

# Multi-Robot Systems

<https://youtu.be/dT7b1j5lj1I>

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# Multi-Robot Systems at CTU in Prague

<http://mrs.felk.cvut.cz/>

<http://mrs.felk.cvut.cz/available-student-projects>



- UAV localization, mapping, SLAM and perception
- UAV stabilization and fast collision mutual avoidance
- Model Predictive Control
- Vision-based techniques
- UAV formation coordination
- Safety-critical & robust applications
- Decentralized control of swarms of aerial vehicles
- Cooperative sensing and data collection by a group of UAVs
- Mutual localization of neighboring vehicles in swarms
- High-level planning, communication and coordination
- Indoor navigation and exploration



3/2017 – MBZIRC 3<sup>rd</sup> challenge:  
1<sup>st</sup> place \$330.000



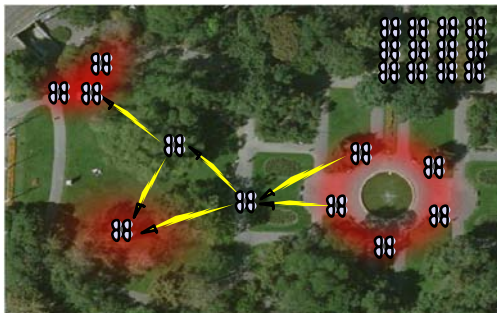
2/2020 – MBZIRC 2<sup>nd</sup> challenge:  
1<sup>st</sup> place \$250.000, TOTAL WINNERS



2019-2020 - DARPA SubT: 2x 1<sup>st</sup> place  
among self-funded teams. \$200k & \$500k

# Multi-Robot Systems

- Single-Robot → Multi-Robot Systems
  - Multiple mobile robots → Multi-Robot System
  - Coordination using communication
- Motivation
  - Robotic problems are often naturally distributed
  - Redundancy and robustness vs. enlarged complexity of the system
  - Faster mission execution (e.g., search and rescue)
  - Several light-weight robots replace a large well-equipped and heavy robot
  - Many tasks not solvable by a single robot
  - Actions realized in distance places in parallel



*Saska 2017 AURO*



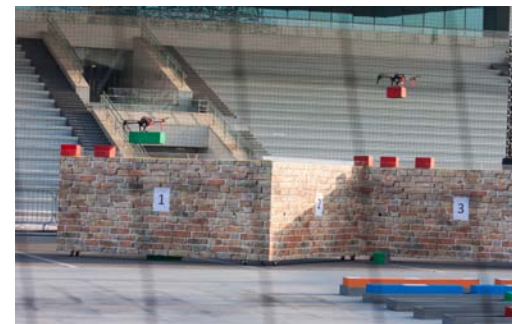
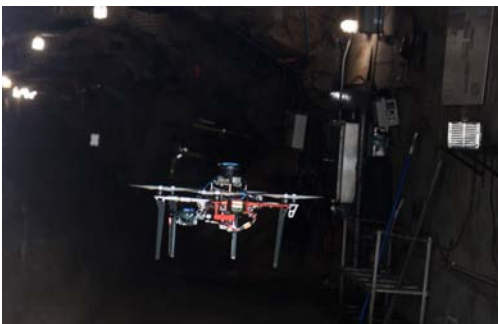
*Saska 2017 ETFA*



*Spurný 2019 ETFA*

# Multi-Robot Systems

- Taxonomy and essential terms
  - Centralized vs. Decentralized control architecture
  - Coordination vs. Cooperation vs. Collaboration
  - Explicit vs. Implicit communication
  - Homogeneous vs. Heterogeneous robots
  - Collective movement - Swarms vs. Formations



# Centralized vs. Decentralized (vs. Distributed)

- Centralized control architecture
  - Single control unit (a decision/commands are distributed to all robots from a central PC)
  - Centralized state estimation of the entire MRS; knowledge of the global state
  - + Usually simpler control design and better performance
  - Requires synchronized and reliable communication
  - Single-point of failure problem
  - Less scalable

# Centralized vs. Decentralized (vs. Distributed)

- Centralized control architecture



# Centralized vs. Decentralized (vs. Distributed)

- Decentralized control architecture
  - Each robot equipped with onboard processing unit makes and executes its own decision obtained based on interactions with other robots
  - Decentralized state estimation (each robot estimates its state and relative states of teammates)
  - + Scalability
  - + Robust to failures
  - Difficult to achieve optimal performance (sub-optimal performance)
  - Difficult to prove optimality

# Centralized vs. Decentralized (vs. Distributed)

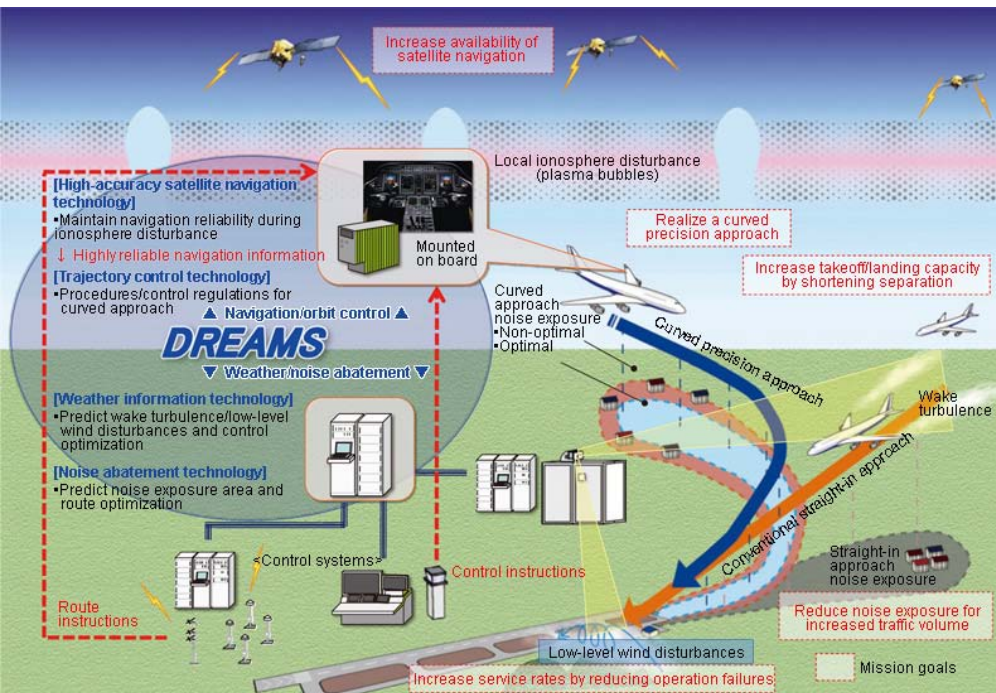
- Decentralized control architecture



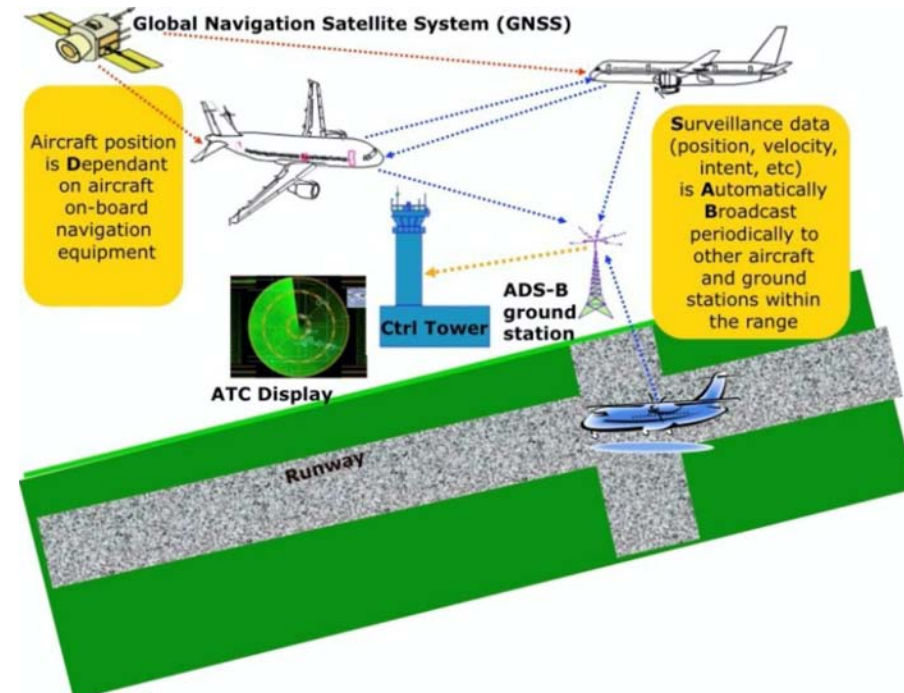


# Centralized vs. Decentralized (vs. Distributed)

- Distributed control architecture
  - The decision is made by a negotiation process between the robots
  - For example autonomous air and car traffic management
  - + Scalability and robust to failures
  - Requires reliable communication



DREAMS (Distributed and Revolutionarily Efficient Air-traffic Management System)



Air traffic management by Imperial College London

# Coordination vs. Cooperation vs. Collaboration

- Coordination
  - Allows a group to complete a task more efficiently than a single robot by its self (according to Vijay Kumar, UPENN)
  - Usually motion coordination and alignment (e.g., to keep a cohesive swarm)
- Cooperation
  - Allows a group to complete a task that an individual robot could not complete on its own at all.
  - Robots cooperate towards a common intention together (e.g., cooperative transportation)
  - It usually requires synchronization and tight sharing workspace
- Collaboration
  - Allows a group of different types of robots with diverse capabilities to complete a task that cannot be completed using just one type of robots

# Coordination – e.g. Treasure hunt at MBZIRC 2017

- Multi-UAV team collecting objects of unknown position – faster and more reliable

## Cooperation – e.g. heavy object transportation

- The object is too heavy or large to be transported by a single UAV with a payload

# Cooperative transport of large objects by multiple UAVs

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Flying through a field  
with obstacles

# Collaboration – e.g. complex fire extinguishing or smart lightning

- MBZIRC 2020: Different robots for different fire locations (ground floor, top floor, outdoor)

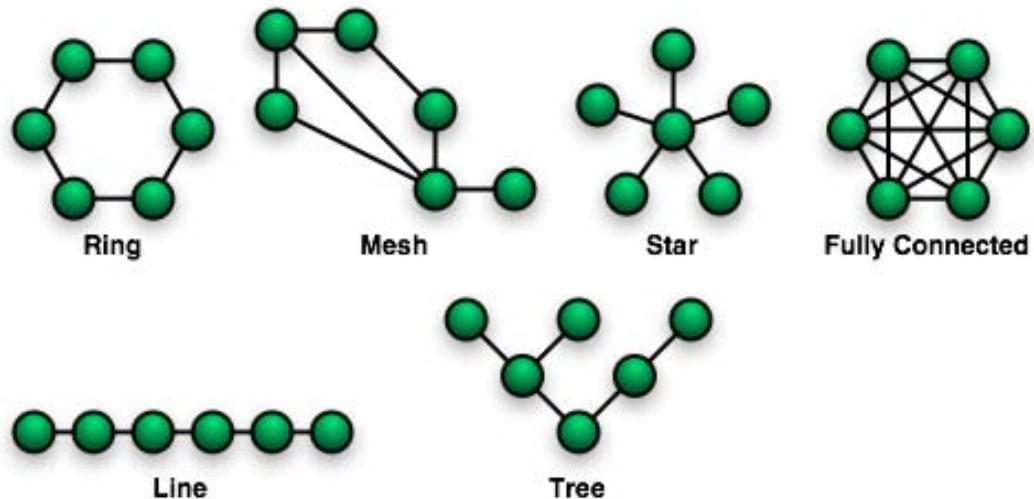


# Explicit vs. Implicit communication

- Explicit communication
  - States of neighbors are unobservable
  - Communication infrastructure required
- Implicit communication
  - Directly through observation of neighbor states (relative or mutual localization)
  - Undirect information exchange by observation of the workspace

# Explicit communication - Topologies

- Range of communication
  - A disc model (only in a simple environment)
- Communication for centralized control/coordination
  - **Fully connected**
  - **Star**, Line, Ring, Tree, Hierarchical topology
- Communication for decentralized control/coordination
  - Mesh
  - Random mesh



# Explicit communication – Line and Mesh topology

- DARPA SubT: Team of ground and aerial robots deployed in underground tunnels



# Implicit communication – relative localization

- Marker-Less Detection and Localization
  - Vision-based (CNN), Lidars, 3D cameras
  - None-cooperating robots, humans, vehicles

2019

Demonstration of an autonomous  
aerial interception prototype platform



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*Vrba 2019 RAL*

[https://youtu.be/r\\_qouOpFMn4](https://youtu.be/r_qouOpFMn4)

*Vrba 2020 RAL*

<https://youtu.be/mr4uqgBslHw>

# Implicit communication – relative localization

- MBZIRC 2020: Team of aerial robots hunting balloons and aerial target (RGB and Lidar)

## MBZIRC 2020 Summary

### Challenge #1

CTU in Prague, UPenn, NYU



**CTU**

CZECH TECHNICAL  
UNIVERSITY  
IN PRAGUE

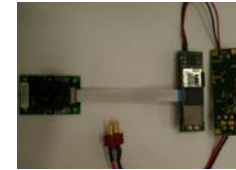


**Penn**  
UNIVERSITY of PENNSYLVANIA



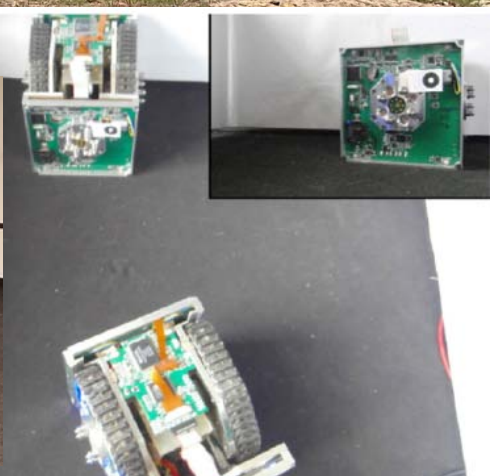
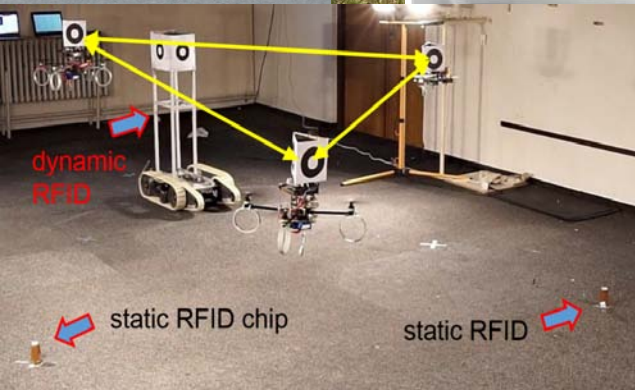
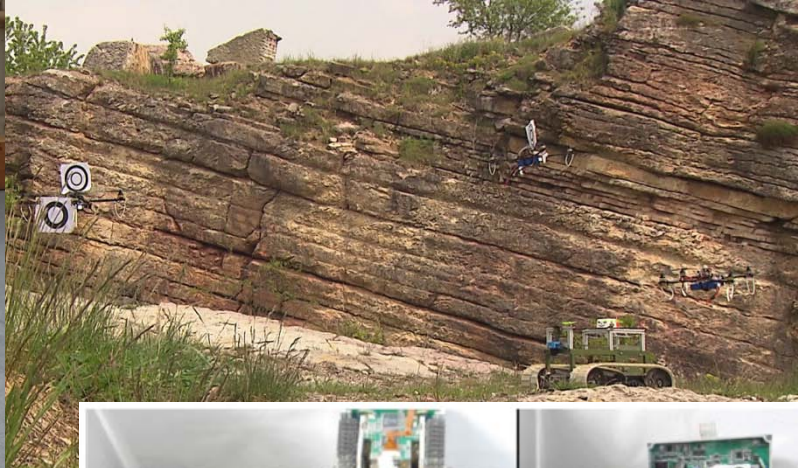
# Implicit communication – relative localization

- Marker-based relative localization
  - Passive markers – color and B&W patterns
  - Active markers – RGB and UV lights



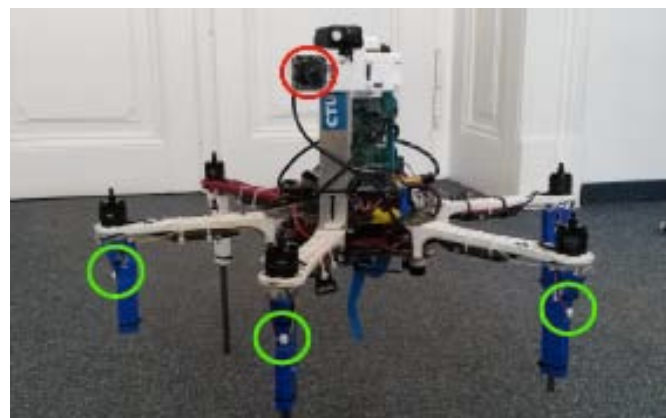
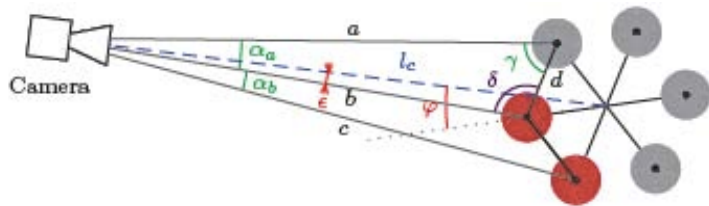
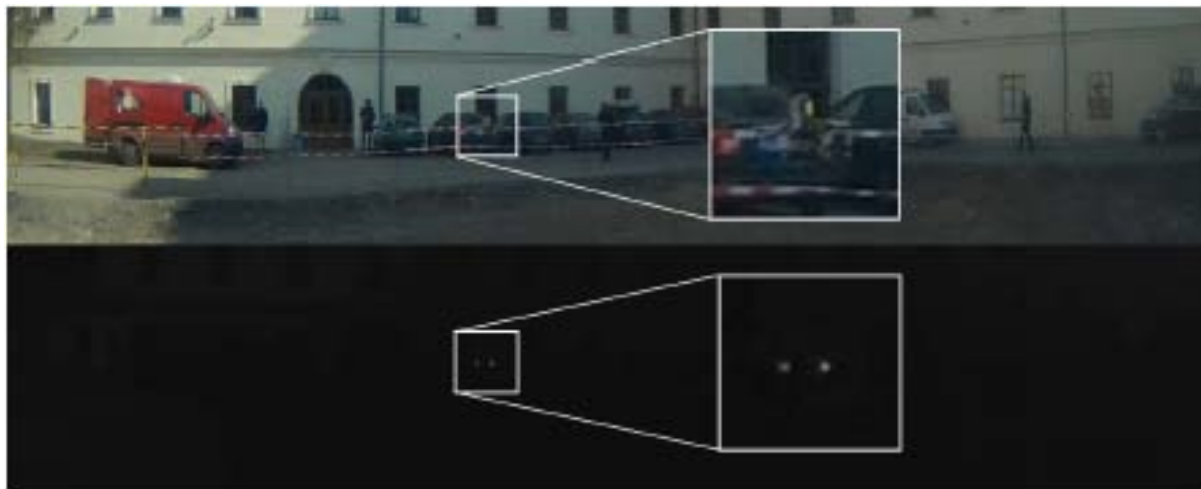
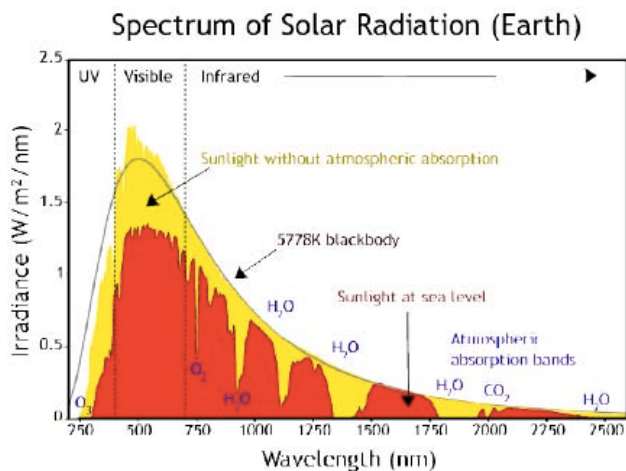
*Faigl 2013 ICRA, Krajnik 2014 JINT*





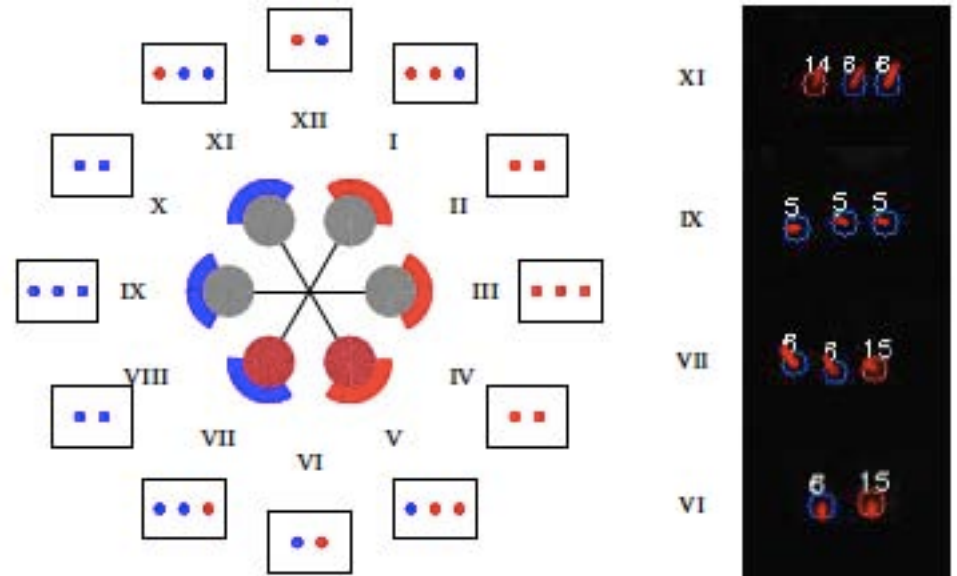
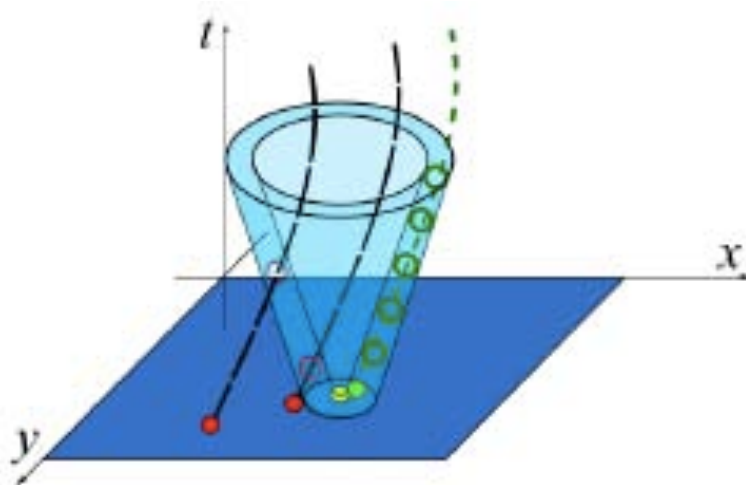
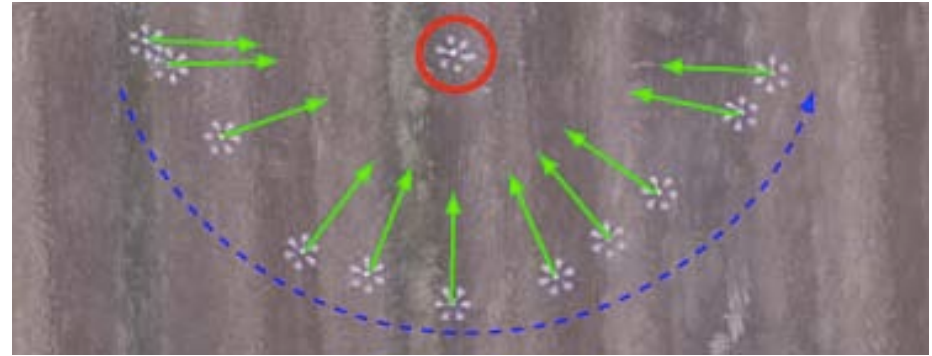
# Implicit communication – relative localization using active UV Markers

- Reduced size of markers, low computational complexity
- Increased reliability



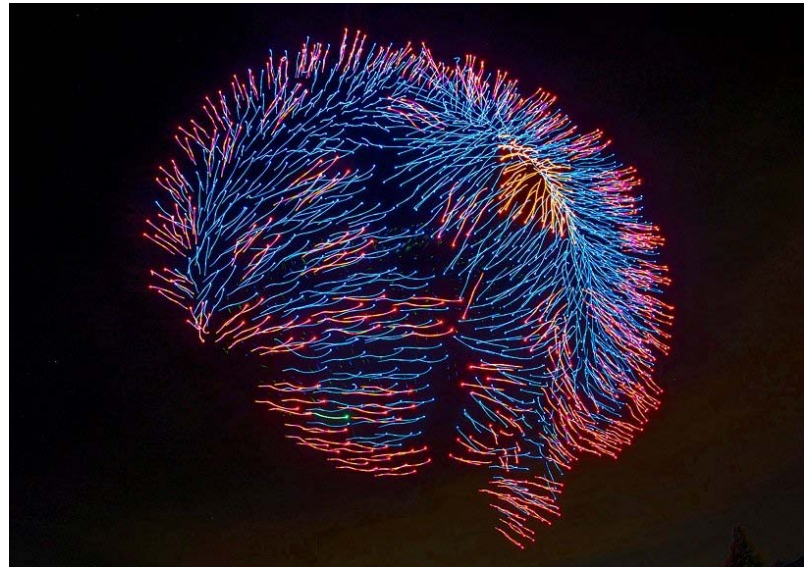
# Beyond implicit communication - Blinking UV markers

- ID encoding and observation
- Relative orientation estimation
- 3D time-position Hough transform
- Robustness increase



# Collective Movement – swarms/flocks

- Inspiration by nature
  - Completely decentralized (no leader), scalable, allows splitting, collective obstacle avoidance, escape ability (from predators), local interactions and relative localization
- Swarms of robots
  - Decentralized – e.g., Boids [Reynolds, 1997] or [Olfati-Saber, 2006]
  - Centralized – drone shows, stochastic optimization methods: PSO, Fish school

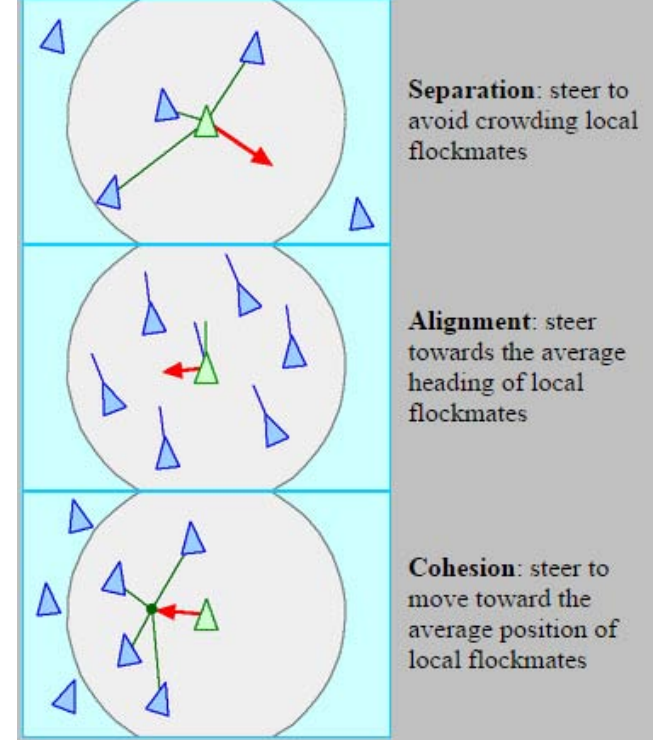


2,018 Intel Shooting Star drones

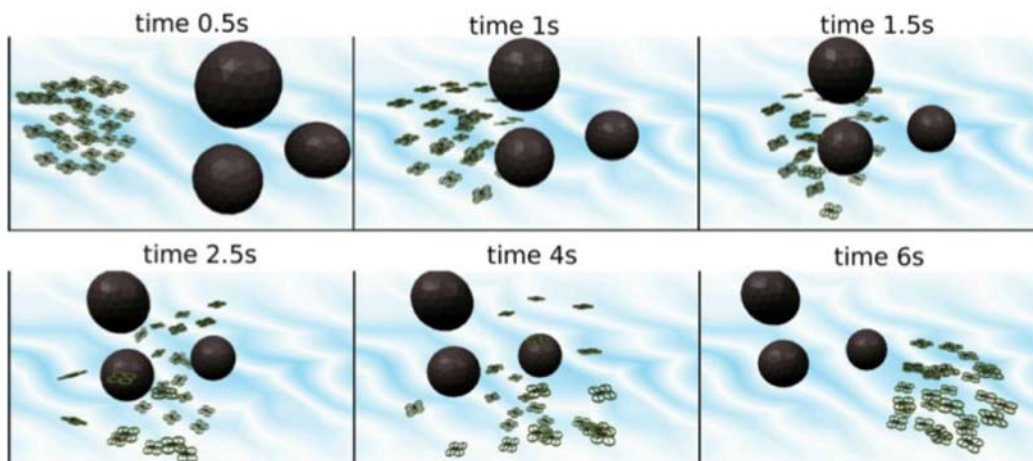
# Collective Movement – swarms/flocks

- Boids by Reynolds

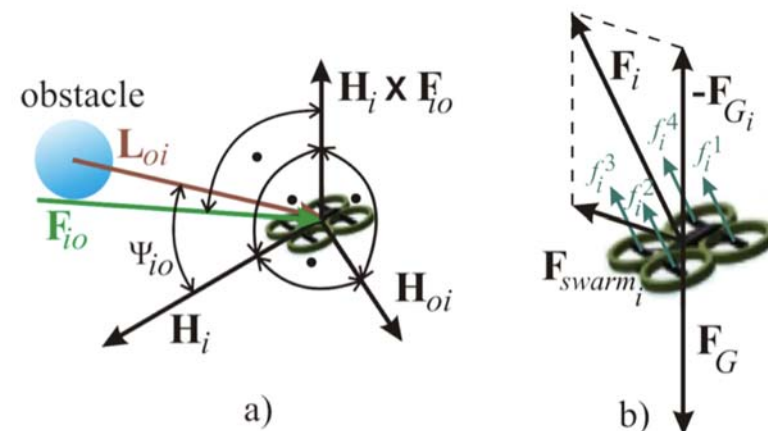
- Originally a computer graphic method to animate flocks
- Each particle reacts to local neighborhood → complexity  $O(N)$
- 3 control rules in the primary method
- For real-world swarms + *obstacle avoidance* and *common intention* rules
- Local sensory system: (e.g., UVDAR)



Reynolds, 1997



Saska 2015 ICUAS



Saska 2014 ICRA

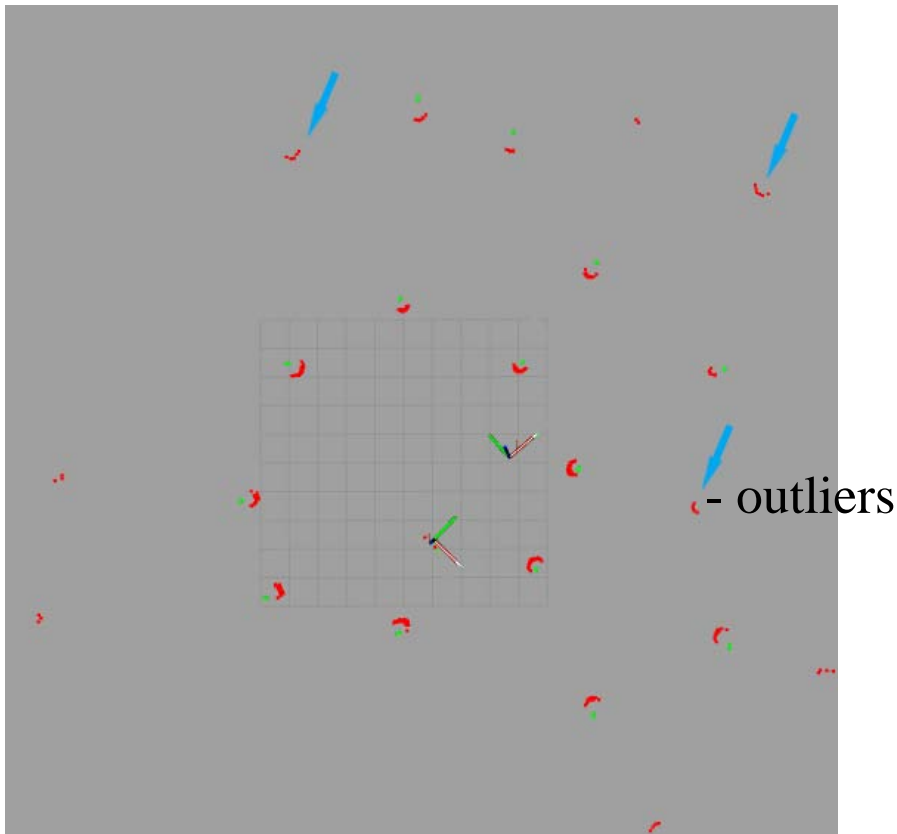


## Collective Movement – swarms in environments with obstacles

- No GNSS, no explicit communication, fully decentralized, implicit UV-based com.

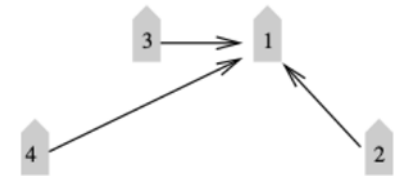
# Implicit communication - undirect

- Explicit communication
  - Undirect information exchange by observation of the workspace
  - Problem of matching features detected from different positions
  - Similar to ICP for SLAM

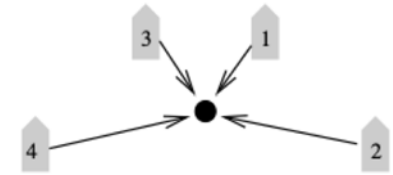


# Collective movement - Formations

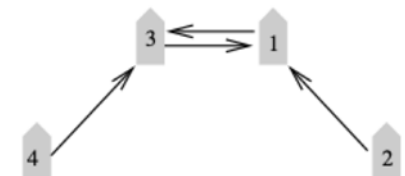
- Formations of cooperating robots
  - Specific geometric configurations
  - Knowledge of states of all robots required
- Formation driving and flying approaches
  - Virtual structures
  - Leader-follower
  - Virtual leader-follower (e.g. unite-center referenced)
  - Neighbor referenced



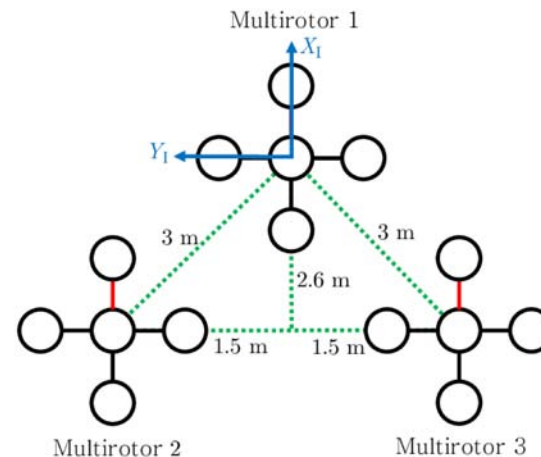
Leader-follower



Unite-center referenced



Neighbor referenced



# Formations – Nonholonomic Leader-Follower model

- Nonholonomic kinematic model
  - Car-like vehicle
  - Limited turning radius

$$\dot{x}_j(t) = v_j(t) \cos \theta_j(t)$$

$$\dot{y}_j(t) = v_j(t) \sin \theta_j(t)$$

$$\dot{\theta}_j(t) = K_j(t)v_j(t) \quad j \in \{1, \dots, n_r, L\}$$

$$\bar{u}_j(t) = \{v_j(t), K_j(t)\} \text{ - control inputs (velocity + curvature)}$$

$$\bar{p}_j(t) = \{x_j(t), y_j(t)\} \text{ - position}$$

$$\psi_j(t) = \{p_j(t), \theta_j(t)\} \text{ - system state (position + heading)}$$



# Formations – Nonholonomic Leader-Follower model

- Position of the followers determined by curvilinear coordinates  $p_i(t), q_i(t)$

$p_i(t)$  - traveled distance between leader and follower  $i$

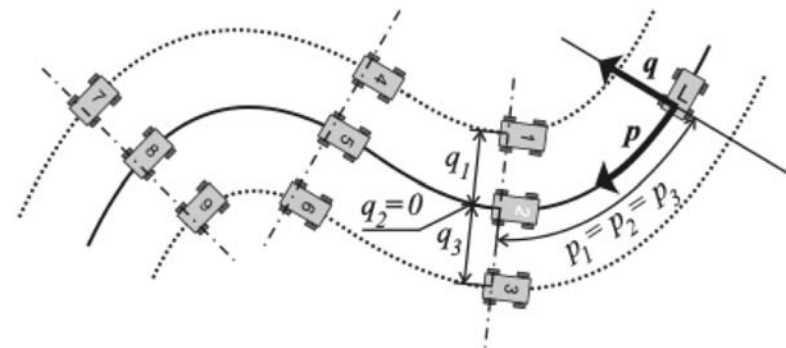
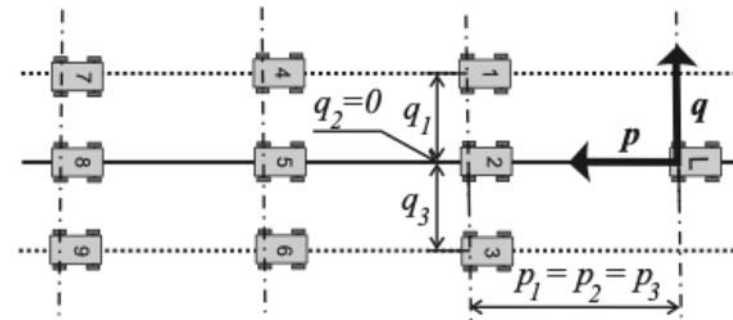
$q_i(t)$  - offset distance between  
leader and follower  $i$

$t_{p_i(t)}$  - time when the leader was  
in traveled distance  $p_i(t)$

$$x_i(t) = x_L(t_{p_i(t)}) - q_i(t_{p_i(t)}) \sin(\theta_L(t_{p_i(t)}))$$

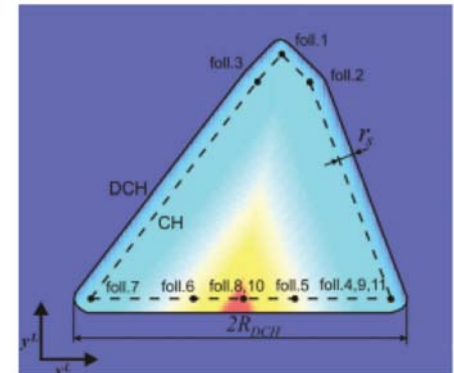
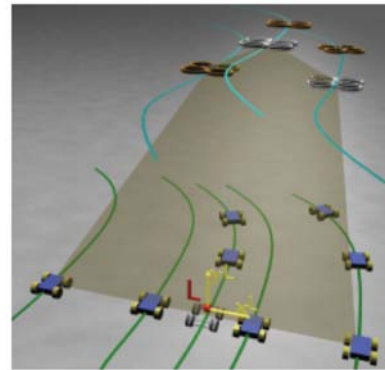
$$y_i(t) = y_L(t_{p_i(t)}) + q_i(t_{p_i(t)}) \cos(\theta_L(t_{p_i(t)}))$$

$$\theta_i(t) = \theta_L(t_{p_i(t)})$$

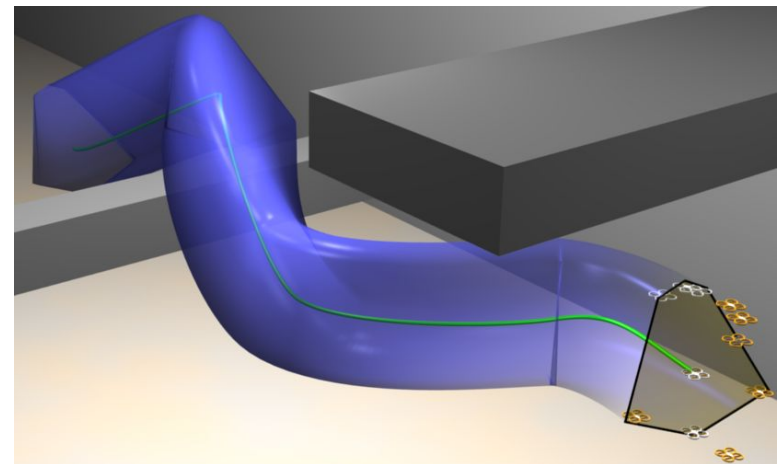
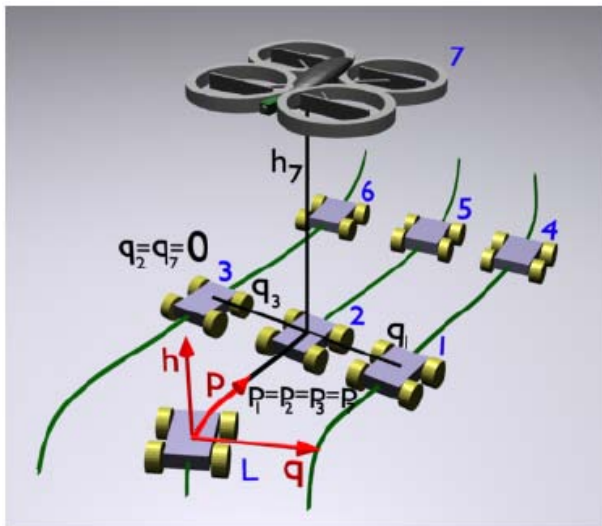


# Formations – Nonholonomic Leader-Follower model

- Heterogenous UAV-UGV formations and 3D UAV formations
- MAV-UGV teams with a "hawk-eye" relative localization

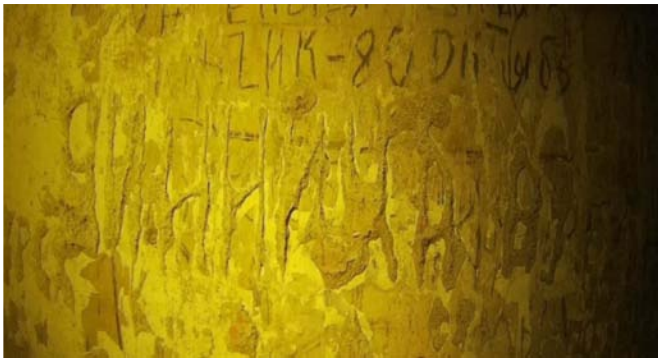
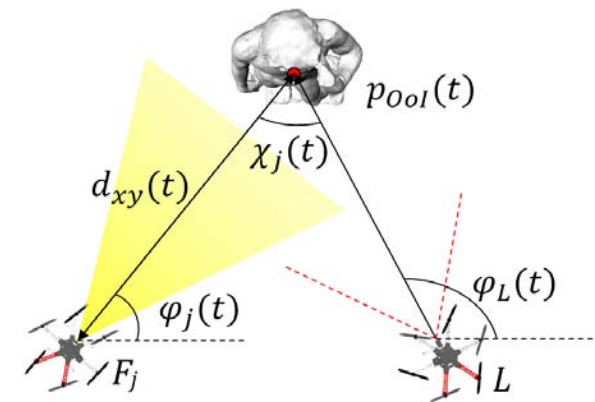
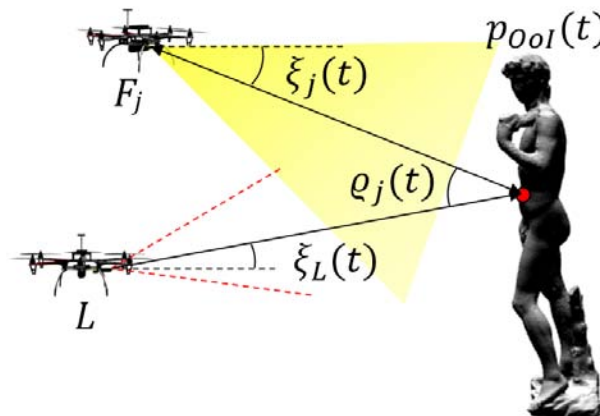
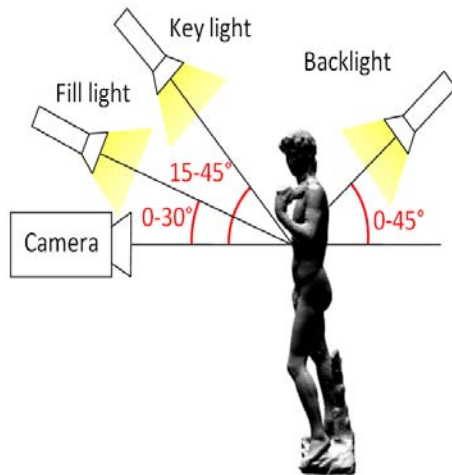


- Complex hull for obstacle avoidance



# Formations –Leader-Follower Applications

- Documentation of dark areas of large historical buildings by a formation of unmanned aerial vehicles
  - Three points lighting technique
  - Cannot be solved by a single robot



*Petráček 2020 RAL  
Krátký 2020 RAL  
Saska 2017 ETFA*

# Dronument

Documentation of historical monuments  
by a team of autonomous aerial vehicles

[mrs.felk.cvut.cz/dronument](https://mrs.felk.cvut.cz/dronument)



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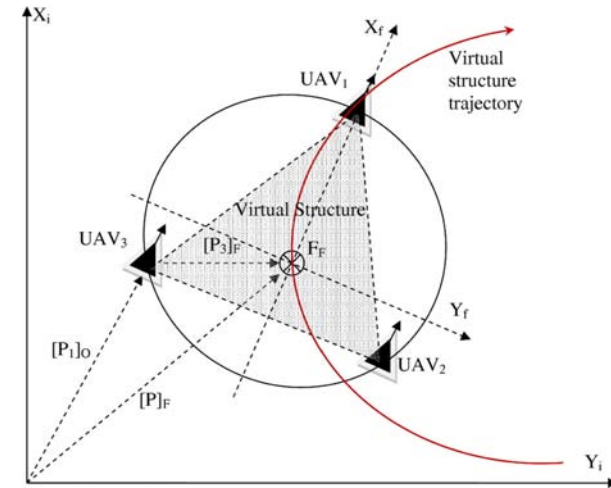
**MULTI-ROBOT  
SYSTEMS  
GROUP**

Video: Pavel Petráček



# Formations – Virtual Structures

- Virtual structures approach
  - + Fixed relative positions between vehicles
  - + Cooperative manipulation with large objects
  - Limited motion constraints
  - Unfeasible for nonholonomic car-like vehicles



*Askari 2015*

MRS Multi-robot systems group  
CTU in Prague

## Cooperative transport of large objects by multiple UAVs

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### Narrow passage experiment

*Spurný 2019*

<https://youtu.be/Pdg3j791I9c>

## Further reading

- Classical graph-based approaches designed for multi-robot systems can be found in:
  - Mesbahi, M. & Egerstedt, M. (2010) Graph theoretic methods in multiagent networks. Princeton University Press.
- Topics related directly to multirotor aerial platforms may be studied from:
  - Franck Cazaurang Kelly Cohen Manish Kumar (2020) Multi-rotor Platform Based UAV Systems. Elsevier.
- An overview of swarming approaches can be found in:
  - Heiko Hamann (2018) Swarm Robotics: A Formal Approach. Springer.

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