Robotic Information Gathering - Exploration of Unknown Environment

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Lecture 04

B4M36UIR - Artificial Intelligence in Robotics



making.

Part I

Part 1 – Robotic Exploration

Robotic Information Gathering and Multi-Goal Planning

It may consist of determining locations to be visited and a combinatorial optimization problem to determine

Robotic information gathering aims to determine an optimal solution to collect the most relevant

It can be considered a general problem for various tasks and missions, including online decision-

and determining a plan according to the particular assumptions and constraints; a plan that is

• Surveillance planning - Find the shortest (a cost-efficient) tour to periodically monitor/capture the given

Data collection planning – Determine a cost-efficient path to collect data from the sensor stations (locations).

In both cases, multi-goal path planning allows solving (or improving the performance) of the

Robotic Exploration of Unknown Environment

It builds on a simple path and trajectory planning - point-to-point planning.

Robotic exploration – create a map of the environment as quickly as possible.

Inspection planning - Find a shortest tour to inspect the given environment

Informative path/motion planning and persistent monitoring.

Robotic Information Gathering

Create a model of phenomena by autonomous mobile robots performing measurements in a dynamic unknown environment.



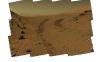














How to address all these aspects altogether to find a cost-efficient solution using in-situ decisions?

Challenges in Robotic Information Gathering

Overview of the Lecture

■ Part 1 - Robotic Information Gathering - Robotic Exploration

• Robotic Information Gathering and Robotic Exploration

Environment Representation

Frontier Based Exploration

Exploration and Search

Where to take new measurements?

How to efficiently utilize more robots?

■ What locations visit first?

Information Theoretic Approaches

Persistent Monitoring of Spatiotemporal Phenomena

robotic information gathering mission.

- about the studied phenomenon.
- considering a limited travel budget.

- Robotic information gathering is challenging problem.
 - Optimal sampling design to Determine locations to be visited w.r.t. the mission objective.
 - Trajectory planning Path/motion planning to find optimal paths/trajectories.
 - Multi-goal path/motion planning for an optimal sequence of visits to the locations.
- In general, the problem is very challenging, and therefore, we consider the most important and relevant constraints, i.e., we address the problem under particular assumptions

information gathering.

particular missions.

How to efficiently utilize a group of mobile robots to create a map of an unknown environment autonomously?

Robotic exploration is a fundamental problem of robotic

Performance indicators vs. constraints.

then executed by the robots.

objects/regions of interest

- Indicators time, energy, map quality.
- Constraints no. of robots, communication

data (measurements) in a cost-efficient way.

- Performance in a real mission depends on the on-line decision-making
- It includes multiple challenges:
 - Map building and localization;
 - Determination of the navigational waypoints;
- Path planning and navigation to the waypoints;
- Coordination of the actions (multi-robot team).

Courtesy of M. Kulich

Informative Motion Planning

 Robotic information gathering can be considered as the informative path planning problem to a determine trajectory \mathcal{P}^* such that

 $\mathcal{P}^* = \operatorname{argmax}_{\mathcal{P} \in \Psi} I(\mathcal{P})$, such that $c(\mathcal{P}) \leq B$, where

- Ψ is the space of all possible robot trajectories,
- $I(\mathcal{P})$ is the information gathered along the trajectory \mathcal{P} ,
- c(P) is the cost of P and B is the allowed budget.
- Searching the space of all possible trajectories is complex and demanding problem.
- A discretized problem can be solved by combinatorial optimization techniques. Usually scale poorly with the size of the problem
- A trajectory is from a continuous domain.
- Sampling-based path/motion planning techniques can be employed for finding maximally informative trajectories.

Hollinger, G., Sukhatme, G. (2014): Sampling-based robotic information gathering algorithms. IJRR.



How to navigate robots to the selected locations?

To improve the phenomena model.

On-line decision-making.

Learning adaptivity

Robotic Information Gathering

Planning uncertainty

To divide the task between the robots/

Improve Localization vs Model.

Persistent environment monitoring is an example of the

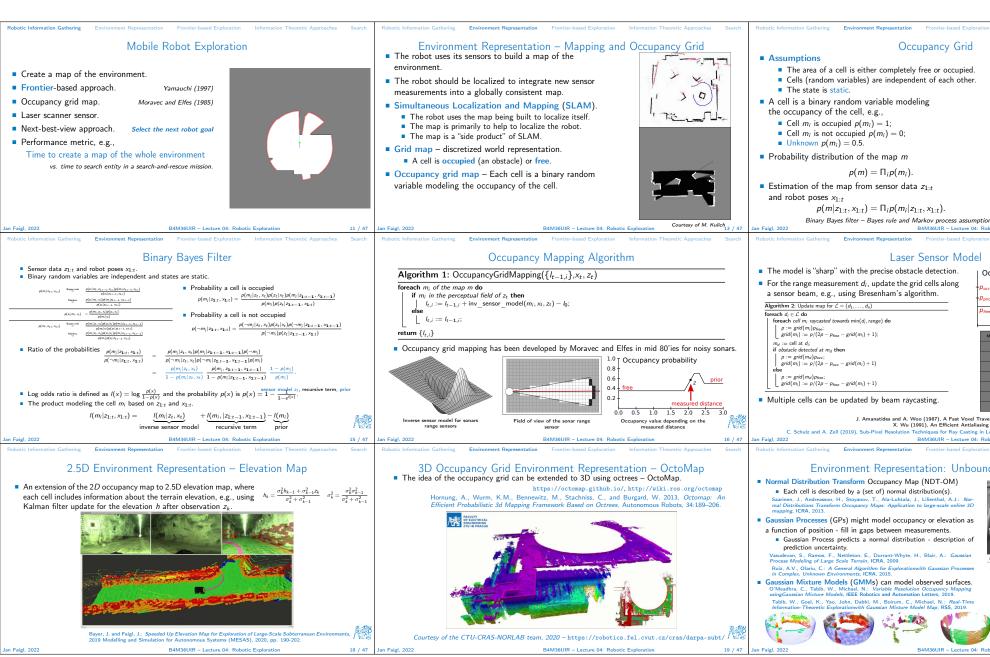
It stands to determine suitable locations to collect data

Determine a cost-efficient path to visit the locations, e.g.,

Collect data and update the phenomenon model.

Search for the next locations to improve the model.

Solutions have to respect, e.g., kinematic and kinodynamic constraints, collision-free paths.



Occupancy Grid

- Cells (random variables) are independent of each other.

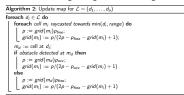
$$p(m|z_{1:t}, x_{1:t}) = \prod_i p(m_i|z_{1:t}, x_{1:t}).$$

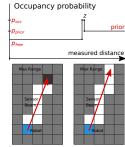
free space

occupied space

Laser Sensor Model

- a sensor beam, e.g., using Bresenham's algorithm.





J. Amanatides and A. Woo (1987), A Fast Voxel Traversal Algorithm for Ray Tracing, Eurographics.

X. Wu (1991), An Efficient Antialiasing Technique, SIGGRAPH Computer Graphics.

Techniques for Ray Casting in Low-Resolution Occupancy Grid Mans. ECMF

Environment Representation: Unbound by Resolution

Gaussian Processes (GPs) might model occupancy or elevation as

a function of position - fill in gaps between measurements.

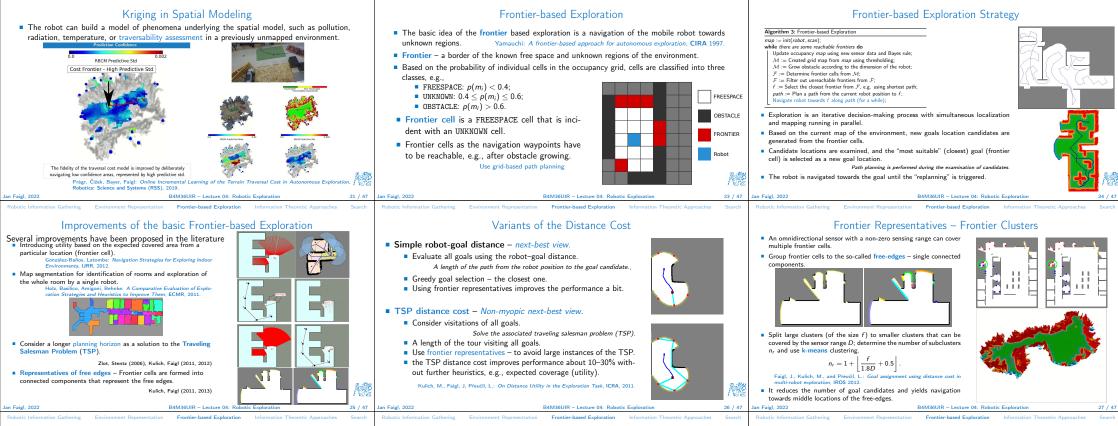
· Gaussian Process predicts a normal distribution - description of











Multi-robot Exploration

- Multi-robot exploration is a problem to efficiently utilize a group of (mobile) robots to autonomously create a model of a priory unknown environment.
- Uncoordinated approach Each robot independently explores the environment, e.g., by following the closest frontier.
- Centralized approaches a central authority assigns the goals, and the goal assignment can be viewed as the task allocation problem.
 - Various strategies have been proposed, such as greedy assignment, Hungarian assignment, and multiple traveling salesman problem assignments.

Considering communication between the exploring units, we can further establish distributed task allocation.

■ Decentralized approaches – Each robot selects its own goal and solves the task allocation based on its (limited) information about other robots.

Existing communication between the exploring units can improve the performance but it is generally not mandatory for "true" decentralized approaches.

7. Perform each plan up to smax operations 8. If |G| == 0 exploration finished, otherwise go to Step 2.

1. Initialize the occupancy grid Occ.

4. Goal candidates G ← generate(F)

5. Assign next goals to each robot $r \in R$.

6. Create a plan P_i for each pair $\langle r_i, g_{r_i} \rangle$.

F ← detect frontiers(M).

2. $\mathcal{M} \leftarrow \mathsf{create}_\mathsf{navigation}_\mathsf{grid}(\mathit{Occ})$.

Multi-robot exploration as an iterative procedure.

 $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(R, G, M).$

At each step, update Occ using new sensor mea

■ We need to assign navigation waypoint to each robot that can be formulated as the task-allocation problem cells of M have values {freespace, obstacle, unknown}

- Several parts of the exploration procedure are important regarding decisionmaking and achieved performance.
 - How to determine goal candidates from the the frontiers?
 - How to plan a paths and assign the goals to the robots?
 - How to navigate the robots towards
- the goal?
- When to replan?

$\mathcal{P} = \mathsf{plan}(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle, \mathcal{M});$ Go to Step 2.

2. Repeat

5. Stop all robots or navigate them to the depot. All reachable parts of the environment are explored.

2.1 Navigate robots using the plans \mathcal{P} :

Until replanning condition is met.

3. Determine goal candidates G from M.

• $(\langle r_1, g_{r_1} \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\mathbf{R}, \mathbf{G}, \mathcal{M}),$

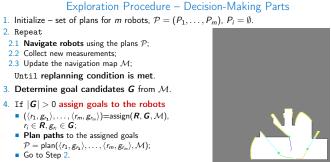
4. If $|\mathbf{G}| > 0$ assign goals to the robots

■ Plan paths to the assigned goals

2.2 Collect new measurements:

 $r_i \in \mathbf{R}, g_r \in \mathbf{G};$

2.3 Update the navigation map M;



Determination of goal locations and path (cost)

Multi-robot Exploration – Overview of Centralized Strategy

■ m-TSP heuristic ⟨cluster-first, route-second⟩

 $\boldsymbol{C} = \{C_1, \ldots, C_m\}, C_i \subseteq \boldsymbol{G}.$

2. For each robot $r_i \in \mathbf{R}, i \in \{1, \dots m\}$ select the next goal g_i from C_i using the TSP

Faigl, J., Kulich, M., Přeučil, L.: Goal Assignment using Distance Cost in Multi-Robot Exploration, IROS 2012.

Influence of Decision-Making - Exploration Strategy

MTSP-based Task-Allocation Approach

Task-allocation problem as the Multiple Traveling Salesman Problem (MTSP).

function depends only on the map.

lecting new measurements).

Performance of the MTSP vs Hungarian Algorithm

Goal Assignment Strategies - Task Allocation Algorithms

■ Exploration strategy can be formulated as the task-allocation problem

$$(\langle r_1, g_r \rangle, \dots, \langle r_m, g_{r_m} \rangle) = \operatorname{assign}(\boldsymbol{R}, \boldsymbol{G}(t), \mathcal{M}),$$

where \mathcal{M} is the current map.

1. Greedy Assignment

Randomized greedy selection of the closest goal candidate.

Yamauchi B., Robotics and Autonomous Systems 29, 1999.

2. Iterative Assignment

• Centralized variant of the broadcast of local eligibility algorithm (BLE).

Werger, B., Mataric, M., Distributed Autonomous Robotic Systems 4, 2001

3. Hungarian Assignment

 \blacksquare Optimal solution of the task-allocation problem for assignment of n goals and m robots in $O(n^3)$. For n < m: use Iterative assignment or dummy tasks; For n > m: add dummy robots with costly assignments.

Stachniss, C., C implementation of the Hungarian method, 2004

4. Multiple Traveling Salesman Problem - MTSP Assignment

Faigl, et al. 2012

The exploration performance depends on the whole solution, albeit

Locally optimal Hungarian algorithm might not necessarily provide

A solution of the particular sub-task (i.e., goal candidate selec-

tion) might have side effects that are exhibited during the missions

■ Vector Field Histogram (VFH) slows down the robot close to

navigated towards them, which results in faster motion because

better solutions than for example the MTSP-based approach.

we can have "best" possible solutions of each part.

- depending on the utilized navigation technique.

it is relatively far from the obstacles.

the obstacles.

1. Cluster the goal candidates G to m clusters (using k-means)

■ Solve the TSP on the set $C_i \cup \{r_i\}$ – the tour starts at r_i . The next robot goal g_i is the first goal of the found TSP tour.

Kulich et al., ICRA (2011)

Information Theory in Robotic Information Gathering

We can avoid such assumption by defining the control policy as a rule how to select the robot

 $\operatorname{argmax}_{a \in A} I_{MI}[x; z|a],$

 $I_{MI}[x;z] = H[x] - H[x|z],$

Example of Autonomous Exploration using CSQMI

where A is a set of possible actions, x is a future estimate, and z is future measurement

action that reduces the uncertainty of estimate by learning measurements:

■ Mutual information – how much uncertainty of x will be reduced by learning z

where H[x] is the current entropy, and H[x|z] is future/predicted entropy.

■ Entropy – uncertainty of x: $H[x] = -\int p(x) \log p(x) dx$.

Replanning as quickly as possible; m = 3, $\rho = 3$ m - The MTSP assignment p

(cluster-first, route-second), the TSP distance cost.

MinPos: Decentralized Exporation Strategy

The robot solves the task allocation based on its (limited) information about other robots.

- **Assumption**: the distance cost matrix C between robots \mathcal{R} and frontiers \mathcal{F} are known to all
- robots In practice, it requires the robots to share the map of the whole environment, which might not be feasible, and therefore, approximations can be employed.
- Each robot ranks each frontier using the relative distance of the robots to the frontier cell (goal candidate).
- The robot is assigned the goal with the minimum rank.



size of the action set and the uncertainty of action results.

where R(a) represents the region sensed by the action a.

We can assume that observation removes all uncertainty from observed areas

selected to maximize the entropy over the sensed regions in the current map.

Gready assignment of goal candidates (frontiers onin O. Charnillet F : MinPos: A Novel Fro Faigl. J., Simonin, O., Charpillet, F.: Comparison of Task-Allocation Algorithms in Fr. me FIIMAS 2014

Computing Mutual Information in Exploration

Sensor placement approach with raycasting of the sensor beam and determination of the dis-

Precise computing of the mutual information is usually not computationally feasible given the

 $I_{MI}[x;z] = H[x] - H[x|z] \approx H[x].$ ■ Then, we can decrease the computational requirements by using simplified approach where the action is

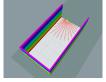
We are maximizing mutual information in the sensor placement problem of observing the region with

 $\operatorname{argmax}_{a \in A} \sum H[p(x)]$

tribution over the range returns.

maximum entropy









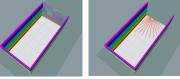
DIES. Borenstein, J. and Koren, Y.: The vector field histogram-fast obstacle avoidance for mobile robots, IEEE Transactions on Robotics, 1991. A side effect of the representatives of free edges is that goal candidates are "in the middle of free-edges" and the robot is



sightsissall related to simplifications we made to solve the challenging autonomous exploration

Actions

Actions are shortest paths to cover the frontiers





Select an action (a path) that maximizes the rate of Cauchy-Schwarz Quadratic Mutual Information.



Planning with trajectory optimization – determine trajectory maximizing I_{CS}.

Ground vehicle

Charrow, B., Kahn, G., Patil, S., Liu, S., Goldberg, K., Abbeel, P., Michael, N., Kumar, V.: Information

Mapping. Robotics: Science and Systems (RSS), 2015





















 Computational cost can be decreased using Cauchy-Schwarz Quadratic Mutual Information (CSQMI) defined similarly to mutual information. Can be evaluated analytically for occupancy grid mapping.

Aerial vehicle

■ Gaussian Process Upper Confidence Bound

Mutual Information in Kriging

- The GP regressors provide an inbuilt representation of uncertainty their prediction is a normal distribution.
 - The differential entropy of a normal distribution is

$$H(\mathcal{N}(\mu, \sigma^2)) = \frac{1}{2} \log(2\pi e \sigma^2),$$

Search in Unknown Environments

In search-and-rescue missions, the performance indicator is the time to find the objects and report their position. • The map is used for navigation, localization of artifacts, and decision-making where to search

A variant of exploration is a search to find objects of interest in an unknown environment

i.e., it is a function of its variance σ^2 .

- We can employ greedy approach sample at the highest prediction variance.
- Example: Building communication maps
- A pairwise problem select locations of two robots to sample the communication signal strength.

Quattrini Li, A., Penumarthi, P.K., Banfi, J., Basilico, N., O'Kane, J.M., Rekleitis, I., Nelakuditi, S., Amigoni, F.: Multi-robot online sensing strategies for the construction of communication maps, Autonomous Robots 44:299—319, 2020.





Wenhao, L., Sycara, K.: Adaptive S of Gaussian Processes, ICRA, 2018.

 $x_t = \operatorname{argmax}_{x \in D} \mu_{t-1}(x) + \beta_t^{\frac{1}{2}} \sigma_{t-1}(x).$

Search in Kriging Scenarios

In exploration scenarios, where we search for some phenomenon, such as searching for

a source of radiation or heat, we search for the modeled function's extrema.

The search strategy needs to balance exploitation and exploration.

It addresses the search as a multi-armed bandit problem.

• The GP-UCB policy to chose the next sampling point x_t is

Exploration of the current model vs. exploration of unknown parts of the environment.

Summary of the Lecture

Exploration with Position Uncertainty

- A reliable localization is needed to map the environment reliably; thus, we might need to consider both the occupancy and localization mutual information:
 - $I = \gamma I_{occupancy} + (1 \gamma) I_{localization}.$ The localization uncertainty can be based on the entropy

$$\frac{1}{2} \log [(2\pi e)^n det P]$$

where P is the covariance of location of the robot and localization landmarks.

- Summing Shannon's entropy of the map and the differential entropy of the pose leads to scaling issues.
 The explorer may stricly prefer to improve either its map or localization that can achieved by adjusting γ.
 - We can use the notion of Rényi's entropy

's entropy
$$H_{lpha}\left[P(x)
ight] = rac{1}{1-lpha}\log_2(\sum p_i^{lpha})$$

where for $\alpha \to 1$ its becomes Shannon's entropy.

The utility function of taking an action a is the difference

$$\operatorname{argmax}_{a} \sum_{x \in R(a)} H^{\operatorname{Shannon}} \left[P(x) \right] - H_{1 + \frac{1}{\delta(a)}}^{\operatorname{R\acute{e}nyi}} \left[P(x) \right]$$

where $\delta(a)$ is related to predicted position uncertainty given the action a Carrillo, H., Dames, P., Kumar, V., Castellanos, J.A.: Autonomous rob based on Renyi's general theory of entropy, Autonomous Robots, 2018

Topics Discussed

Topics Discussed

- Robotic information gathering informative path planning
- Robotic exploration of unknown environment
 - Occupancy grid map
 - Frontier based exploration
 - Exploration procedure and decision-making
 - TSP-based distance cost in frontier-based exploration
 - Multi-robot exploration and task-allocation
- Mutual information and informative path planning

Motivation for the semestral project





■ Next: Multi-goal planning



