Question 1.

Consider the instance space $X = \mathbb{R}^2$ and a concept $c \subseteq X$ given as



- (a) Name some concept classes C that contain c.
- (b) Recall the SVM algorithm and decision trees. What hypothesis classes \mathcal{H} do they work with and how do they internally represent their hypotheses? Would they be appropriate to learn the concept c?

Question 2.

Consider the generalization algorithm for learning conjunctions.

- (a) What is the algorithm's mistake bound? Describe a scenario when we achieve it.
- (b) Assume we work on n = 4 logical variables. Assume the sequence of examples

 $x_1 = (1, 0, 0, 1)$ with label $y_1 = 1$ $x_2 = (1, 1, 0, 0)$ with label $y_2 = 0$ $x_3 = (0, 1, 1, 1)$ with label $y_3 = 1$ $x_4 = (1, 1, 1, 0)$ with label $y_4 = 0$

Write the initial (internal) hypothesis as well as how it will gradually change when processing examples above. Assuming that the concept class is in fact a set of all conjunctions, can we claim that the final hypothesis describes the target concept?

- (c) Adapt the algorithm to learn k-DNF. What is the mistake bound now? Are we still learning efficiently?
- (d) How can we use the new algorithm to learn k-clause CNF? What is *improper* learning?