Randomized Sampling-based Motion Planning Methods Jan Faigl Department of Computer Science Baculty of Electrical Engineering Czech Technical University in Prague Lecture 08 B4M36UIR – Artificial Intelligence in Robotics	Overview of the Lecture Part 1 – Randomized Sampling-based Motion Planning Methods Sampling-Based Methods Probabilistic Road Map (PRM) Characteristics Rapidly Exploring Random Tree (RRT) Part 2 – Optimal Sampling-based Motion Planning Methods Optimal Motion Planners Rapidly-exploring Random Graph (RRG) Informed Sampling-based Methods Part 3 – Multi-Goal Motion Planning (MGMP) Multi-Goal Motion Planning Physical Orienteering Problem (POP)	Sampling-Based Methods Probabilistic Road Map (PRM) Characteristics Rapidly Exploring Random Tree (RRT) Part I Part 1 – Sampling-based Motion Planning
Jan Faigl, 2022 B4M36UIR – Lecture 08: Sampling-based Motion Planning 1 / 72 Sampling-Based Methods Probabilistic Road Map (PRM) Characteristics Rapidly Exploring Random Tree (RRT)	Jan Faigl, 2022 B4M36UIR – Lecture 08: Sampling-based Motion Planning 2 / 72 Sampling-Based Methods Probabilistic Road Map (PRM) Characteristics Rapidly Exploring Random Tree (RRT)	Jan Faigl, 2022 B4M36UIR – Lecture 08: Sampling-based Motion Planning 3 / 72 Sampling-Based Methods Probabilistic Road Map (PRM) Characteristics Rapidly Exploring Random Tree (RRT)
 (Randomized) Sampling-based Motion Planning t uses an explicit representation of the obstacles in <i>C-space</i>. A "black-box" function is used to evaluate if a configuration q is a collision-free using geometrical models of the objects (robot and environment). 2D or 3D shapes of the robot and environment can be represented as sets of triangles – tesselated models. Collision test is then a test of for the intersection of the triangles. Collision free configurations form a discrete representation of C_{free}. Configurations in C_{free} can be sampled randomly and connected to a (probabilistic) roadmap. Rather than the full completeness they provide probabilistic completeness or resolution completeness. It is probabilisticy complete if for increasing number of samples, an admissible solution would be found (if exist). 	 Debabilistic Roadmaps A discrete representation of the continuous <i>C</i>-space generated by randomly sampled configurations in <i>C</i>_{free} that are connected into a graph. Nodes of the graph represent admissible configurations of the robot. Edges represent a feasible path (trajectory) between the particular configurations. Improve the part of the graph represent admissible configurations of the robot. The graph represent a feasible path (trajectory) between the particular configurations. 	 Incremental Sampling and Searching Single query sampling-based algorithms incrementally create a search graph (roadmap). Initialization – G(V, E) an undirected search graph, V may contain q_{start}, q_{goal} and/or other points in C_{free}. Vertex selection method – choose a vertex q_{cur} ∈ V for the expansion. Local planning method – for some q_{new} ∈ C_{free}, attempt to construct a path τ : [0, 1] → C_{free} such that τ(0) = q_{cur} and τ(1) = q_{new}, τ must be checked to ensure it is collision free. If τ is not a collision-free, go to Step 2. Insert an edge in the graph – Insert τ into E as an edge from q_{cur} to q_{new} and insert q_{new} to V if q_{new} ∉ V. How to text q_{new} is in V? Check for a solution – Determine if G encodes a solution by using a single search tree or graph search technique. Repeat Step 2 – iterate unless a solution has been found or a termination condition is satisfied. LaValle, S. M.: Planning Algorithms (2006), Chapter 5.4.
Sampling-Based Methods Probabilistic Road Map (PRM) Characteristics Rapidly Exploring Random Tree (RRT)	Sampling-Based Methods Probabilistic Road Map (PRM) Characteristics Rapidly Exploring Random Tree (RRT)	Sampling-Based Methods Probabilistic Road Map (PRM) Characteristics Rapidly Exploring Random Tree (RRT)
Probabilistic Roadmap Strategies Multi-Query strategy is to create a roadmap that can be used for several queries. • Generate a single roadmap that is then used for repeated planning queries. • An representative technique is Probabilistic RoadMap (PRM). Marki, L., Svestka, P., Jatomke, JC., Overmar, M. H.B. Probabilistic Roadmaps for Path Planning in Right Dimensional Configuration Space, IEET Transactions on Robotics, 12(4):966–900, 1990. Marki, L., Svestka, P., Latomke, JC., Wermark, M. B.B. Probabilistic Roadmaps for Path Planning in Right Dimensional Configuration Space, IEET Transactions on Robotics, 12(4):966–900, 1990. Marki, D., Latomke, JC., Kurniawati, H.: On the Probabilistic Foundations of Probabilistic Roadmap Planning. The Transactions on Robotics, 12(4):966–900, 1990. Single-Query strategy is an incremental approach. • For each planning problem, it constructs a new roadmap to characterize the subspace of C-space that is relevant to the problem. • Rapidly-exploring Random Tree – RRT; LaValle, 1998 • Expansive-Space Tree – EST; Hsu et al., 1997 • Sampling-based Roadmap of Trees – SRT. A combination of multiple-query and single-query approaches.	Multi-Query Strategy Build a roadmap (graph) representing the environment. 1. Learning phase 1.1 Sample n points in Cfree. 1.2 Connect the random configurations using a local planner. 2. Query phase 2.1 Connect start and goal configurations with the PRM. t Using a local planner. 2.2 Use the graph search to find the path. Image: Probabilistic Roadmaps for Path Planning in High Dimensional Configuration Spaces Lydia E. Kavraki and Petr Svestka and Jean-Claude Latombe and Mark H. Overmars, IEEE Transactions on Robotics and Automation, 12(4):566-580, 1996. First planner that demonstrates ability to solve general planning problems in more than 4-5 dimensions.	#1 Given problem domain #2 Random configuration #3 Connecting samples #4 Connected roadmap #5 Query configuration #6 Final found path #5 Query configuration #6 Final found path
	Jan Faigl, 2022 B4M36UIR - Lecture 08: Sampling-based Motion Planning 10 / 72	Jan Faigl, 2022 B4M36UIR – Lecture 08: Sampling-based Motion Planning 11 / 72
Jan Faigi, 2022 B4M30UIK – Lecture 08: Sampling-based Motion Manning 8 / 72	Jan raig, 2022 B4M30UIK – Lecture U8: Sampling-based Motion Planning 10 / 72	Jan Faigi, 2022 B4M30UIK – Lecture UK: Sampling-based Motion Planning 11 / 72











