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KATEDRA POČÍTAČOVÉ GRAFIKY A INTERAKCE

APG – Filling Algorithms

JIŘÍ ŽÁRA

Filling areas

- Outline (border)

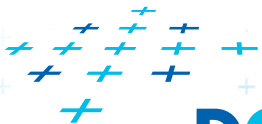
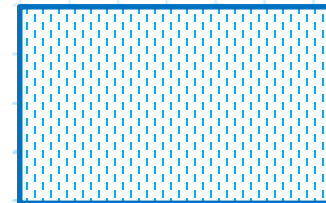
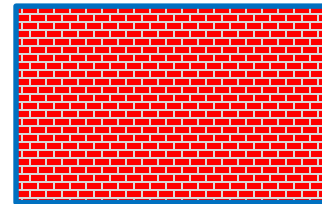
What to fill?

1. Defined by **geometry** (polyline)
2. Already stored in a **raster** (image memory)

- Filling

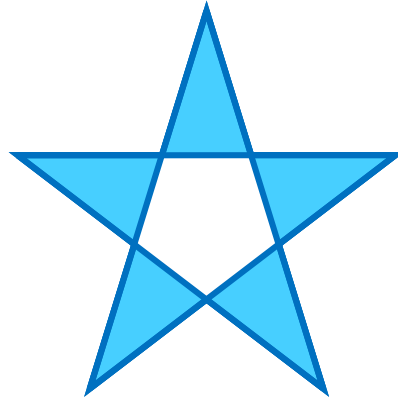
How to fill?

- Solid fill (color)
- Pattern fill (color array)
- Hatching (dashed **lines**)

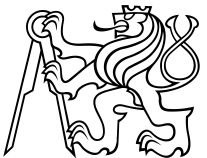
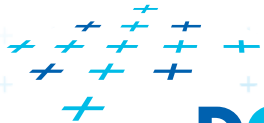
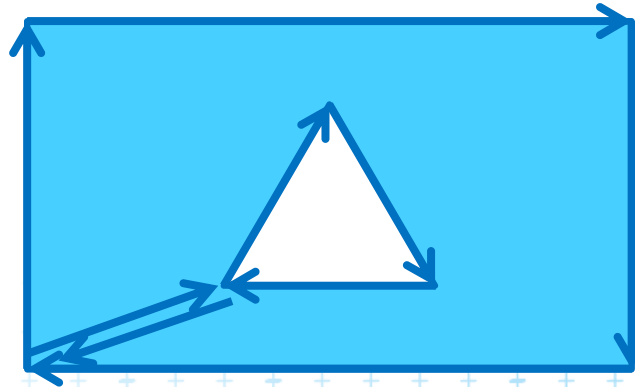


Complex borders

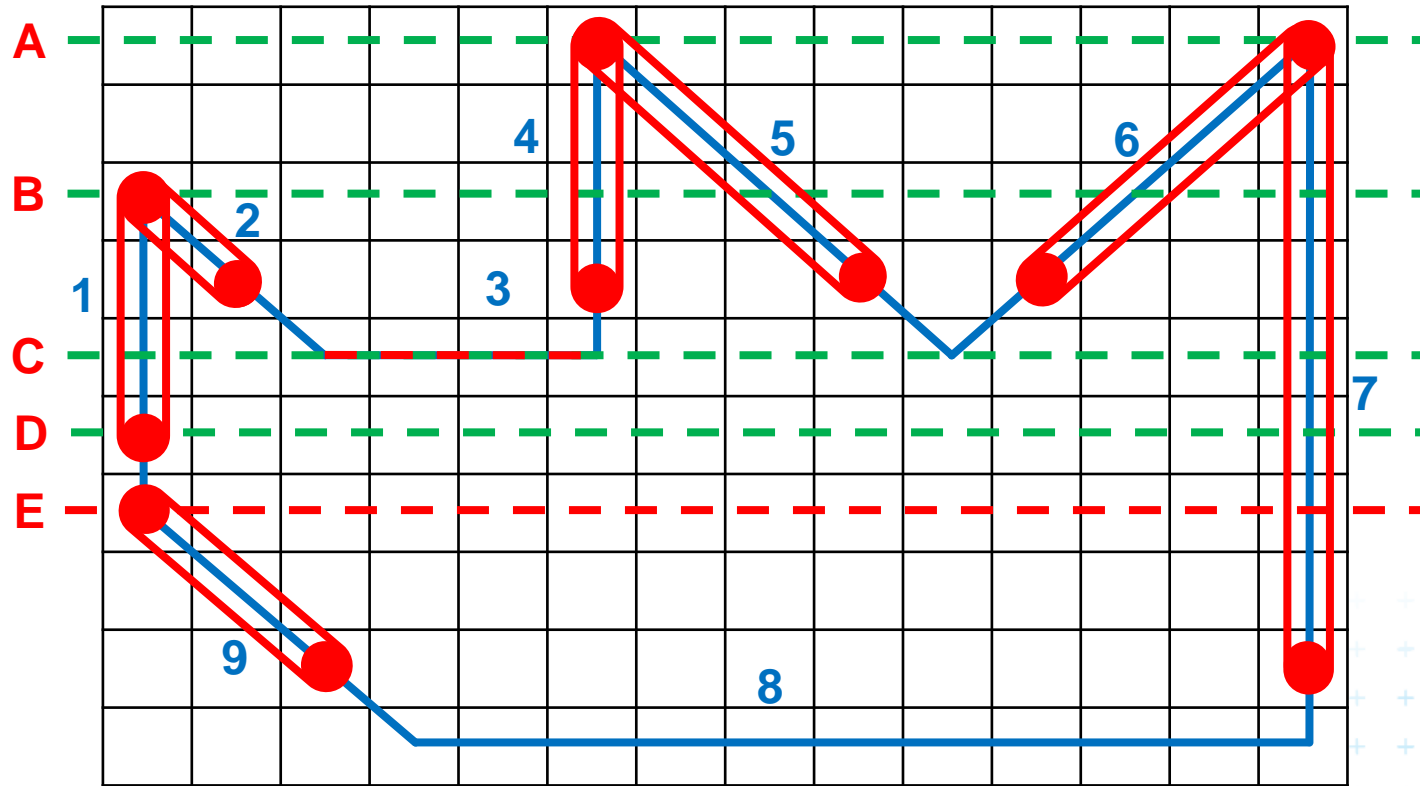
- Self crossing



- Multiple



1. Scan line filling algorithm



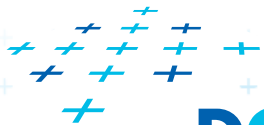
A: 4-5, 6-7

B: 1-2, 4-5, 6-7

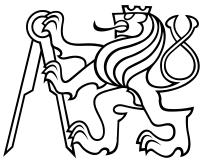
C: 1-2, 3, 4-5, 6-7

D: 1-7

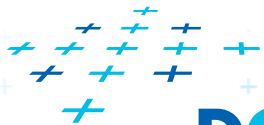
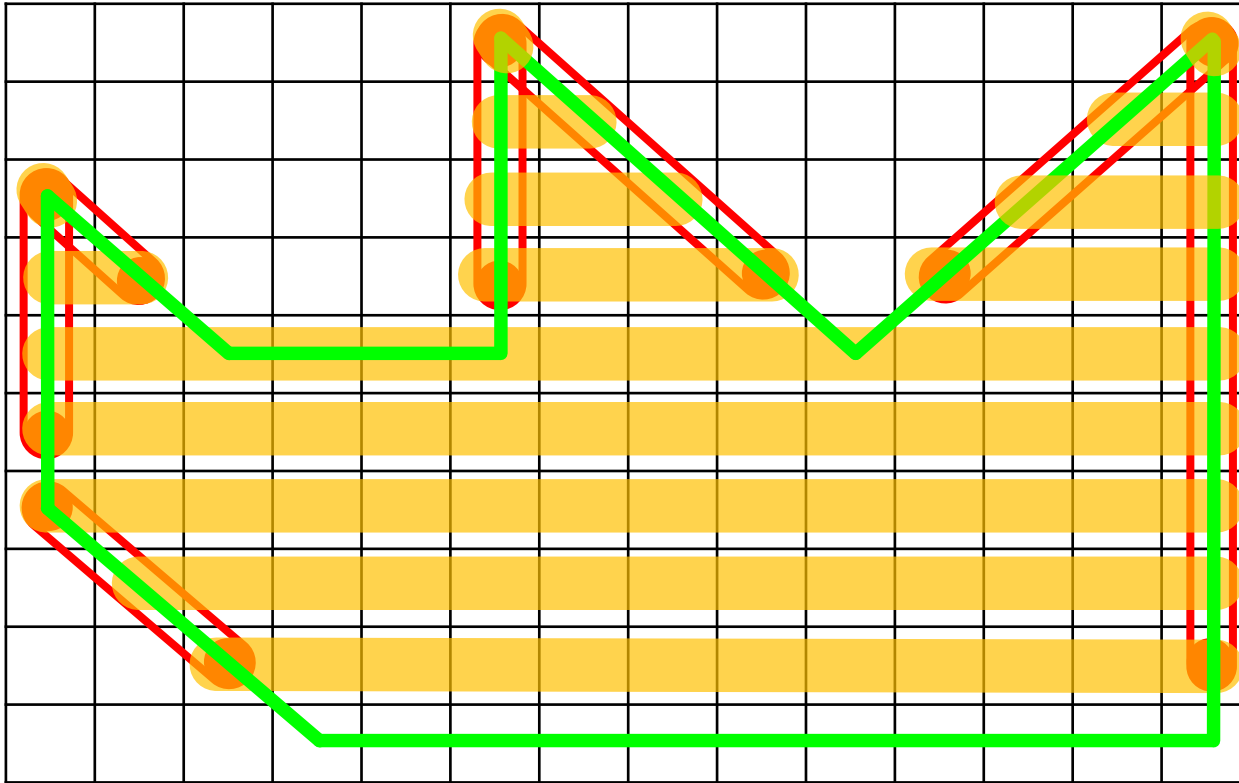
E: 1-9, 7?



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Scan line filling algorithm (cont.)



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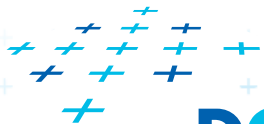
Scan line filling algorithm (cont.)

- Top-down orientation
 - Remove horiz. edges
 - Edge shortening
 - Finding Y_{MAX} , Y_{MIN}
- Initial phase

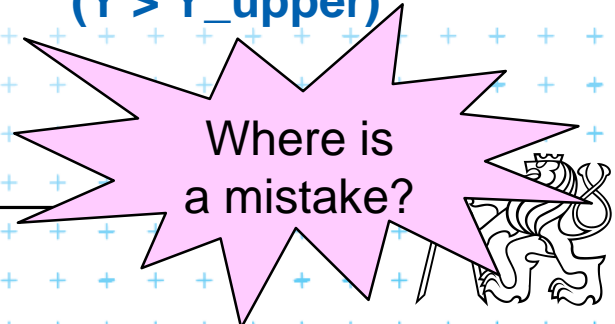
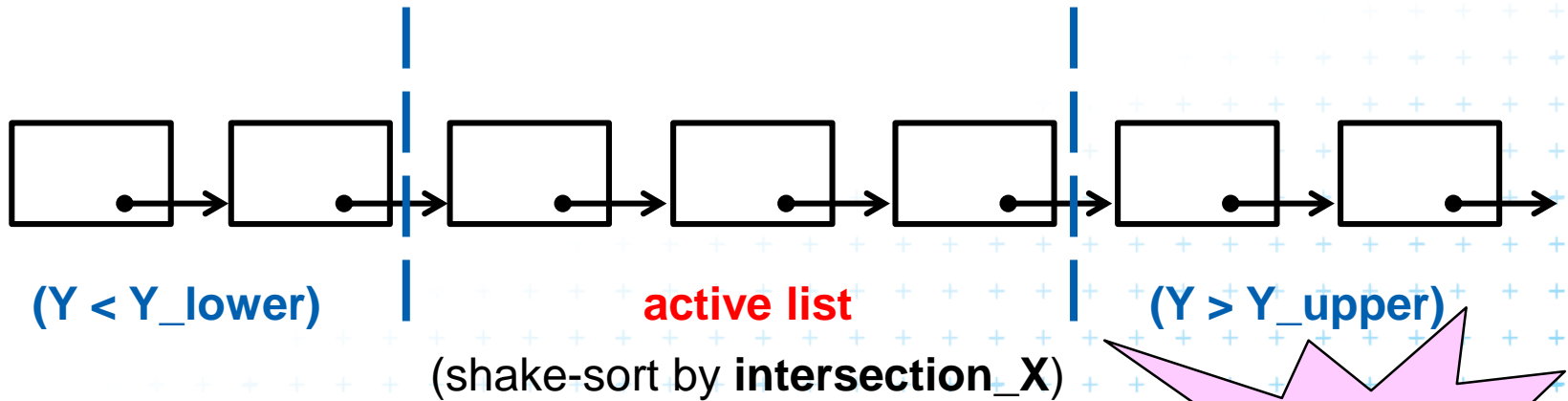
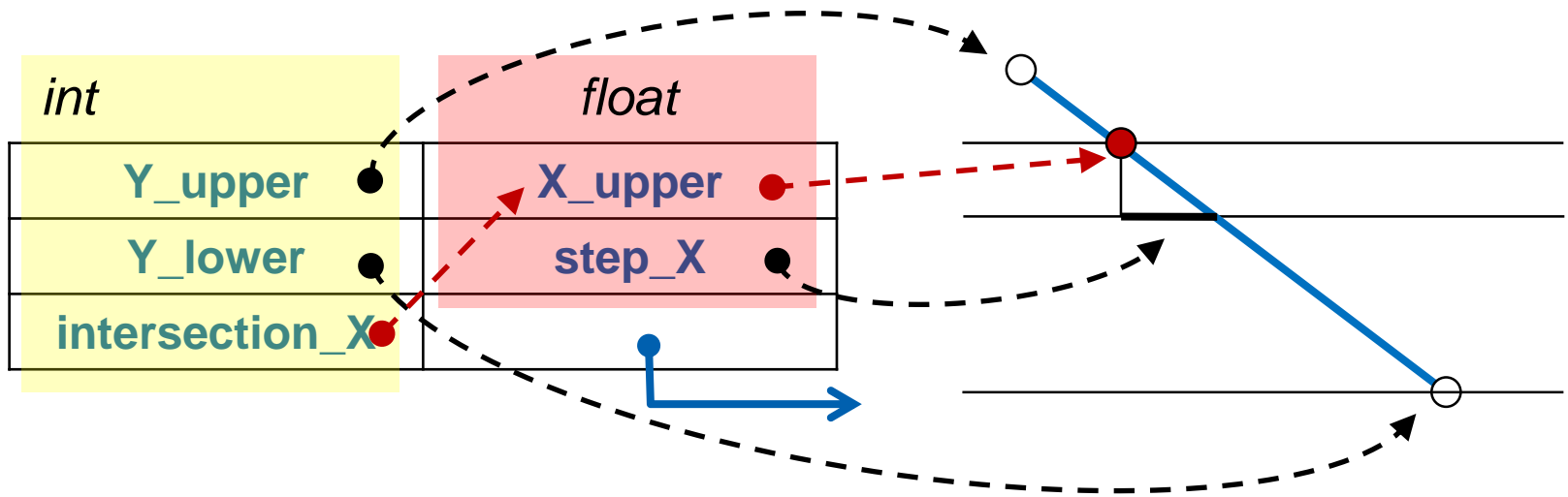
```
for (int i =  $Y_{MAX}$ ; i >=  $Y_{MIN}$ ; i--) {
```

- Find intersections: scan-line Y + edges // topology
- Line up intersections by X coordinate // sorting
- Draw/fill horizontal segments

```
}
```



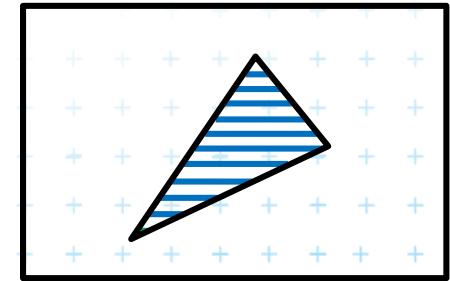
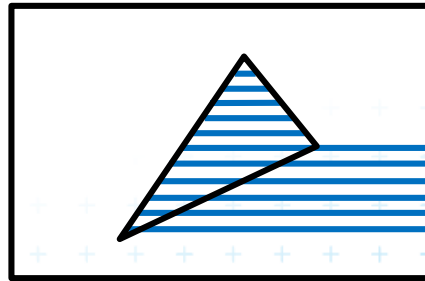
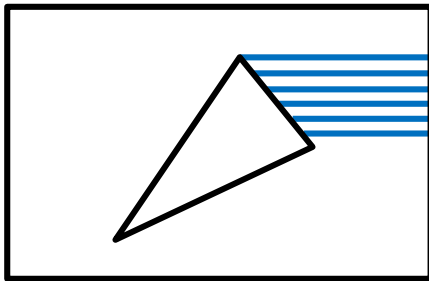
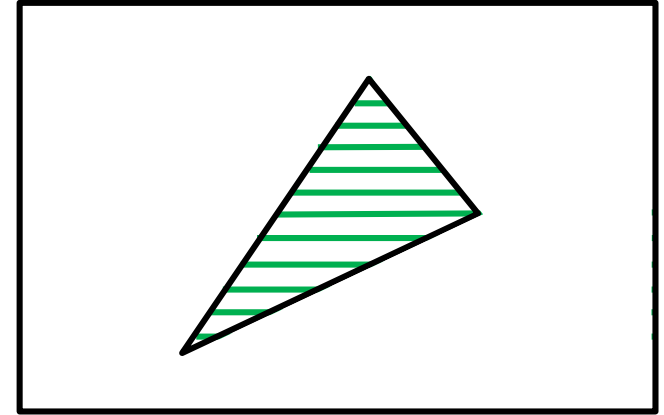
Data structure: Edge



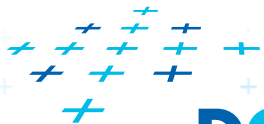
Inverse filling (using XOR logical function)

No sorting! 😊

1. Edge shortening (as before)
2. For each edge:
 - Digitizing/Sampling by $\Delta y = 1$
 - **XOR_LINE** to X_{\max}



Filled area does not cover previously drawn objects...



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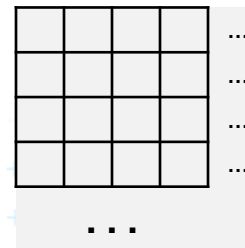


Using stencil buffer

- To improve previous method
- Put values to additional data structure (i.e. stencil buffer) first, then convert/interpret them into image memory.

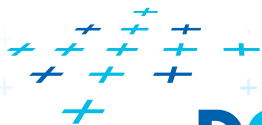
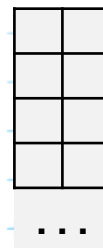
a) Non convex areas

- One-bit buffer (for XOR operation results)



b) Convex areas

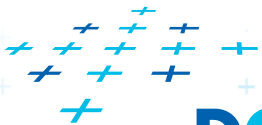
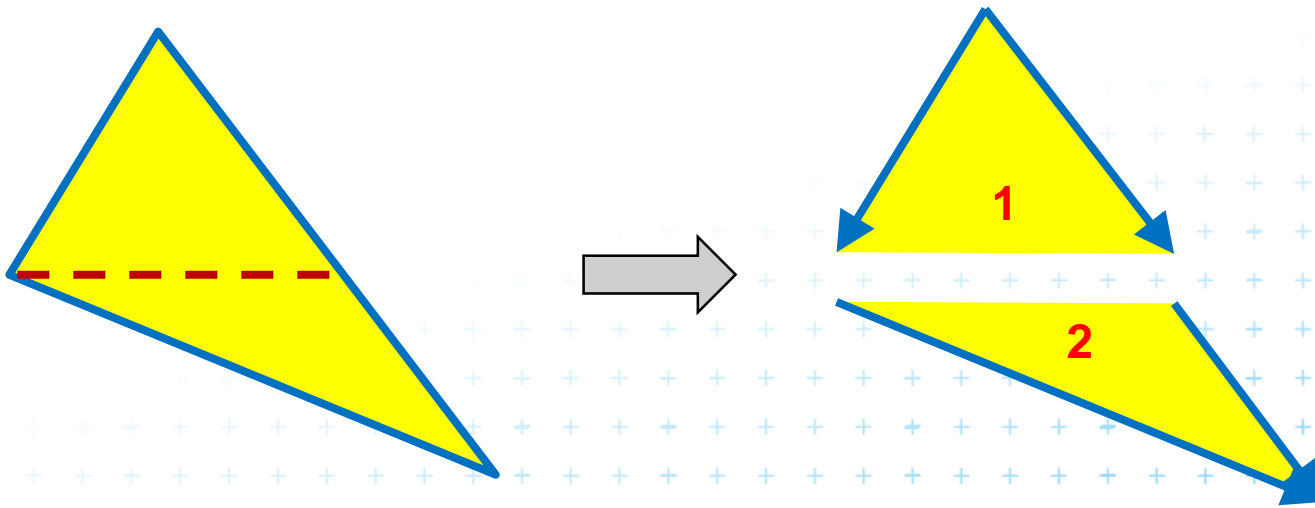
- Array of integer pairs $[X_L, X_R]$ only (initialized by -1 values)



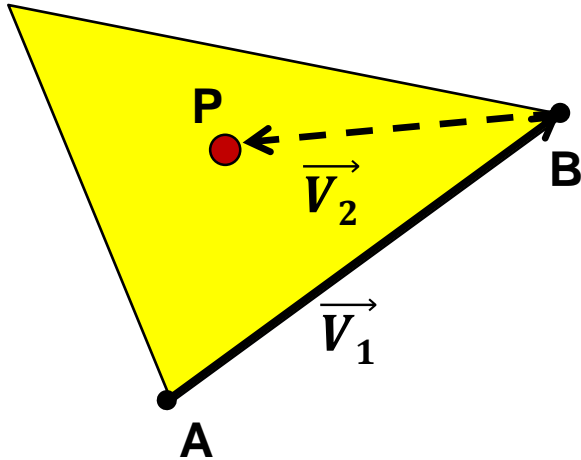
Filled triangle

The most often processed object in 3D graphics

- High speed processing required
- Always convex object 😊
- Decompose it to 2 areas limited by edge pairs
➡ no sorting (preprocessing only)



Juan Pineda: Filling triangle



$$\begin{aligned} &\overrightarrow{(x_1, y_1, z_1)} \times \overrightarrow{(x_2, y_2, z_2)} \\ &= \text{perpendicular vector} \\ &\text{(in 3D)} \end{aligned}$$

$$z_3 = x_1 \cdot y_2 - x_2 \cdot y_1$$

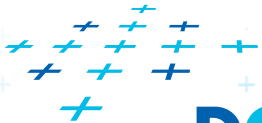
Positive z \longrightarrow P is on the left from $\overrightarrow{V_1}$

Edge function $E(x_P, y_P)$:

$$E(x_P, y_P) = \Delta x \cdot (y_P - y_B) - \Delta y \cdot (x_P - x_B)$$

\vdots

$$E(x_P + 1, y_P) = E(x_P, y_P) - \Delta y$$



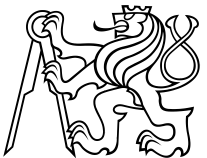
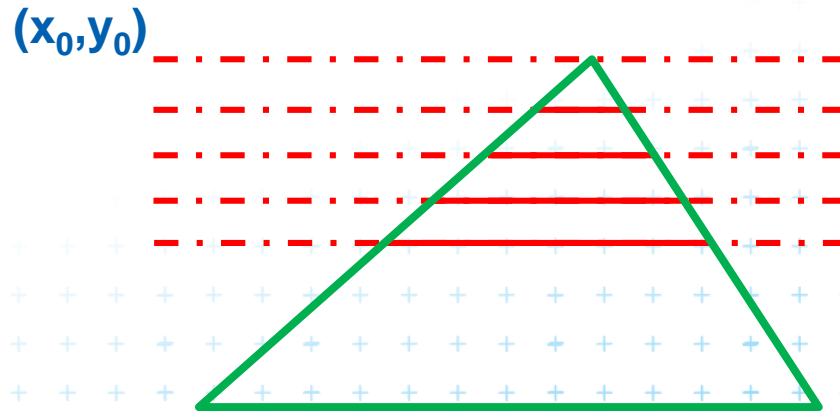
Juan Pineda: Algorithm

1) Initialization:

- Compute $E_i(x_0, y_0)$ for each edge i

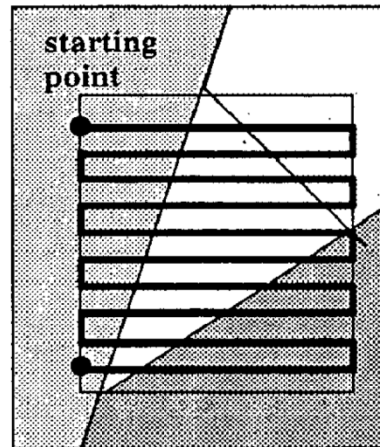
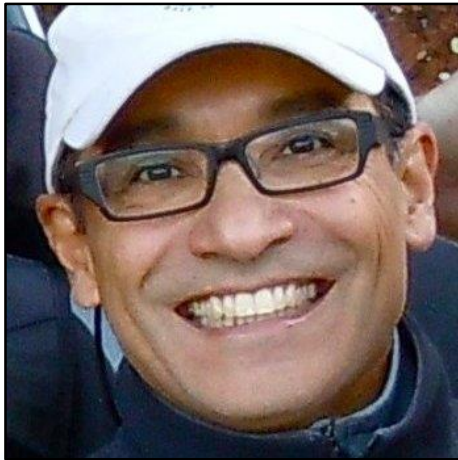
2) Systematically evaluate bounding rectangle:

- For each pixel
 - Update all three E_i (incrementally)
 - Pixel is inner, when $\forall E_i > 0$

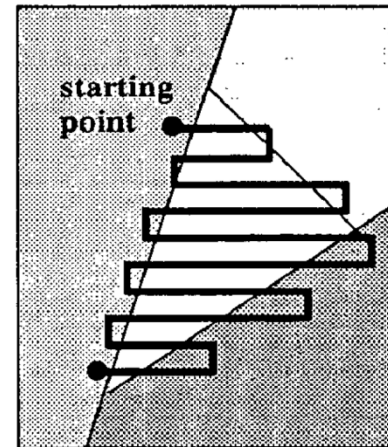


Juan Pineda

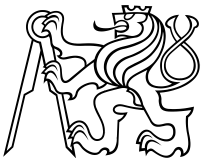
- Bc. at MIT 1978 (physics)
- Ms. at Brandeis Univ. 1982
- „*A Parallel Algorithm for Polygon Rasterization*“
- SIGGRAPH 1988, 4 pages
- Apollo Computer



Traversing the Bounding Box

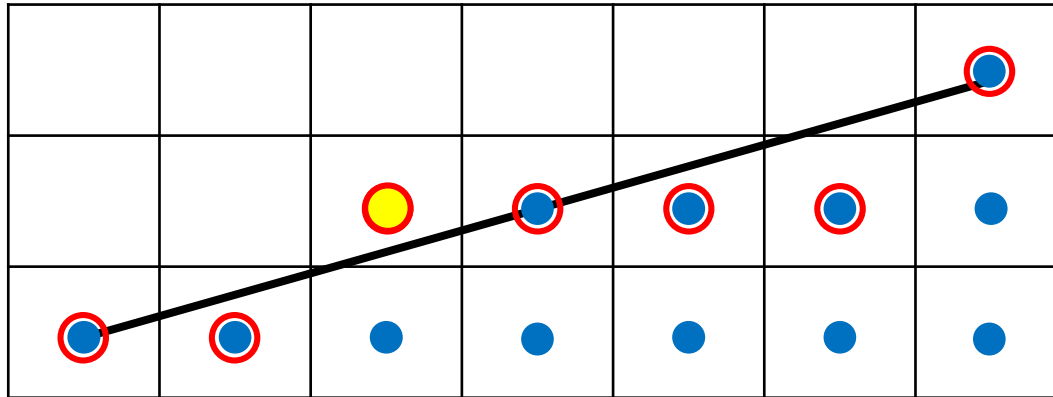


A More Efficient Traversal Algorithm



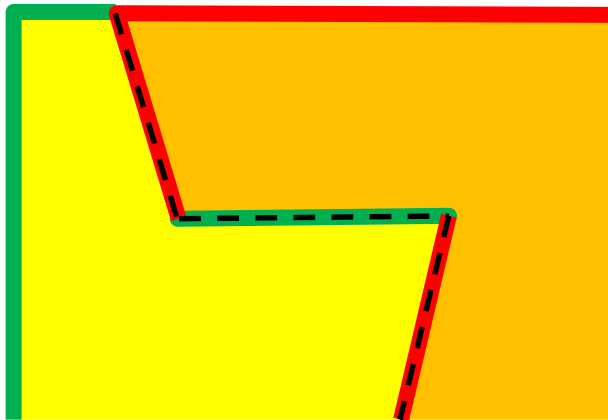
Border issues

- Are border edges covered by filling pixels?

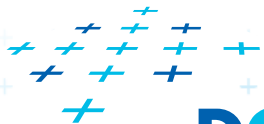


- Why?
- When?

- Who is the owner of border?



- Left and upper border belongs to filled area (see slide Nr. 5)
- Minimizes re-drawing
- Order independent



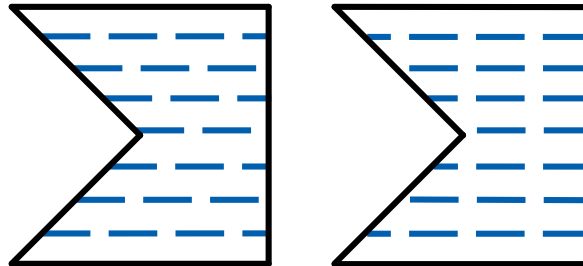
Hatching - using lines

1) Slashed lines

- Rotate border edges (outline) by α
- Find horizontal lines (scan-line algorithm)
- Rotate horizontal line segments back by $-\alpha$

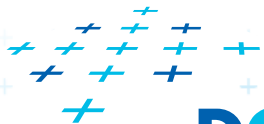
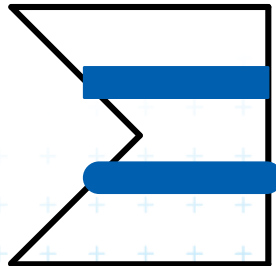


2) Dashed lines

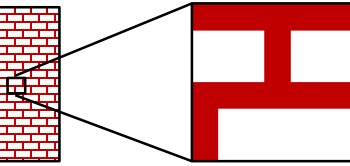
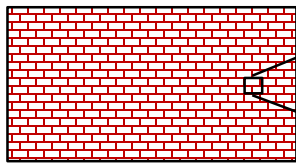


Beginning of dashed lines?
(carpet VERSUS window)

3) Thick lines



Hatching – using patterns



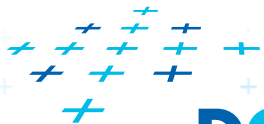
Pattern
6x6 pixels

Color **pattern** [dimensionX] [dimensionY];

...

PutPixel (X, Y, **pattern** [X **mod** dimensionX]
[Y **mod** dimensionY]);

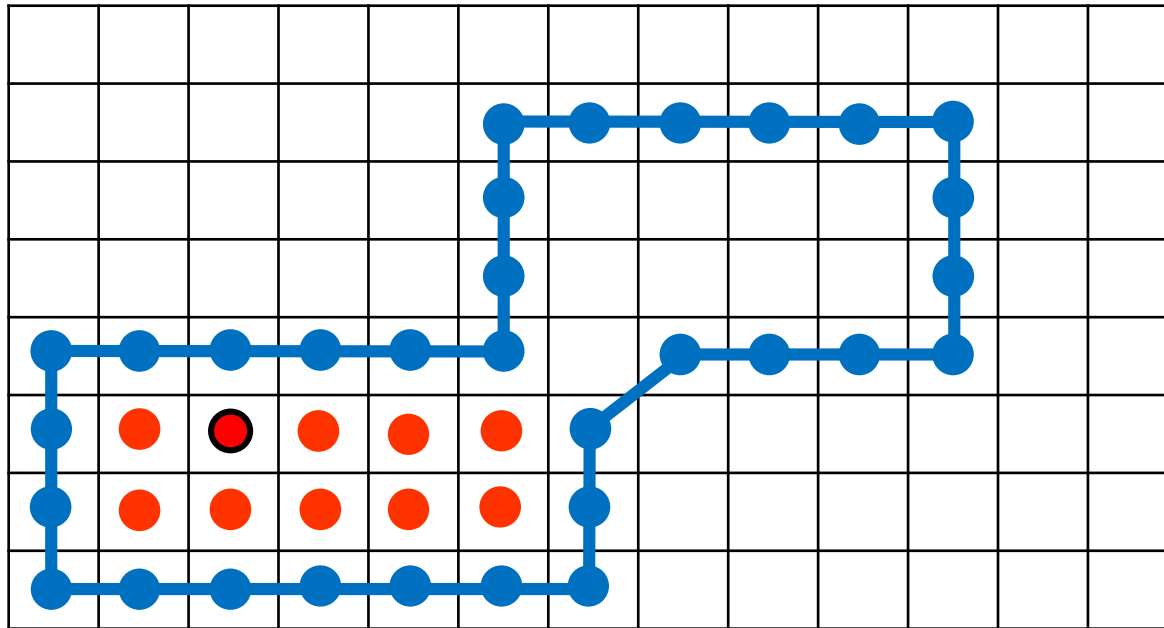
...



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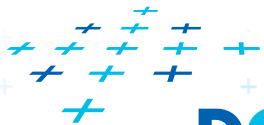
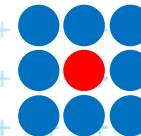
2. Filling raster area (in image memory)



4-connected
neighborhood



8-connected
neighborhood



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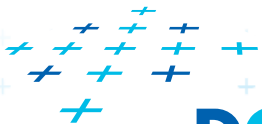


Seed-fill algorithm

```
void seed (int x, int y) {  
    PutPixel (x, y, Fill_Color);  
    if (Get_Pixel (x+1, y) != Border_Color &&  
        Get_Pixel (x+1, y) != Fill_Color) {  
        seed (x+1, y);  
    }  
    if ... (x-1, y) ...  
    if ... (x, y+1) ...  
    if ... (x, y-1) ...  
}
```

Params: Border_Color, Fill_Color, Seed coordinates

of recursion calls ~ # of inner pixels!



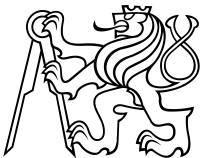
Scan-line seed-fill algorithm

Push (X, Y) into stack;

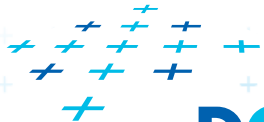
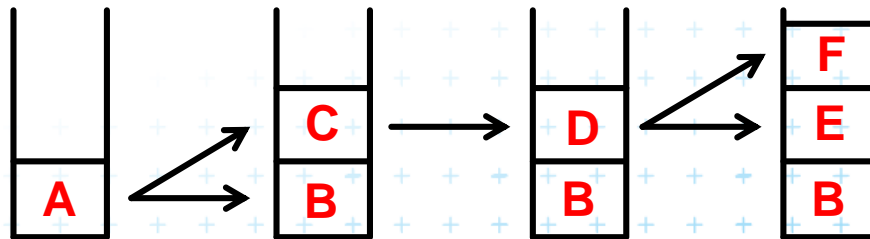
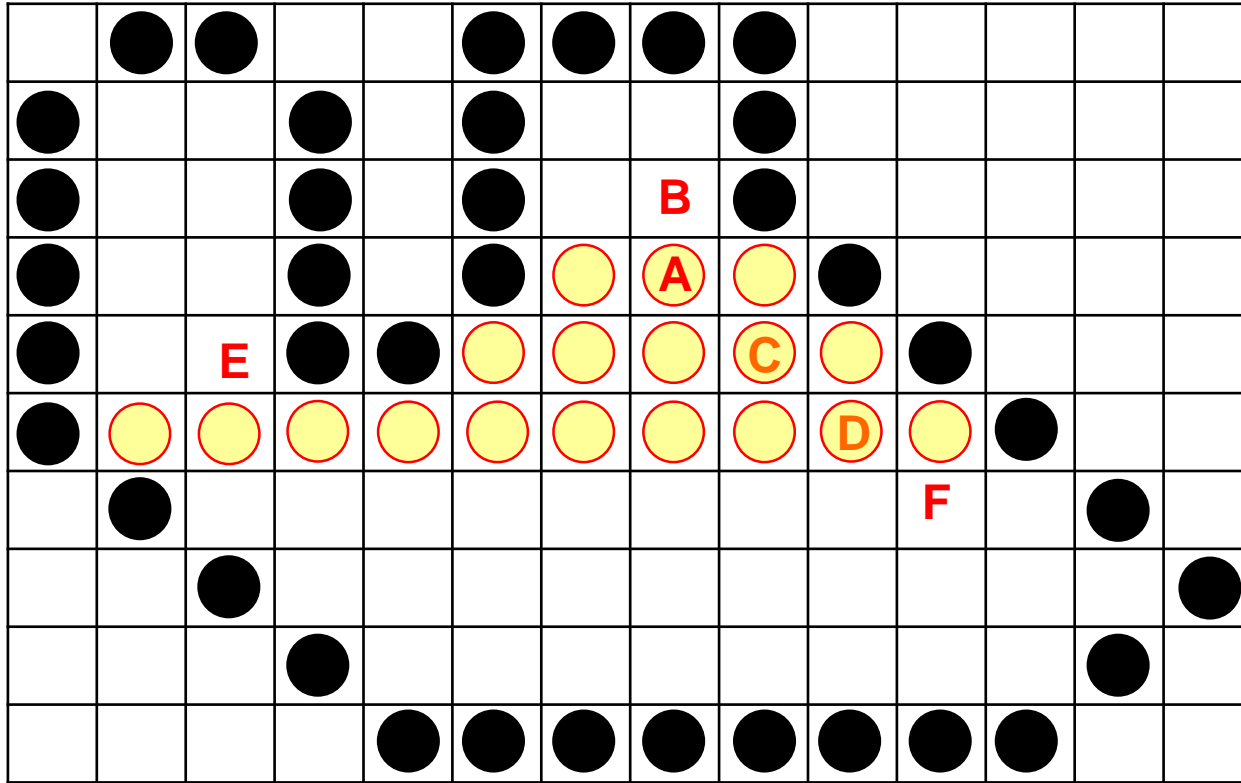
do {

- Pop a **seed** from stack;
- Find left and right border and fill this **horizontal line** segment;
- Analyze pixels **above** this line. For each free segment – push one seed into stack;
- Analyze pixels **below** this line. For each free segment – push one seed into stack;

} while (!stack.empty());



Scan-line seed-fill



Thank you for your attention

Jiří Žára, 28.01.2021

