			Ectopic gastric mucosa imaging (Meckel's)	$400^{\mathrm{a}}$
			First-pass blood-flow imaging	800a
	99Tcm	Phosphonate and phosphate compounds	Bone imaging	600a, 800 (SPECT)a
<sup>99</sup> Tc <sup>m</sup>		Sestamibi	Myocardial imaging Tumour imaging, breast imaging	300°, 400 (SPECT)° 900°
99Tcm		Sulesomab	Infection/inflammation imaging	750a
99Tcm		Technegas	Lung ventilation imaging	$40^{\mathrm{a}}$
<sup>99</sup> Tc <sup>m</sup>		Tetrofosmin	Myocardial imaging Parathyroid imaging	300a, 400 (SPECT)a 900a
<sup>111</sup> In		Capromab Pendetide	Biopsy-proven prostate carcinoma imaging	185 <sup>b</sup>
<sup>111</sup> In		DTPA	GI transit Cisternography	$10^{a}$ $30^{a}$

**Typical** 

Radionuclide	Pharmaceutical	Indication/Use	Typical Administered Activity (MBq)	
<sup>111</sup> In	Leucocytes	Infection/inflammation imaging	20 <sup>a</sup>	
<sup>111</sup> In	Pentetreotide	Somatostatin receptor imaging	110a, 220 (SPECT)a	
<sup>111</sup> In	Platelets	Thrombus imaging	$20^{a}$	
$^{123}\mathrm{I}$	Iodide	Thyroid uptake	2ª	
		Thyroid imaging	20 <sup>a</sup>	
		Thyroid metastases imaging	400 <sup>a</sup>	
123 <b>I</b>	Ioflupane	Striatal dopamine transporter visualisation	185 <sup>a</sup>	
$^{123}\mathrm{I}$	mIBG	Neuroectodermal tumour imaging	400a	
$^{131}\mathbf{I}$	mIBG	Neuroectodermal tumour imaging	20 <sup>a</sup>	
$^{131}I$	Iodide	Thyroid uptake	0.2a	
		Thyroid metastases imaging	400 <sup>a</sup>	
<sup>133</sup> Xe	Xenon gas	Lung ventilation studies	400 <sup>a</sup>	
<sup>201</sup> T1	Thallous chloride	Myocardial imaging	80-120 <sup>a</sup>	
		Parathyroid imaging	80a	
		Tumour imaging	150 <sup>a</sup>	

Radionuclide	Pharmaceutical	Indication/Use	Typical Administered Activity (MBq)
<sup>111</sup> In	Leucocytes	Infection/inflammation imaging	20 <sup>a</sup>
<sup>111</sup> In	Pentetreotide	Somatostatin receptor imaging	110a, 220 (SPECT)a
<sup>111</sup> In	Platelets	Thrombus imaging	20a
123 <b>I</b>	Iodide	Thyroid uptake	2ª
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		Thyroid metastases imaging	$400^{a}$
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$^{123}\mathrm{I}$	mIBG	Neuroectodermal tumour imaging	400a
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		Thyroid metastases imaging	$400^{a}$
<sup>133</sup> Xe	Xenon gas	Lung ventilation studies	400a
$^{201}\text{Tl}$	Thallous chloride	Myocardial imaging	80-120 <sup>a</sup>
		Parathyroid imaging	80ª
		Tumour imaging	150a

and others: selenium <sup>75</sup>Se...

Pharmaceuticals for PET imaging

# Oxygen <sup>15</sup>O

- ► Half-life <sup>15</sup>O is 2.5 min.
- **▶ Carbon dioxide (**CO<sub>2</sub>**)** brain blood flow
- **Oxygen**  $(O_2)$  oxygen consumption in myocardium, tumors
- ▶ Water (H<sub>2</sub>O) myocardium perfusion
  - + not influenced by metabolism
  - background <sup>15</sup>O activity in lungs and blood vessels

# Nitrogen <sup>13</sup>N

- ► Half-life <sup>13</sup>N is 10 min.
- ▶ Ammonia (NH<sub>3</sub>) myocardium perfusion, blood flow
  - metabolized in tissue

## Carbon <sup>11</sup>C

- ► Half-life <sup>11</sup>C is 20.4 min.
- ▶ Acetic acid (CH<sub>3</sub>COOH) myocardium perfusion, tumor metabolism
- Cocain, carfentanil,... brain opiod receptor mechanisms
- ▶ **Deprenyl** monoamine oxidase inhibitor, to study Parkinson disease
- ▶ Leucin, methionine... amino acid tracer, brain tumor detection

## Fluorine <sup>18</sup>F

- ► Half-time <sup>18</sup>F is 109 min.
- ► Haloperidol neuroreceptor ligand, drug effects
- ▶ Sodium fluoride  $Na^{18}F^-$  skeletal imaging, osseous blood-flow, metastases. Better signal than  $^{99m}\mathrm{Tc}$
- ▶ Fluorodopa... metabolised to dopamine, neurotransmiter studies
- Flourouracil... drug, nucleic acid tracer, chemotherapy dosage
- ► Fluorodeoxyglucose (FDG) glucose metabolism; neurology, cardiology, oncology. Penetrates blood-brain barier

# **Delivery Strategies: Metabolic pathways**

FDG 2-fluoro-2-deoxy-glucose

*B*-D-glucose

## FDG usage

- ► Brain function mapping
- ightharpoonup .... glucose provides energy to the brain (for adults  $\sim 100\,\mathrm{g/den})$

## FDG usage

- ► Brain function mapping
- ightharpoonup . . . . glucose provides energy to the brain (for adults  $\sim 100\,\mathrm{g/den})$
- ► Tumor mapping
- ...tumors have no metabolic barier

# **FDG** in Oncology

- FDG transport into tumors occurs at a higher rate than in the surrounding normal tissues.
- FDG is de-phosphorylated and can then leave the cell.
- The dephosphorylation occurs at a *slower* rate in tumors.

#### Applications of FDG

- Locating unknown primaries
- •Differentiation of tumor from normal tissue
- •Pre-operative staging of disease (lung, breast, colorectal, melanoma, H&N, pancreas)
- •Recurrence vs necrosis
- •Recurrence vs post-operative changes (limitations with FDG)
- ·Monitoring response to therapy

#### Rubidium <sup>82</sup>Rb

- ► Half-life <sup>82</sup>Rb is 1.25 min.
- + Produced by a generator from Sr, (no cyclotron needed)
- Long positron free path  $\longrightarrow$  low spatial spatial resolution.
- + Short half-life  $\longrightarrow$  good temporal resolution
- Short half-life  $\longrightarrow$  weak signal
- Behaves like K
- Myocardium perfusion
- Blood-brain barrier study

Principles of nuclear imaging

Radioactivity

Gamma camera

SPECT

PET

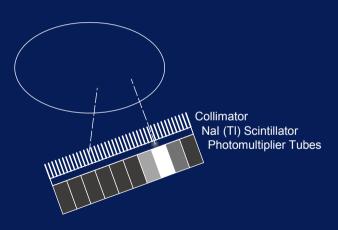
Conclusions

# Gamma camera

Scintigraphy



# Single Photon Detection with Gamma Camera



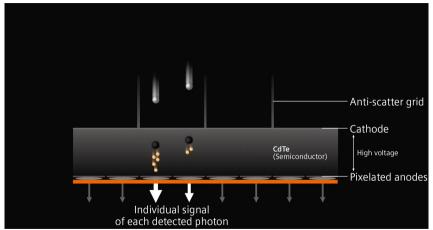
#### Scintillator materials

Scintillator	Density (g cm <sup>-3</sup> )	Effective Z	Relative light yield	Decay constant (ns)	Wavelength of emission (nm)
Sodium Iodide (NaI)	3.67	50	100	230	410
Bismuth Germanate (BGO)	7.13	74	12	300	480
Barium Fluoride (BaF <sub>2</sub> )	4.89	54	5 15	0.6 - 0.8 630	220 (195) 310

- ► High Z advantageous
- ▶ BGO good for 511 keV
- ► For speed, use BaF<sub>2</sub> UV light produced

# Photon Counting Detector (PCD)

Timepix/Medipix



- Signal propagation directed by electric field
- ► High quantum efficiency
- ► High spatial resolution

#### Principles of nuclear imaging

Radioactivity

Gamma camera

Artefacts

Clinical applications of gamma camera

**SPECT** 

**PET** 

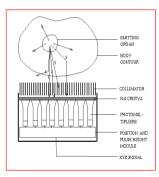
Conclusions



# **Artifacts: scattering**

#### Scattering of photons in patient

- Because of limited energy resolution of the detector, primary and scattered photons which pass the collimator can not be classified properly. (In the ideal case, only primary photons are used to contribute to the image)
- Effects: haziness of images, quantization is degraded.





#### **Artifacts: collimator blur**

#### Collimator blur

- Because of the size of the holes, photons which are not entering the detector exactly perpendicular to the detector surface are also detected. This introduces uncertainty about the exact path the photon traveled.
- Effect: blurring which increases with larger holes. Trade off between sensitivity and resolution has to be found.



#### **Artifacts: noise**

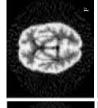
#### Noise due to limited number of detected photons

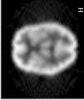
- Doses and scanning time are limited while the efficiency of the collimator is also limited.
- Effects: Noise in the images. Low pass digital filtering required. This results in reduced resolution. Tradeoffs between dose, scanning time and collimator hole size have to be made.



# **Phantom experiments**

Ground truth phantom





Detector + attenuation

Detector + attenuation + scatter





Detector + attenuation + scatter + noise

#### Principles of nuclear imaging

Radioactivity

Gamma camera

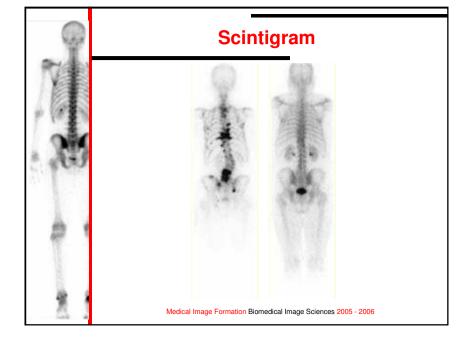
Artefacts

Clinical applications of gamma camera

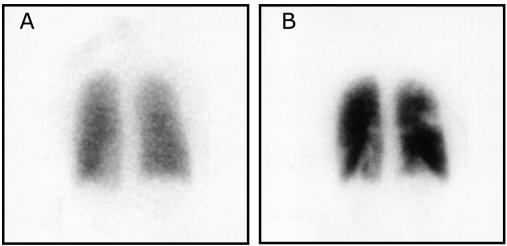
**SPECT** 

**PET** 

Conclusions



# Lung scintigraphy



Most frequent use. Ventilation (Xe), perfusion ( $^{99m}$ Tc). Pulmonary embolism (blocked artery)

Principles of nuclear imaging

Radioactivity

Gamma camera

**SPECT** 

PET

Conclusions



#### **SPECT**

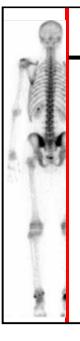
Single Photon Emission Computed Tomography (SPECT)

Image is acquired by rotating the  $\gamma\text{-camera}$  around the patient and taking images at different angles



#### **SPECT**

- Patient is injected with a γ-emitting radio-pharmaceutical
- Preferred energy: 100-250 keV
- Use of collimaters
- Collimated camera projections are acquired from different equidistant angles (30-120 projections over 180-360 degrees)
- Images are reconstructed using Filtered Back Projection (FBP) or Iterative Reconstruction
- Resolution: 12-20 mm
- To increase count-rate often two or three γ-camera heads are used

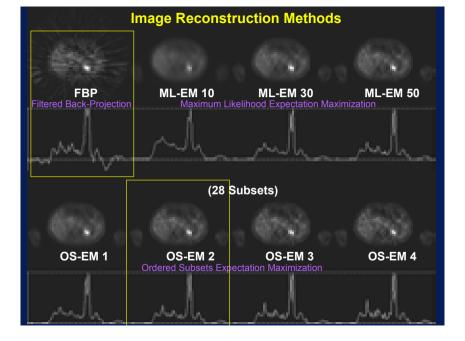


# **SPECT**



# SPECT, brain imaging





#### Principles of nuclear imaging

Radioactivity

Gamma camera

**SPECT** 

Princip

Clinical applications of SPECT

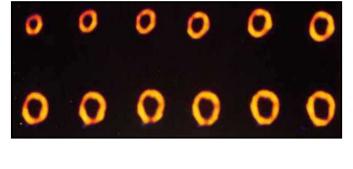
**PET** 

Conclusions

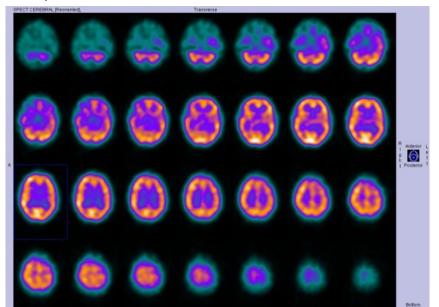


# **SPECT: Applications**

Cardiac Imaging



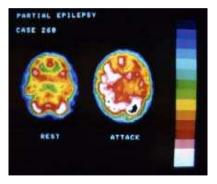
# SPECT, Brain perfusion



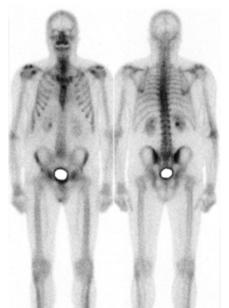


# **SPECT: Applications**

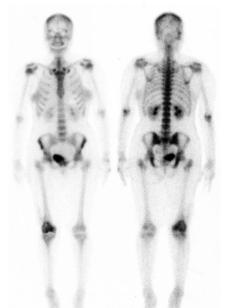
#### **Epilepsy**



# SPECT, Whole-body imaging



# SPECT, Whole-body imaging



Principles of nuclear imaging

Radioactivity

Gamma camera

**SPECT** 

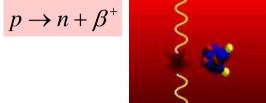
PET

Conclusions

#### **Principle of PET** An Positron and electron annihilation A<sub>1</sub> Positron emission in the brain and emission of gamma rays Gamma ray Site of positron annihilation Electron (imaged point) Gamma ray 0-9mm Unstable Positron photon resolution radionuclide limit From: Principles of Neural Science (4th. Ed.) Kandel, Schwartz, & Jessell, p. 377. Columbia fMRI



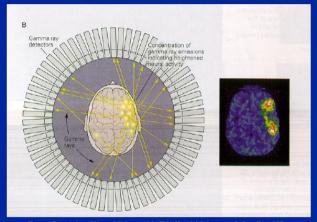
### **PET:** annihilation



Annihilation Coincidence Detection

Isotope	Maximum
	Positron Range (mm)
F-18	2.6
C-11	3.8
Ga-68	9.0
Rb-82	16.5

# **Gamma Ray Detections to Location of Function**



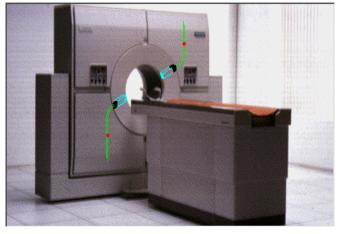
From: Principles of Neural Science (4th. Ed.) Kandel, Schwartz, & Jessell, p. 377.

🚃 Columbia fMRI 🚃

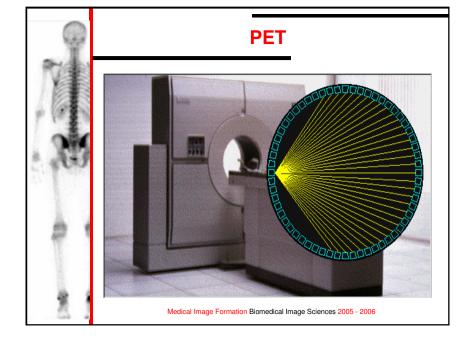


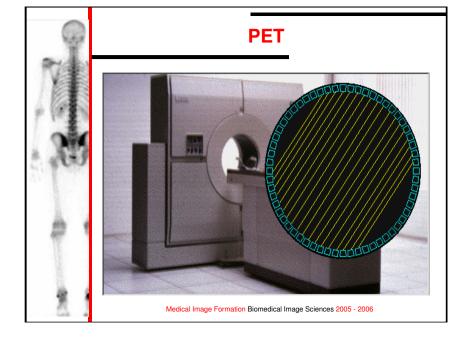


# **PET**



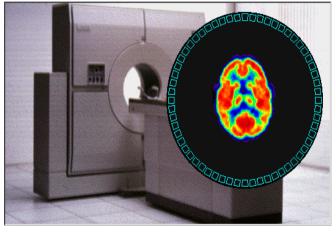
Medical Image Formation Biomedical Image Sciences 2005 - 2006







## **PET**



Medical Image Formation Biomedical Image Sciences 2005 - 2006

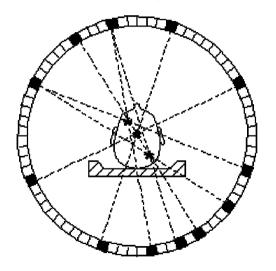
# **Coincidence Event**

#### Electronic collimation

- Associate detections within interval  $\tau$  (a few ns)
- ▶ Start timer and wait for the second detection → increment count
- ▶ *List mode* store detections with time stamps, postprocess
- ▶ No lead collimators → higher sensitivity wrt SPECT

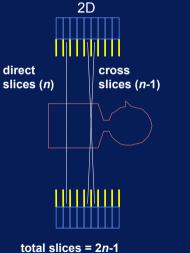
# Time of Flight PET

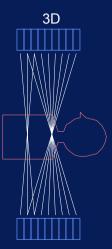
▶ Measure time interval between coincident photones



# Multiple Rings, 2D - 3D

#### For *n* detector rings:





#### Principles of nuclear imaging

Radioactivity

Gamma camera

**SPECT** 

#### **PET**

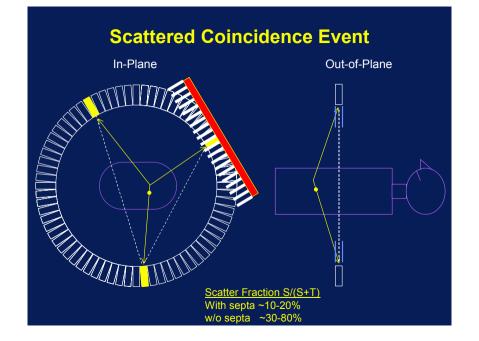
Principle

Artefacts and corrections

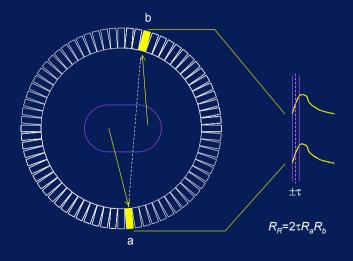
Clinical applications of PET

Kinetic studies

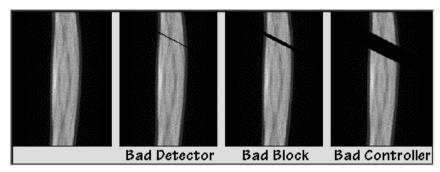
#### Conclusions



# **Random Coincidence Event**

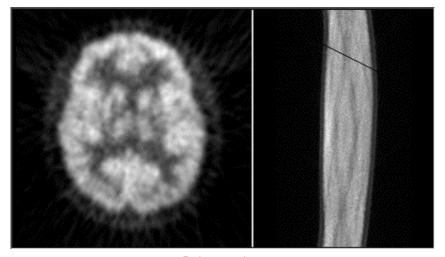


#### Detector failure



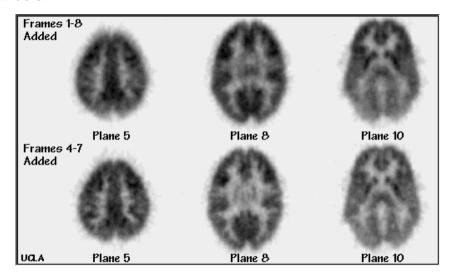
Sinogram

# Detector failure

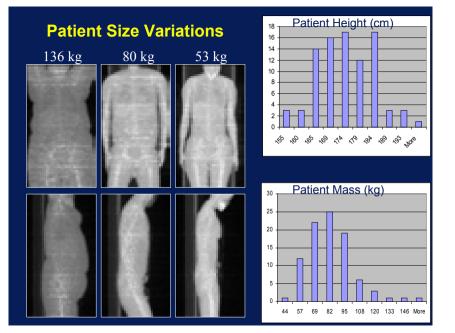


Rekonstrukce

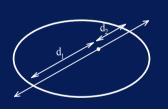
#### Patient motion



Lower row only uses images without motion.



#### **Coincidence Attenuation**

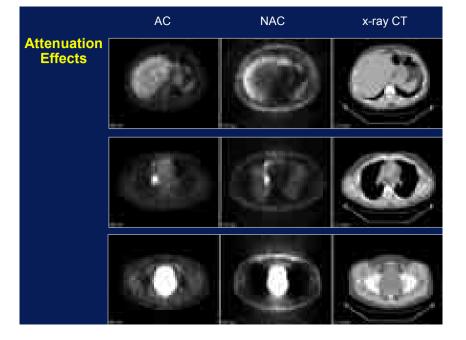


$$P_C = P_1 P_2$$

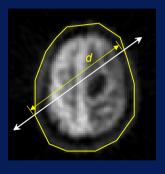
$$= e^{-\mu \cdot d_1} e^{-\mu \cdot d_2}$$

$$= e^{-\mu \cdot (d_1 + d_2)}$$

Annihilation radiation emitted along a particular line of response has the same attenuation probability, regardless of where it originated on the line.

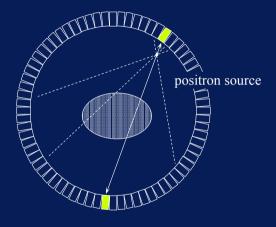


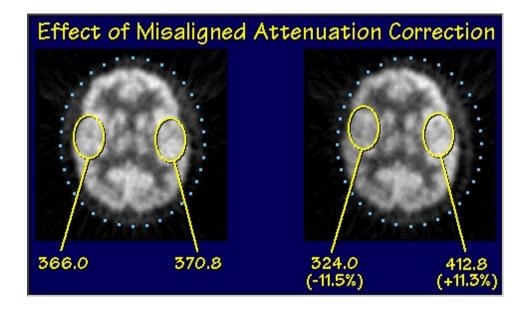
# **Calculated Attenuation Correction**

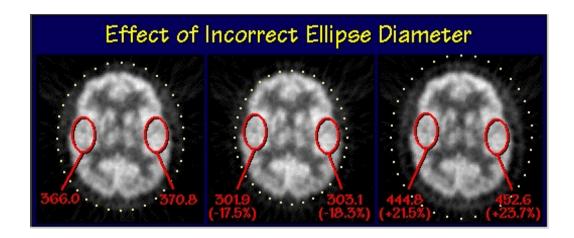


$$I = I_0 e^{-\mu d}$$

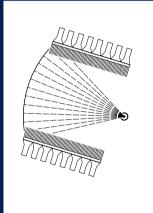
# Transmission Attenuation Measurement





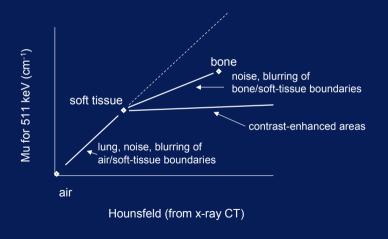


# SPECT/CT





# Converting Attenuation Map from Hounsfeld to 511 keV attenuation Coefficients



### PET — parameters

- ▶ Effective resolution  $8 \sim 10 \, \mathrm{mm}$
- ► Isotropic sampling 3 mm
- ► Transaxial FOV 60 cm, axial 10 cm. Increase axial FOV by increasing number of detectors (=higher cost), or shift the patient (=longer time, higher dose).
- ▶  $16 \sim 64$  detector planes

#### Principles of nuclear imaging

Radioactivity

Gamma camera

**SPECT** 

#### **PET**

Principle

Artefacts and corrections

Clinical applications of PET

Kinetic studies

#### Conclusions

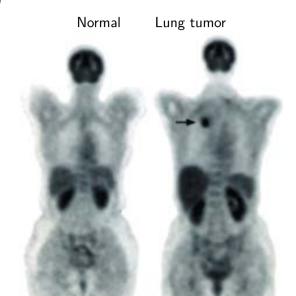
# PET, whole body imaging

Tumor has faster metabolism  $\longrightarrow$  contrast agents accumulates there



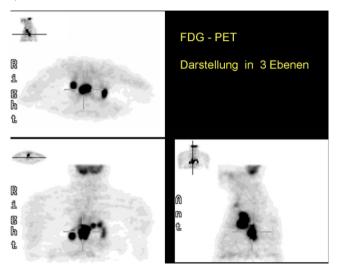
 $\mathsf{PET} + \mathsf{FDG}$ 

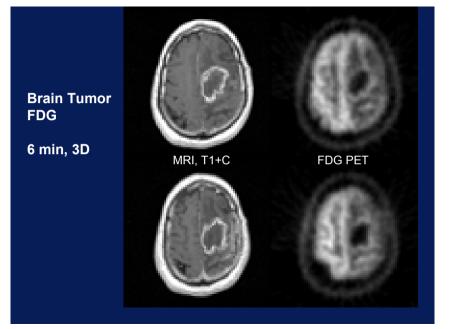
 $^{18}\mathrm{F}$  glucose (FDG)



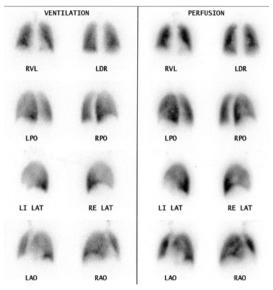
### PET + FDG

 $^{18}\mathrm{F}$  glucose (FDG). Tumor detection.

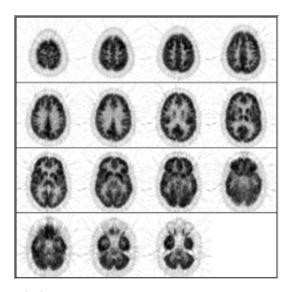




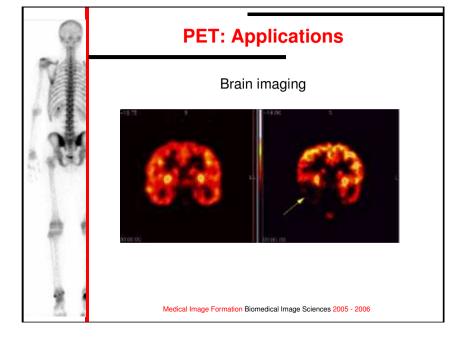
# PET. Lung ventilation and perfusion



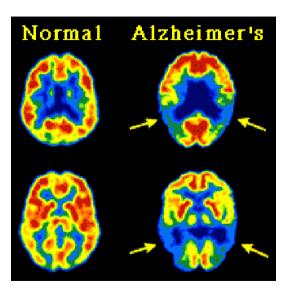
# PET, head



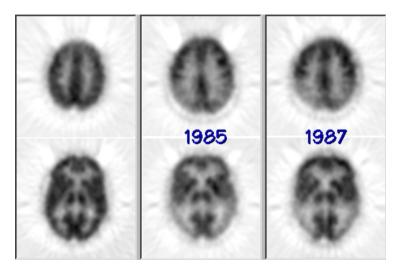
perfusion, glucose metabolism



## PET, brain



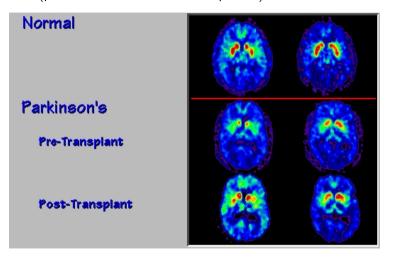
#### Alzheimer disease



Hypometabolismus.

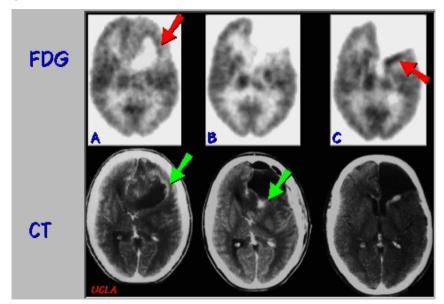
#### Parkinson disease

 $^{18}\text{F} - \text{DOPA PET}$  (precursor of neurotransmiter dopamine)



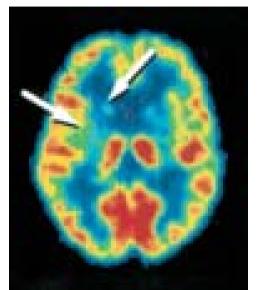
Transplantation of dopamin producing cells.

## Brain tumor



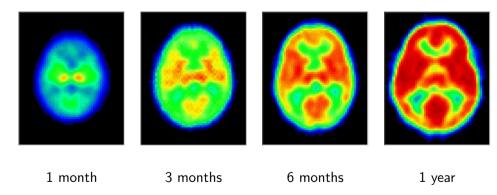
# PET, Huntington disease

Reduced glucose metabolism



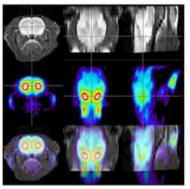
# Brain development

FDG





#### Fusion of anatomical and functional data



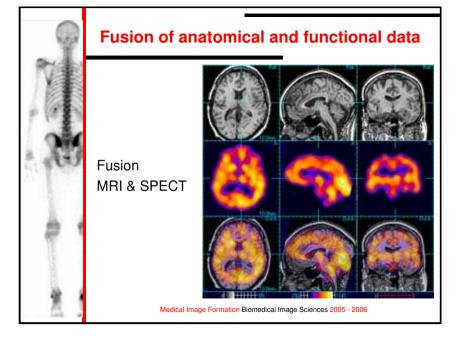
op: MR1 images of a rat brain (axial, multi-slice 256 sq x 16 acquisition, coronal/sagittal views are interpolated)

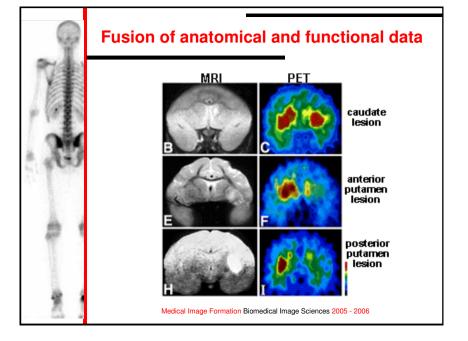
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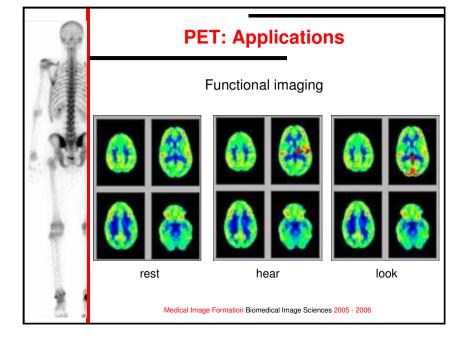
Center: 18p-labeled specific ligand for the dopamin-transport protein.
Compound accumulates in brain areas with a high level of dopamin containing neurons (striatum).

Bottom: Overlay in all three major directions.

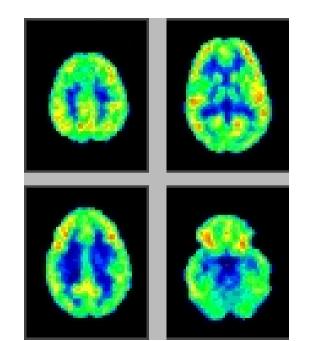
Medical Image Formation Biomedical Image Sciences 2005 - 2006



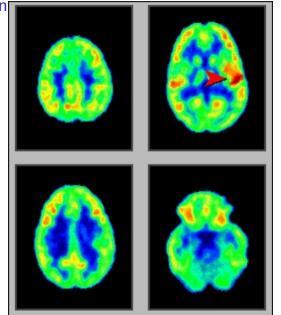




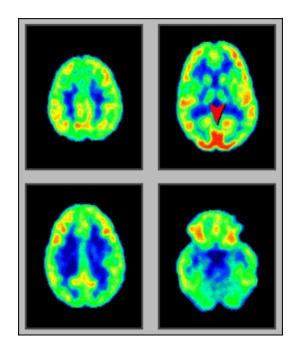
# Brain at rest



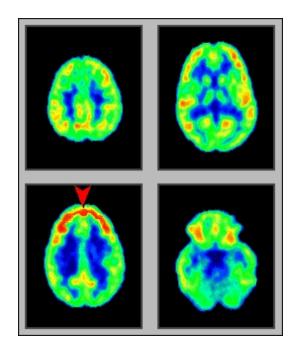
Acoustic stimulation



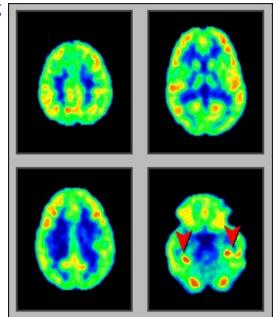
# Visual stimulation



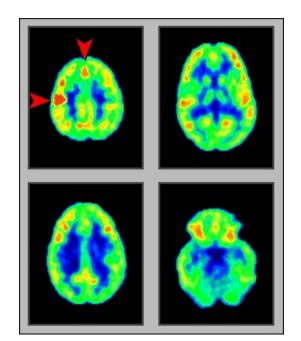
# Cognitive activity

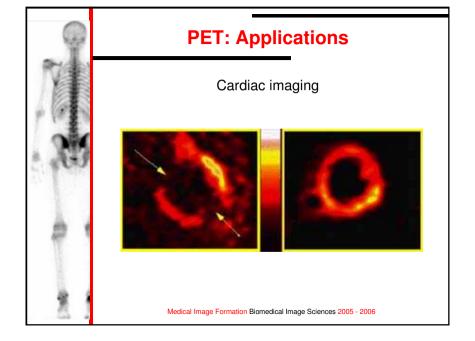


Memory and learning [



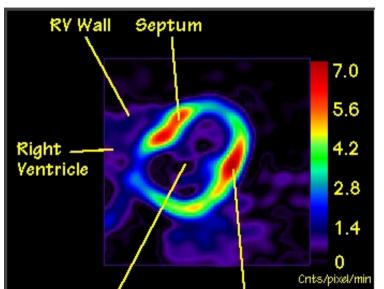
## Movement





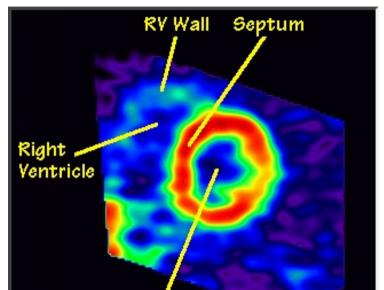
#### PET, heart

#### Contrast agent FDG

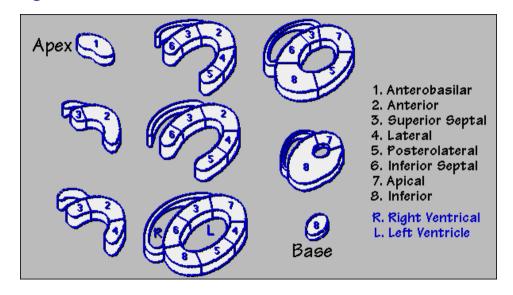


## PET, heart

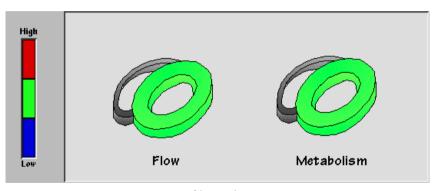
Contrast agent FDG



#### Heart segments

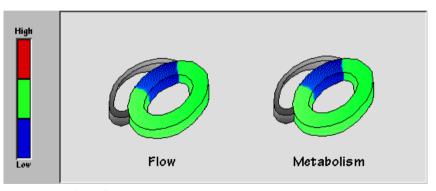


Flow (e.g.  $NH_3$ ) Metabolism (e.g. FDG)



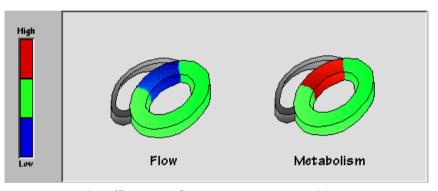
Normal

Flow (e.g.  $NH_3$ ) Metabolism (e.g. FDG)



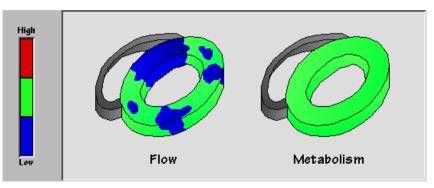
Not functional tissue, treatment not possible.

Flow (e.g. NH<sub>3</sub>) Metabolism (e.g. FDG)



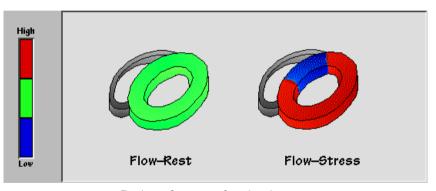
Insufficient perfusion, treatment possible.

Flow (e.g.  $NH_3$ ) Metabolism (e.g. FDG)

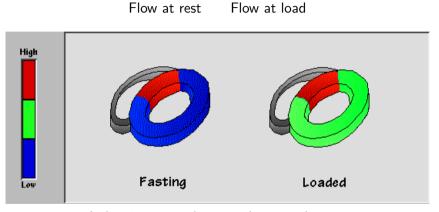


Bad perfusion (ischemic), enlarged myocardium. Treatment possible if the metabolism is normal or increased.

Flow (e.g.  $NH_3$ ) Metabolism (e.g. FDG)

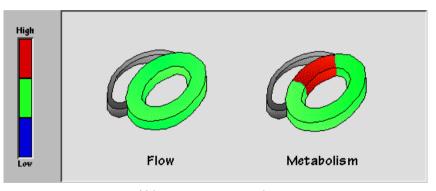


Bad perfussion after load test.



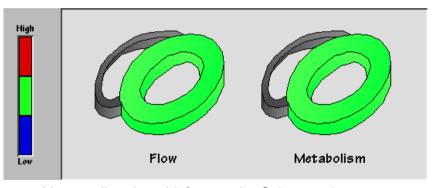
Ischemic myocardium needs more glucose.

Fasting After glucose is administerd



Hibernating myocardium.

Flow (e.g.  $NH_3$ ) Metabolism (e.g. FDG)



Idiopatically enlarged left ventricle. Only transplantation.

#### Principles of nuclear imaging

Radioactivity

Gamma camera

#### **SPECT**

#### **PET**

Principle
Artefacts and corrections
Clinical applications of PE

Kinetic studies

#### Conclusions

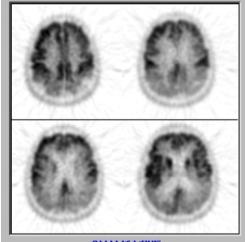
#### Kinetic study

- ▶ Study the evolution of the radiotracer concentration in time
- ▶ Identify model parameters (time and transport constants)

#### Kinetic study

- ▶ Study the evolution of the radiotracer concentration in time
- Identify model parameters (time and transport constants)
- ► → Reproducibility

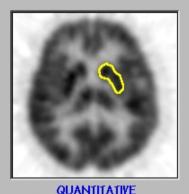
# Qualitative $\times$ quantitative analysis



QUALITATIVE

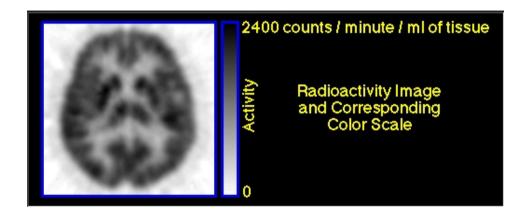
"This pattern is characteristic
of Alzheimer's Disease."

# Approaches to Image Analysis

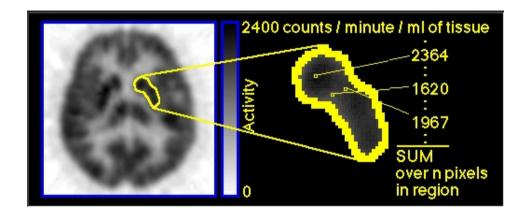


"Metabolic rate for glucose in this region is 8.37 mg/min/100g tissue"

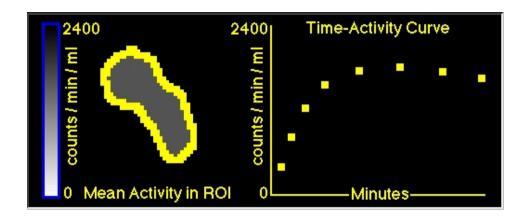
# Normalized radioactivity image



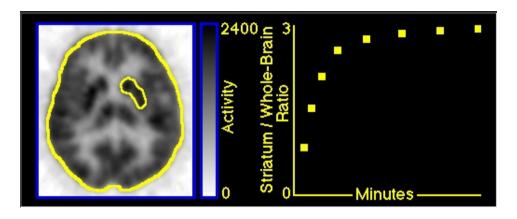
#### Mean ROI value



#### Time-activity ROI curve

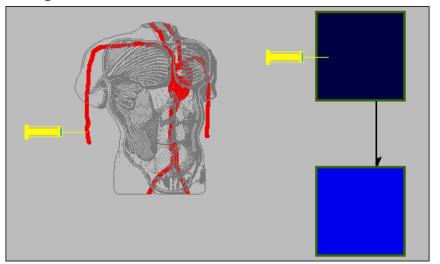


# Normalized time-activity ROI curve



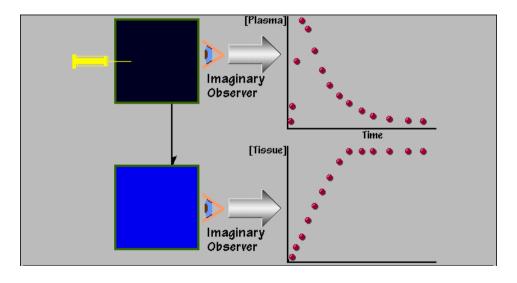
Ratio of regional and total activity.

#### Tracer modeling of the ROI curve

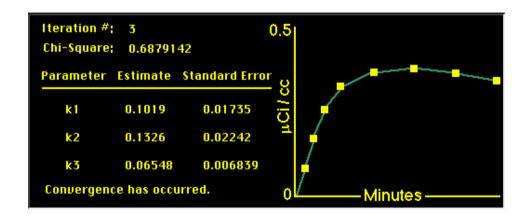


► Find biophysical model parameters — blood flow, concentrations, diffussion coefficients.

# Tracer modeling of the ROI curve

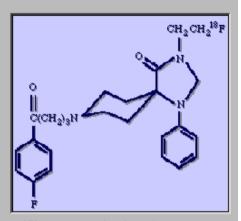


#### Tracer modeling of the ROI curve



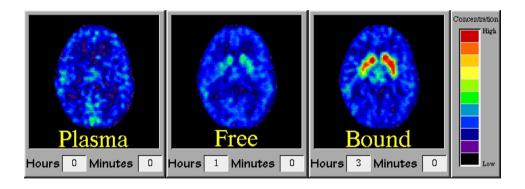
#### Brain



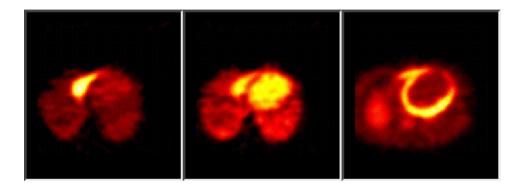


Fluoroethylspiperone

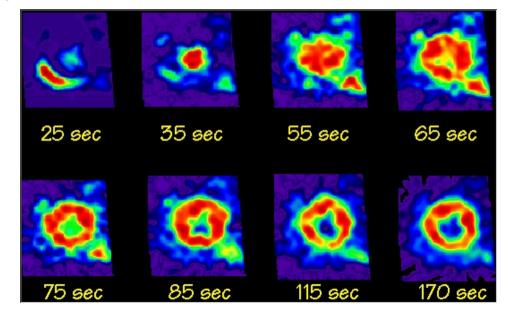
#### Brain

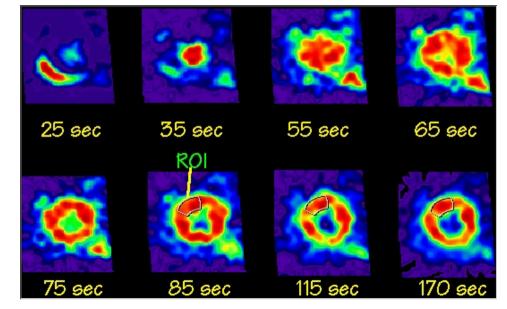


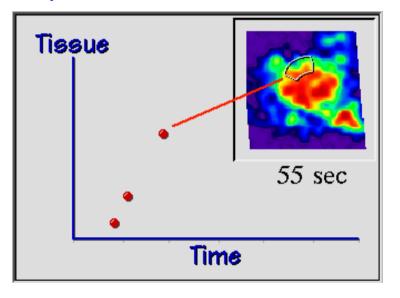
# Heart

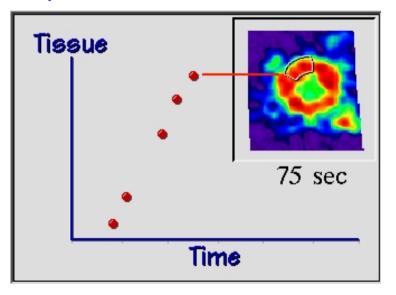


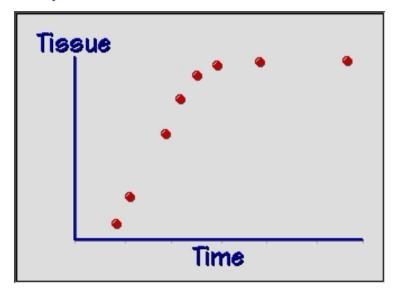
#### Heart

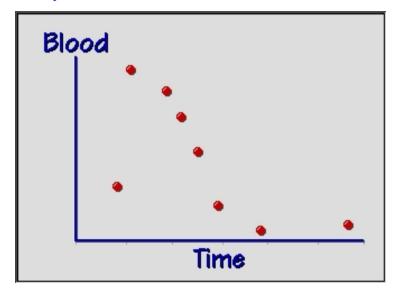












## Nuclear imaging — summary

- + Functional imaging; intensity of the metabolic processes
- + Targeted and specific imaging, perfussion, oncology
- Radiation dose
- Manufacturing radiopharmaceuticals, expensive
- Only partial anatomy information
- Bad spatial resolution