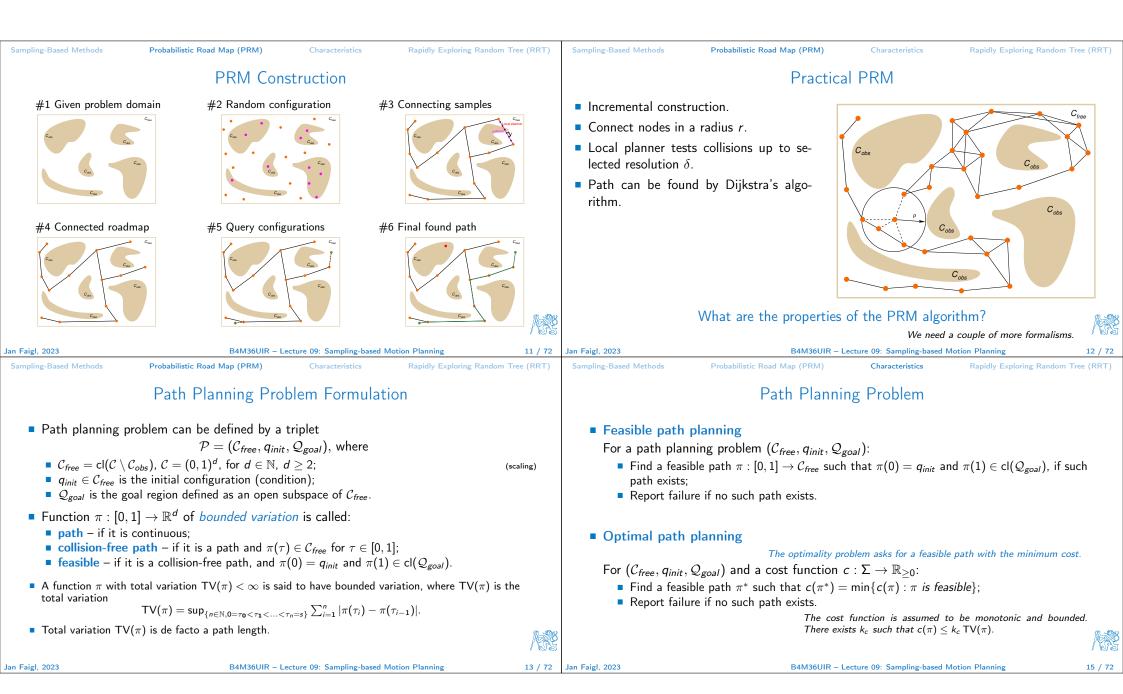
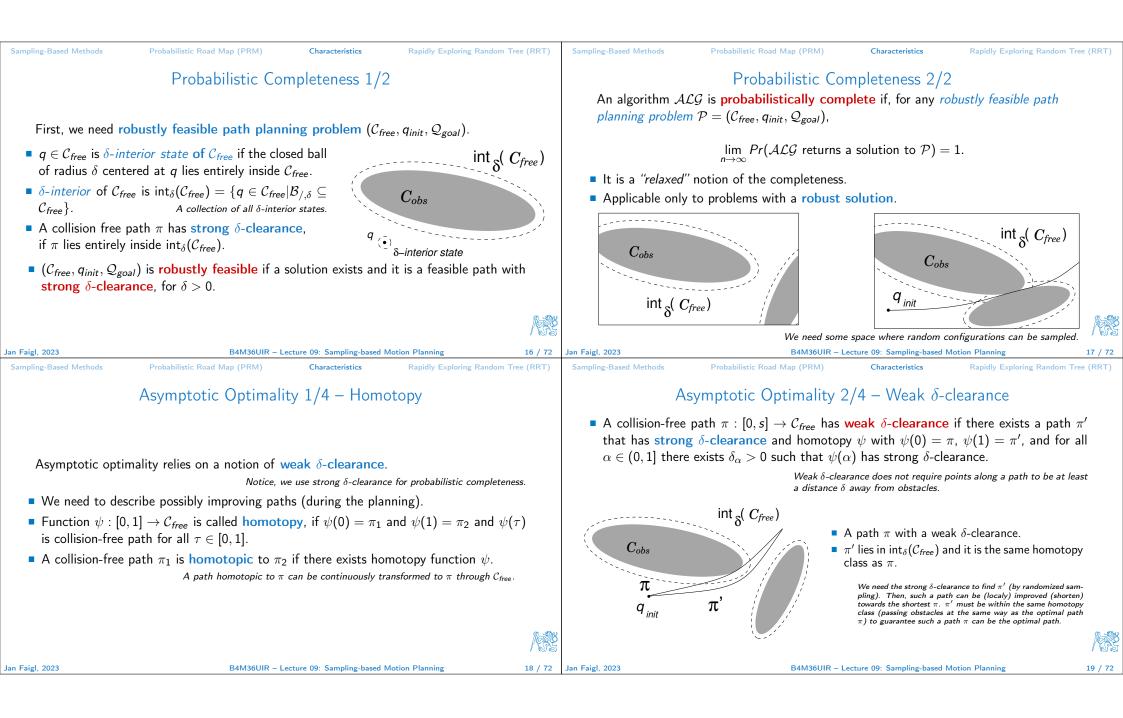
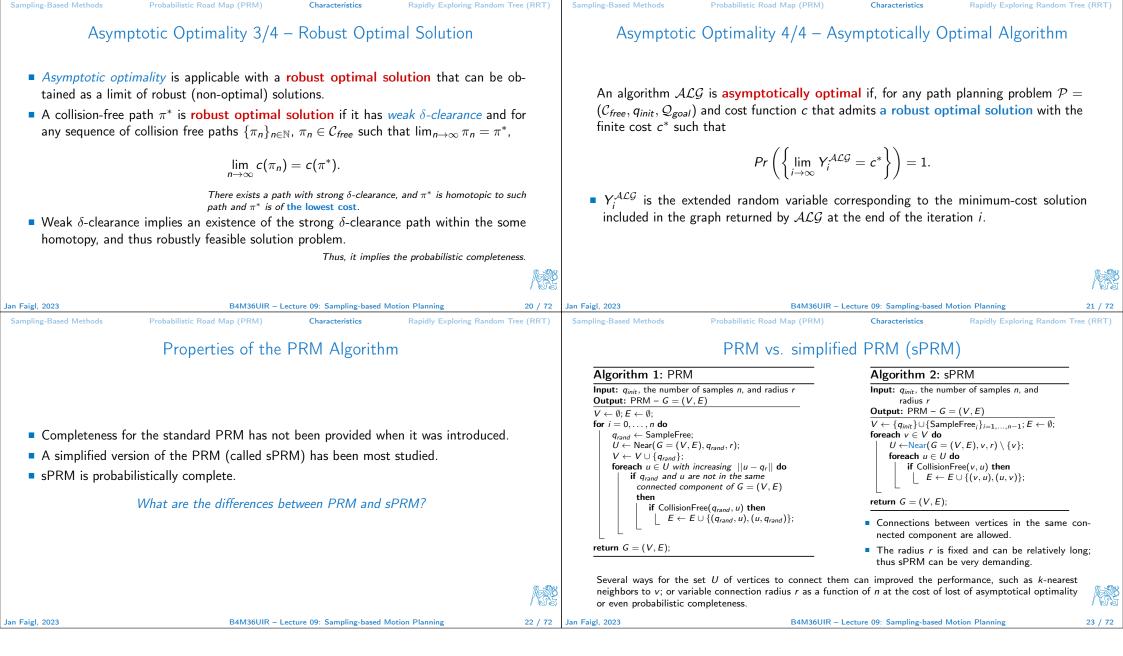
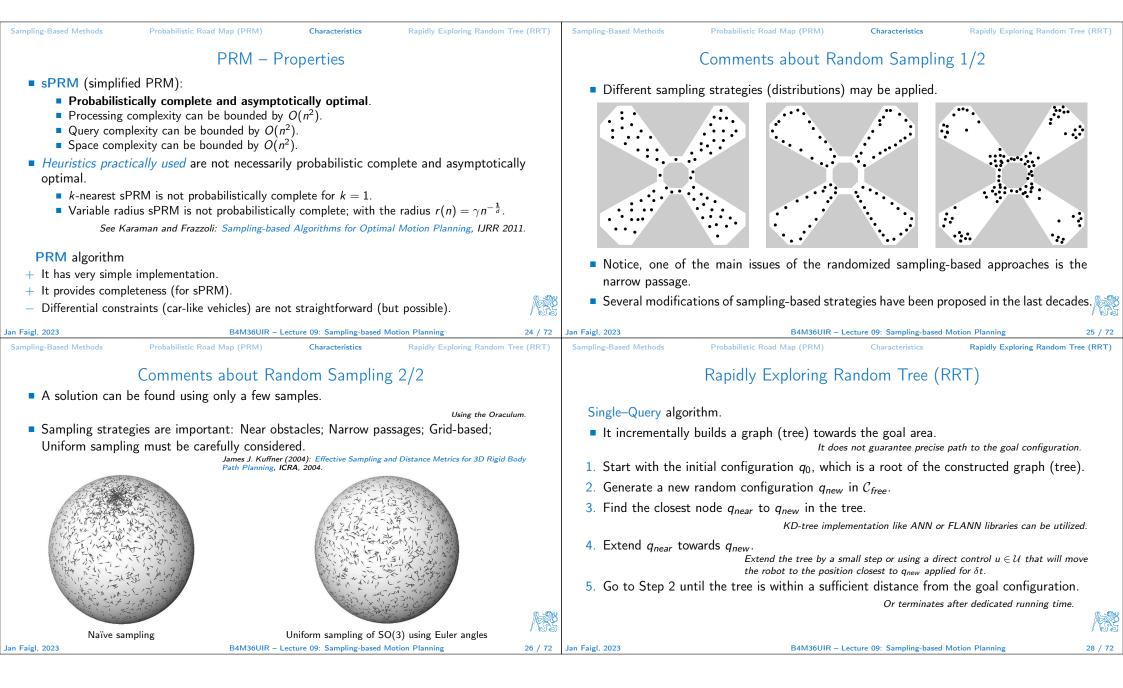


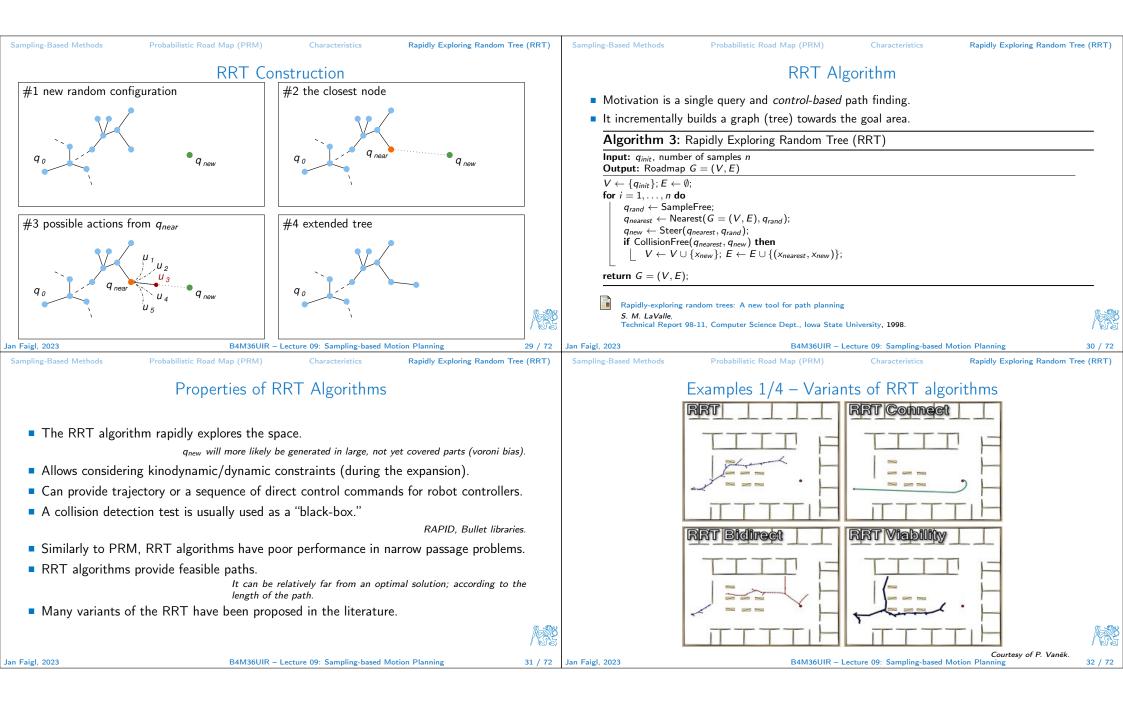
Sampling-Based Methods	Probabilistic Road Map (PRM)	Characteristics	Rapidly Exploring Random Tree (RRT)	Sampling-Based Methods	Probabilistic Road Map (PRM)	Characteristics	Rapidly Exploring Random Tr	ee (RRT)
	Probabilistic	Roadmaps		Incremental Sampling and Searching				
•	resentation of the continuous (in \mathcal{C}_{free} that are connected into		by randomly sampled	 Single query sampling-based algorithms incrementally create a search graph (roadmap). 				
Nodes of t	ne graph represent admissible co	nfigurations of the r		 Initialization - G(V, E) an undirected search graph, V may contain q_{start}, q_{goal} and/or other points in C_{free}. Nexture asketic terms and a share search graph, C is the search graph. 				
Edges represented in the second se	esent a feasible path (trajectory)	between the partice	ular configurations.	 Vertex selection method – choose a vertex q_{cur} ∈ V for the expansion. Local planning method – for some q_{new} ∈ C_{free}, attempt to construct a path τ : [0, 1] → C_{free} such that τ(0) = q_{cur} and τ(1) = q_{new}, τ must be checked to ensure it is collision free. If τ is not a collision-free, go to Step 2. Insert an edge in the graph – Insert τ into E as an edge from q_{cur} to q_{new} and insert q_{new} to V if q_{new} ∉ V. How to test q_{new} is in V? Check for a solution – Determine if G encodes a solution by using a single search tree or graph search technique. Repeat Step 2 – iterate unless a solution has been found or a termination condition is satisfied. 				
	Having the graph, the final path (trajed	ctory) can be found by a	graph search technique.		LaValle, S. I	M.: Planning Algorith	ms (2006), Chapter 5.4.	<u>A</u>
Jan Faigl, 2023	B4M36UIR – Le	ecture 09: Sampling-based Mo	tion Planning 6 / 72	Jan Faigl, 2023	B4M36UIR – L	ecture 09: Sampling-based M	lotion Planning	7 / 72
Sampling-Based Methods	Probabilistic Road Map (PRM)	Characteristics	Rapidly Exploring Random Tree (RRT)	Sampling-Based Methods	Probabilistic Road Map (PRM)	Characteristics	Rapidly Exploring Random Tr	ee (RRT)
	Probabilistic Road	dmap Strategies	;	Multi-Query Strategy				
Multi-Query	strategy is to create a roadmap	o that can be used f	or several queries.	Build a roadmap (graph) representing the environment.				
 Generate a 	single roadmap that is then used	for repeated plann	ing queries.	1. Learning phase				
An represen	tative technique is Probabilistic	c RoadMap (PRM).	1.1 Sample <i>n</i> points in C_{free} .				
•	Kavraki, L., Svestka, P., Latombe, JC., C High Dimensional Configuration Spaces, IEI	Overmars, M. H.B: Probabilist	, ic Roadmaps for Path Planning in	1.2 Connect the random configurations using a local planner.				
	Hsu, D., Latombe, JC., Kurniawati, H.: C The International Journal of Robotics Rese	On the Probabilistic Foundation		2. Query phase				
				2.1 Connect start and goal configurations with the PRM.				
-	y strategy is an incremental app			t Using a loca	al planner			
•	anning problem, it constructs a	new roadmap to ch	aracterize the subspace	2.2 Use the graph search to find the path.				
Rapidly	-exploring Random Tree – RRT;		LaValle, 1998	- Drobabilistic Readma	ung far Dath Diagning in High Dimon	cional Configuration Spa		
Expansive-Space Tree – EST; Hsu et al., 1997			Probabilistic Roadmaps for Path Planning in High Dimensional Configuration Spaces Lydia E. Kavraki and Petr Svestka and Jean-Claude Latombe and Mark H. Overmars,					
Samplir	ng-based Roadmap of Trees – SRT.		1130 CL 81., 1991	IEEE Transactions or	n Robotics and Automation, 12(4):50	56–580, 1996.		
·			nd single-query approaches. Plaku et al., 2005	First planner that demonstrates ability to solve general planning problems in more than 4-5 dimensions.				
Jan Faigl, 2023	B4M36UIR – Le	ecture 09: Sampling-based Mo	tion Planning 8 / 72	Jan Faigl, 2023	B4M36UIR – L	ecture 09: Sampling-based M	lotion Planning	10 / 72

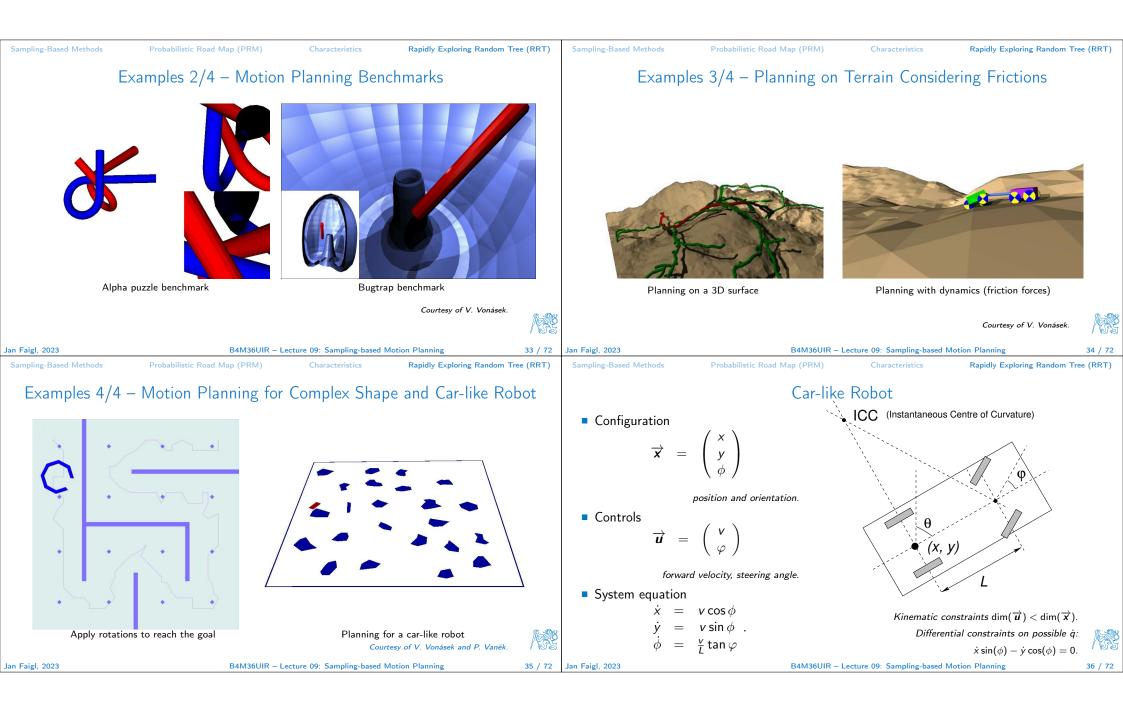


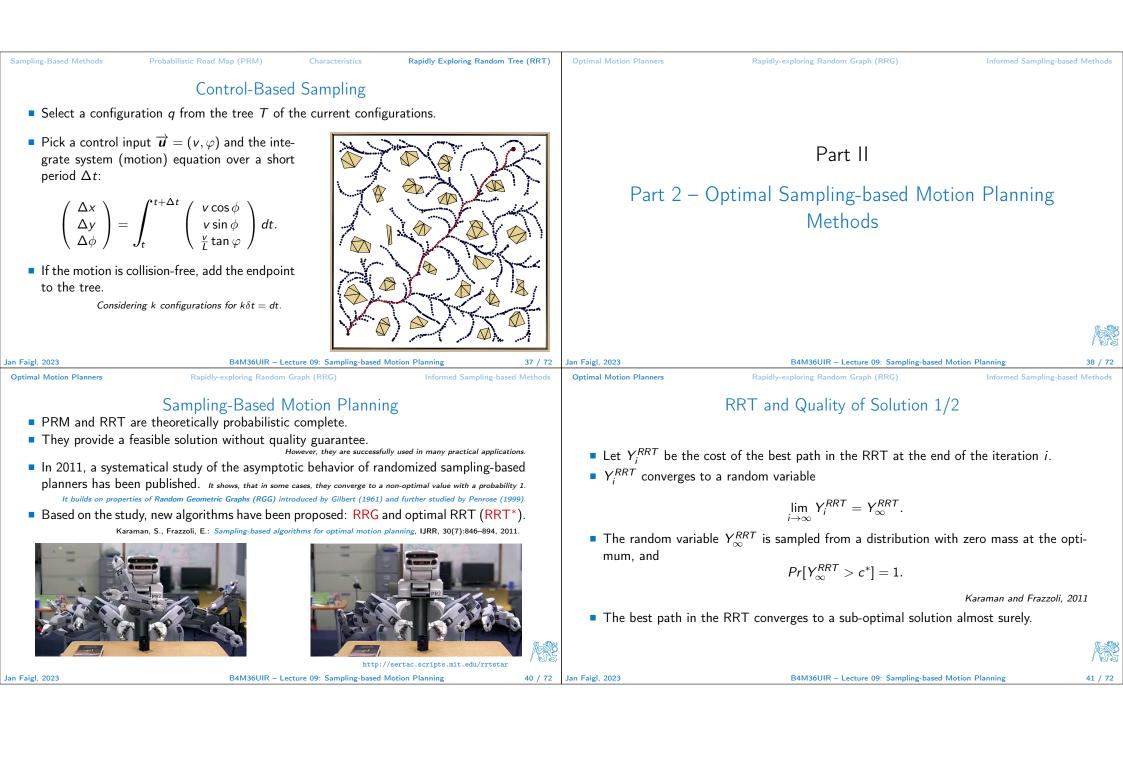


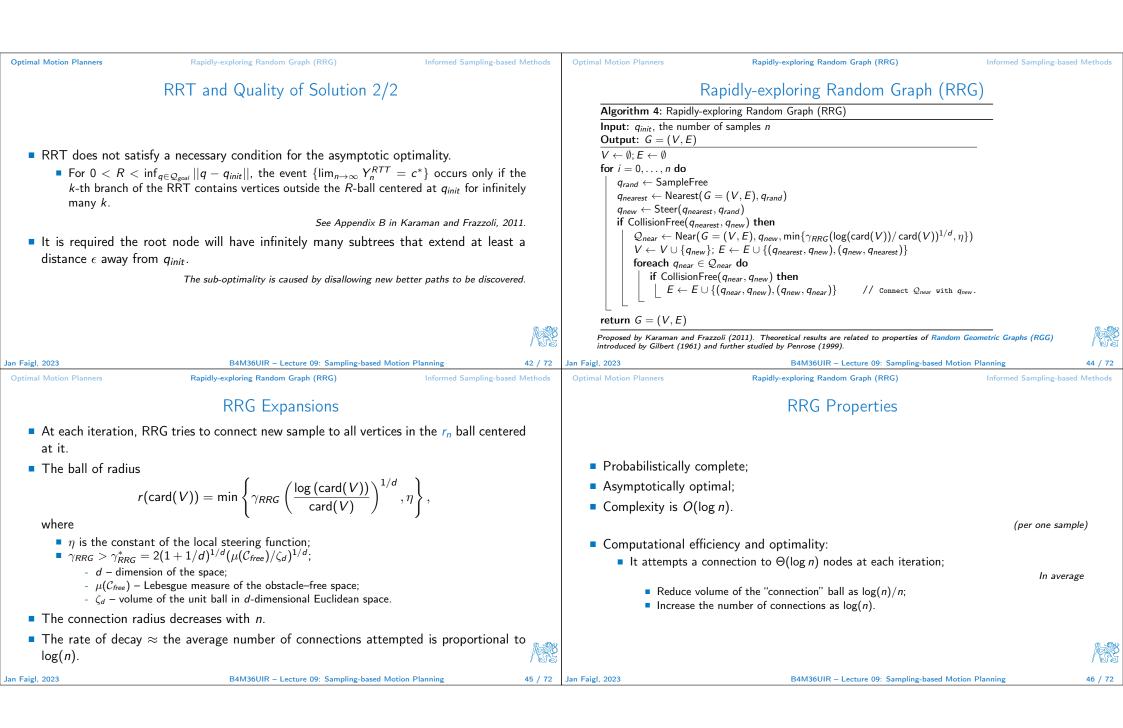


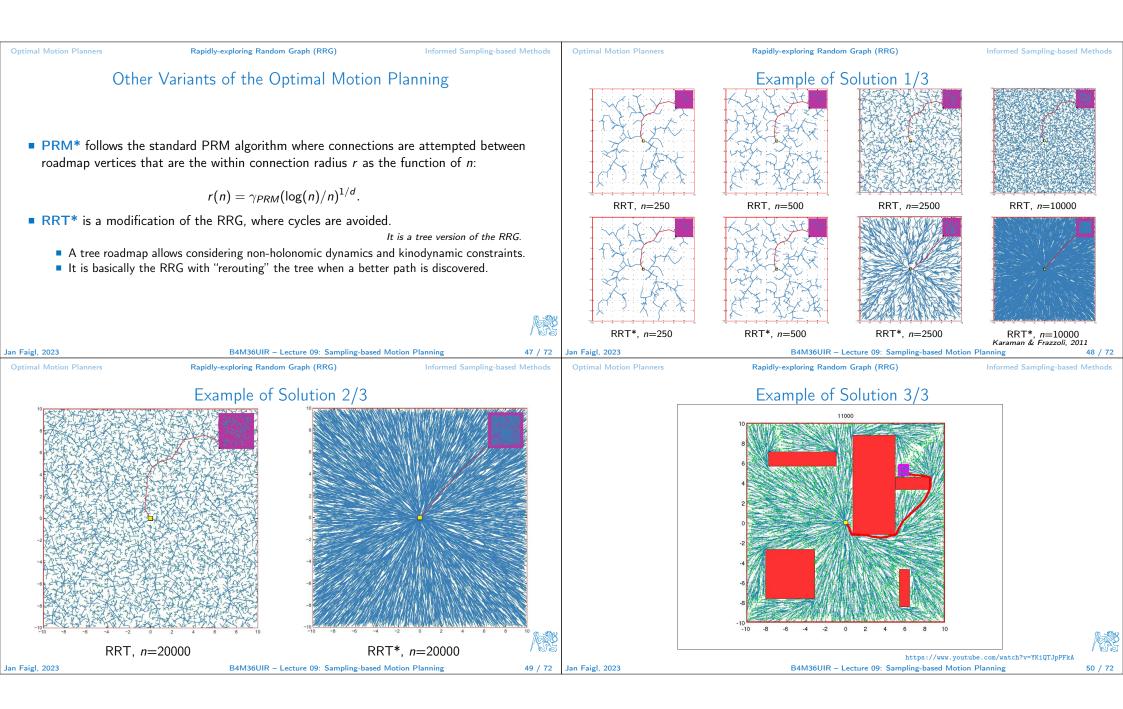


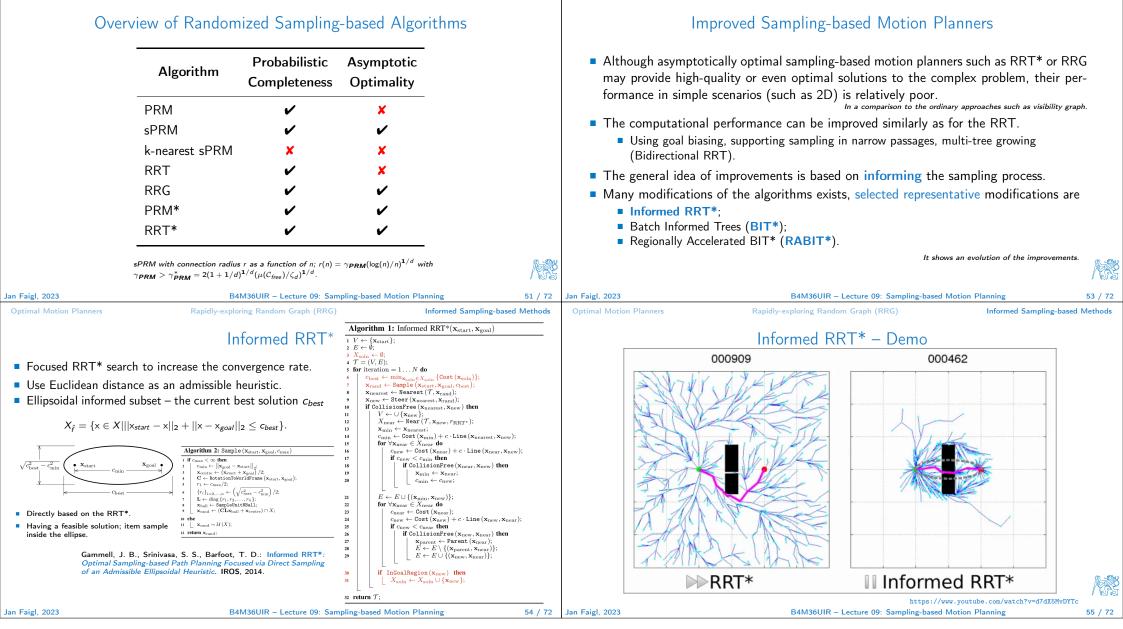












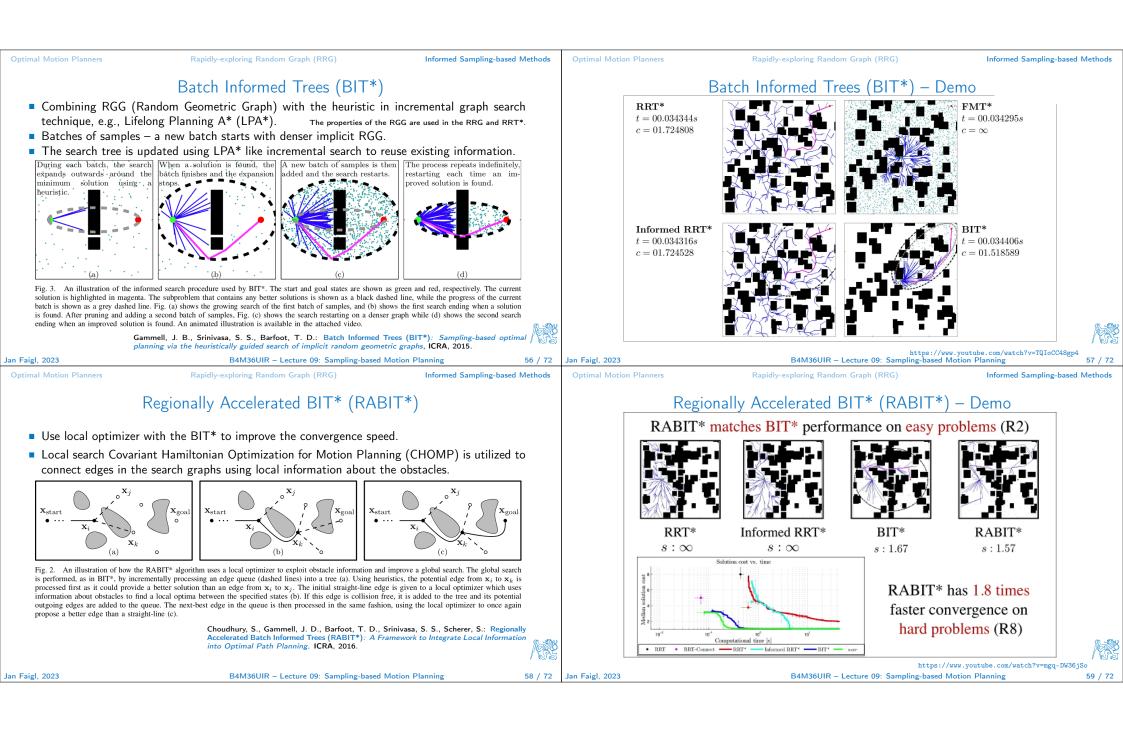
Rapidly-exploring Random Graph (RRG)

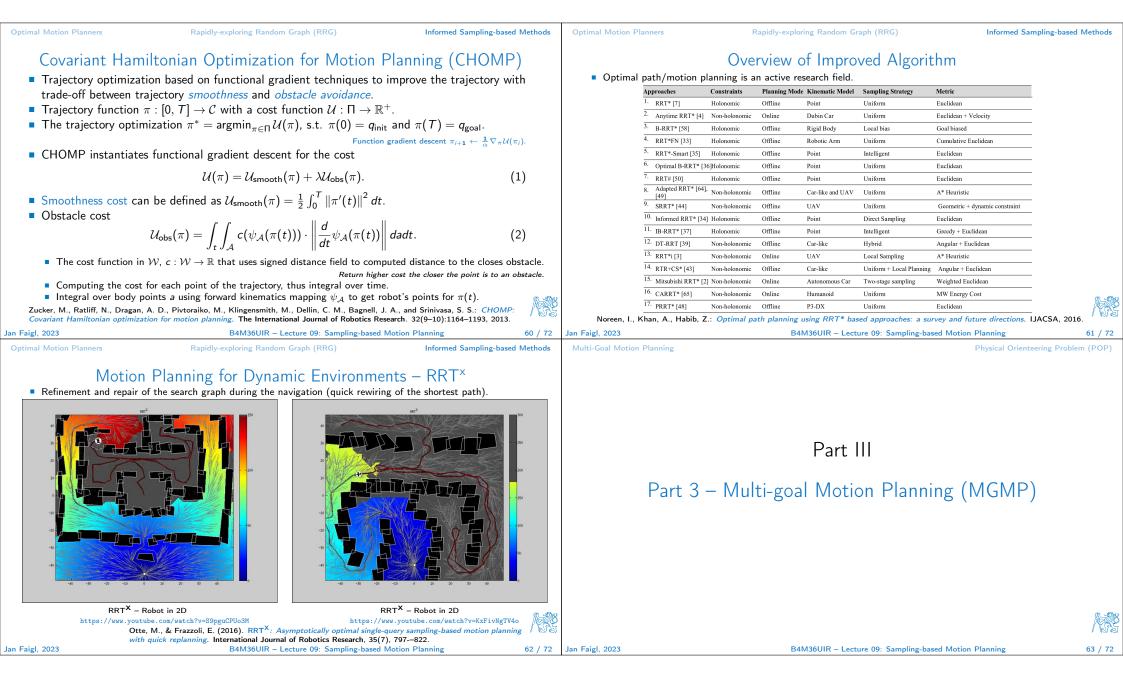
Informed Sampling-based Methods Op

sed Methods Optimal Motion Planne

Rapidly-exploring Random Graph (RRG)

Informed Sampling-based Methods





Multi-Goal Motion Planning

Physical Orienteering Problem (POP) Mu

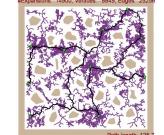
P) Multi-Goal Motion Planning

Physical Orienteering Problem (POP)

Multi-Goal Motion Planning

- In the previous cases, we consider existing roadmap or relatively "simple" collision free (shortest) paths in the polygonal domain.
- However, determination of the collision-free path in high dimensional configuration space (C-space) can be a challenging problem itself.
- Therefore, we can generalize the MTP to multi-goal motion planning (MGMP) considering motion planners using the notion of C-space for avoiding collisions.
- An example of MGMP can be to plan a cost efficient trajectory for hexapod walking robot to visit a set of target locations.





Problem Statement – MGMP Problem

- The working environment $\mathcal{W} \subset \mathbb{R}^3$ is represented as a set of obstacles $\mathcal{O} \subset \mathcal{W}$ and the robot configuration space \mathcal{C} describes all possible configurations of the robot in \mathcal{W} .
- For q ∈ C, the robot body A(q) at q is collision free if A(q) ∩ O = Ø and all collision free configurations are denoted as C_{free}.
- Set of *n* goal locations is $\mathcal{G} = (g_1, \ldots, g_n)$, $g_i \in \mathcal{C}_{free}$.
- Collision free path from q_{start} to q_{goal} is $\kappa : [0,1] \rightarrow C_{free}$ with $\kappa(0) = q_{start}$ and $d(\kappa(1), q_{end}) < \epsilon$, for an admissible distance ϵ .
- Multi-goal path τ is admissible if $\tau : [0, 1] \rightarrow C_{free}$, $\tau(0) = \tau(1)$ and there are *n* points such that $0 \le t_1 \le t_2 \le \ldots \le t_n$, $d(\tau(t_i), v_i) < \epsilon$, and $\bigcup_{1 < i < n} v_i = \mathcal{G}$.
- The problem is to find the path τ^* for a cost function c such that $c(\tau^*) = \min\{c(\tau) \mid \tau \text{ is admissible multi-goal path}\}.$

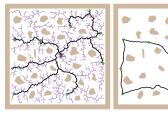
8 . S	Path length: 125.7				
Jan Faigl, 2023	B4M36UIR – Lecture 09: Sampling-based Motion Planning	65 / 72 Jan Faigl, 202	B4M36UIR	R – Lecture 09: Sampling-based Motion Planning	66 / 72
Multi-Goal Motion Planning	Physical Orienteering	g Problem (POP) Multi-Goal M	lotion Planning	Physical Orienteering	; Problem (POP)

MGMP – Existing Approches

- Determining all paths connecting any two locations $g_i, g_j \in \mathcal{G}$ is usually very computationally demanding.
- Considering Euclidean distance as an approximation in the solution of the TSP as the Minimum Spanning Tree (MST) – Edges in the MST are iteratively refined using optimal motion planner until all edges represent a feasible solution. Saha M. Roughgarden T. Latomber L.C. Sánchaz Ante, G.: Planning Tours of Robotic Arms among

On. Saha, M., Roughgarden, T., Latombe, J.-C., Sánchez-Ante, G.: Planning Tours of Robotic Arms among Partitioned Goals., International Journal of Robotics Research, 5(3):207–223, 2006

- Synergistic Combination of Layers of Planning (SyCLoP) A combination of route and trajectory planning. Plaku, E., Kavraki, L.E., Vardi, M.Y. (2010): Motion Planning With Dynamics by a Synergistic Combination of Layers of Planning, IEEE Transactions on Robotics, 26(3):469–482, 2010.
- Steering RRG roadmap expansion by unsupervised learning for the TSP.
- Steering PRM* expansion using VNS-based routing planning in the Physical Orienteering Problem (POP).

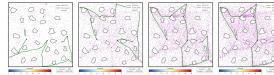




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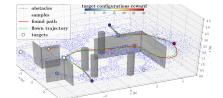
Multi-Goal Trajectory Planning with Limited Travel Budget Physical Orienteering Problem (POP)

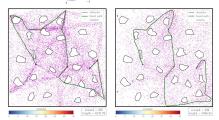
- Orienteering Problem (OP) in an environment with obstacles and motion constraints of the data collecting vehicle.
- A combination of motion planning and routing problem with profits.
- VNS-PRM* VNS-based routing and motion planning is addressed by PRM*.
- An initial low-dense roadmap is continuously expanded during the VNS-based POP optimization to shorten paths of promising solutions.
- Shorten trajectories allow visiting more locations within T_{max}



 Pēnička, Faigl and Saska: Physical Orienteering Problem for Unmanned Aerial Vehicle Data Collection Planning in Environments with Obstacles. IEEE Robotics and Automation Letters 4(3):3005–3012, 2019.

67 / 72 Jan Faigl, 2023





B4M36UIR - Lecture 09: Sampling-based Motion Planning

69 / 72

Jan Faigl, 2023

