

# Lecture 10: Logical Agents and Planning

Viliam Lisý & Branislav Božanský

Artificial Intelligence Center  
Department of Computer Science, Faculty of Electrical Eng.  
Czech Technical University in Prague

[viliam.lisy@fel.cvut.cz](mailto:viliam.lisy@fel.cvut.cz)

April, 2023

# Plan of today's lecture

- 1 Logic in AI in the past and now
- 2 Logical problem representations
- 3 Situation calculus
- 4 Intelligent planning

## └ Plan of today's lecture

- Logic in AI in the past and now
- Logical problem representations
- Situation calculus
- Intelligent planning

Example of use of logic in a realistic system - slow, but does the job. Potentially useful for getting guarantees in AI. Will there be a logic renaissance? Structured knowledge useful - e.g. automatic construction of heuristics and their study = AI planning. Very core of classical AI and potential in the future = part of ZUI

Slides are heavily based on J. Klema's slides. For more details on logical agents see his [video](#) from the last year.

There has been a big hype of logical agents in 60s and 70s.

- + It can represent knowledge about the world
- + It can represent intelligent reasoning
  - It is not very convenient for working with uncertainty
  - It is usually extremely computationally expensive  
( expressivity vs. completeness vs. effectivity )

Logic in AI 2020s

- Interpretable safe AI
- Relational ML/RL
- Theorem proving
- Model checking
- Knowledge graphs
- Automated planning

## └ Logics in AI

There has been a big hype of logical agents in 60s and 70s.

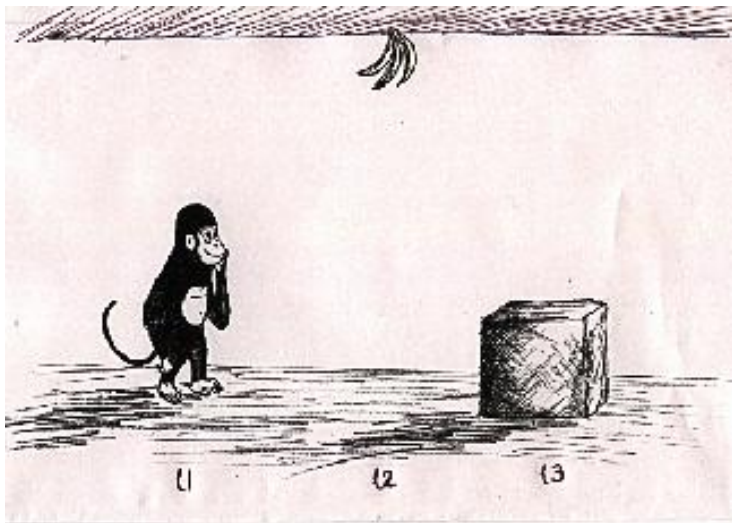
- + It can represent knowledge about the world
- + It can represent intelligent reasoning
- It is not very convenient for working with uncertainty
- It is usually extremely computationally expensive  
( expressivity vs. completeness vs. effectivity )

## Logic in AI 2020s

- Interpretable safe AI
- Relational ML/RL
- Theorem proving
- Model checking
- Knowledge graphs
- Automated planning

It is not mainstream at the moment, but clearly belongs to ZUI

# Motivation example monkey and banana

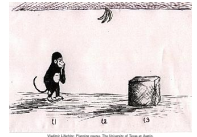


Vladimir Lifschitz: Planning course, The University of Texas at Austin.

2023-05-01

## Introduction to Artificial Intelligence

└ Motivation example: monkey and banana



Explain how would it be represented so far. And in CSP?



## Problem description

- a monkey is in a room, a banana hangs from the ceiling,
- the banana is beyond the monkey's reach,
- the monkey is able to walk, move and climb objects, grasp banana,
- the room is just the right height so that the monkey can move a box, climb it and grasp the banana,
- the goal is to generate this plan (sequence of actions) automatically.

## Key characteristics

- a deterministic task
- a general description available
  - all the necessary knowledge is provided
  - we need to **represent it** in some **language**
  - and perform certain **reasoning / inference**
- a planning task

Remember B0B01LGR: Logic and Graphs

## Jazyk

*Jazyk predikátové logiky* obsahuje tyto symboly:

### 1 logické symboly

- proměnné; Var je množina všech proměnných
- logické spojky:  $\neg, \wedge, \vee, \Rightarrow, \Leftrightarrow$ , popř. též  $\text{tt}, \text{ff}, |, \downarrow, \oplus$
- kvantifikátory  $\forall$  (obecný) a  $\exists$  (existenční)
- symbol rovnosti:  $=$

### 2 speciální symboly

- predikátové, kde každý má svou aritu  $n \geq 0$ ;  
Pred je množina predikátových symbolů
- funkční, kde každý má svou aritu  $n > 0$ ;  
Func je množina funkčních symbolů
- konstantní; Kons je množina konstantních symbolů

### 3 pomocné symboly, jako jsou závorky $(, )$ a čárka $,$

The following slides would, in principle, work with stronger logic!  
Modal Logic, epistemic logic, temporal logic, ATL

Remember B0B01LGR: Logic and Graphs

## First order logic

The language of first order predicate logic includes:

- logical symbols
  - variables:  $\{a, b, c\} \subset Var$
  - logical operators:  $\neg, \wedge, \vee, \rightarrow, \leftrightarrow$
  - quantifiers:  $\forall, \exists$
  - equality operator:  $=$
- special symbols
  - predicates (with a fixed arity  $n \geq 0$ )
  - functions (with a fixed arity  $n > 0$ )
  - constants
- auxiliary symbols, such as brackets ( ) and comma ,

The following slides would, in principle, work with stronger logic!  
Modal Logic, epistemic logic, temporal logic, ATL

**Situation calculus** is one way to represent changing world in FOL

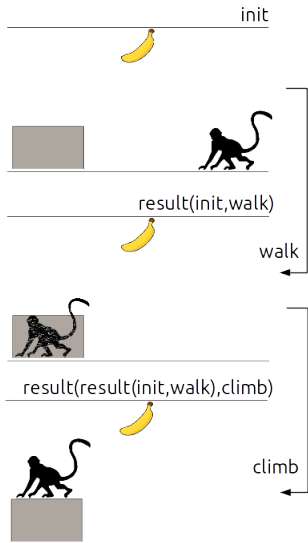
- facts hold in particular situations ( $\approx$  world state histories)
- predicates either rigid (eternal) or fluent (changing)
- fluent predicates include a situation argument  
e.g., *agent(monkey, at\_ban, now)*, term *now* denotes a situation
- rigid predicates hold regardless of a situation  
e.g., *walks(monkey)*, *moveable(box)*
- situations are connected by the *result* function  
if *s* is a situation than *result(s, a)* is also a situation

The monkey problem state can be represented using two predicates

- *agent(agent name, agent position, stands on, situation)*
- *object(object name, object position, who stands, situation)*

# Keeping track of evolving situations

*agent(agent name, agent position, stands on, situation)*  
*object(object name, object position, who stands, situation)*



`agent(monkey, right, ground, init).`  
`object(box, left, none, init).`

`agent(monkey, left, ground, result(init,walk)).`  
`object(box, left, none, result(init,walk)).`

`agent(monkey, left, box, result(result(init,walk),climb)).`  
`object(box, left, monkey, result(result(init,walk),climb)).`

*agent(agent name, agent position, stands on, situation)*  
*object(object name, object position, who stands, situation)*

Action “effect” axiom for  $walk(X, P_1, P_2)$ :

$$\forall X, P_1, P_2, Z (agent(X, P_1, ground, Z) \wedge walks(X) \\ \rightarrow agent(X, P_2, ground, result(Z, walk(X, P_1, P_2))))$$

Action “effect” axiom for  $climb(X)$ :

$$\forall X, P, Z (agent(X, P, ground, Z) \wedge object(box, P, none, Z) \\ \rightarrow agent(X, P, box, result(Z, climb(X))) \\ \wedge object(box, P, X, result(Z, climb(X))))$$

Action axioms describe how fluents change between situations  
What happens to fluents, which are not used in the actions?  
e.g., the objects while the agent walks

**Frame problem:** how to cope with the unchanged facts smartly

- many “frame” axioms may be necessary to express them in FOL

$$\forall X, V, W, Z, P_1, P_2 \\ (object(X, V, Y, Z) \rightarrow object(X, V, Y, result(Z, walk(P_1, P_2))))$$

- $f$  fluent predicates and  $a$  actions require  $O(f \cdot a)$  frame axioms
- many applications of axioms each step is computationally expensive
- some tricks diminish the problem, but it never goes away

FOL can be used to represent **states** and **actions**

Goal of planning: logical representation of the desired state

$$\mathcal{G} \equiv \exists Z \text{ agent}(\textit{monkey}, \textit{middle}, \textit{box}, Z)$$

**Reasoning** checks whether the goal formula follows from KB

$$KB \models \mathcal{G}$$

- knowledge base (KB) are the inference rules and the initial state
- reasoning finds a suitable  $Z$  or proves it does not exist
- desirable properties: **soundness, completeness, efficiency**
- reasoning procedures: **resolution**, deductive inference, etc.
  - see B0B01LGR
  - generally extremely computationally hard, possibly undecidable
  - the solution is correct, if reasoning successfully finishes
  - can be efficient and useful with **additional restrictions**



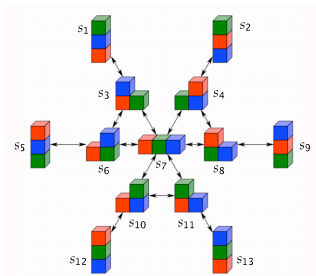
Subfield of AI dealing (mainly) with

- representation languages with reasonable tradeoffs of expressivity and efficiency
- algorithms for finding plans for problems expressed in these languages

(The following slides are heavily based on Carmel Domshlak's slides)

## What is in common?

- All these problems deal with **action selection** or **control**
- Some notion of problem **state**
- (Often) specification of **initial state** and/or **goal state**
- Legal moves or **actions** that transform states into other state



For now focus on:

- **Plans** (aka **solutions**) are sequences of moves that transform the initial state into the goal state
- Intuitively, not all solutions are equally desirable

What is our task?

- 1 Find out whether there is a solution
- 2 Find any solution
- 3 Find an optimal (or near-optimal) solution
- 4 Fixed amount of time, find best solution possible
- 5 Find solution that satisfy property  $\aleph$  (what is  $\aleph$ ? you choose!)

# Three Key Ingredients of Planning

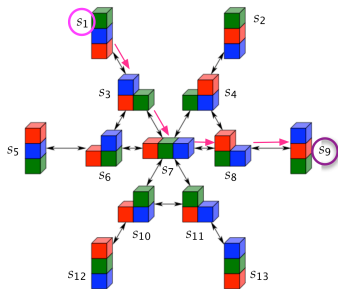
Planning is a form of **general problem solving**

Problem  $\implies$  Language  $\implies$  **Planner**  $\implies$  Solution

- 1 **models** for defining, classifying, and understanding problems
  - what is a *planning problem*
  - what is a *solution (plan)*, and
  - what is an *optimal solution*
- 2 **languages** for representing problems
- 3 **algorithms** for solving them

# Why planning is difficult?

- Solutions to planning problems are **paths from an initial state to a goal state in the transition graph**
- Dijkstra's algorithm solves this problem in  $O(|V| \log(|V|) + |E|)$
- Can we go home??



- Solutions to planning

## └ Why planning is difficult?

- Solutions to planning problems are paths from an initial state to a goal state in the transition graph
- Dijkstra's algorithm solves this problem in  $O(|V| \log (|V|) + |E|)$
- Can we go home??



- Solutions to planning problems are paths from an

Example with logistics with 50 trucks servicing 100 cities

# What is “classical” planning?

- dynamics: **deterministic**, nondeterministic or probabilistic
  - observability: full, partial or **none**
  - horizon: **finite** or infinite
  - ...
- 1 **classical planning**
  - 2 conditional planning with full observability
  - 3 conditional planning with partial observability
  - 4 conformant planning
  - 5 Markov decision processes (MDP)
  - 6 partially observable MDPs (POMDP)

# Succinct representation of transition systems

- More **compact** representation of actions than as relations is often
  - **possible** because of symmetries and other regularities,
  - **unavoidable** because the relations are too big.
- Represent different aspects of the world in terms of different **state variables**.  $\rightsquigarrow$  A state is a **valuation of state variables**.
- Represent actions in terms of changes to the state variables.



## Key issue

Models represented **implicitly** in a **declarative language**

Play two roles

- **specification**: concise model description
- **computation**: reveal useful info about problem's *structure*

A problem in **STRIPS** is a tuple  $\langle P, A, I, G \rangle$

- $P$  stands for a finite set of **atoms** (boolean vars)
- $I \subseteq P$  stands for **initial situation**
- $G \subseteq P$  stands for **goal situation**
- $A$  is a finite set of **actions**  $a$  specified via  $\text{pre}(a)$ ,  $\text{add}(a)$ , and  $\text{del}(a)$ , all subsets of  $P$

- States are **collections of atoms**
- An action  $a$  is applicable in a state  $s$  iff  $\text{pre}(a) \subseteq s$
- Applying an applicable action  $a$  at  $s$  results in  $s' = (s \setminus \text{del}(a)) \cup \text{add}(a)$

# Why STRIPS is interesting?

- STRIPS operators are **particularly simple**, yet expressive enough to capture general planning problems.
- In particular, STRIPS planning is **no easier** than general planning problems.
- Many algorithms in the planning literature are **easier to present in terms of STRIPS**.

(The following example is based on Antonin Komanda's slides)

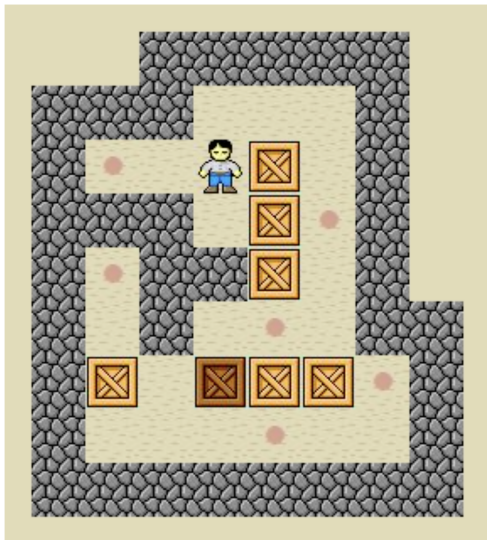
# Sokoban - Example planning domain

## State representation:

```
positions: a1, ... a6, ...  
           f1, ..., f2  
box_at(P), free(P)  
player_at(P)  
adjacent(P1,P2)  
adjacent2(P1,P2)
```

## Operators (Actions):

```
move(X,Y):  
  pre: player_at(X)  
       adjacent(X,Y)  
       free(Y)  
  add: player_at(Y)  
  del: player_at(X)  
  
push(X, Y, Z):  
  pre: player_at(X)  
       box_at(Y)  
       free(Z)  
       adjacent(X,Y)  
       adjacent(Y,Z)  
       adjacent2(X,Z)  
  
...
```



# Grounding of Actions

## Operators (Actions):

```
move(X,Y):  
  pre: player_at(X)  
       adjacent(X,Y)  
       free(Y)  
  add: player_at(Y)  
  del: player_at(X)  
  
push(X, Y, Z):  
  pre: player_at(X)  
       box_at(Y)  
       free(Z)  
       adjacent(X,Y)  
       adjacent(Y,Z)  
       adjacent2(X,Z)  
  add: player_at(Y)  
       box_at(Z)  
       free(Y)  
  del: player_at(X)  
       box_at(Y)  
       free(Z)
```

## Grounding:

```
move_a1_a2  
  pre: player_at_a1, adjacent_a1_a2, free_a2  
  add: player_at_a2  
  del: player_at_a1  
  
move_a2_a3  
  pre: player_at_a2, adjacent_a2_a3, free_a3  
  add: player_at_a3  
  del: player_at_a2  
  
...  
  
push_a1_a2_a3  
  pre: player_at_a1, box_at_a2, free_a3  
       adjacent_a1_a2, adjacent_a2_a3,  
       adjacent_a1_a3  
  add: player_at_a2, box_at_a3, free_a2  
  del: player_at_a1, box_at_a2, free_a3  
  
...
```

# STRIPS Representation of Sokoban

A problem in **STRIPS** is a tuple  $\langle P, A, I, G \rangle$

- $P$  stands for a finite set of **atoms** (boolean vars)
- $I \subseteq P$  stands for **initial situation**
- $G \subseteq P$  stands for **goal situation**
- $A$  is a finite set of **actions**  $a$  specified via  $\text{pre}(a)$ ,  $\text{add}(a)$ , and  $\text{del}(a)$ , all subsets of  $P$

$P = \{ \text{player\_at\_a2}, \dots, \text{player\_at\_d3},$   
 $\text{box\_at\_a2}, \dots, \text{box\_at\_d3},$   
 $\text{free\_a2}, \dots, \text{free\_d3},$   
 $\text{adjacent\_a2\_b2}, \dots, \text{adjacent\_d2\_d3},$   
 $\text{adjacent2\_a2\_c2}, \dots, \text{adjacent2\_d1\_d3} \}$

$I = \{ \text{player\_at\_b2}, \text{box\_at\_c1}, \text{box\_at\_c2},$   
 $\text{free\_a2}, \text{free\_b1}, \dots, \text{free\_d3},$   
 $\text{adjacent\_a2\_b2}, \dots, \text{adjacent\_d2\_d3}, \text{adjacent2\_a2\_c2}, \dots, \text{adjacent2\_d1\_d3} \}$

$G = \{ \text{box\_at\_a2}, \text{box\_at\_d1} \}$



We can just use A\*:

- State: a set of true atoms
- Applicable actions: based on preconditions
- Action application: add the “add” atoms and delete the “del” atoms  
(No need for separate simulator implementation)

Problem structure allows **automated** construction of **heuristics!**

- Allows exploring general heuristics domain independently
- Simple heuristic:  $h(s) = |G \setminus s|$
- Solve a suitable **simpler** version of the problem
- Abstraction: solve a smaller problem  
e.g., completely remove a predicate from the problem
- **Relaxation**: solve a less constraint problem
- Landmarks

Whole sub-field of planning in STRIPs and beyond

- Relaxation is a general technique for heuristic design:
  - **Straight-line heuristic** (route planning): Ignore the fact that one must stay on roads.
  - **Manhattan heuristic** (15-puzzle): Ignore the fact that one cannot move through occupied tiles.
- We want to apply the idea of relaxations to planning.
- Informally, we want to ignore **bad side effects** of applying actions.

## Example (8-puzzle)

If we move a tile from  $x$  to  $y$ , then the **good effect** is (in particular) that  $x$  is now free.

The **bad effect** is that  $y$  is not free anymore, preventing us from moving tiles through it.



In STRIPS, good and bad effects are easy to distinguish:

- Effects that make atoms true are good (**add effects**).
- Effects that make atoms false are bad (**delete effects**).

Idea for the heuristic: **Ignore all delete effects.**

## Definition (relaxation of actions)

The **relaxation**  $a^+$  of a STRIPS action  $a = \langle \text{pre}(a), \text{add}(a), \text{del}(a) \rangle$  is the action  $a^+ = \langle \text{pre}(a), \text{add}(a), \emptyset \rangle$ .

## Definition (relaxation of planning tasks)

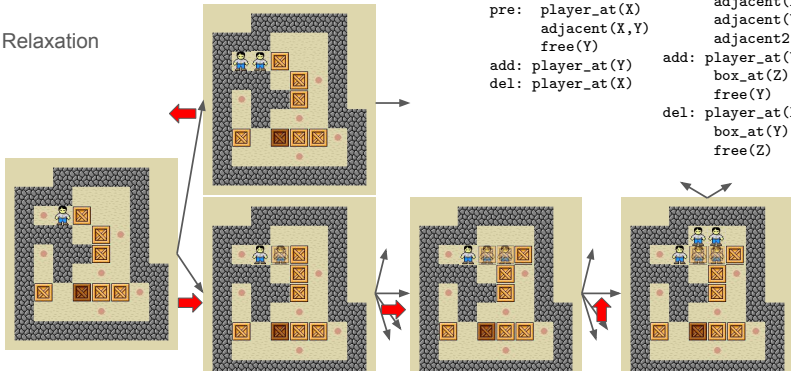
The **relaxation**  $\Pi^+$  of a STRIPS planning task  $\Pi = \langle P, A, I, G \rangle$  is the planning task  $\Pi^+ := \langle P, \{a^+ \mid a \in A\}, I, G \rangle$ .

## Definition (relaxation of action sequences)

The **relaxation** of an action sequence  $\pi = a_1 \dots a_n$  is the action sequence  $\pi^+ := a_1^+ \dots a_n^+$ .

# Relaxation of actions in Sokoban

Relaxation



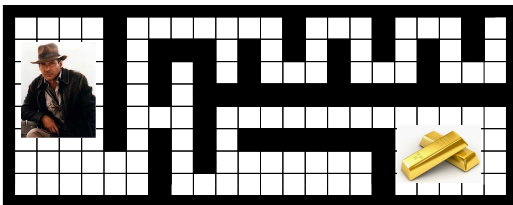
move(X,Y):

```
pre: player_at(X)
     adjacent(X,Y)
     free(Y)
add: player_at(Y)
del: player_at(X)
```

push(X, Y, Z):

```
pre: player_at(X)
     box_at(Y)
     free(Z)
     adjacent(X,Y)
     adjacent(Y,Z)
     adjacent2(X,Z)
add: player_at(Y)
     box_at(Z)
     free(Y)
del: player_at(X)
     box_at(Y)
     free(Z)
```

## Questionnaire



### Question!

In this domain,  $h^+$  is equal to?

- (A): Manhattan Distance.
- (B): Horizontal distance.
- (C): Vertical distance.
- (D):  $h^*$ .

# Building Relaxed Planning Graph

Computing the optimal relaxed plan is still NP hard

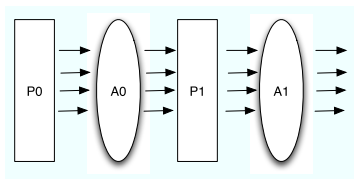
But we can do something simpler

- Build a layered **reachability graph**  $P_0, A_0, P_1, A_1, \dots$

$$P_0 = \{p \in I\}$$

$$A_i = \{a \in A \mid \text{pre}(a) \subseteq P_i\}$$

$$P_{i+1} = P_i \cup \{p \in \text{add}(a) \mid a \in A_i\}$$



- Terminate when  $G \subseteq P_i$

$$I = \{a = 1, b = 0, c = 0, d = 0, e = 0, f = 0, g = 0, h = 0\}$$

$$a_1 = \langle \{a\}, \{b, c\}, \emptyset \rangle$$

$$a_2 = \langle \{a, c\}, \{d\}, \emptyset \rangle$$

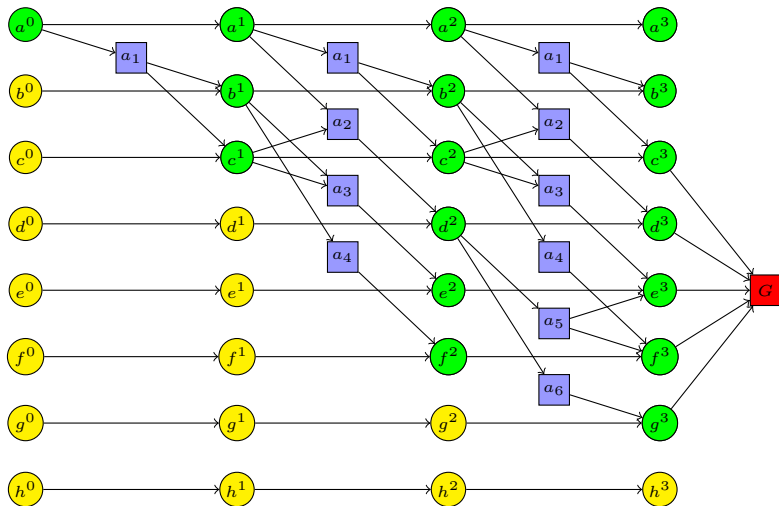
$$a_3 = \langle \{b, c\}, \{e\}, \emptyset \rangle$$

$$a_4 = \langle \{b\}, \{f\}, \emptyset \rangle$$

$$a_5 = \langle \{d\}, \{g\}, \emptyset \rangle$$

$$G = \{c = 1, d = 1, e = 1, f = 1, g = 1\}$$

# Relaxed Planning Graph

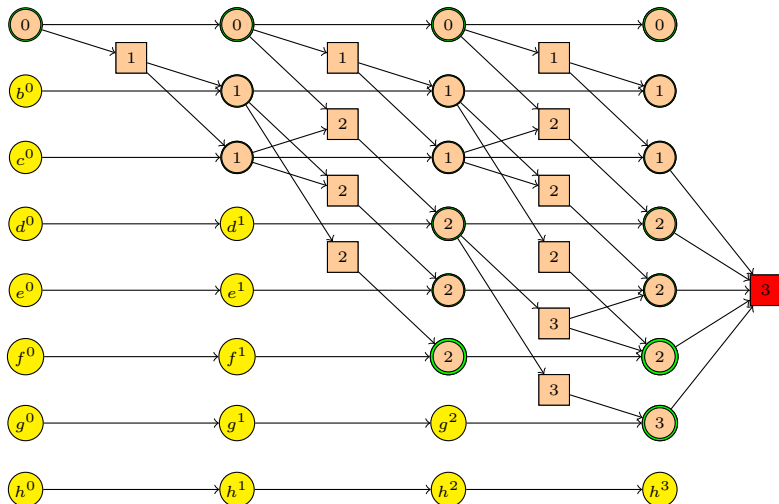


Forward cost heuristic  $h_{max}$

- Computes a lower bound on the cost of achieving the **most expensive** goal atom
- Propagate cost layer by layer from start to goal
- At actions, take maximum cost of achieving preconditions +1
- At propositions, take the cheapest action to achieve it



# Computing heuristic $h_{max}$



Logic is a powerful language for describing **diverse AI problems**

Situation calculus is a logical formalism for reasoning about situations **developing in time**

Of-the-shelf logical reasoning methods, such as resolution, are usable for **problem-independent** planning

However, **expressivity** goes against **efficiency**

The field of **AI planning** creates logical representations and algorithms specially designed for planning

**STRIPS** is a simple, but powerful language for representing planning problems

Logical representation of problems allows **automated construction** of A\* **heuristics**