

Magnetic Particle Imaging

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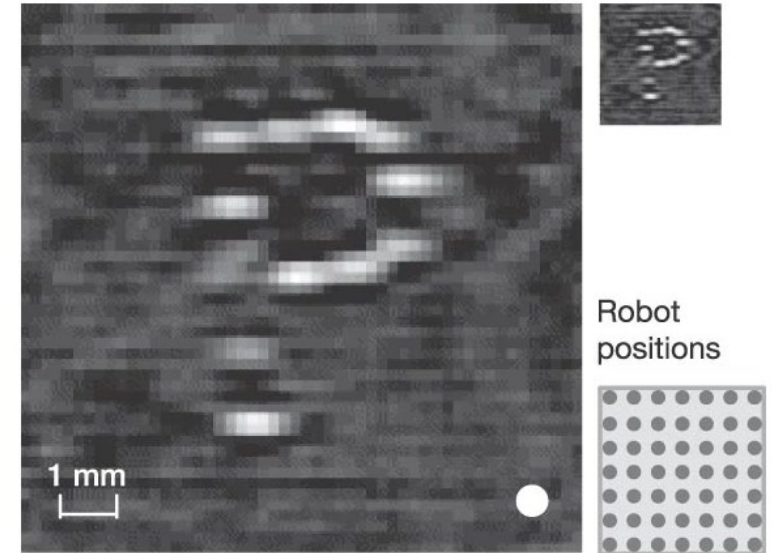
Magnetic Particle Imaging

- Novel tomographic method, uses magnetic fields
- No ionizing radiation, non-invasive imaging
- **Requires a tracer!**
- No native imaging, no anatomical information
- Requires colocalization with another imaging methods (X-Ray, MRI, CT, optical...)

Tracer – **superparamagnetic particles**

History

2001 – first MPI image



2005 – Gleich B, Weizenecker J. Tomographic imaging using nonlinear response of magnetic particles. Nature 2005; 435:1214-1217

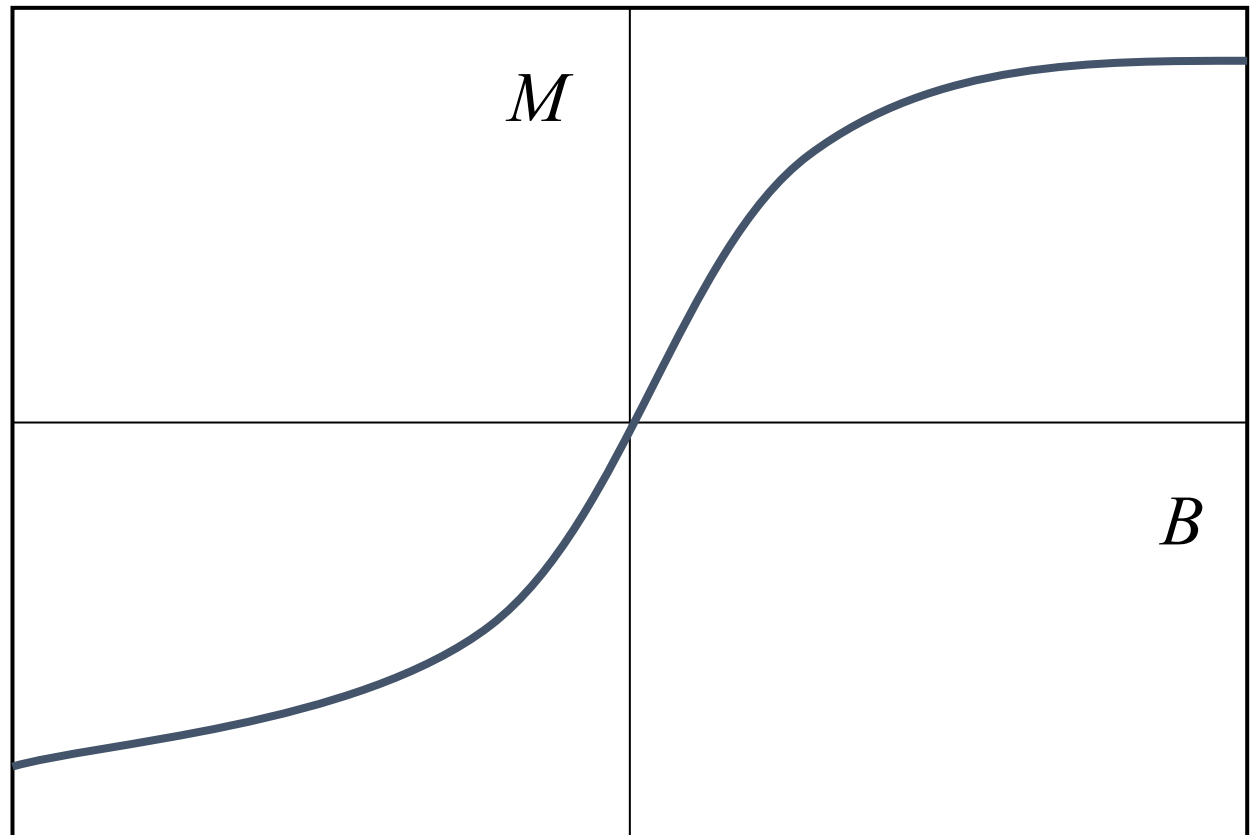
2008 – Gleich B, Weizenecker J, Borgert J. Experimental results on fast 2D-encoded magnetic particle imaging. Physics in Medicine and Biology 2008;53:N81-N84

A small detour...

Paramagnetism

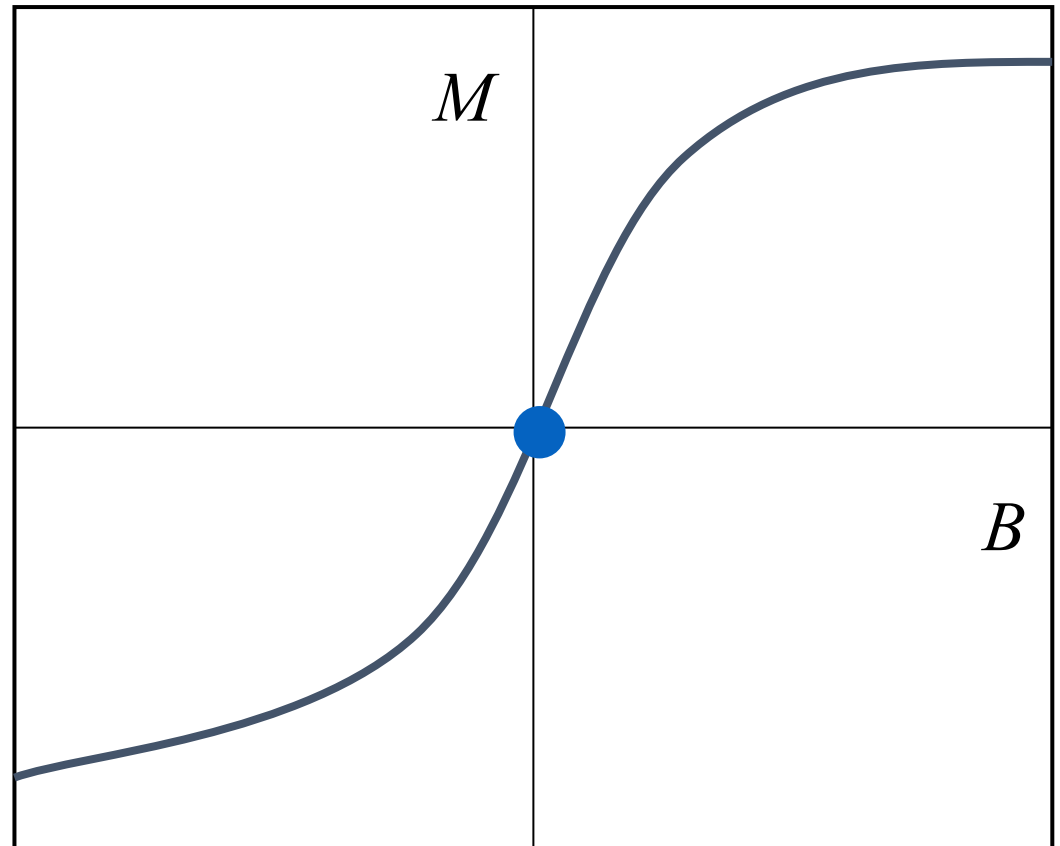
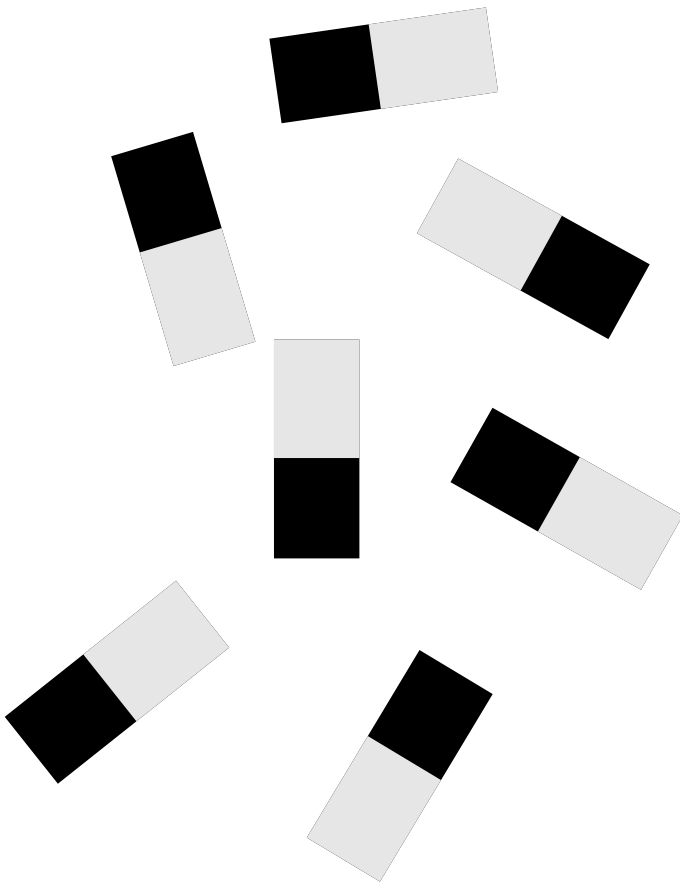
Ferromagnetism

Superparamagnetism



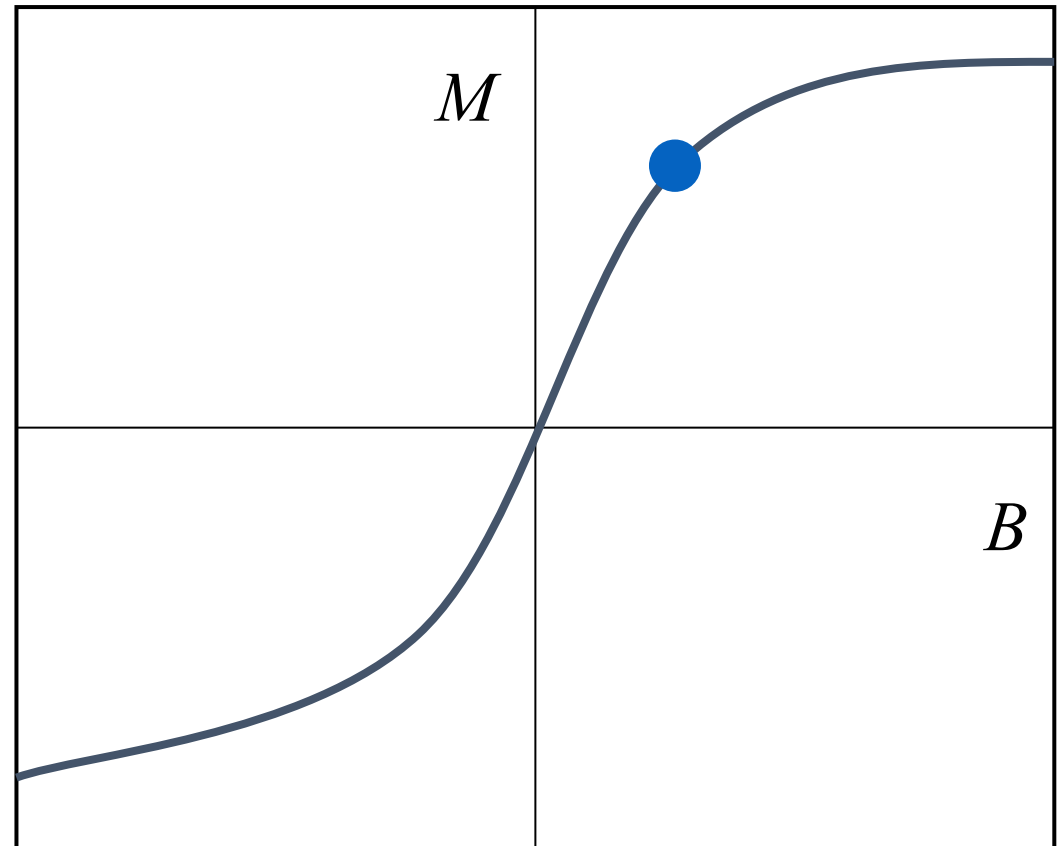
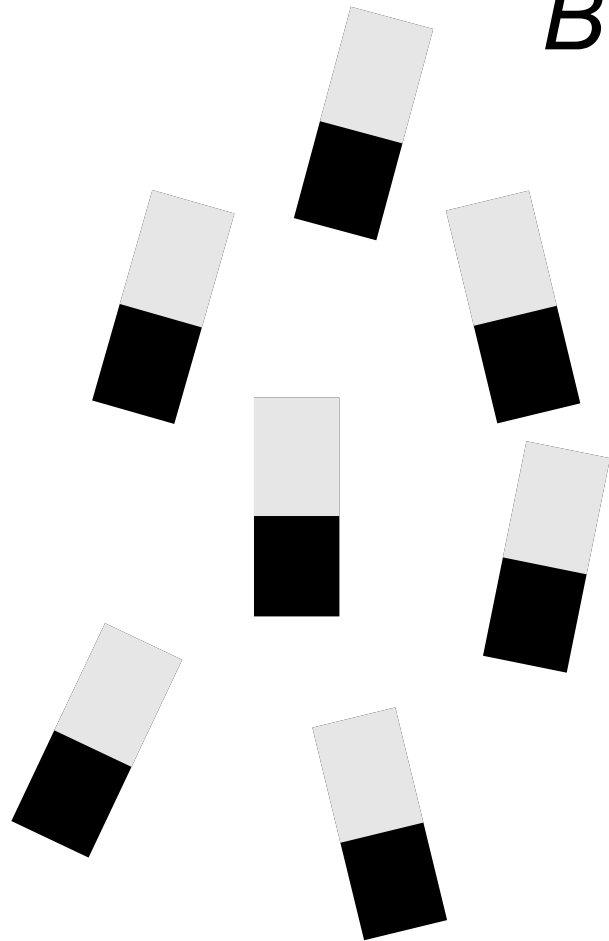
Paramagnetism

$$B = 0, M = 0$$



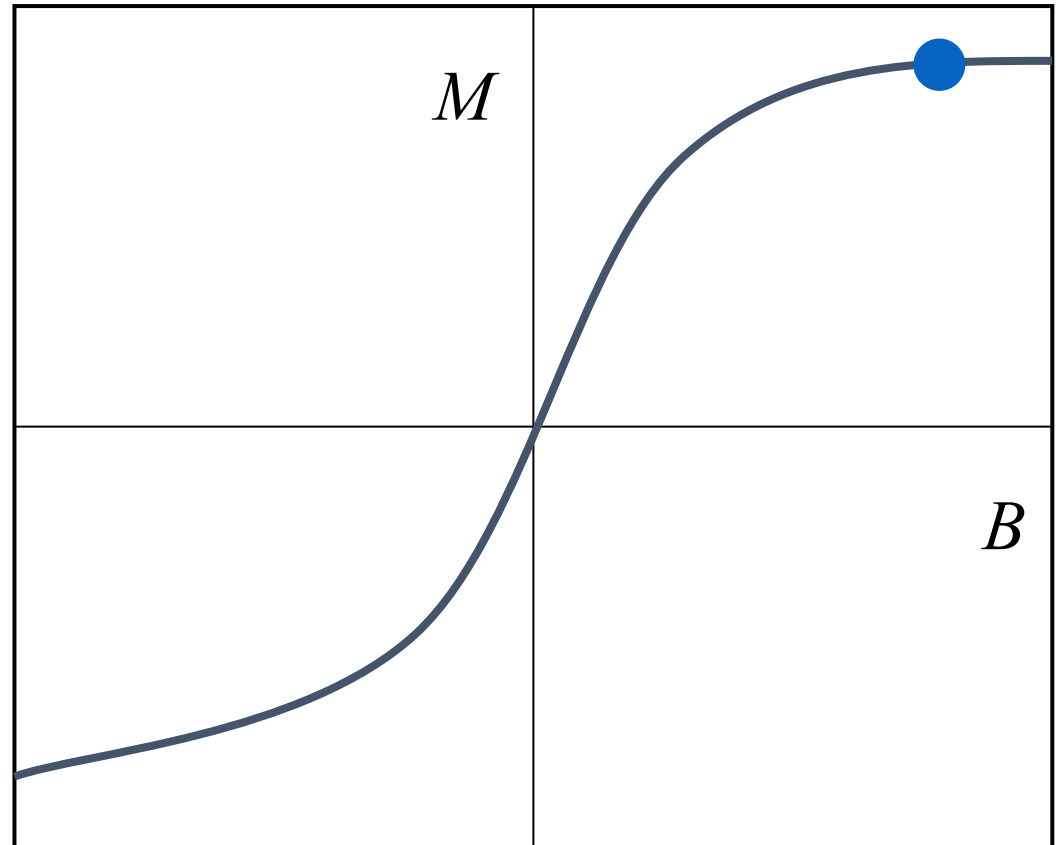
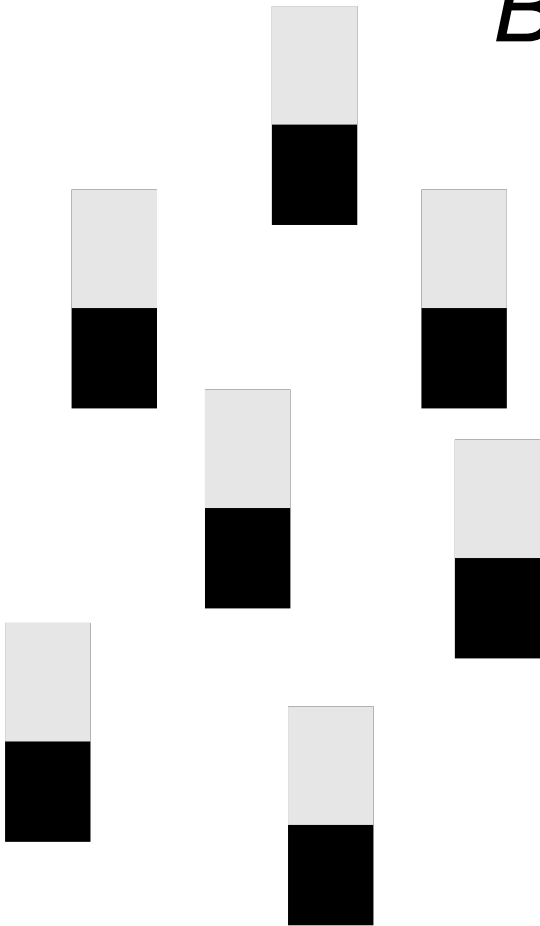
Paramagnetism

$$B \neq 0, M \neq 0$$



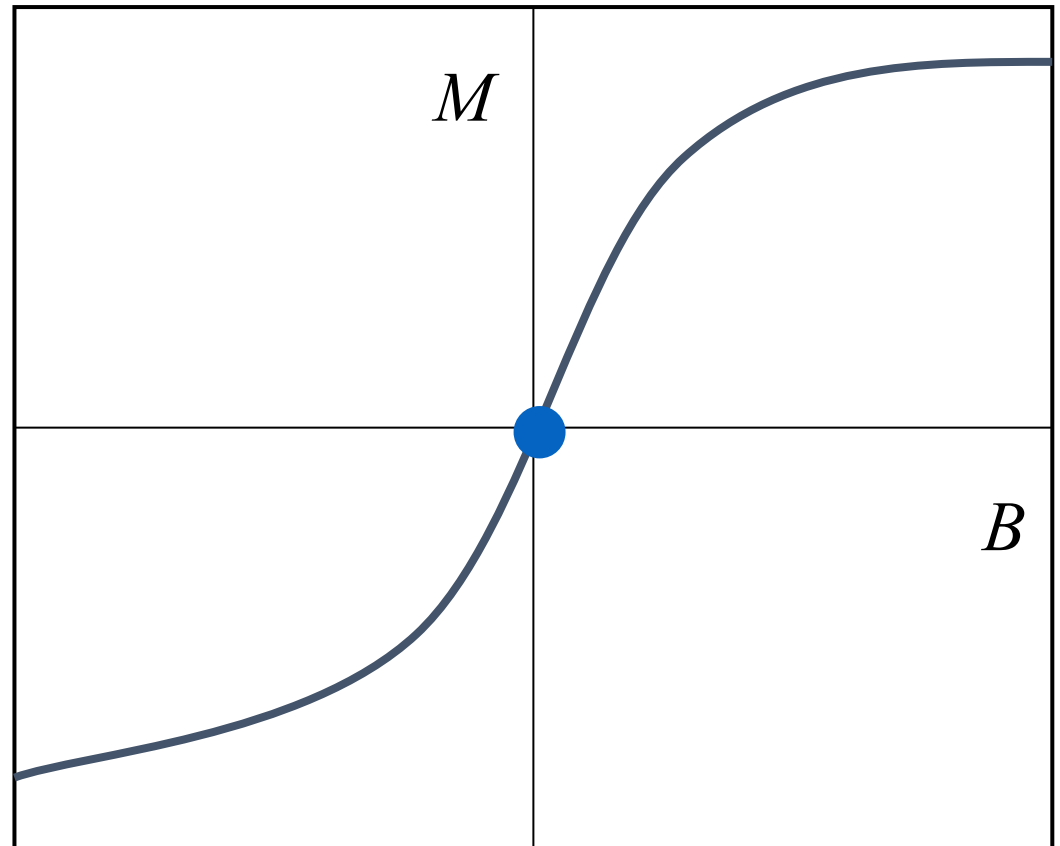
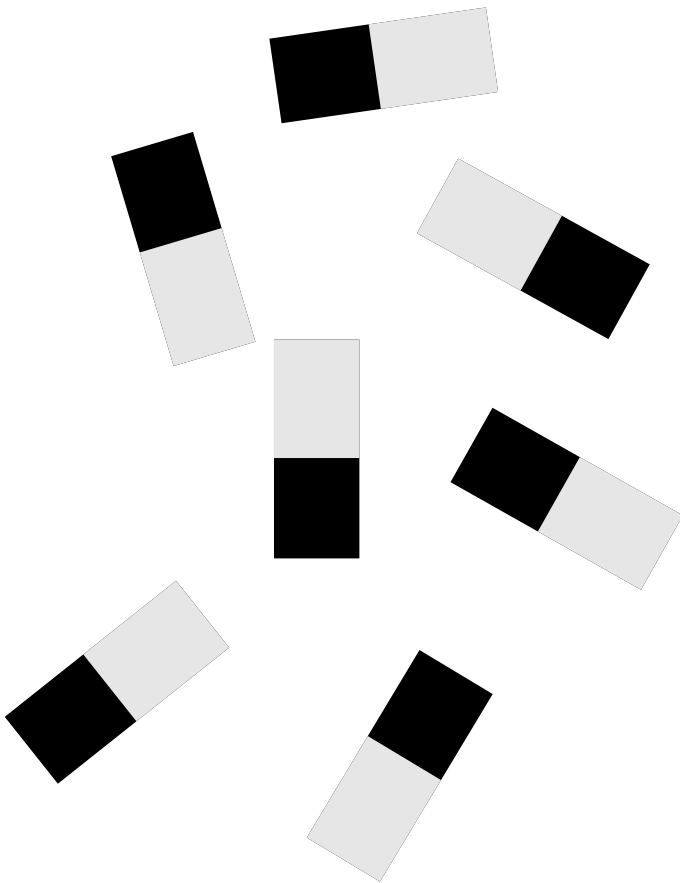
Paramagnetism

$$B \neq 0, M \neq 0$$



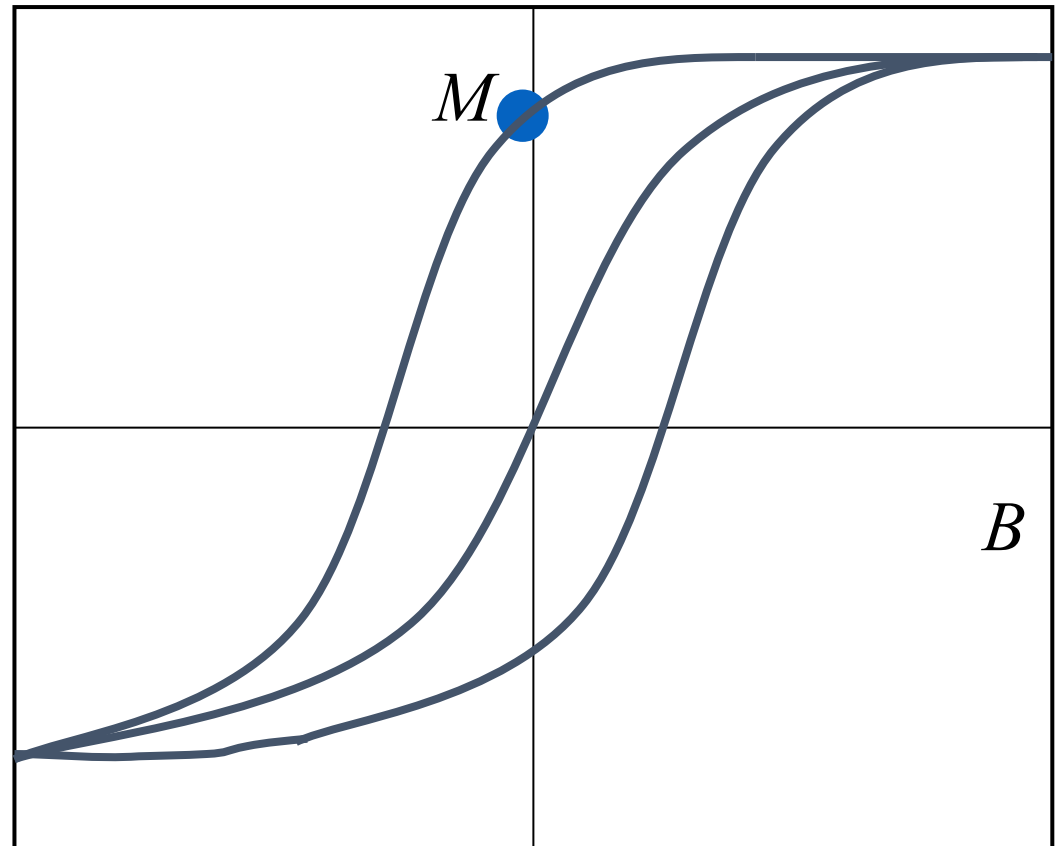
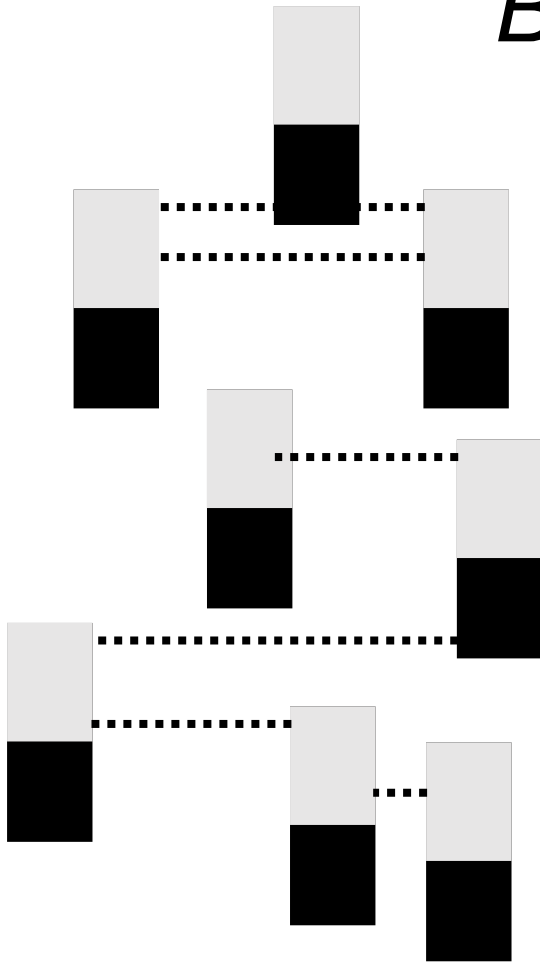
Paramagnetism

$$B = 0, M = 0$$



Ferromagnetism

$$B = 0, M \neq 0$$

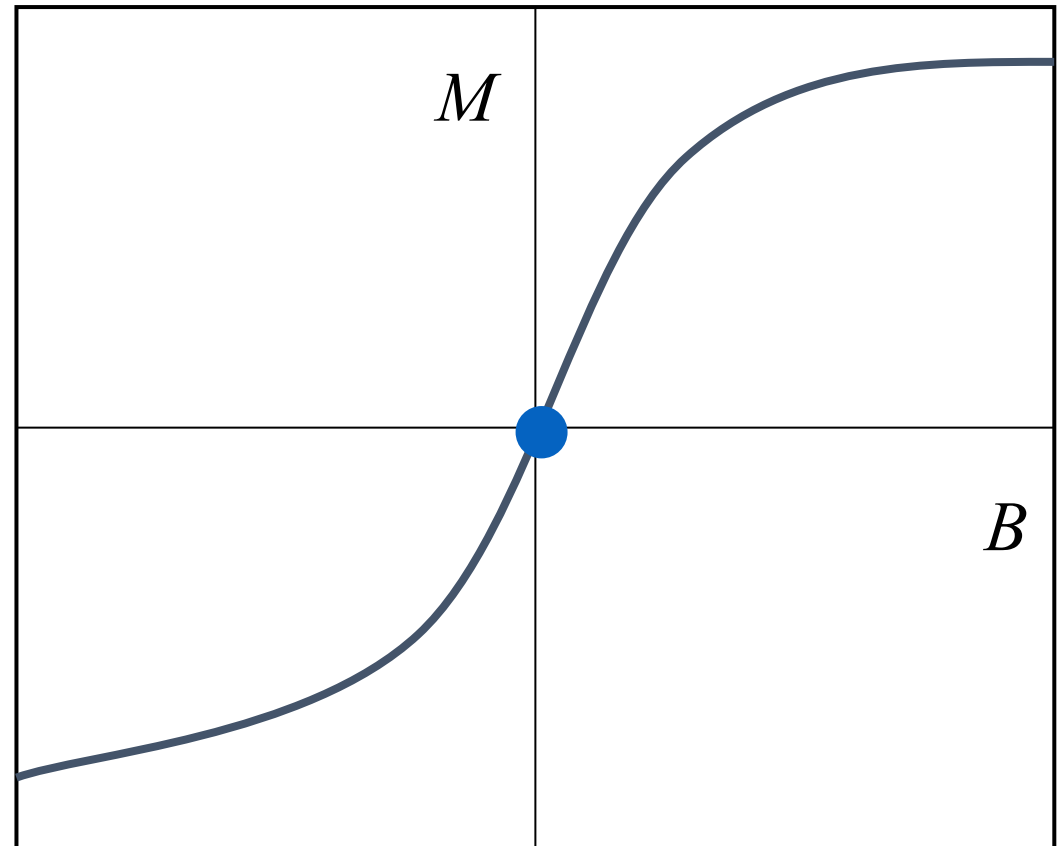
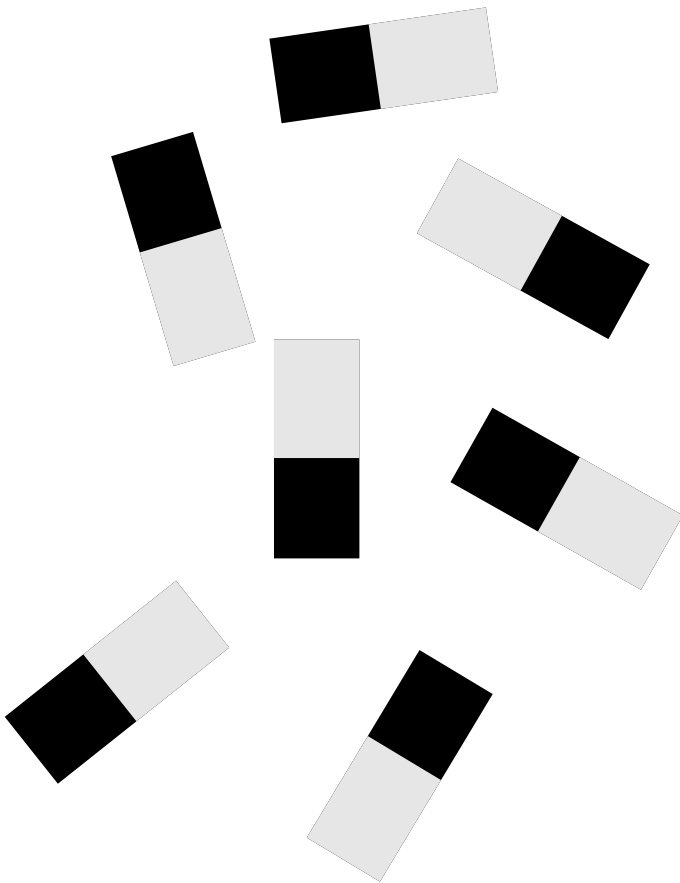


Ferromagnetism



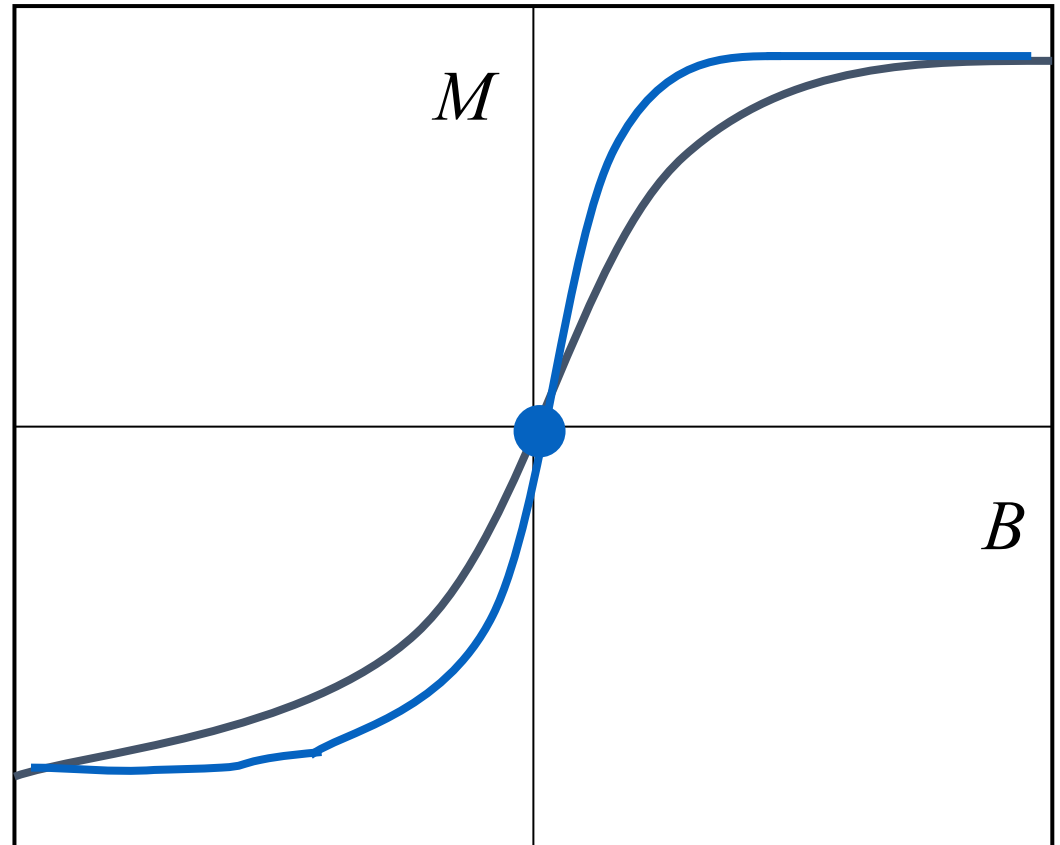
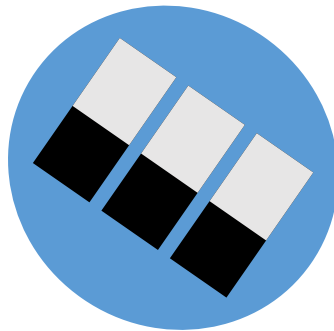
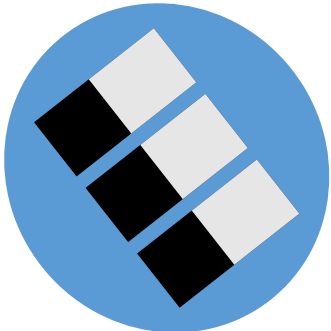
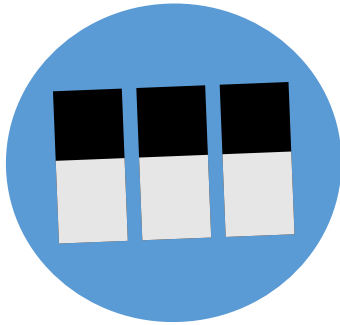
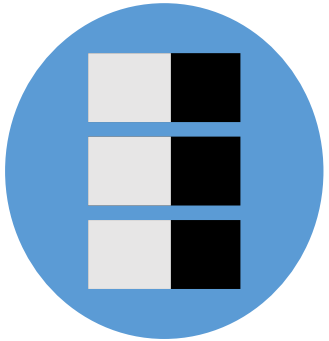
Changes to paramagnetism
above Currie temperature

$$B = 0, M = 0$$



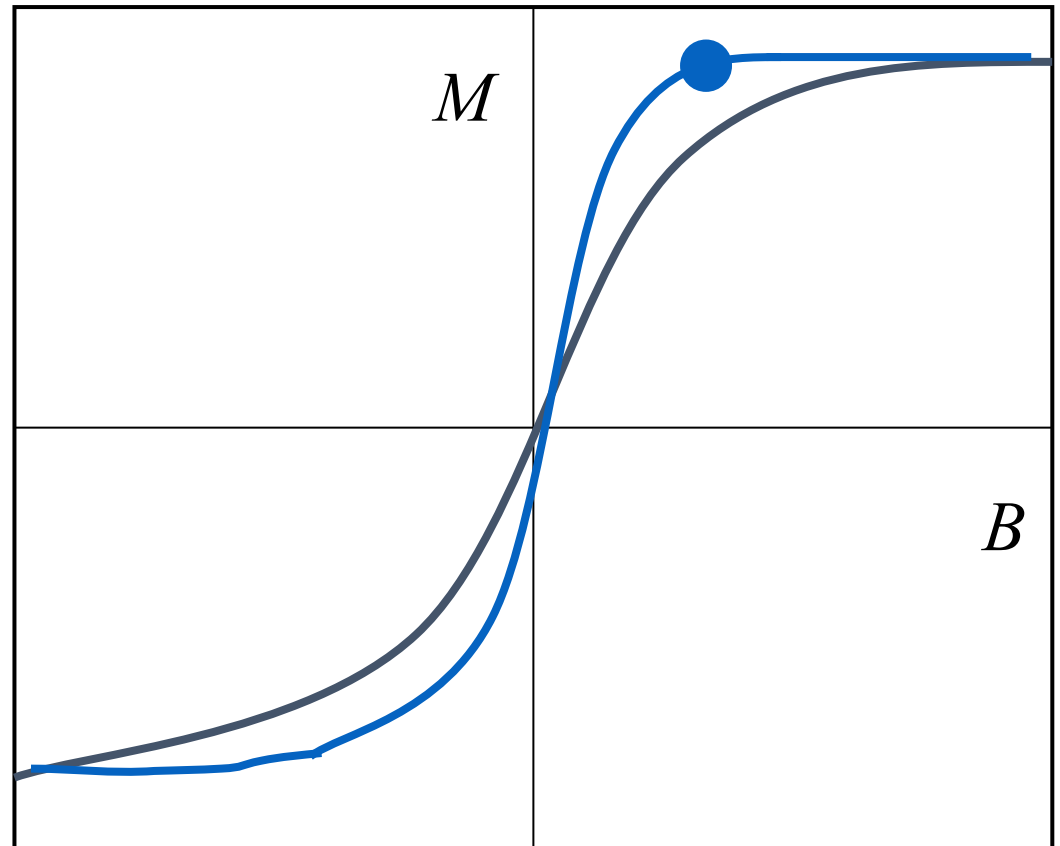
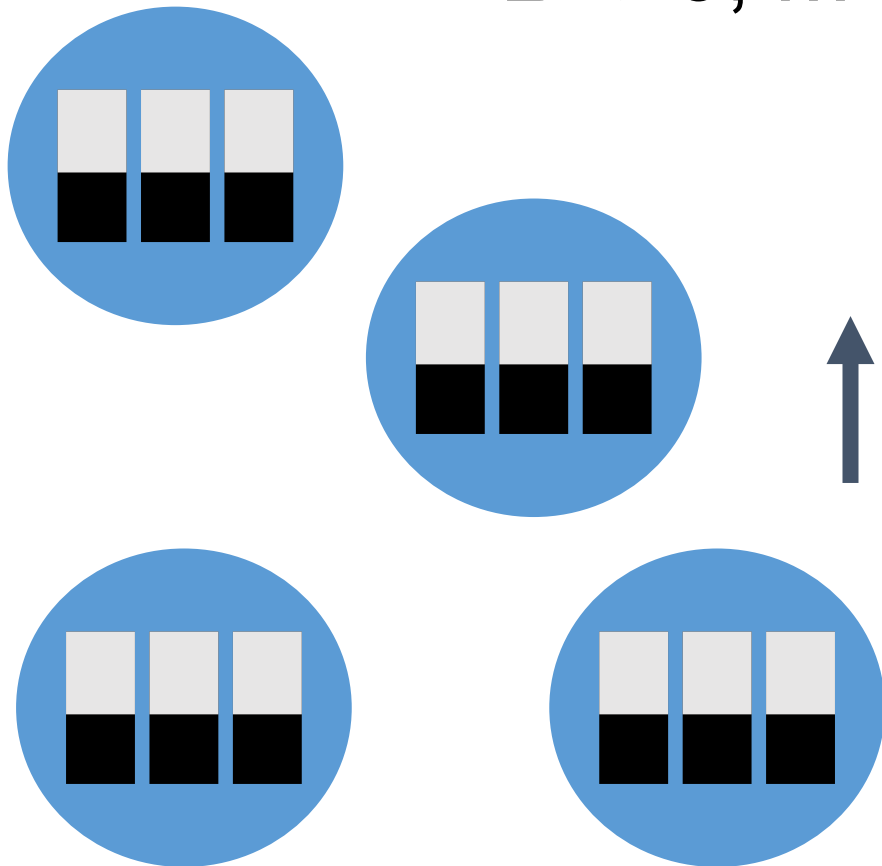
Superparamagnetism

$$B = 0, M = 0$$

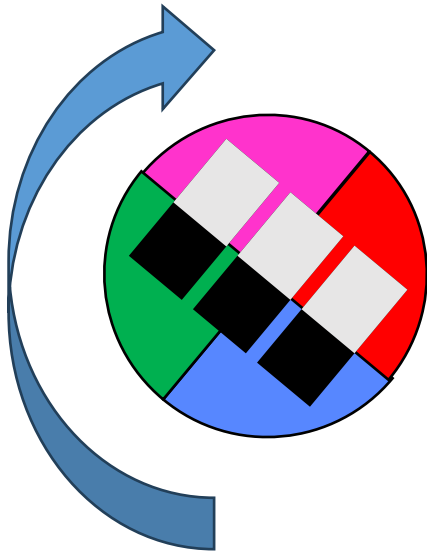


Superparamagnetism

$$B \neq 0, M \neq 0$$

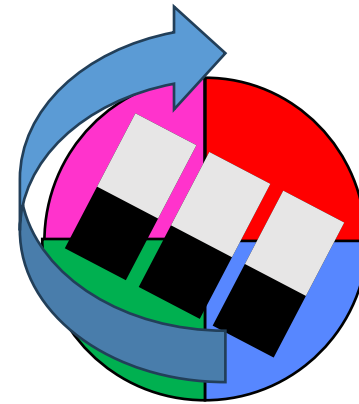


Superparamagnetism



Brownian rotation
(rotates whole NP)

vs.



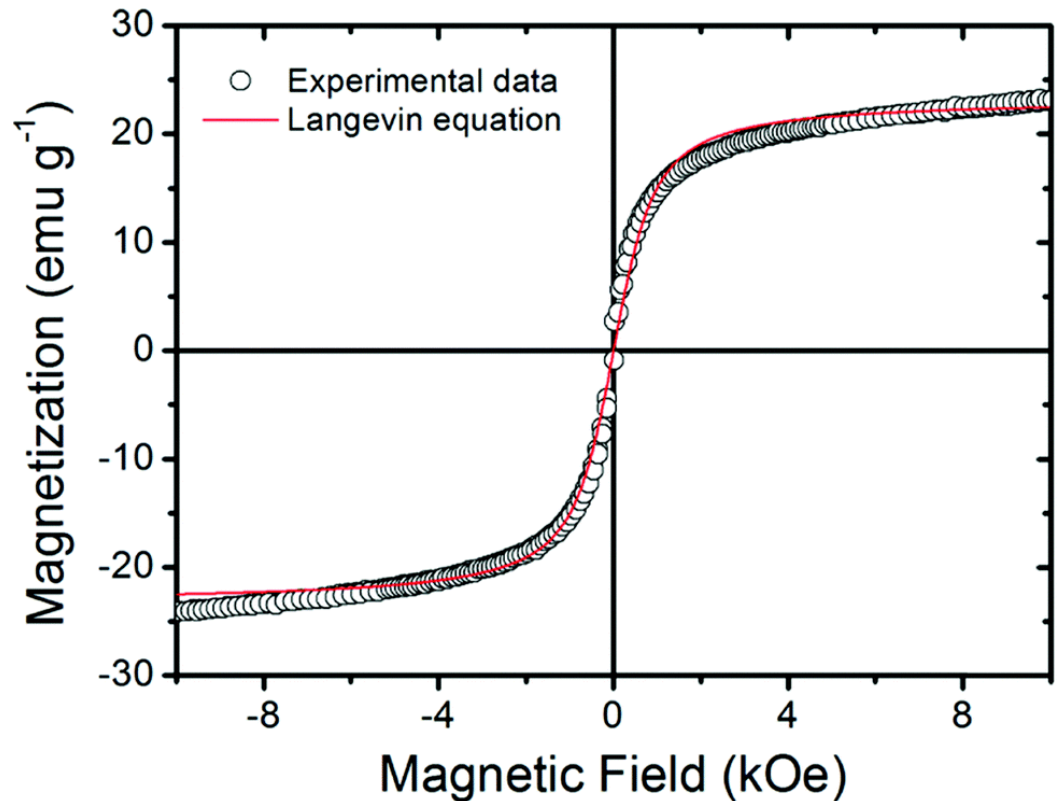
Néel rotation
(rotates just
the mag. moment)

MPI Principle

Superparamagnetic particle in a magnetic field

A response to the external field: alignment with

- Néel relaxation
- Brownian relaxation

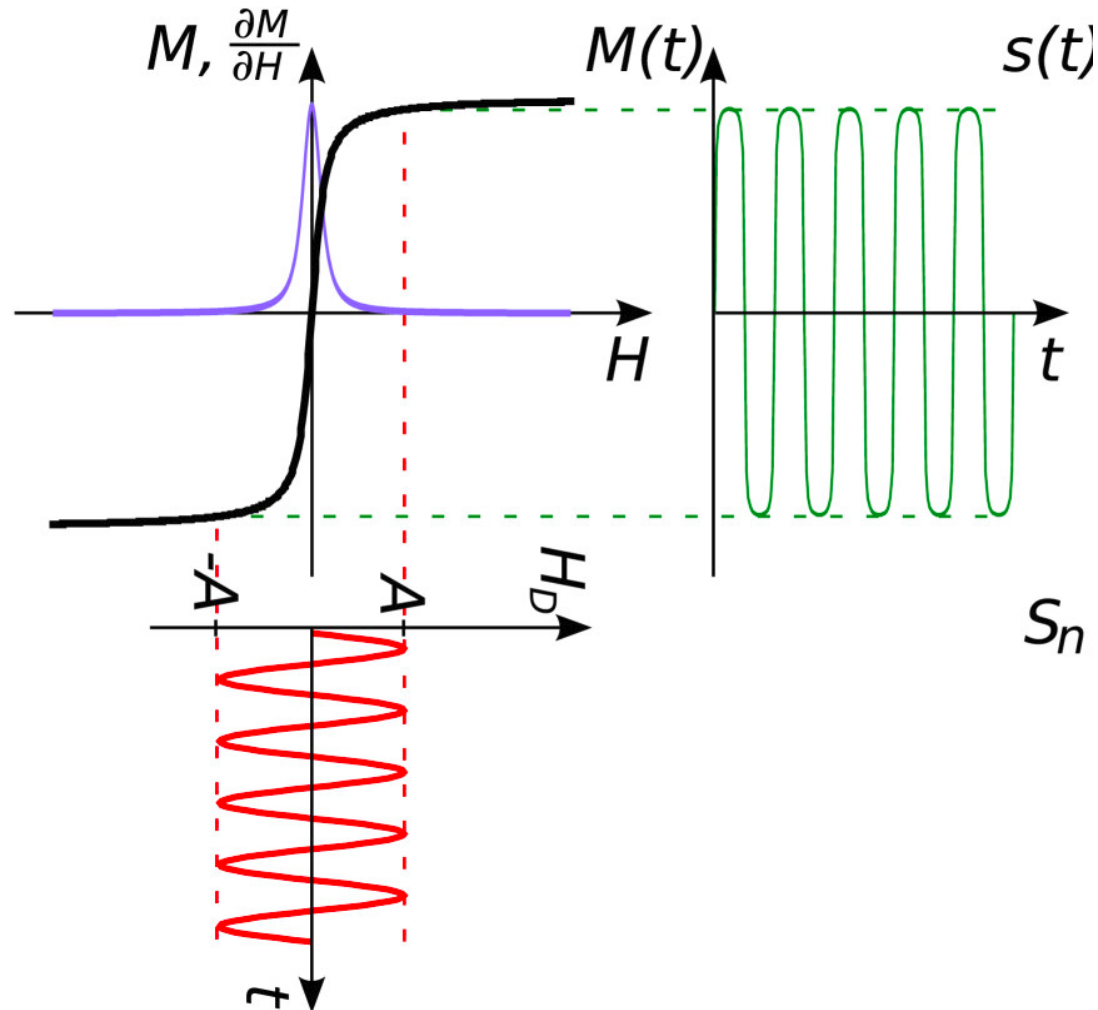


In equilibrium, magnetization M of superparamagnetic particles (with a magnetic moment μ) in the external magnetic field B is described by Langevin equation

$$M(B) = N \mu L(\mu B/kT)$$

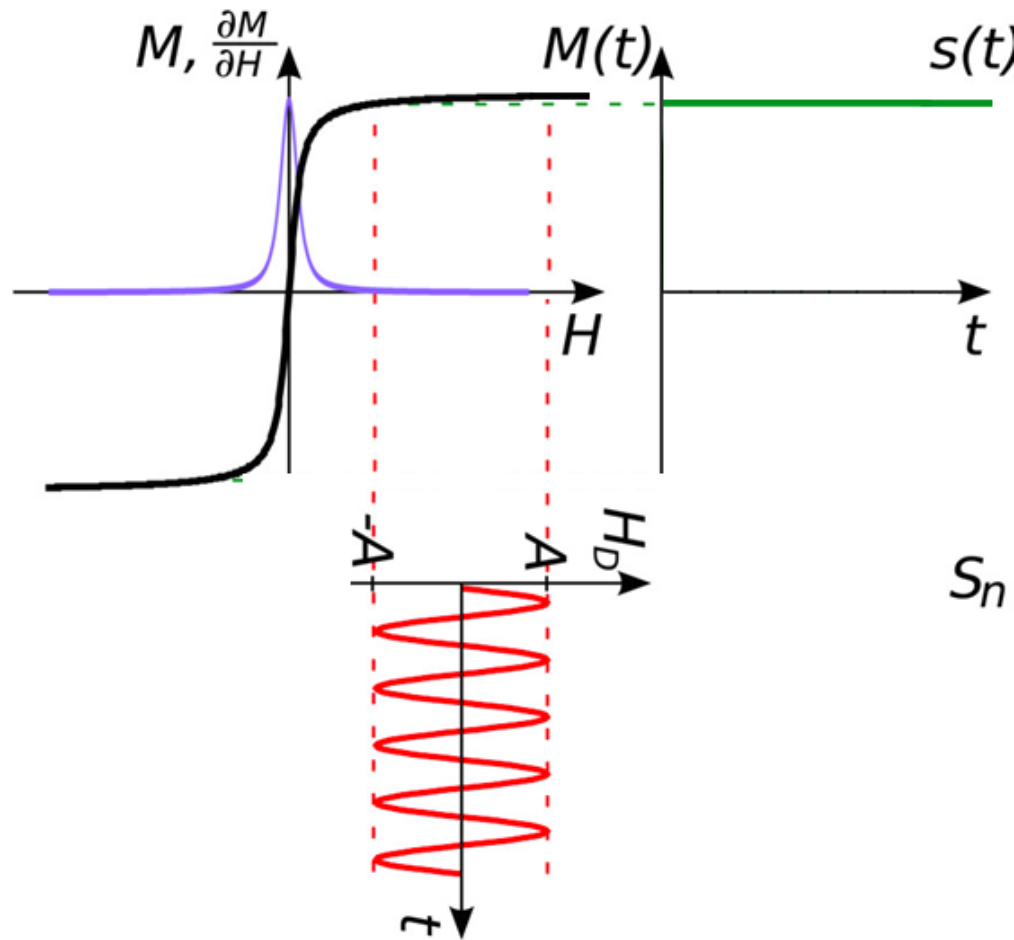
Principle of MPI

External alternating mag. field („drive field“) induces change of magnetization



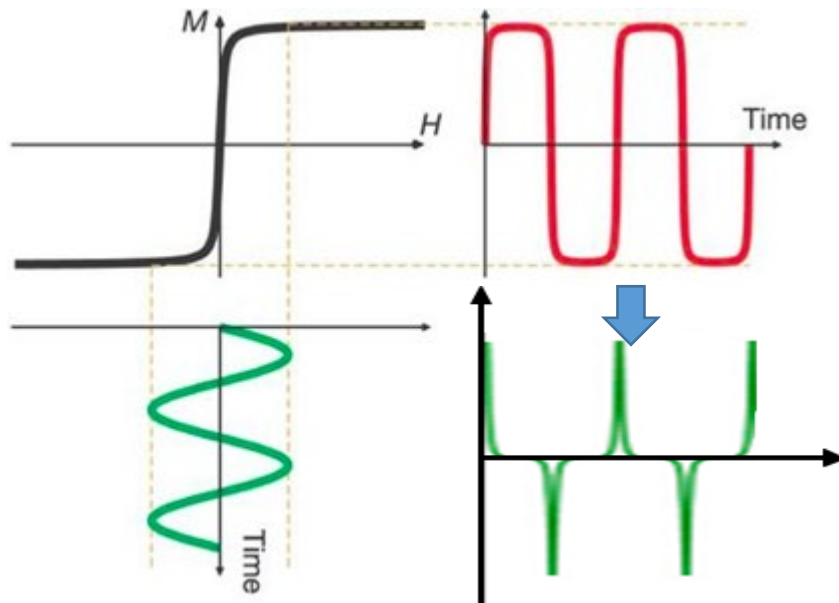
Principle of MPI

In the presence of a static external mag. field

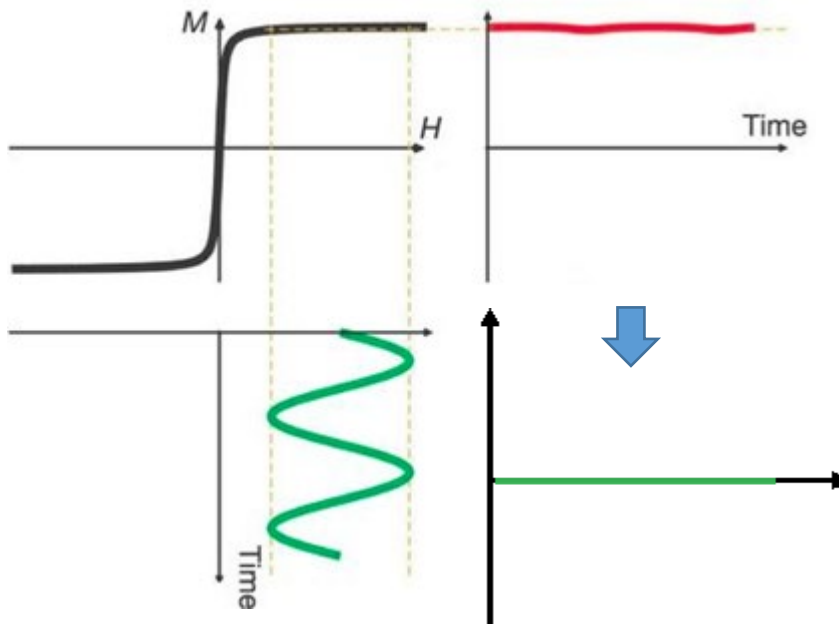


Nanoparticles are saturated, alternating field („drive field“) does not induce change of magnetization!

Principle of MPI



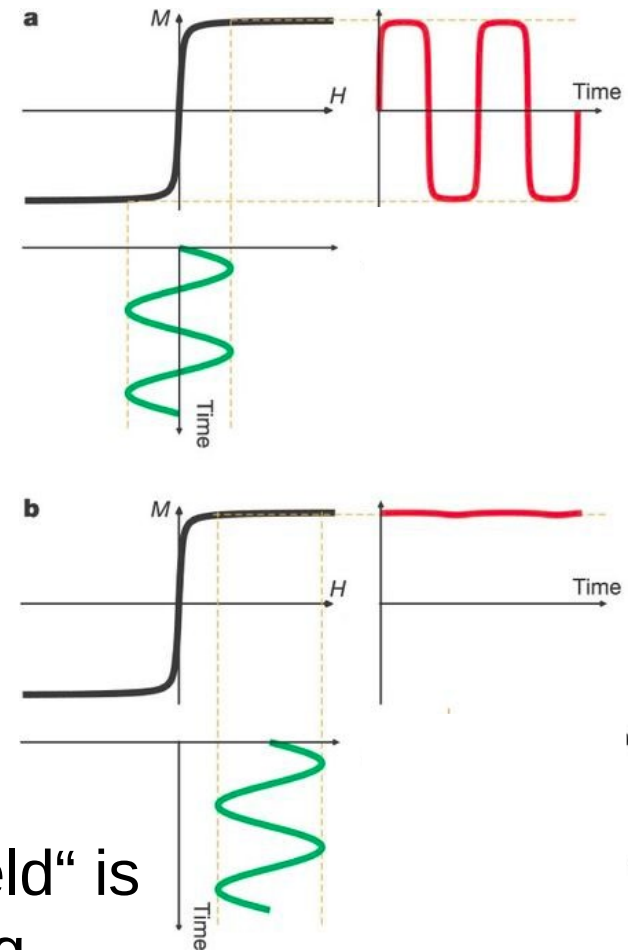
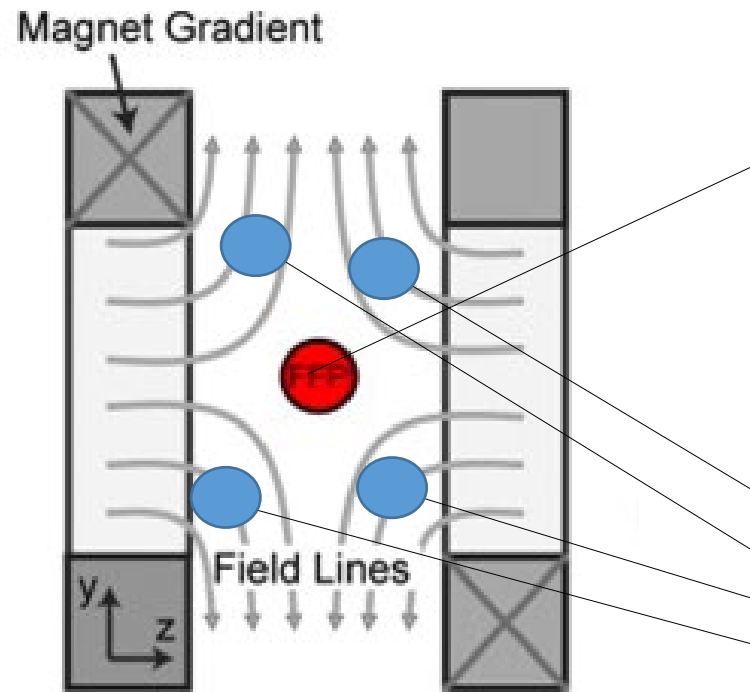
We do not detect magnetization, but its change = derivative!



At saturation, derivative is zero

Principle of MPI

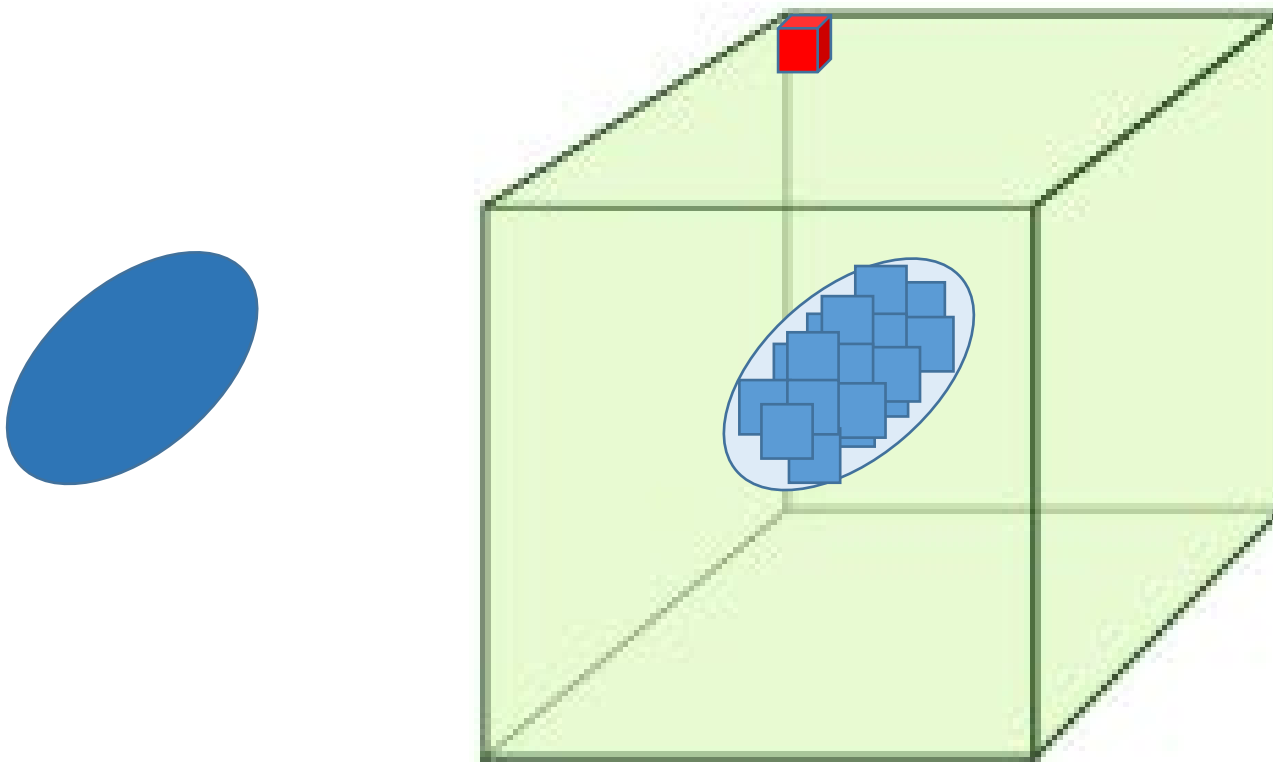
External static gradient field in the space („selection field“)



Change of magnetization induced by the „drive field“ is observed in a small region in the center, remaining particles are saturated

Principle of MPI

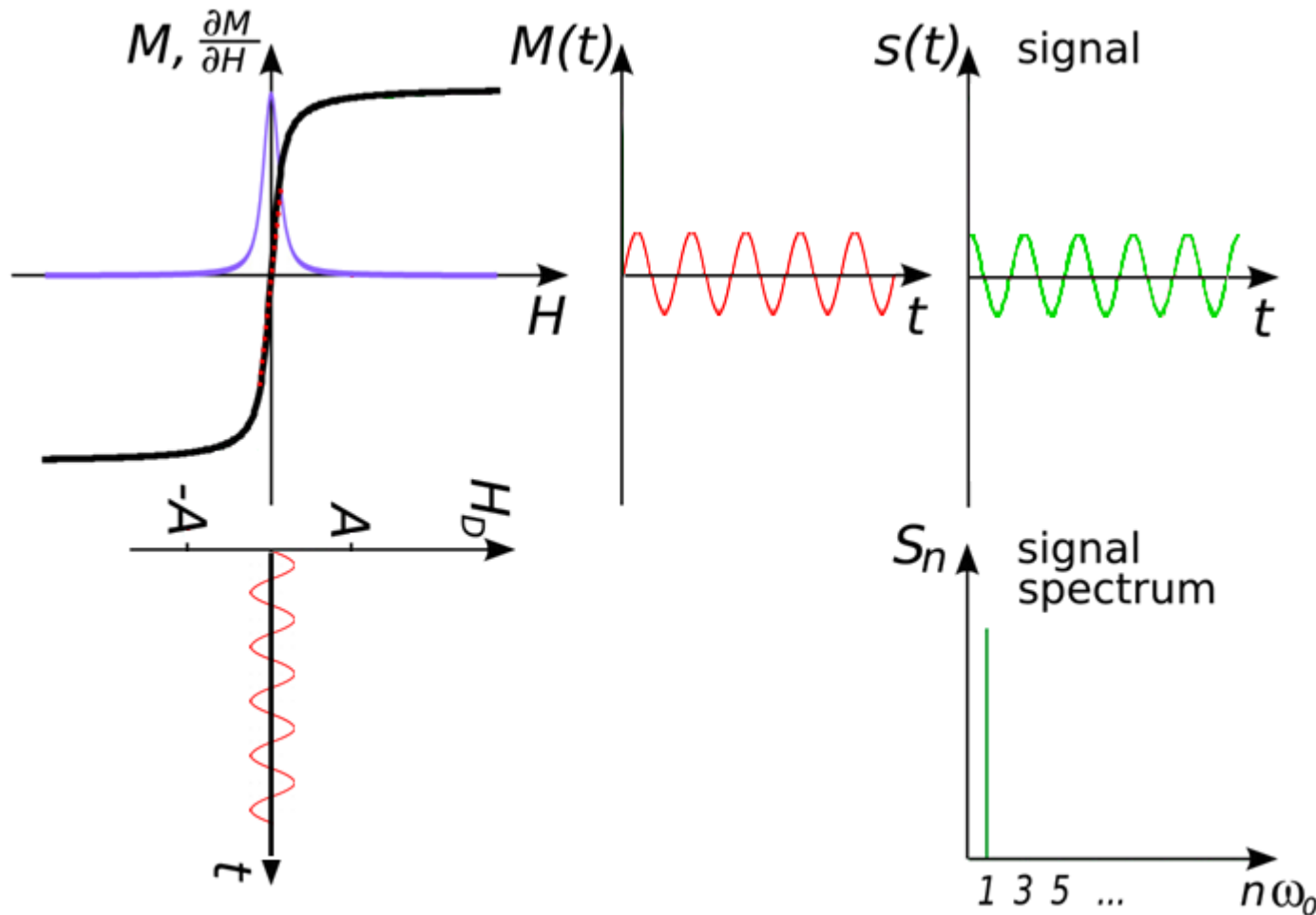
We can scan by the „field free point“ whole space and thus find out the nanoparticle distribution



Problems

- Physical (acquisition during excitation)
- Technical (is it possible to build an apparatus with sufficient field strengths?)
- Practical (sequential scanning of a 3D space would take ages)
- Material (pure superparamagnetic particles are needed, nontoxic, biocompatible...)

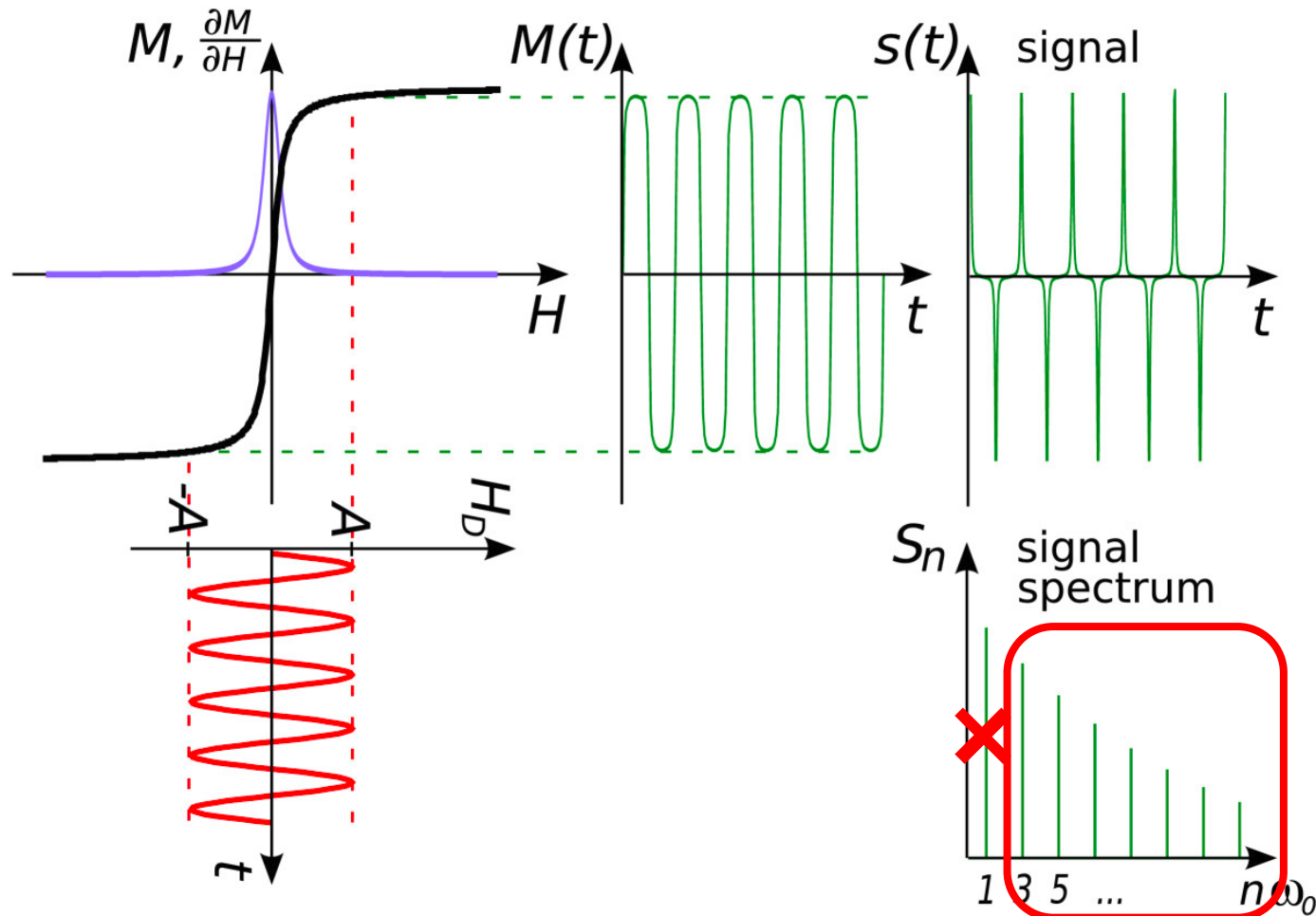
Acquisition during excitation



If amplitude of the alternating „drive field“ is low (i.e., in the linear part of the magnetization curve), the magnetization follows a sinus function and also the signal is sinusoidal

- We record one frequency only

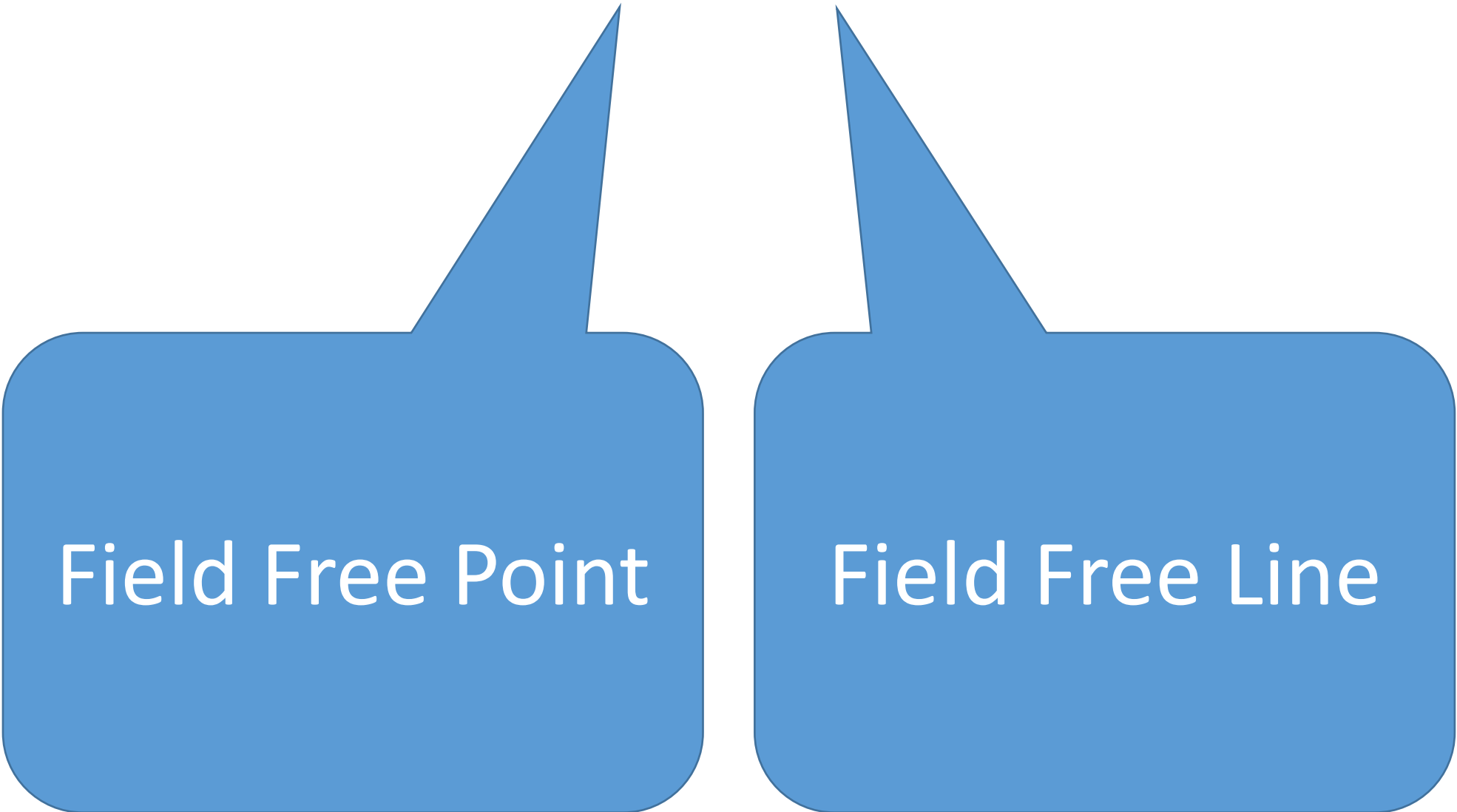
Acquisition during excitation



Amplitude of the alternating „drive field“ should reach non-linear part of the magnetization curve

- Then we record also higher harmonics; basic frequency can be filtered out

How to gain spatially resolved data?
Two approaches:

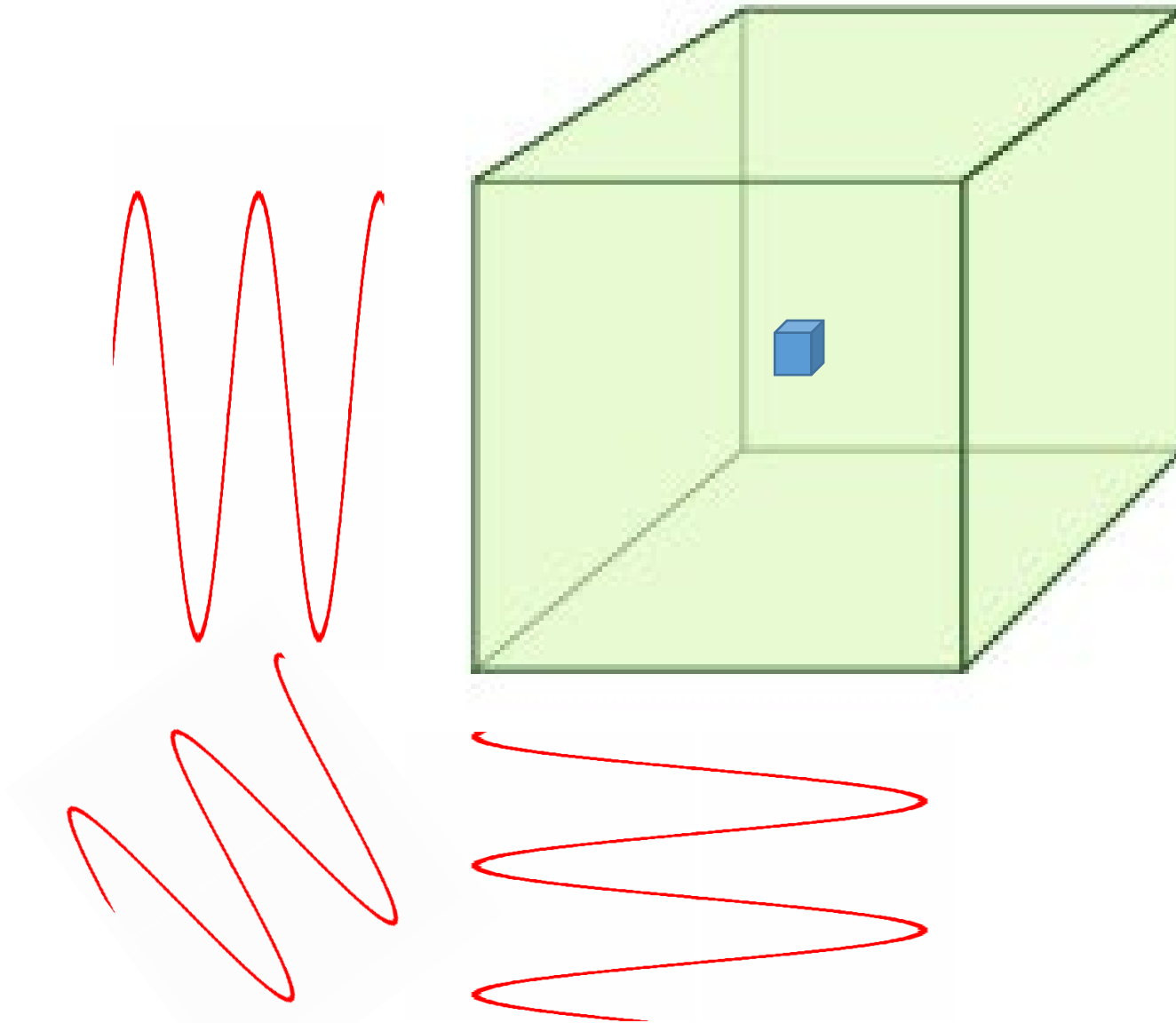


Field Free Point

Field Free Line

Field Free Point Approach

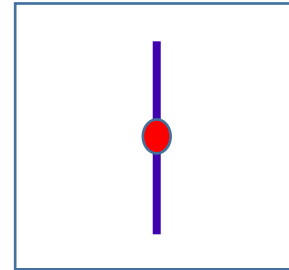
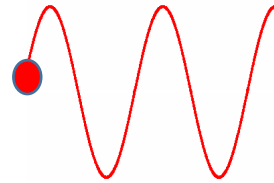
Alternating „drive field“ is applied in all three directions
Drive field simultaneously excites and moves the FFP



Field Free Point Approach

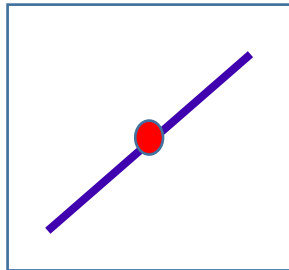
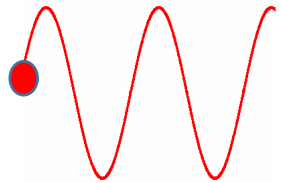
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In one direction:

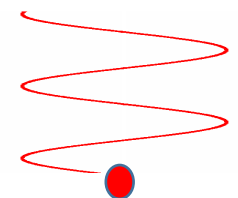
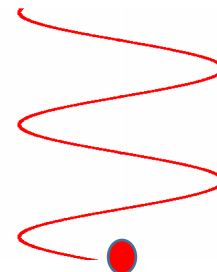
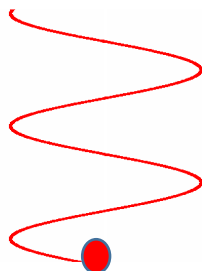
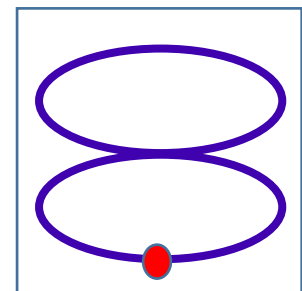
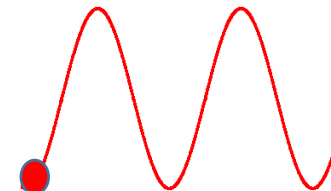
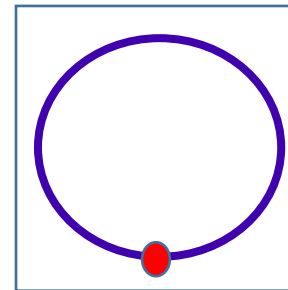
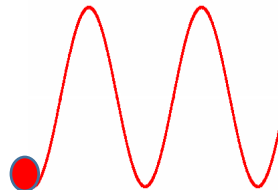


$$x = 0, y = B \sin(b \cdot t)$$

2D Lissajous trajectory...



$$x = A \sin(a \cdot t + \delta), y = B \sin(b \cdot t)$$

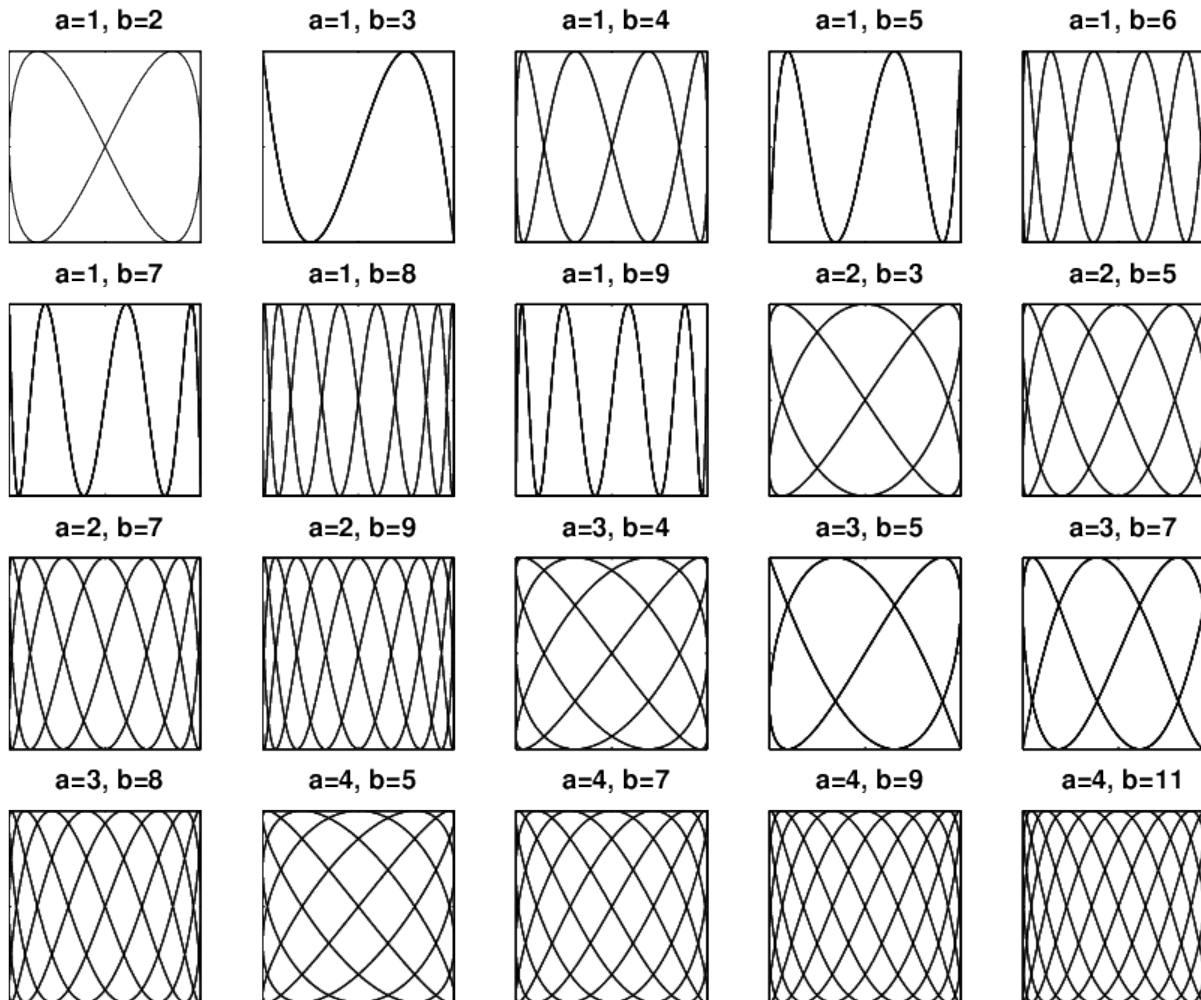


Field Free Point Approach

Alternating „drive field“ is applied in all three directions
Drive field simultaneously excites and moves the FFP

2D Lissajous trajectory...

$$x = A \sin(a*t + \delta), y = B \sin(b*t)$$

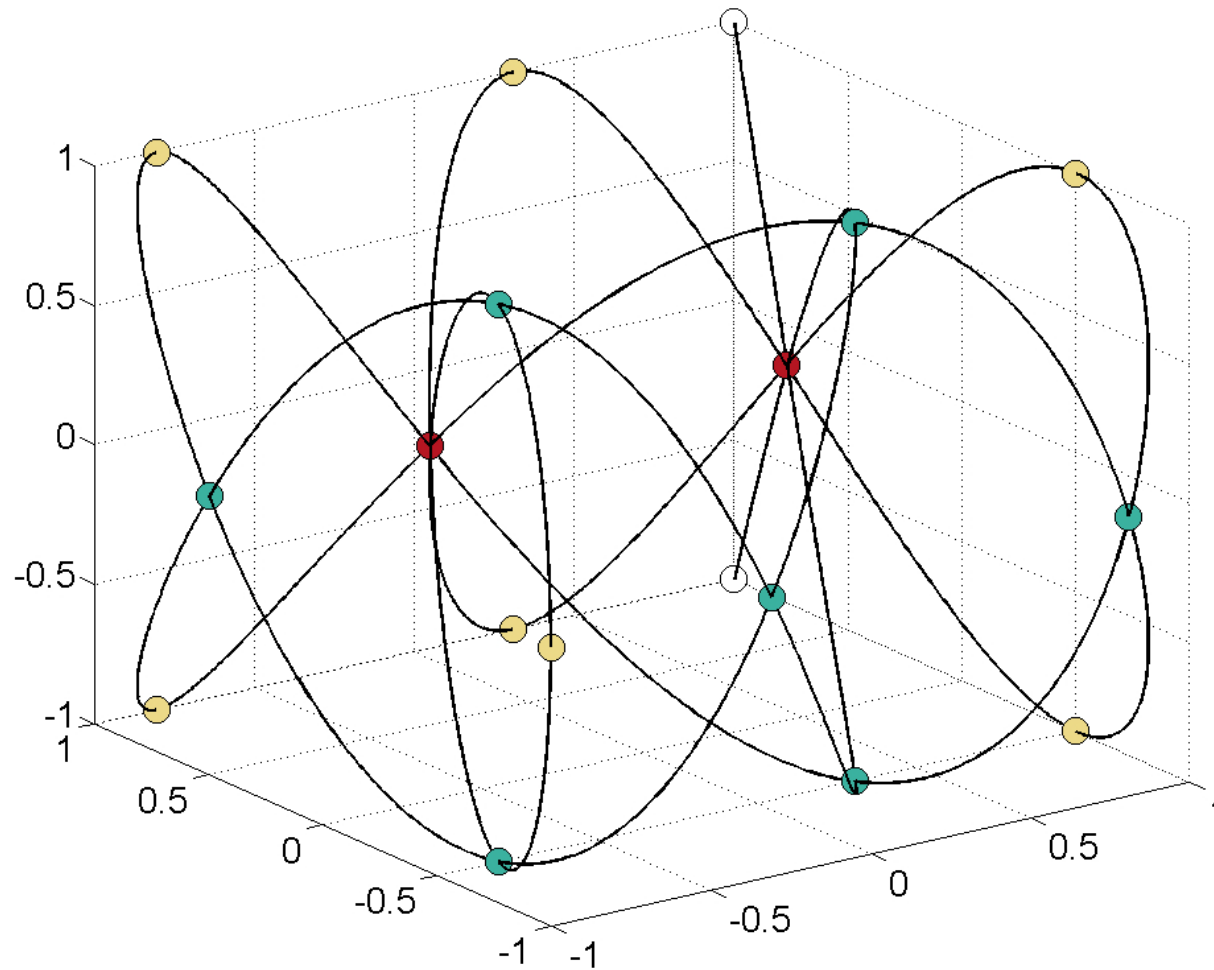


The higher the least common multiple of the frequencies, the more dense trajectory!

Field Free Point Approach

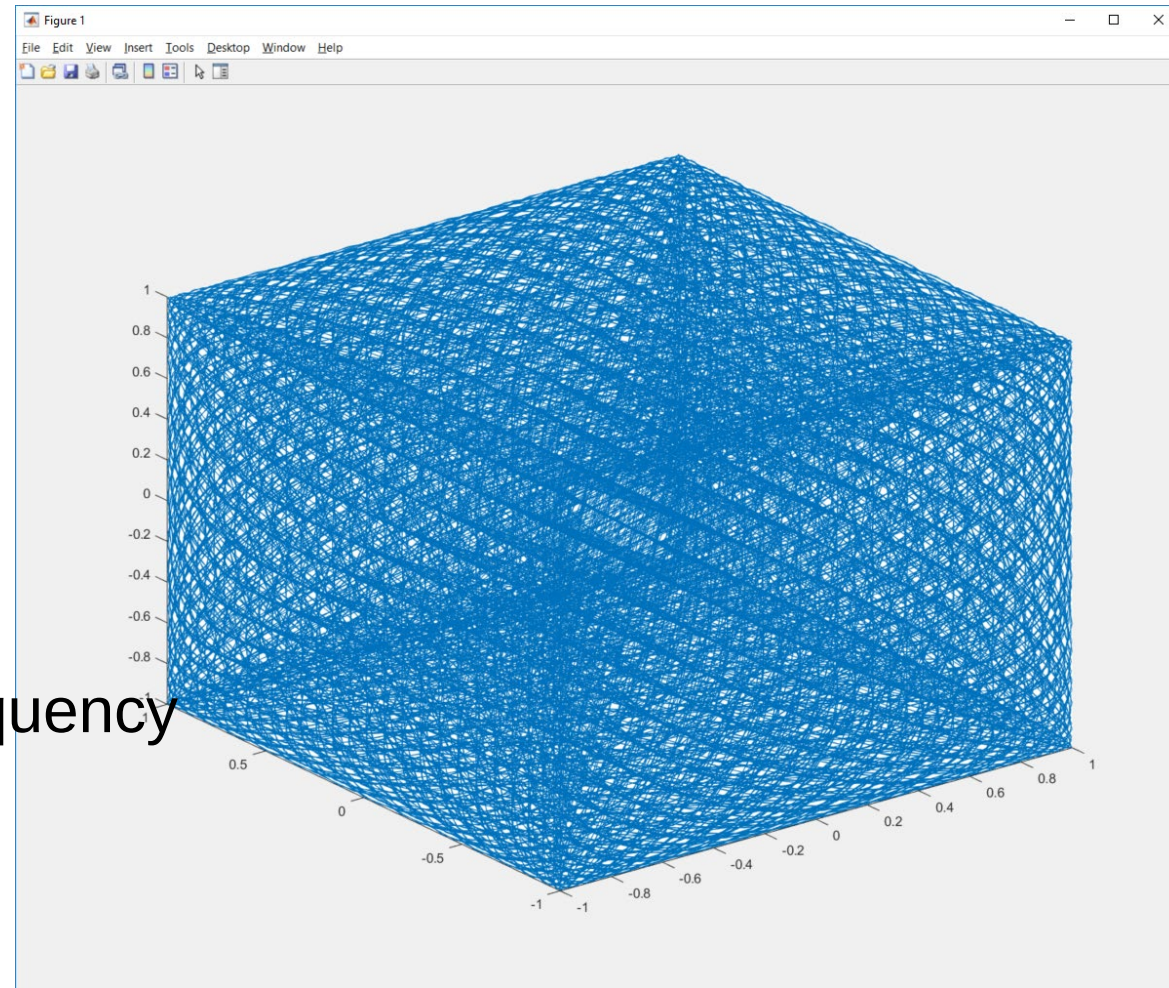
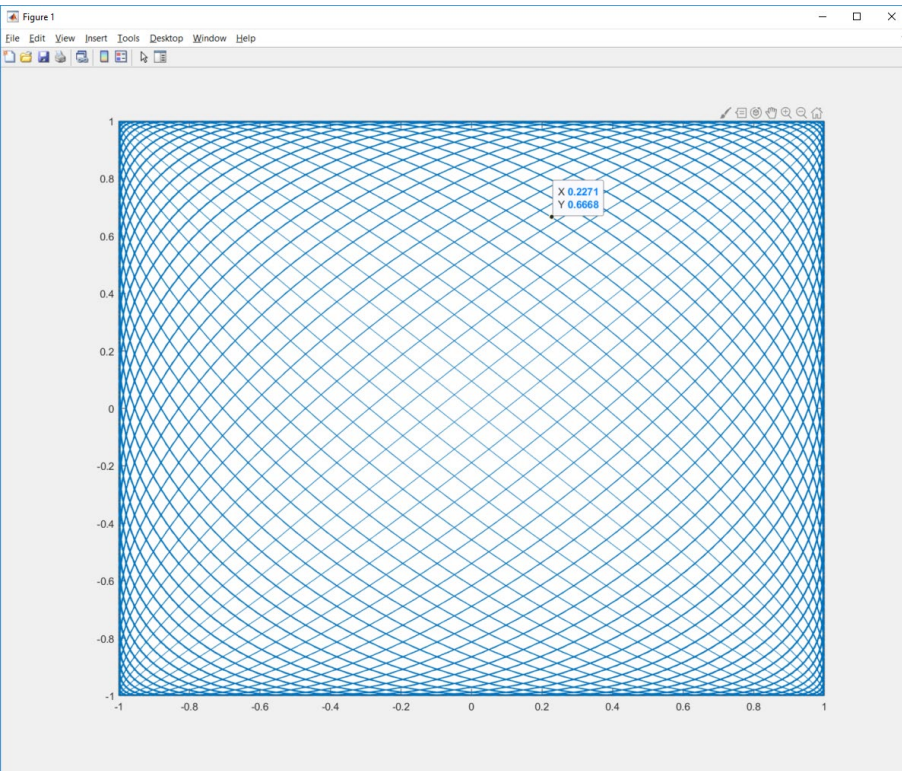
Alternating „drive field“ is applied in all three directions
Drive field simultaneously excites and moves the FFP

3D Lissajous trajectory... $x = A \sin(a \cdot t + \delta_1)$, $y = B \sin(b \cdot t + \delta_2)$, $z = C \sin(c \cdot t)$



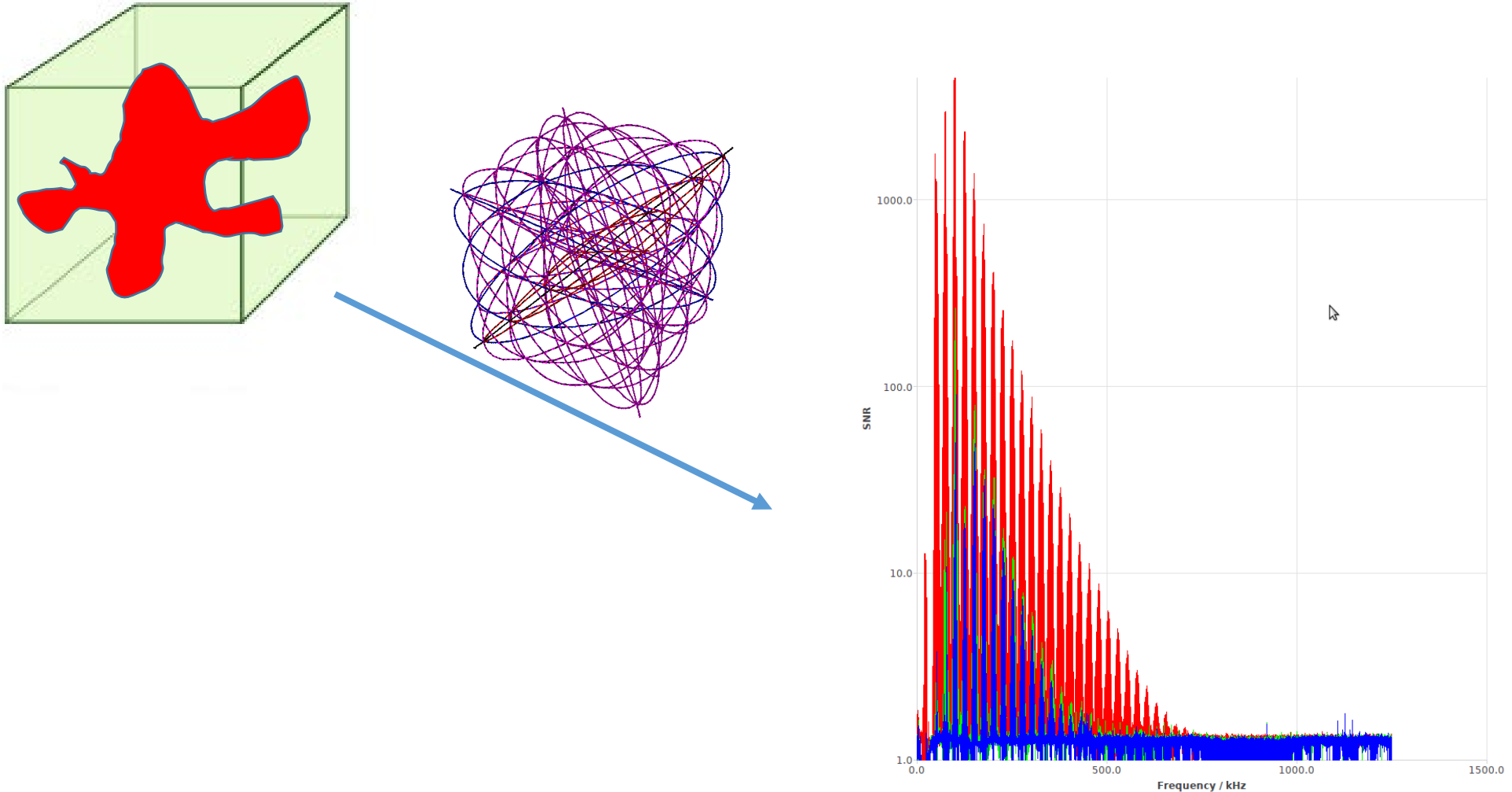
Virtual basic frequency $f = 2.5$ MHz,
Frequencies in three directions are derived as $f/96$, $f/99$, $f/102$

3D trajectory repeats with a frequency
 $2.5 \text{ MHz}/53856 = 46,42 \text{ Hz}$ (21.5 ms)



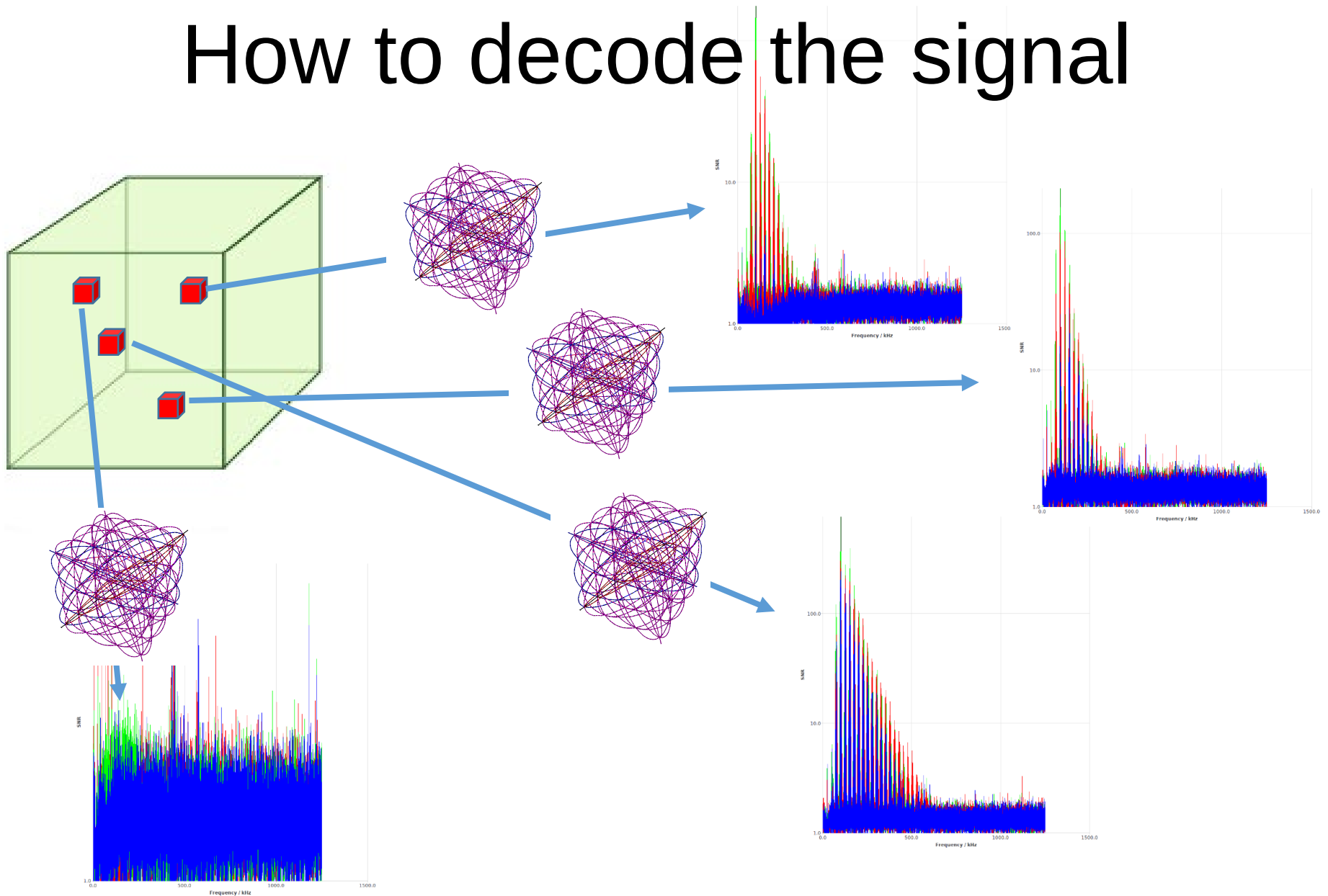
2D trajectory repeats with a frequency
 $2.5 \text{ MHz}/3168 = 789.1 \text{ Hz}$
(1.27 ms)

How to decode the signal



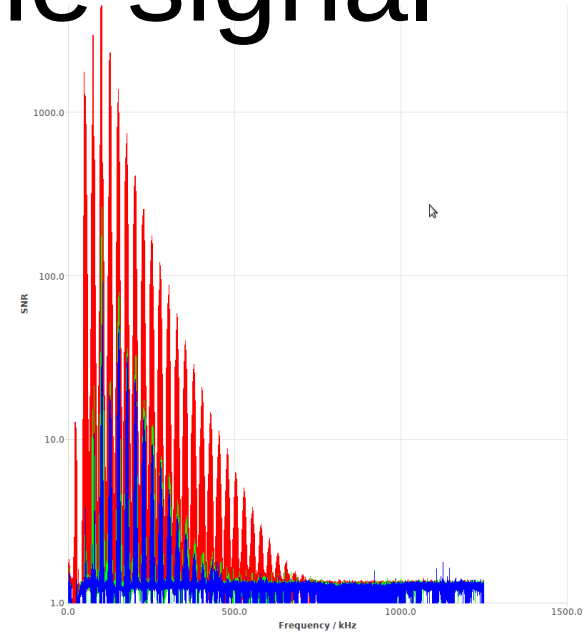
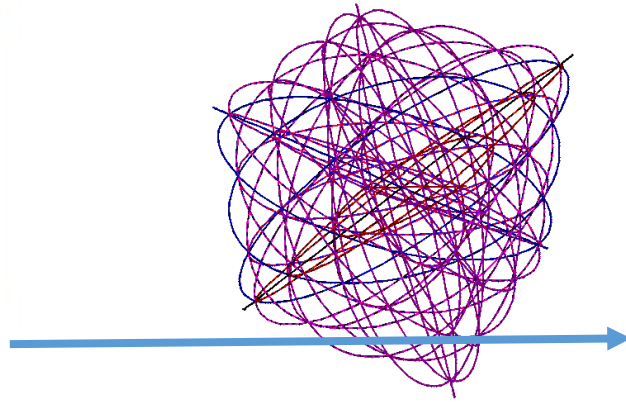
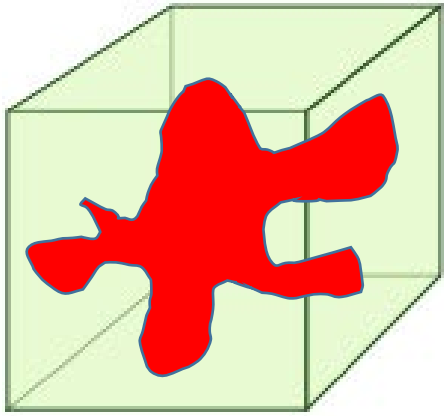
The acquired signal will be a sum of all the signals from the whole volume recorded along the Lissajous trajectory! **How to decode it?**

How to decode the signal



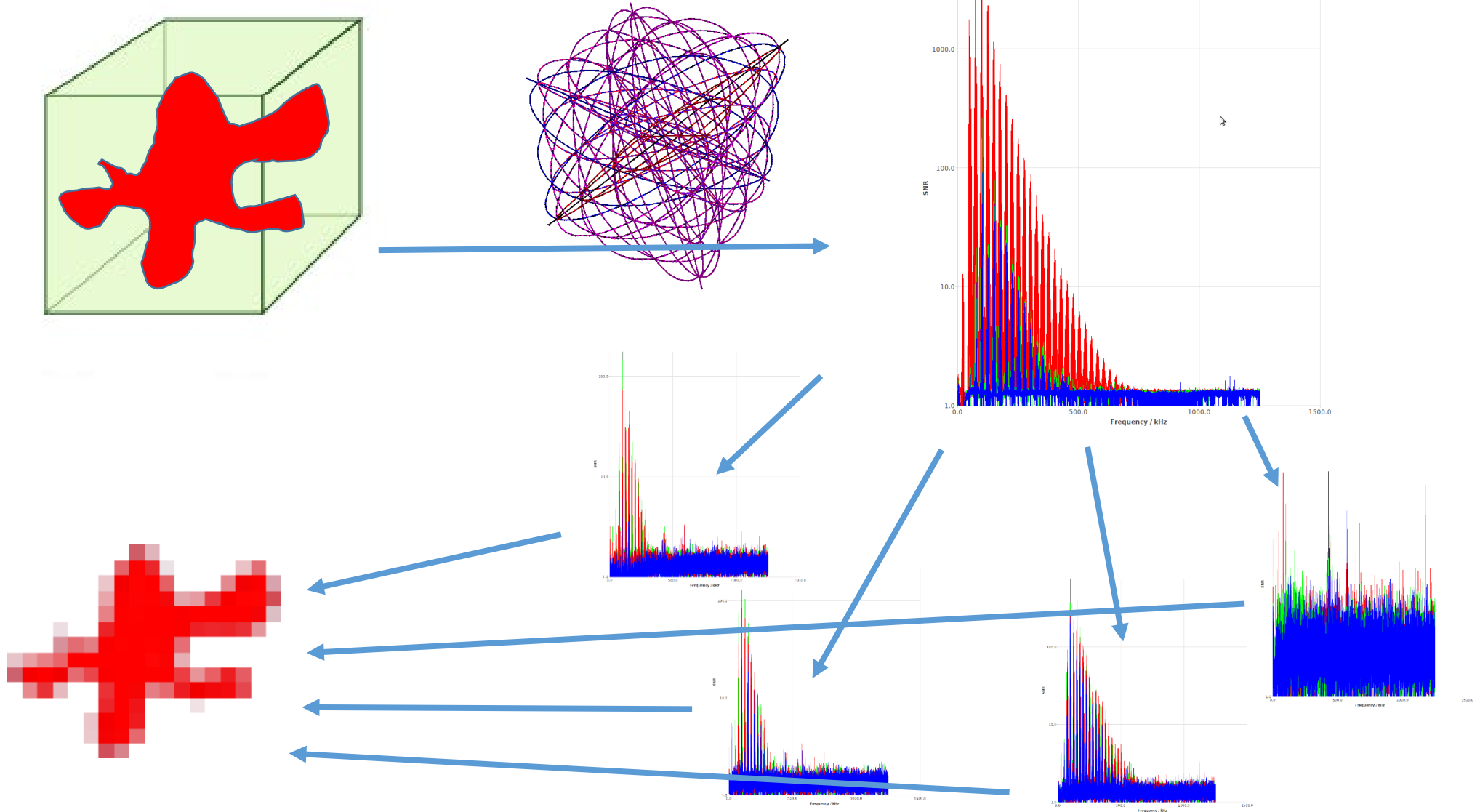
1. We perform a calibration using a known sample: a step-by-step measurement in ALL points of the scanned space – and its signal is recorded along the Lissajous trajectory

How to decode the signal



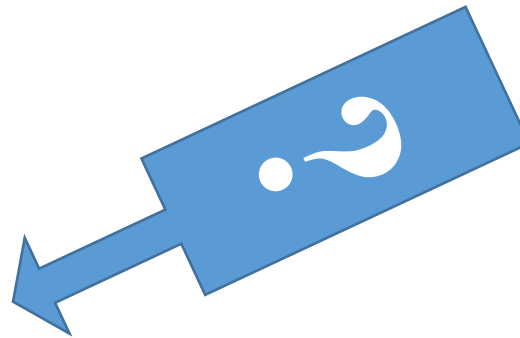
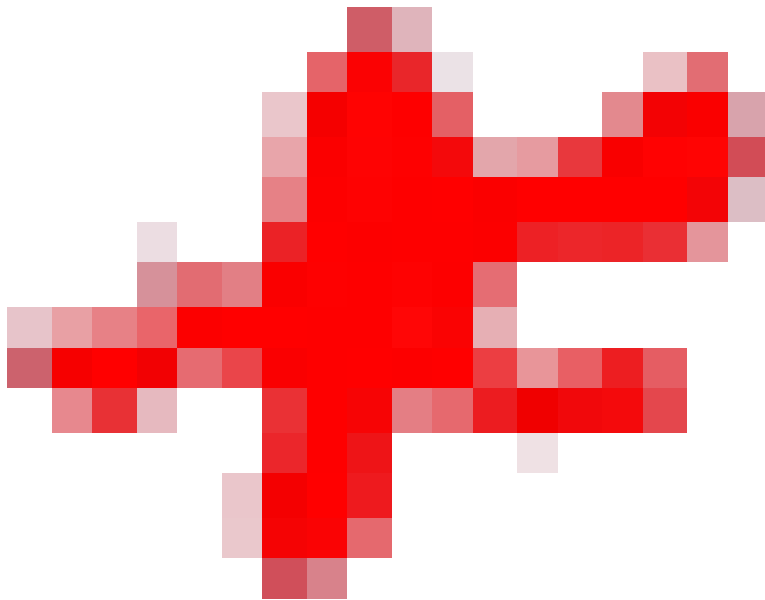
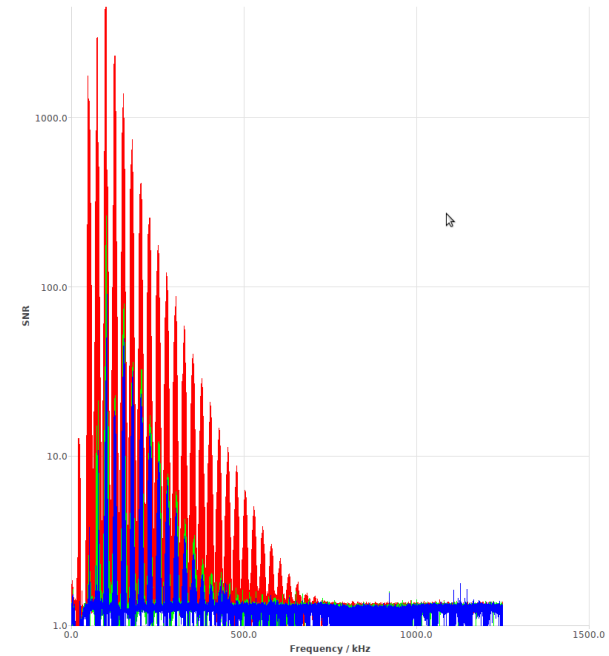
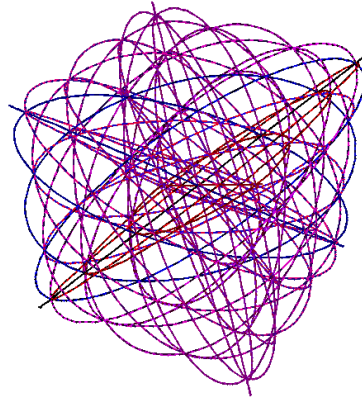
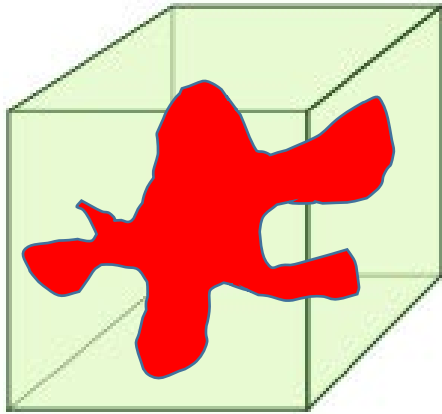
2. Unknown sample is scanned once, its signal contains information from the whole volume.

How to decode the signal



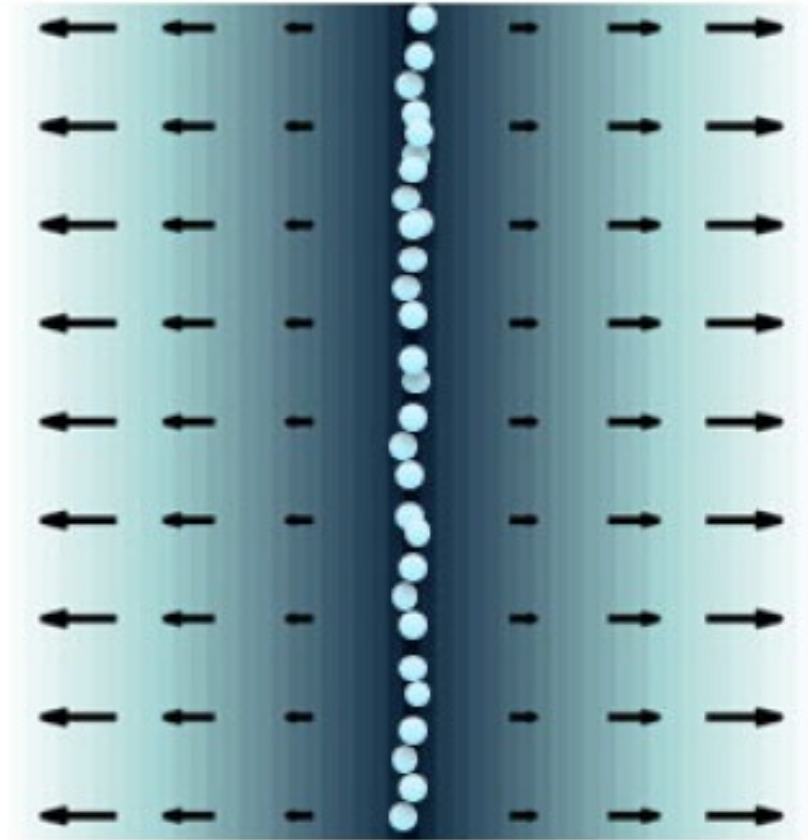
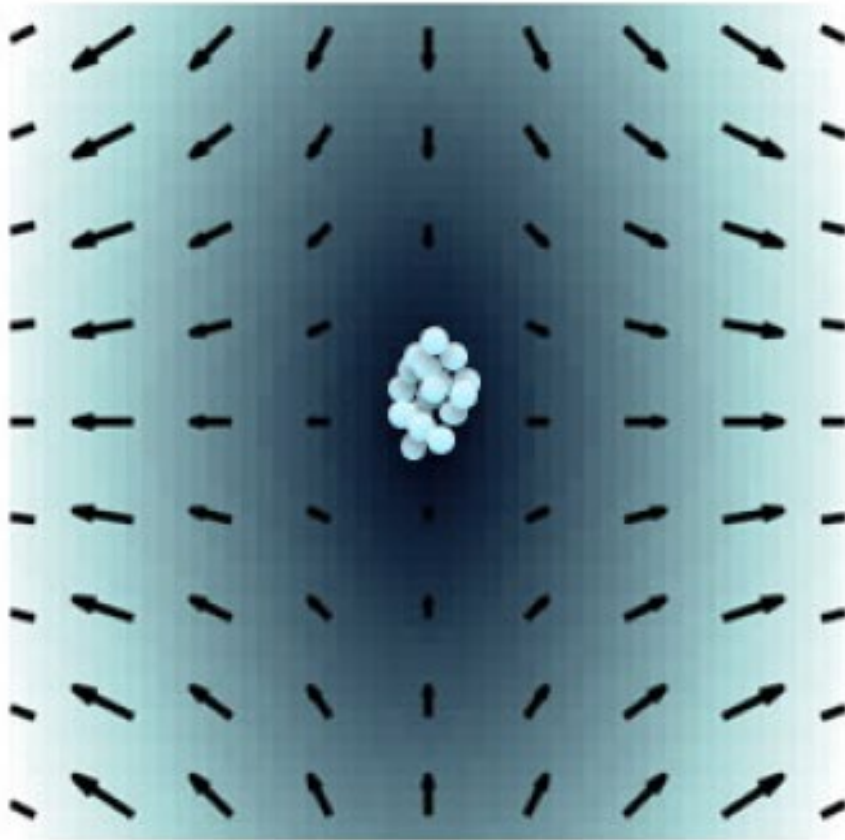
3. Signal of the sample is fitted by a linear combination of calibration signals, the linear coefficients define distribution of the nanoparticles. The sample has to contain the SAME particles!

Is it possible to decode the signal directly?



Probably not unambiguously...

Field Free Line Approach



Field Free Line Approach

Signal distribution in x-y plane:

$$f(\mathbf{x}) = f(x, y)$$

Signal along a straight line L :

$$Rf(L) = \int_L f(\mathbf{x}) |d\mathbf{x}|$$

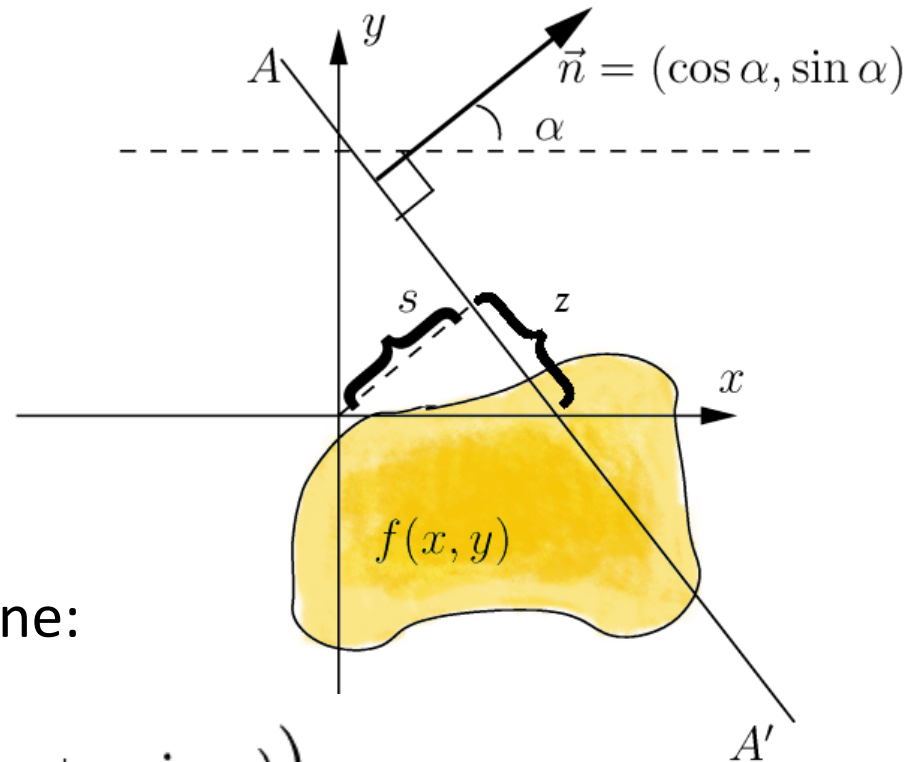
Introducing a parametric equation of a line:

$$(x(z), y(z)) = \left((z \sin \alpha + s \cos \alpha), (-z \cos \alpha + s \sin \alpha) \right)$$

Then:

$$Rf(\alpha, s) = \int_{-\infty}^{\infty} f(x(z), y(z)) dz = \int_{-\infty}^{\infty} f((z \sin \alpha + s \cos \alpha), (-z \cos \alpha + s \sin \alpha)) dz$$

(Ray integral – Radon transformation)



Field Free Line Approach

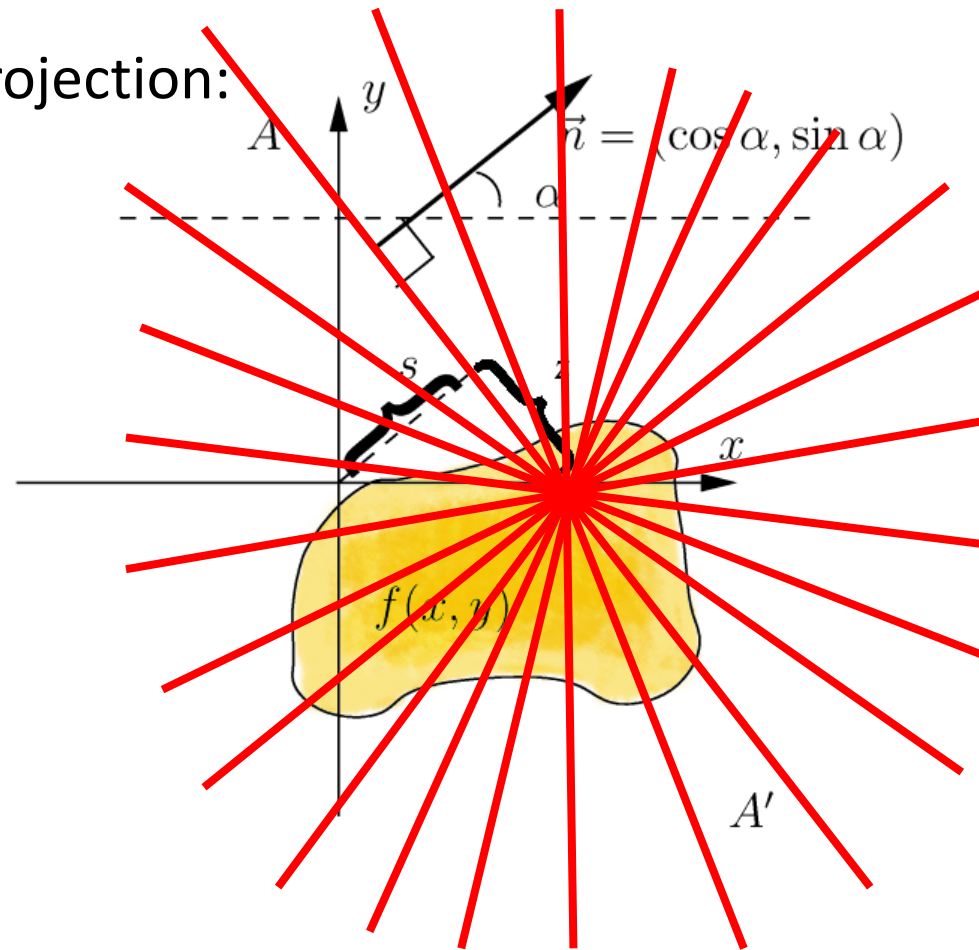
Inverse Radon transformation – back-projection:

Search for

$$f(\mathbf{x}) = f(x, y)$$

in

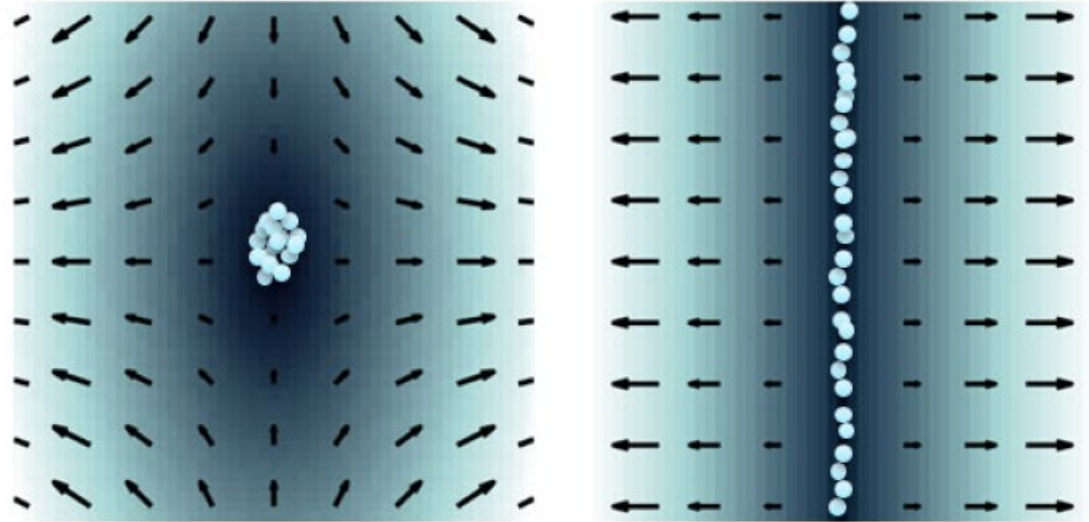
$$Rf(\alpha, s) = \int_{-\infty}^{\infty} f(x(z), y(z)) dz$$



→ → necessary to fill Radon space by measurement at various angles α

As there is a limited number of α (discrete values), a discrete inverse Radon transformation is needed

Field Free Line Approach



Advantages

- Higher sensitivity (obtaining higher signal during a single scan)
- Easier reconstruction using Radon transformation

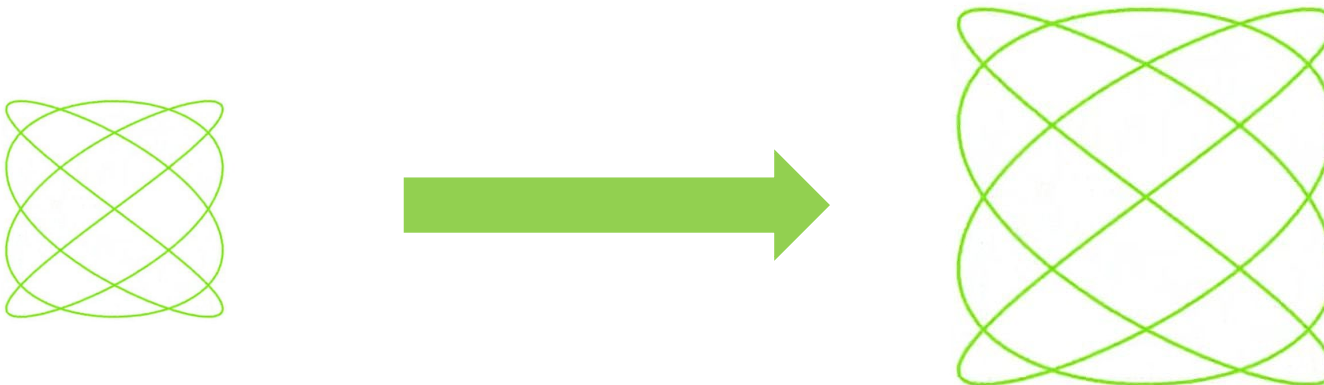
Scanning volume in FFP method

Gradient „selection field“ and alternating „drive field“ define the scanning volume

14 mT + 2.5 T/m: $32 \times 32 \times 16 \text{ mm}^3$

To cover a volume of a mouse: $48 \times 36 \times 24 \text{ mm}^3$ (DF 14 mT; 9 mT; 14 mT, SF = 1 T/m)

Lower gradients increase the volume, but decrease spatial resolution!

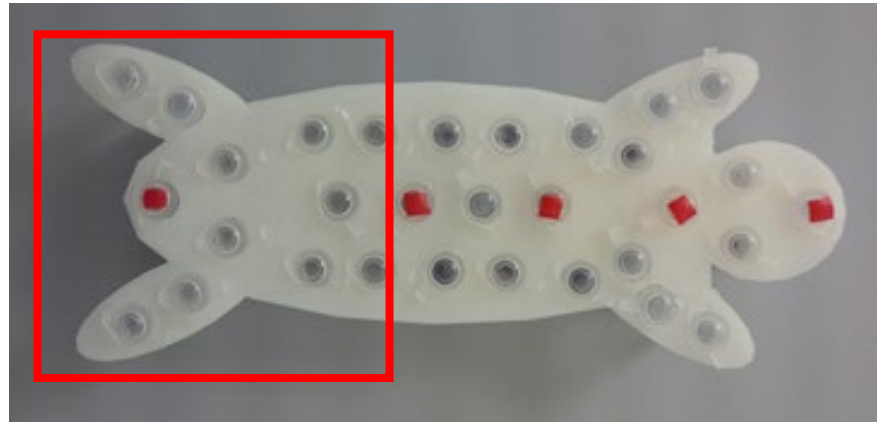


Low gradients stretch the same field range into bigger volume, but the data have same size

Scanning volume

FOV can be enlarged

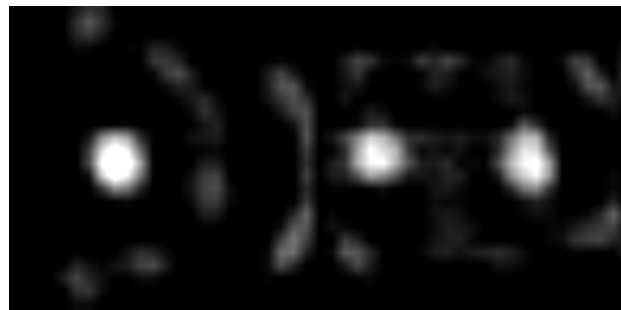
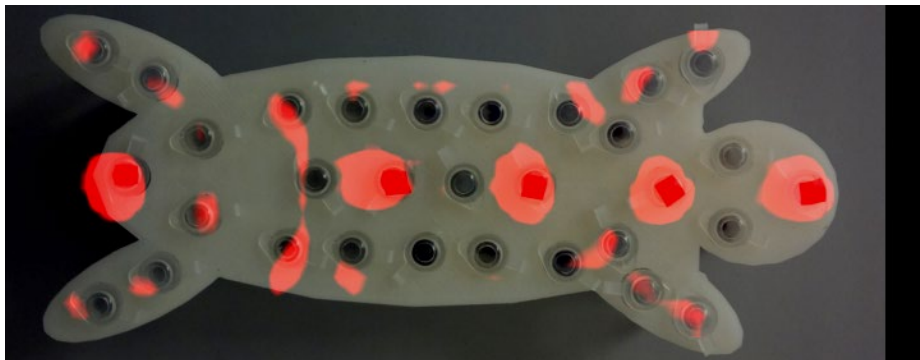
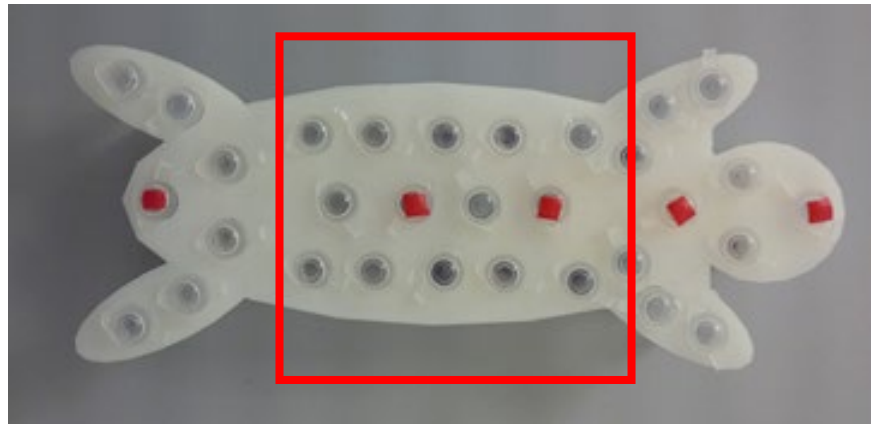
- „table move“ – shift of the scanned sample, a sequence of images
- is then merged into one
- focus fields – another magnetic fields, which shifts FOV in the space



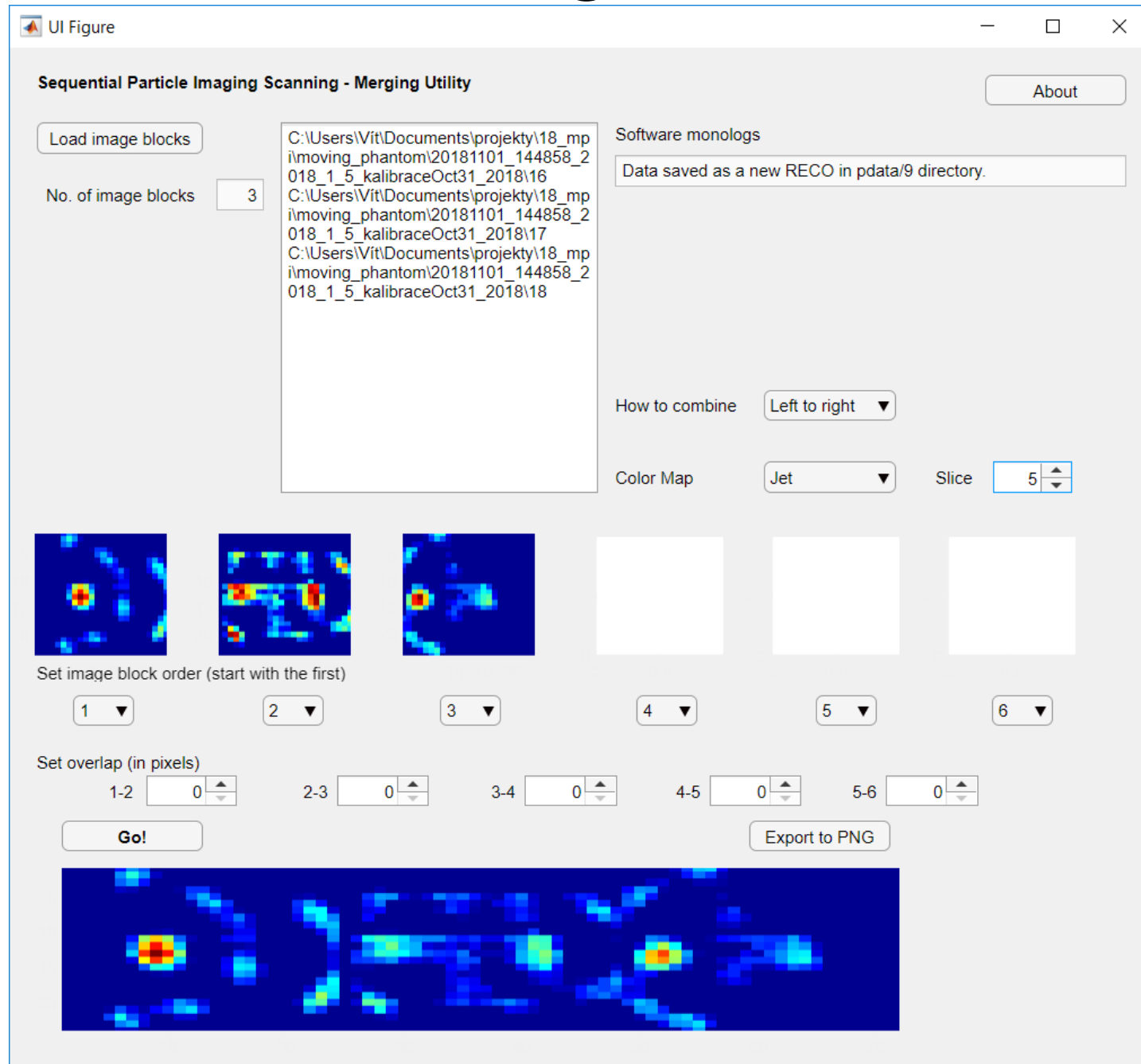
Scanning volume

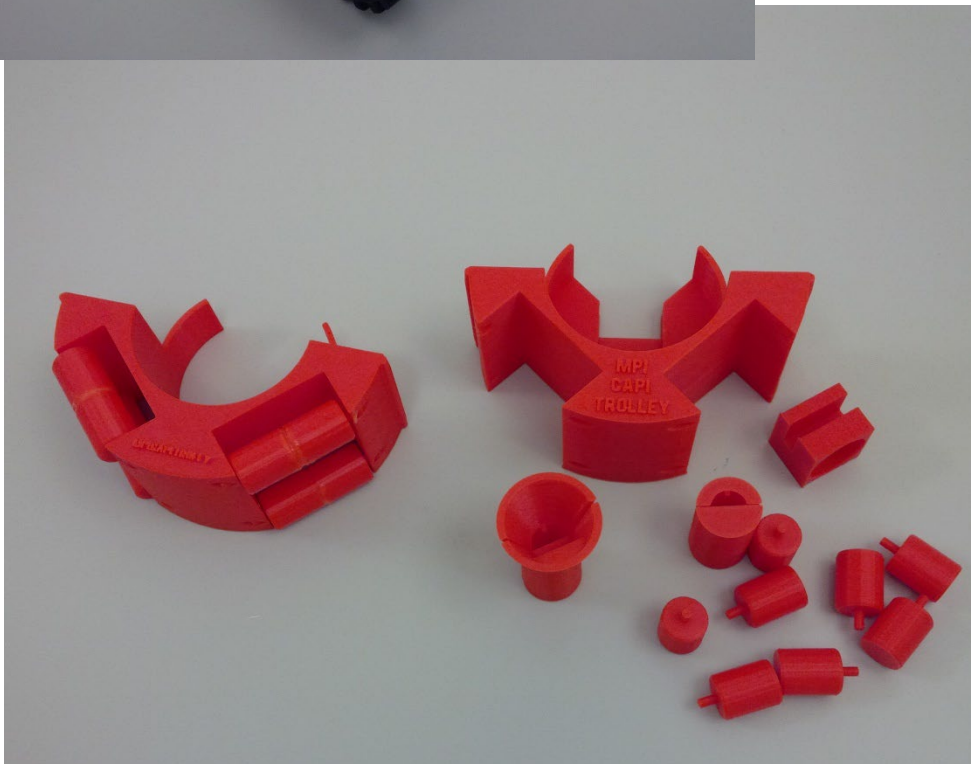
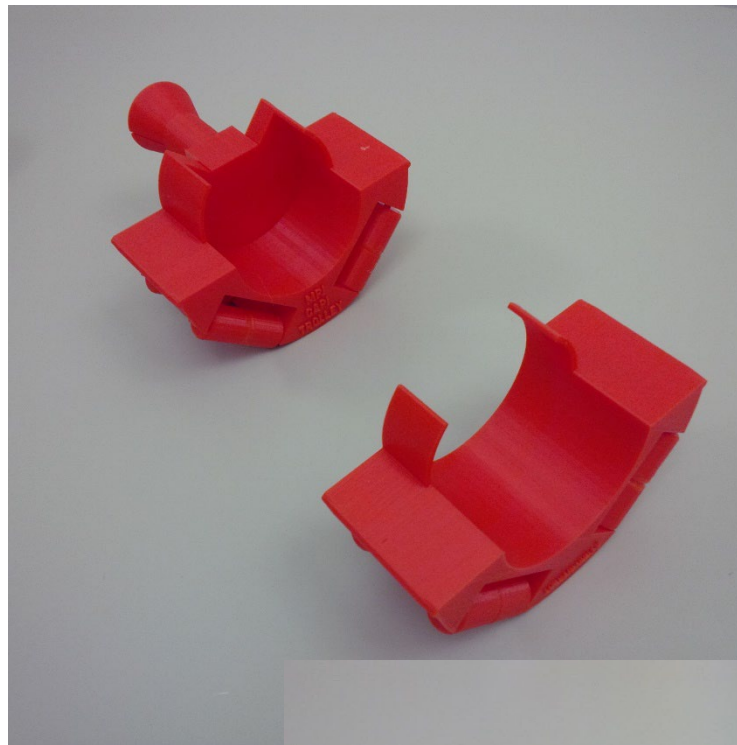
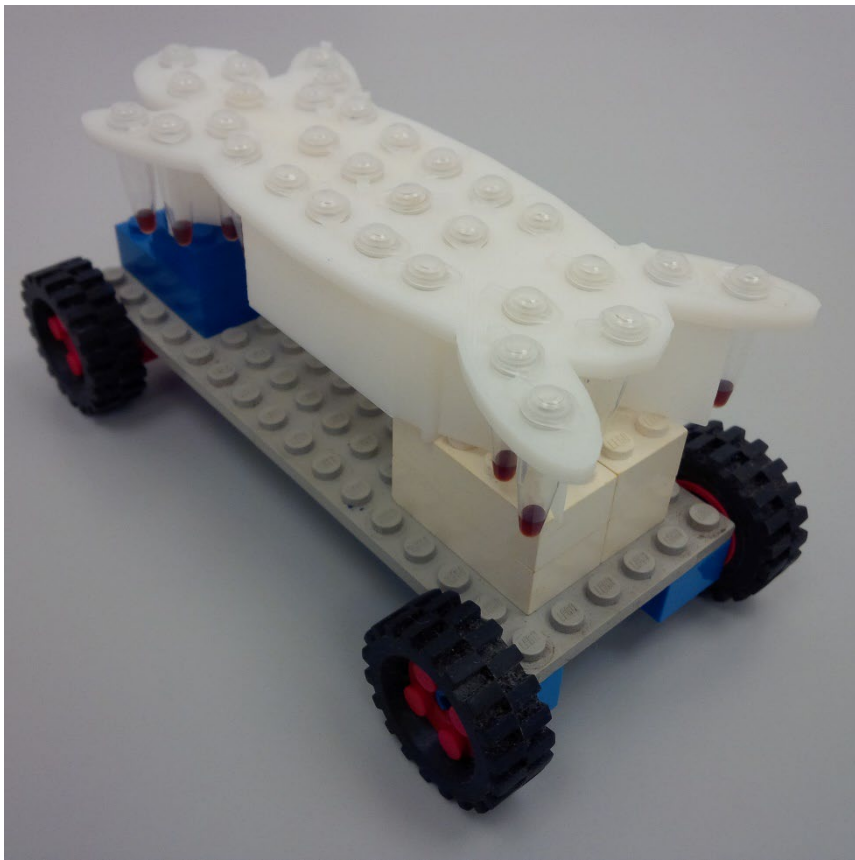
FOV can be enlarged

- „table move“ – shift of the scanned sample, a sequence of images is then merged into one
- focus fields – another magnetic fields, which shift FOV in the space



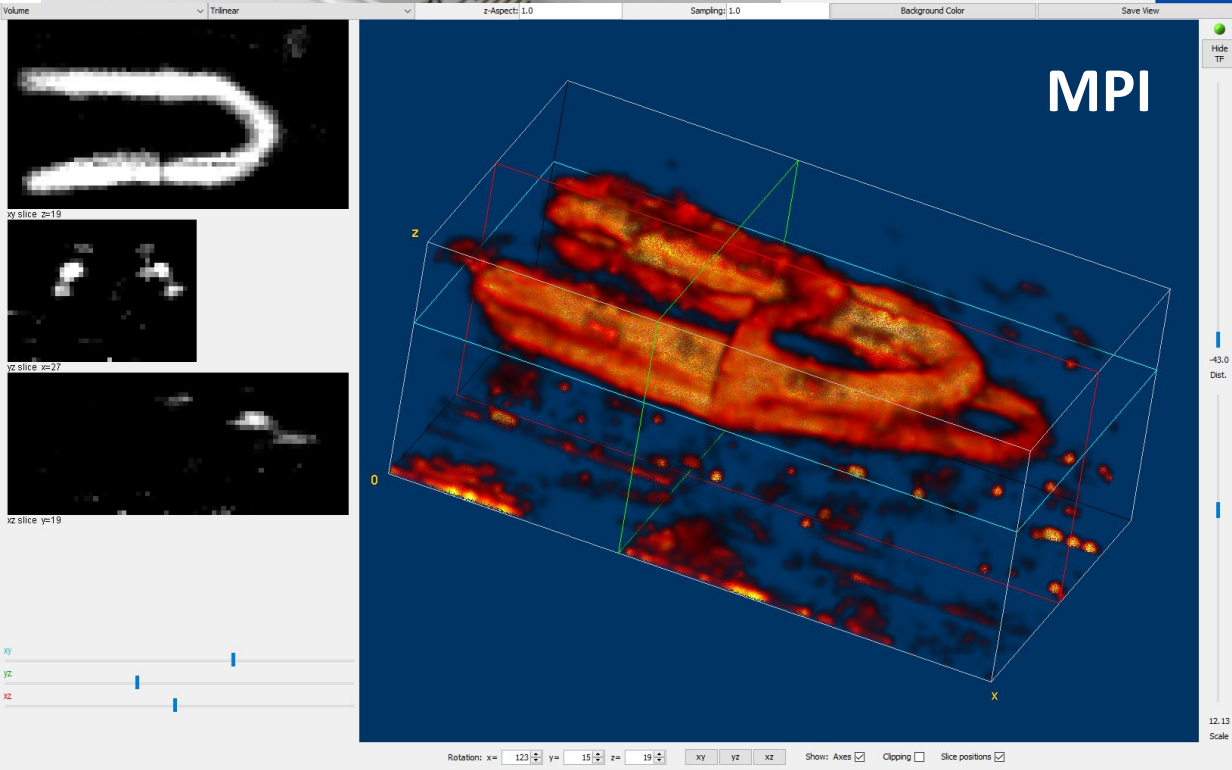
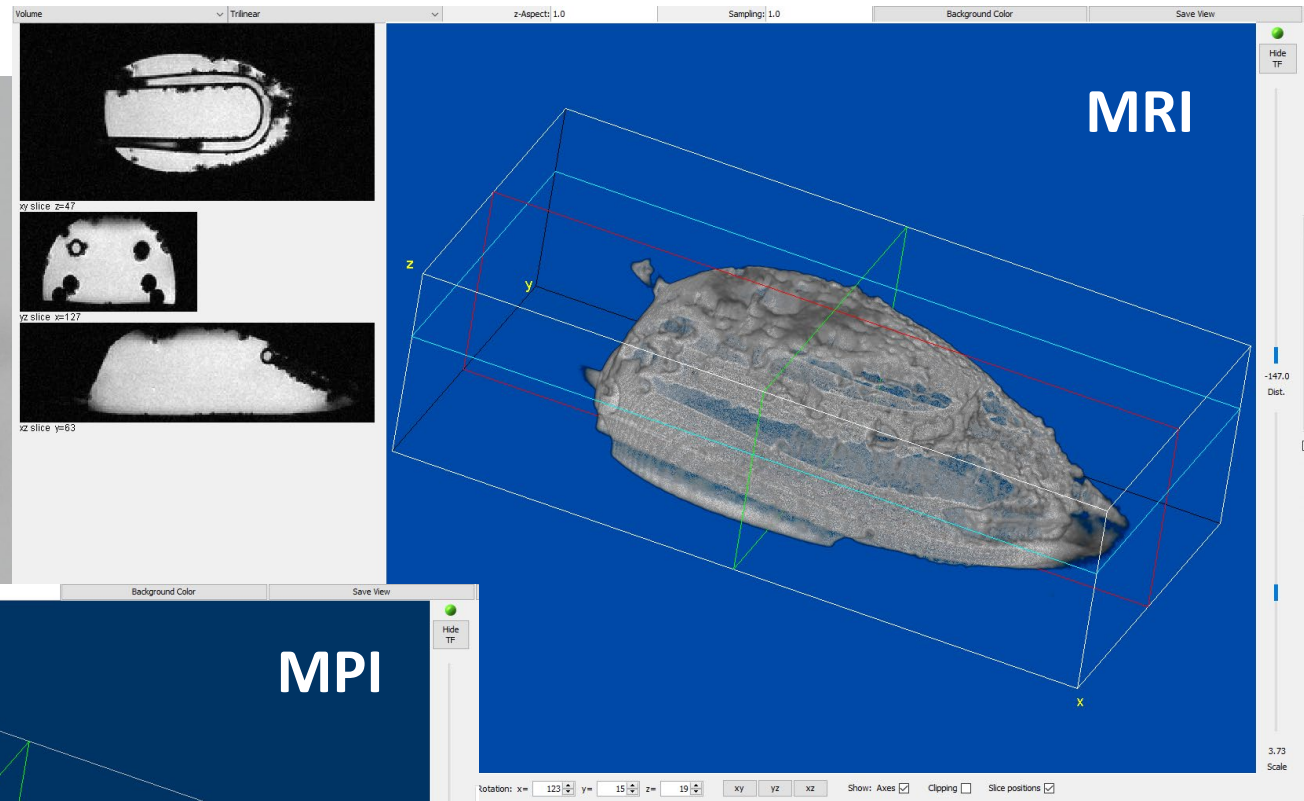
Scanning volume





Scanning volume

Focus field application:



FOV $72 \times 40 \times 30 \text{ mm}^3$

1 mm resolution

Magnetic nanoparticles in imaging

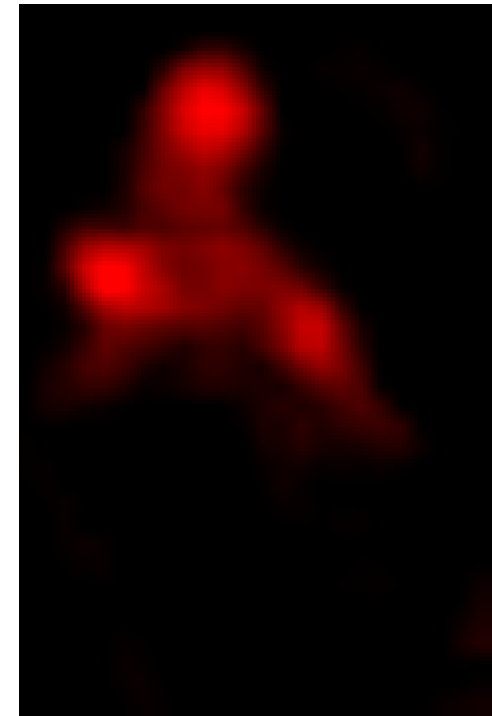
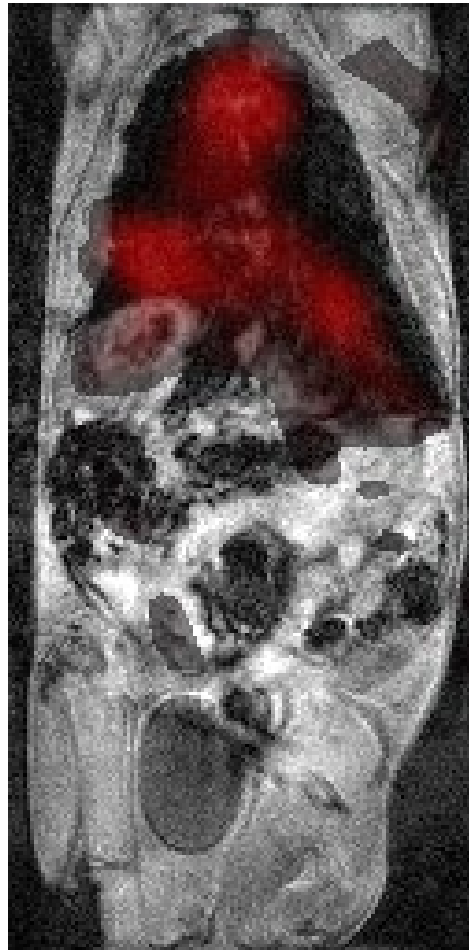
MRI vs. MPI

MRI: measurement of $1H$ distribution, signal influenced by nanoparticles



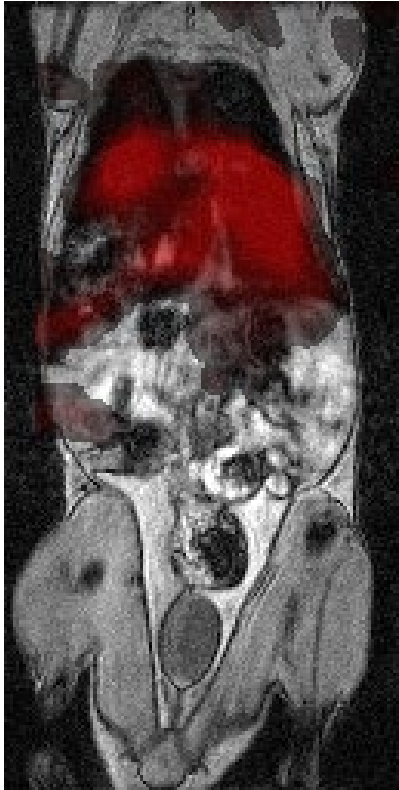
MRI provides anatomical information with an unspecific signal in areas with nanoparticles

- MPI: measurement directly distribution of magnetic nanoparticles

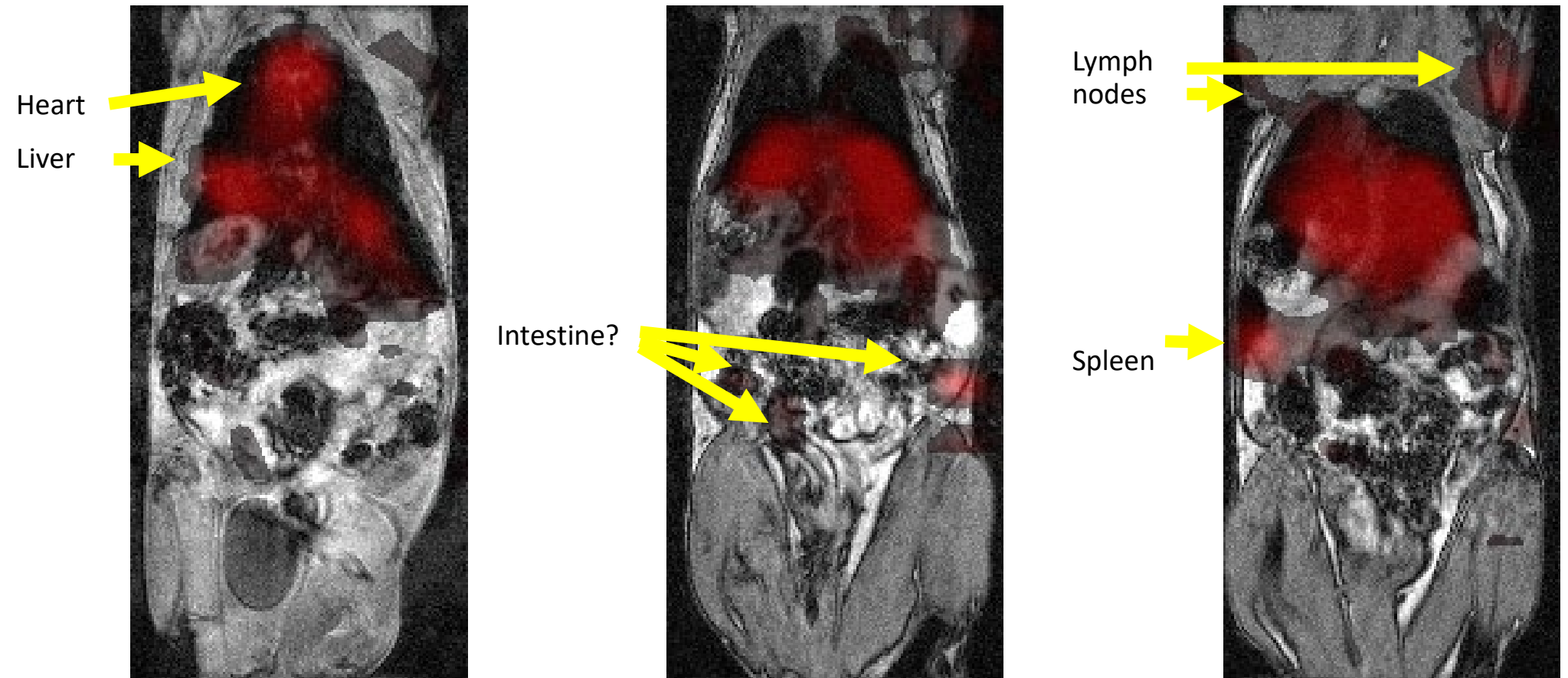


MPI provides highly specific information about nanoparticle distribution with no anatomical image

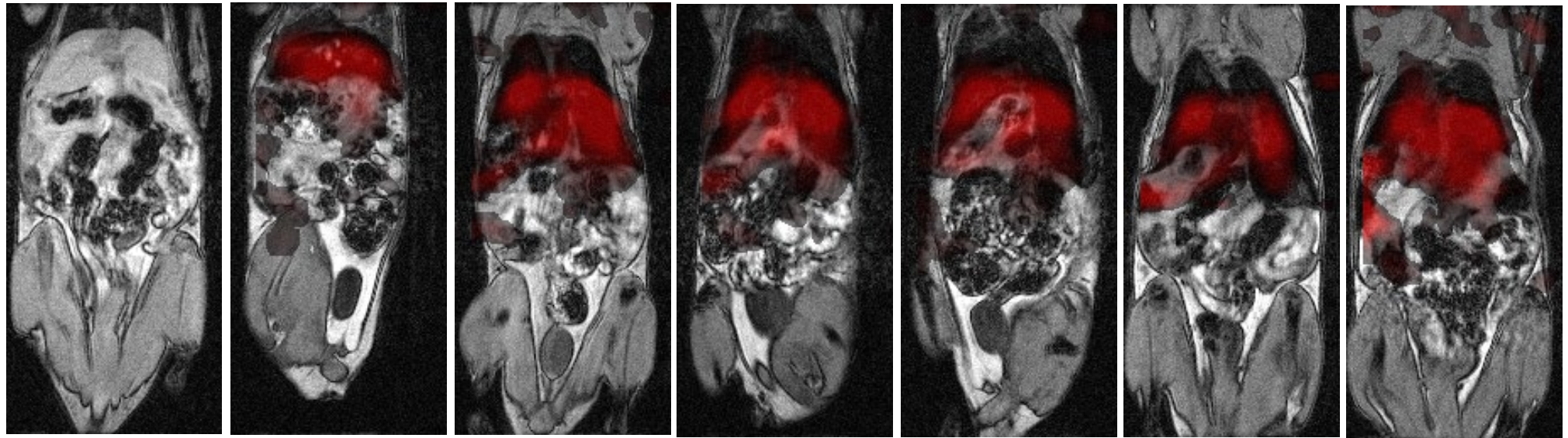
3D reconstruction



In vivo imaging – nanoparticle distribution



Particle distribution in time



Before app.

immediately after

1 day

2 days

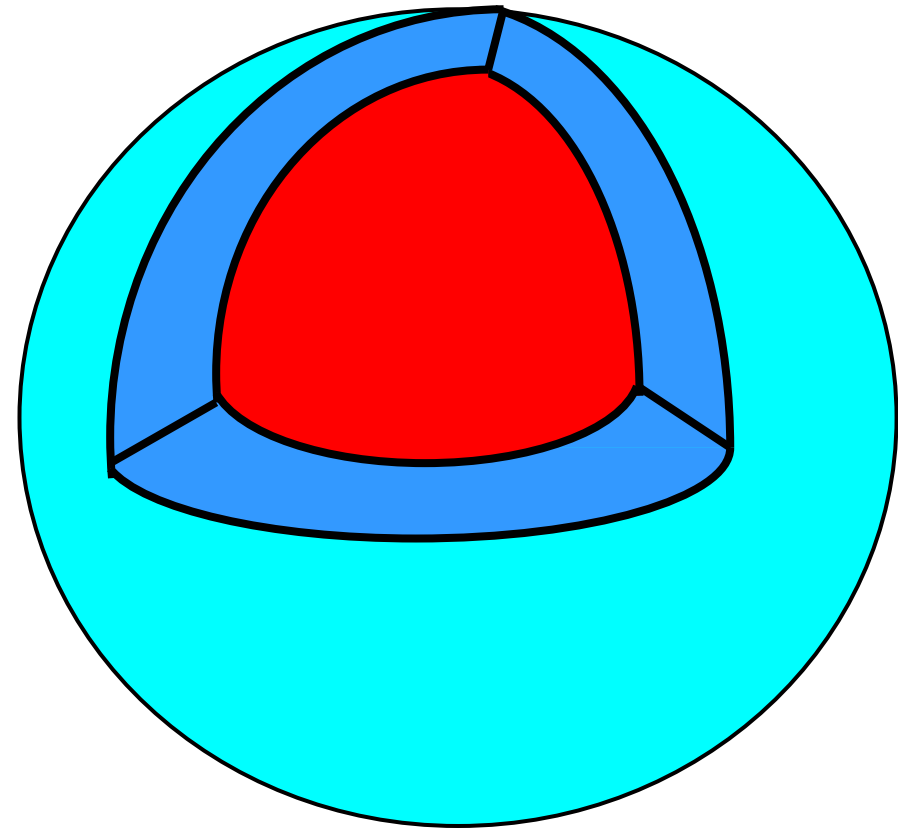
7 days

14 days

21 days

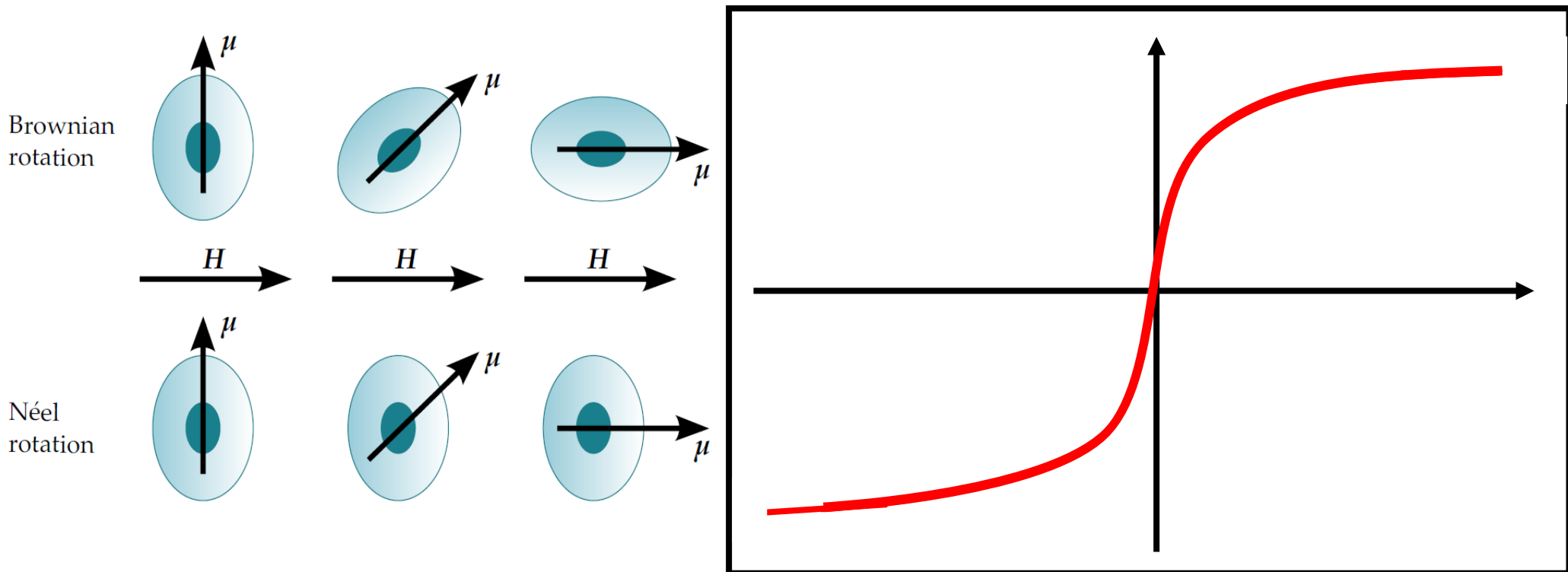
Contrast agents - nanoparticles

- Usually iron oxide nanocrystals
- Coated by sugars (dextran etc.) or polymers (poly-L-lysine...), or inorganic compounds (silica)



Physical properties define
image quality

Nanoparticle relaxation and signal



Reorientation is a dynamic process, speed of the response to the external field is crucial

Change of magnetization is effected by

- Néel rotation (change of magnetization due to reorientation of the inner magnetization with respect to the crystal structure)
- Brownian rotation (rotation of the whole particle)

Nanoparticle relaxation

Néel rotation is characterized by a relaxation time:

$$\tau_N = \tau_0 \exp(K_{\text{eff}} V / kT)$$

K_{eff} magnetic anisotropy energy density

τ_0 corresponds the frequency of gyromagnetic rotation

Brownian rotation

$$\tau_B = 3 \eta V_H / kT$$

η - viscosity

Both relaxation times are involved in magnetization change

Néel relaxation is faster (in term of orders)

The equations show that the size and shape of particles is important

Nanoparticle relaxation

Combined - efficient relaxation time:

$$\tau_{\text{eff}} = \tau_{\text{Brown}} \tau_{\text{Néel}} / (\tau_{\text{Brown}} + \tau_{\text{Néel}})$$

1. small particles will most likely exhibit Néel rotation,
2. particles of intermediate volume will perform a combined rotation,
3. large particles will be dominated by the Brownian rotation due to the blocked Néel rotation

The blocking volume / blocking temperature – a crystal critical volume at the given temperature, at which the magnetization is locked during the measuring time (or critical temperature at the given volume)

Nanoparticle relaxation and signal

Why to bother with relaxation?

Why not to just slow down the acquisition if the sample slowly reacts?

Generated signal in the coil $\sim$ electric voltage

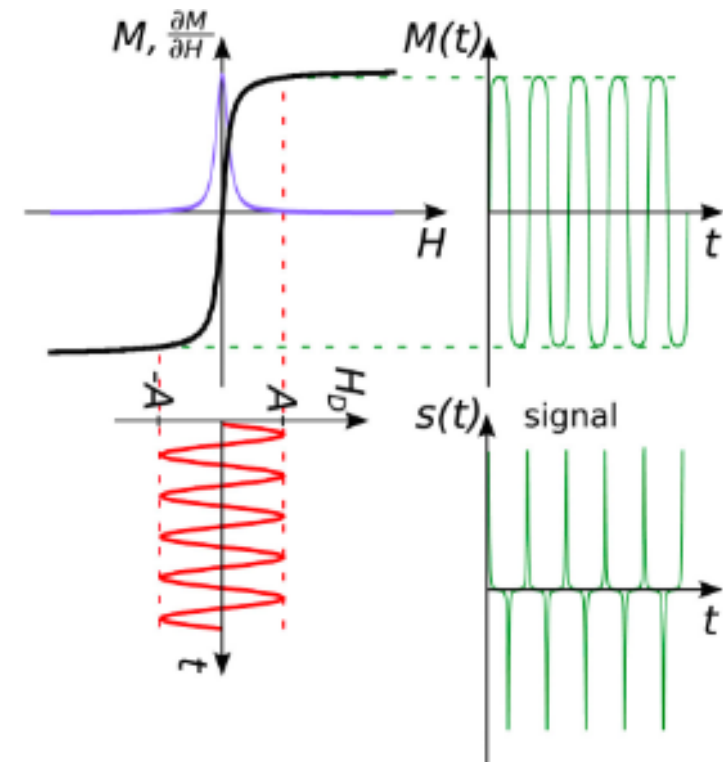
$$u(t) = -\mu_0 \int_{\Omega} \frac{d}{dt} \mathbf{M}(\mathbf{H}(\mathbf{r}, t), \mathbf{r}, t) \mathbf{p}(\mathbf{r}) d^3 r$$

coil sensitivity

If

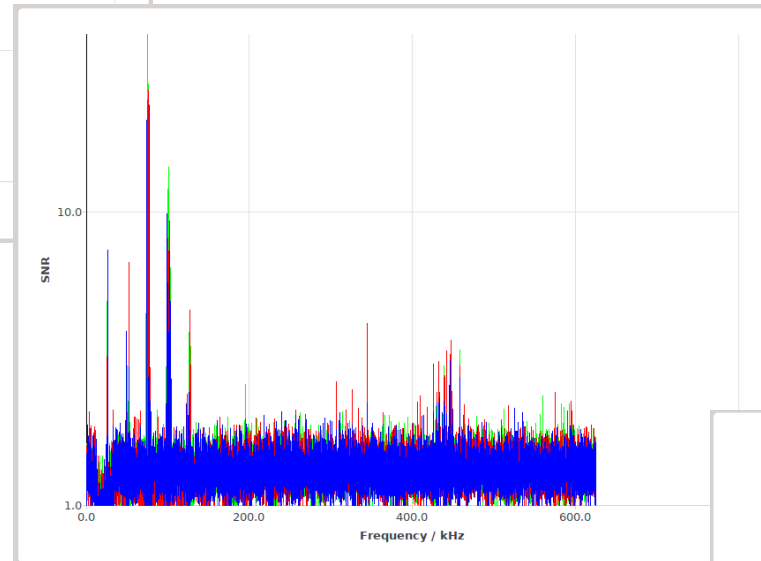
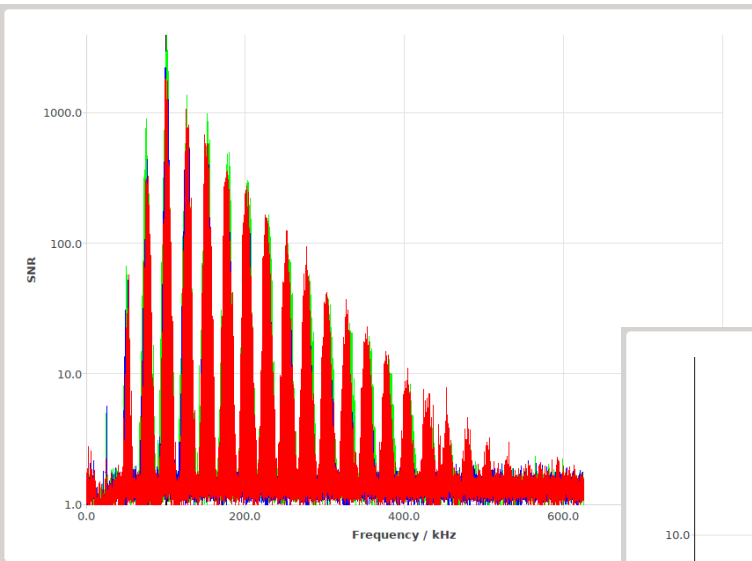
- External field is homogeneous in the given volume, i.e., p is constant
- Particle distribution is approximated by δ – distribution...

$$u(t) = -\mu_0 p \frac{d}{dt} M(H(t))$$

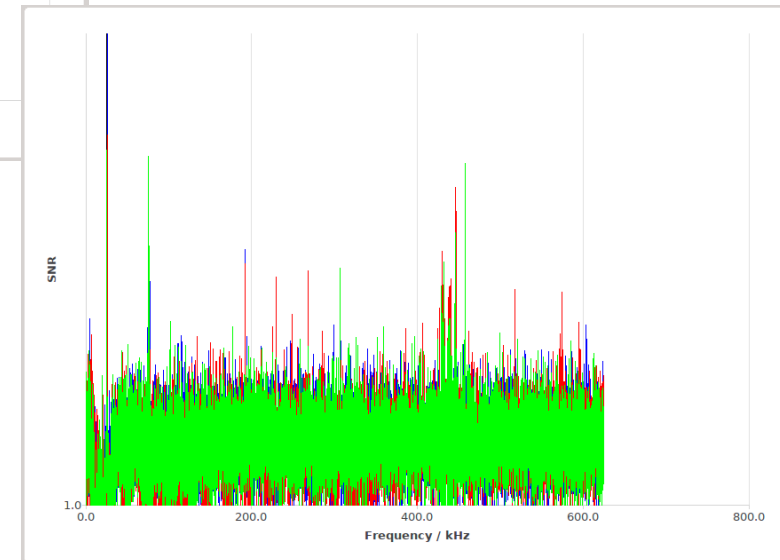


Nanoparticle relaxation and signal

Particles with fast Néel and Brownian relaxations



Particles with slow Néel relaxation, and fast Brownian relaxation



Particles with slow Néel and Brownian relaxations

Size and spatial resolution

$$M(B) = N \mu L(\mu B/kT)$$

The bigger the particles, the higher resolution!

N – number of particles

μ - magnetic moment

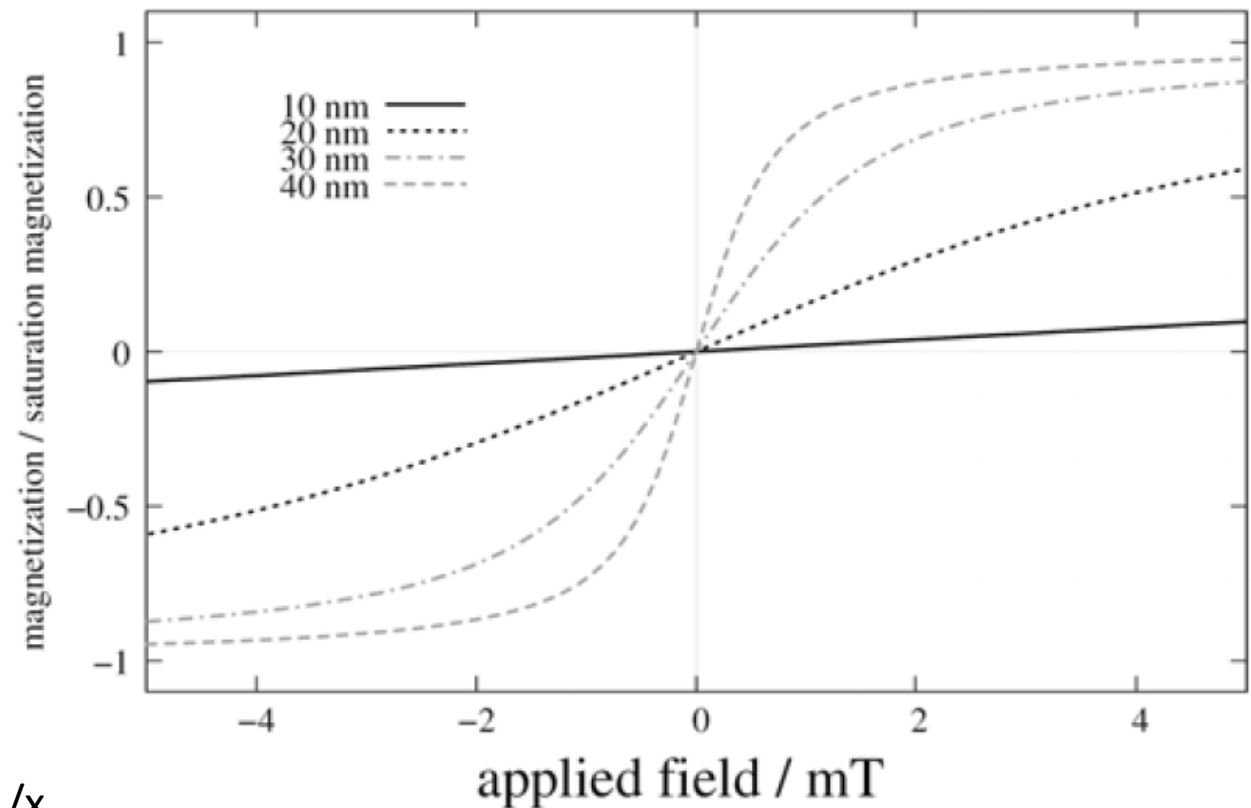
B – magnetic induction

k – Boltzman constant

T – temperature

L – Langevin function, $L = \coth(x) - 1/x$

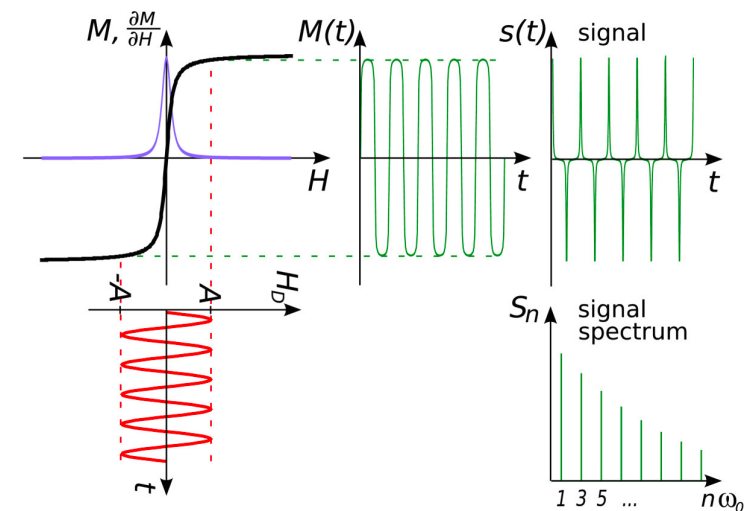
core size effects the curve through μ



Size and spatial resolution

Diameter	saturation field	resolution at $3 T \mu_0^{-1} / \text{m}$
10 nm	$31 \text{ mT} \mu_0^{-1}$	21 mm
15 nm	$9.1 \text{ mT} \mu_0^{-1}$	6.1 mm
20 nm	$3.8 \text{ mT} \mu_0^{-1}$	2.5 mm
25 nm	$2.0 \text{ mT} \mu_0^{-1}$	1.3 mm
30 nm	$1.1 \text{ mT} \mu_0^{-1}$	0.7 mm
35 nm	$0.72 \text{ mT} \mu_0^{-1}$	0.5 mm
40 nm	$0.48 \text{ mT} \mu_0^{-1}$	0.3 mm

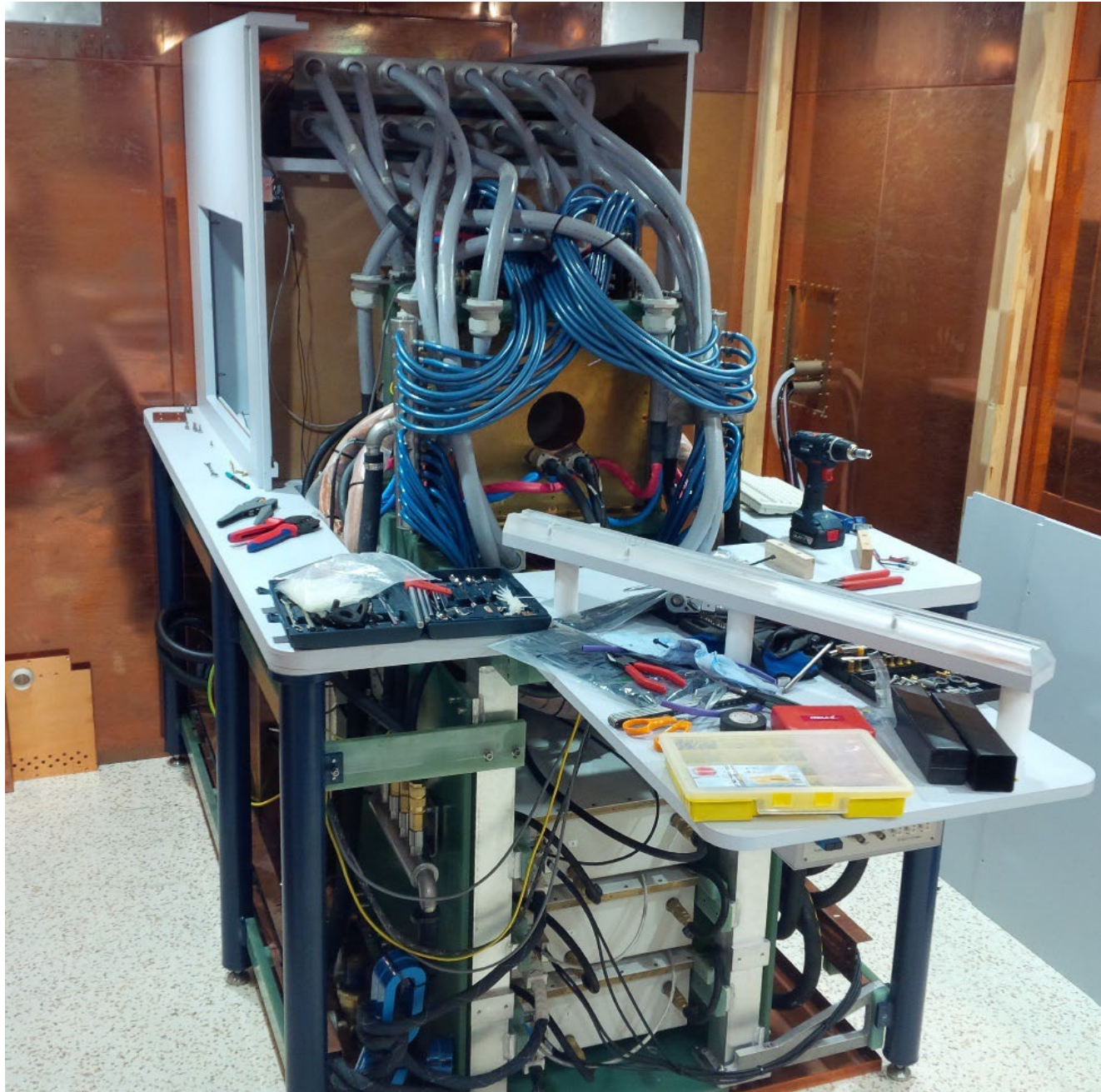
In real life, we can reach higher resolution by detection of higher number of higher harmonics



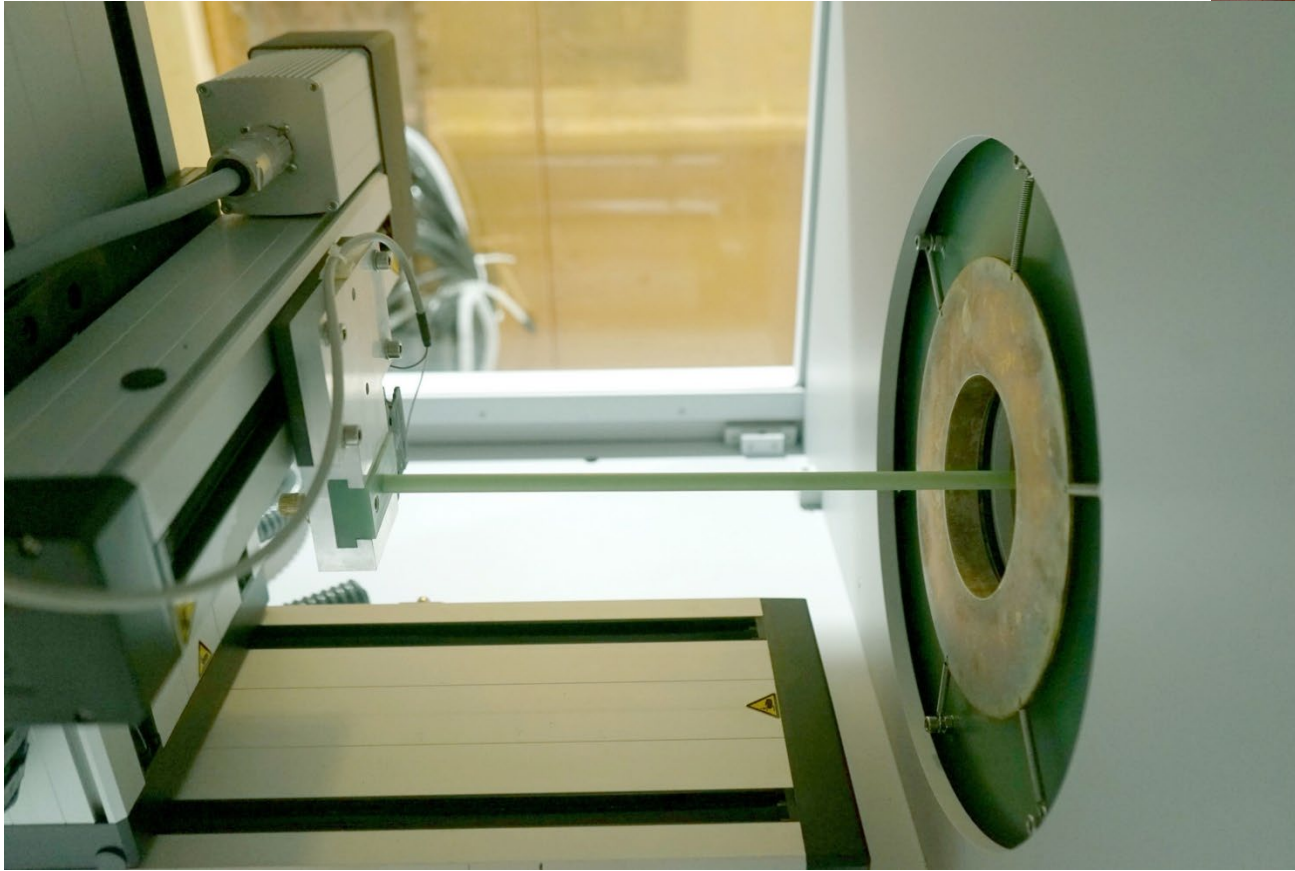
How the machine looks like...



How the machine looks like...



Robot for calibration



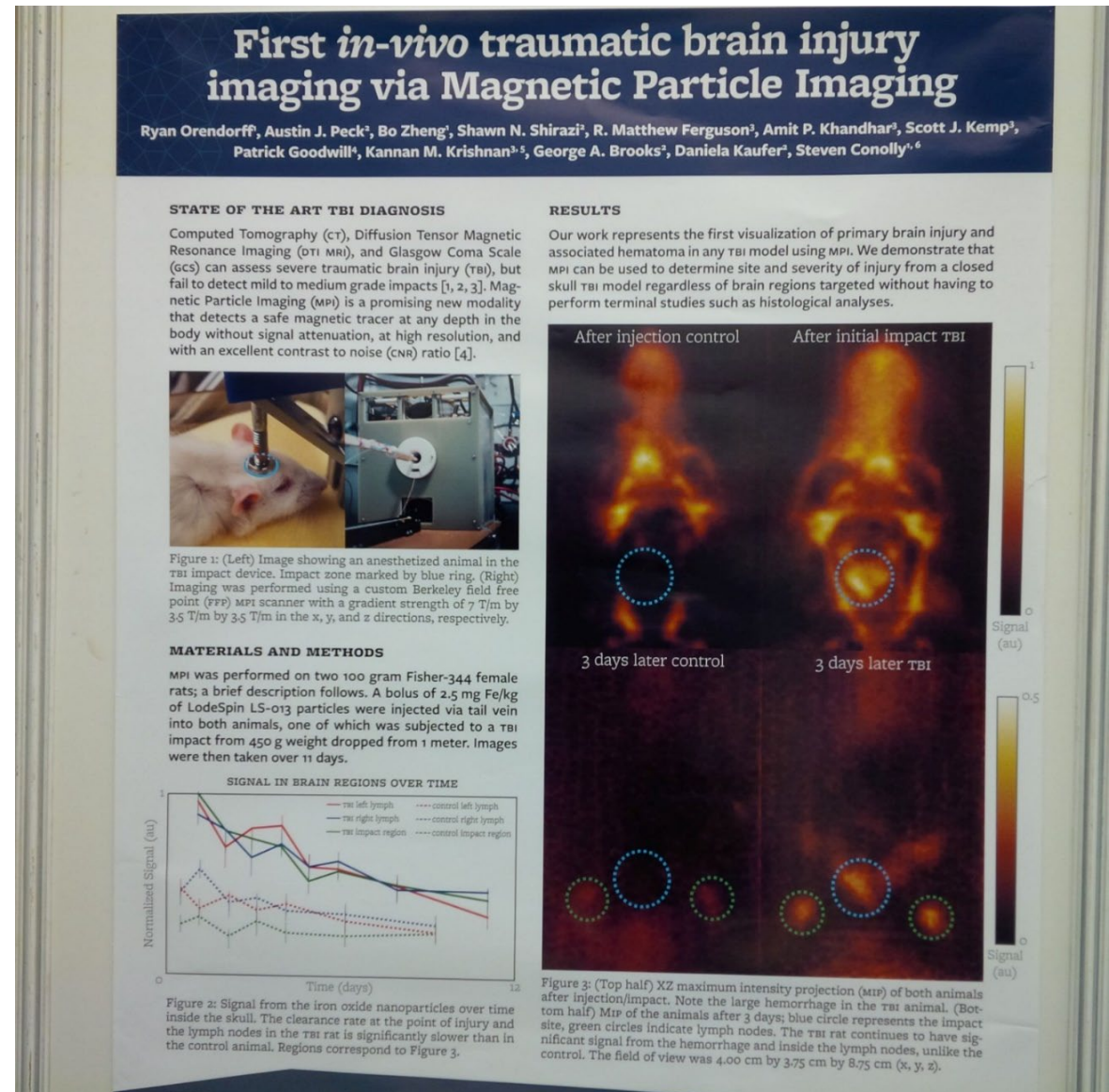
Possible applications

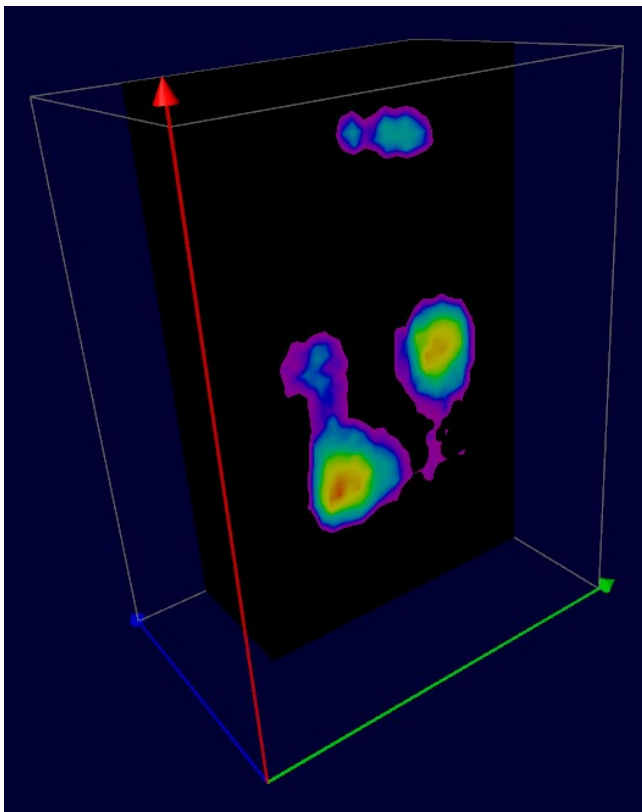


Int J Mag Part Imag

Temperature mapping using MPI

Stroke





Conclusion

MPI

Potentially interesting imaging method, although its possibilities are not completely appreciated yet

Requires a contrast agent – only the tracer is imaged

Requires a colocalization with another imaging method

Area for research

- Data acquisition and processing
- Nanoparticle development
- Applications

