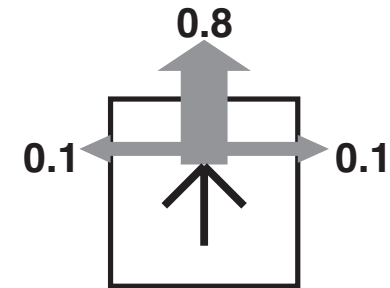
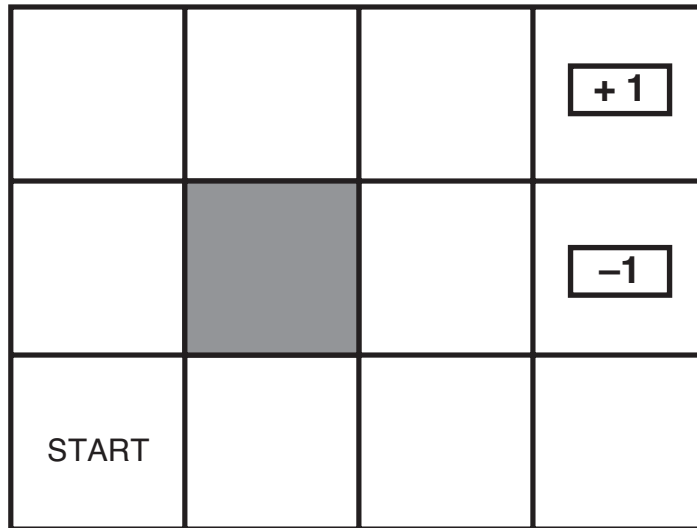


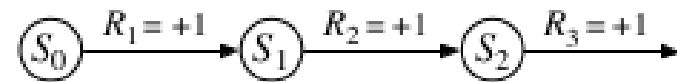
MDP Introduction

F. Gama



We have:

- State: S
- Action: A
- Transition model: $T(s, a, s') \equiv P(s, a, s')$, we are in state s , make action a , and arrive in state s'
- Reward: $r(s), r(s, a), r(s, a, s')$ immediate reward/evaluation
- Policy: agent/robot behaviour strategy
- Episode: sequence of states with rewards
- Return/Utility sequence: $G_t = \sum_{k=0}^{\infty} \gamma^k R_{t+k+1}$



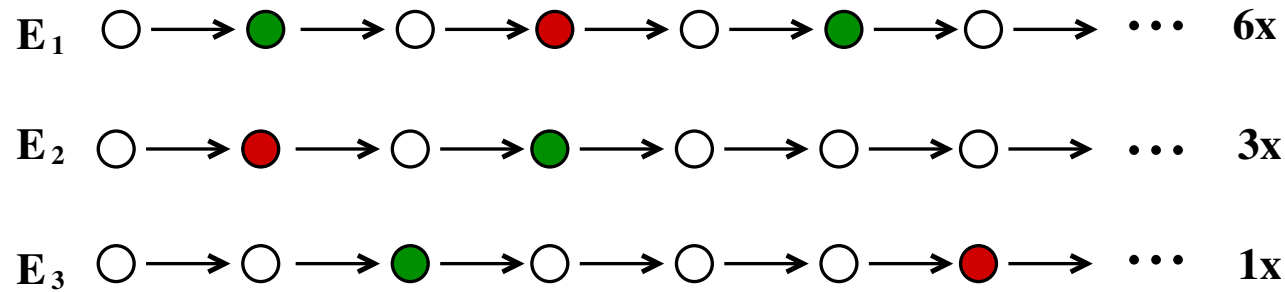
Policy Evaluation: How good is the strategy?

E₁ ○ → ● → ○ → ● → ○ → ● → ○ → ... **6x**

E₂ ○ → ● → ○ → ● → ○ → ○ → ○ → ... **3x**

E₃ ○ → ○ → ● → ○ → ○ → ○ → ○ → ● → ... **1x**

Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence:

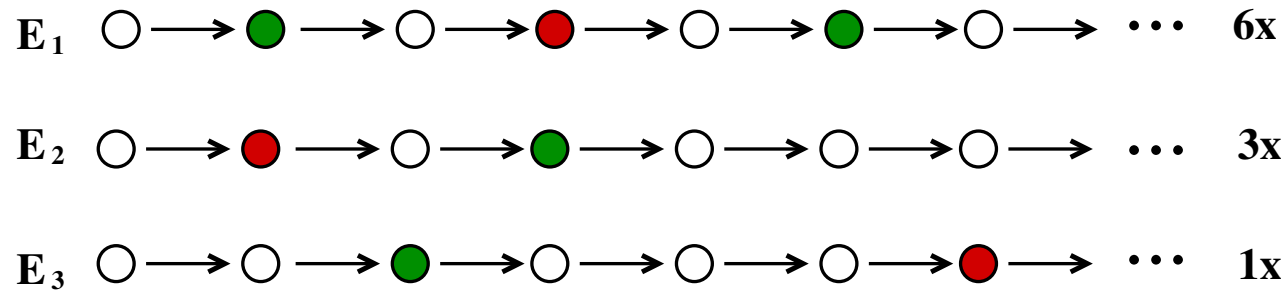
A: State Value $V(s)$

B: Immediate reward $r(s)$

C: Return/Utility G

D: Policy π

Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$

○ 0 ● 1 ● -0.3

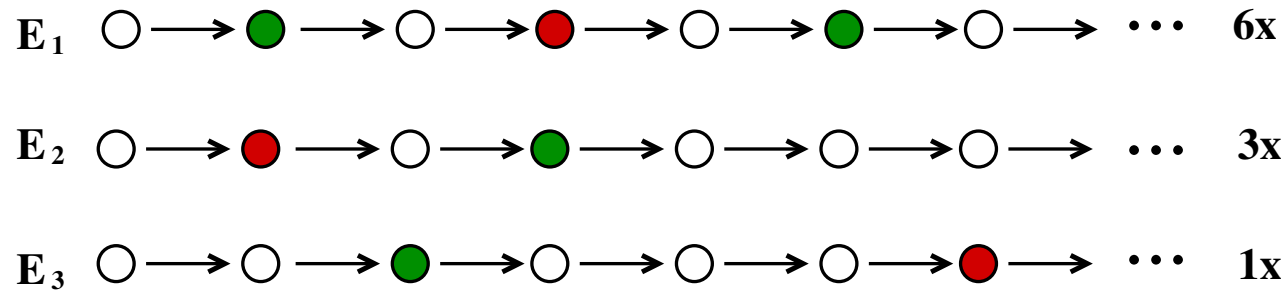
A: State Value $V(s)$

B: Immediate reward $r(s)$ ←

C: Return/Utility G

D: Policy π

Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$

○ 0 ● 1 ● -0.3

2. Episode length::

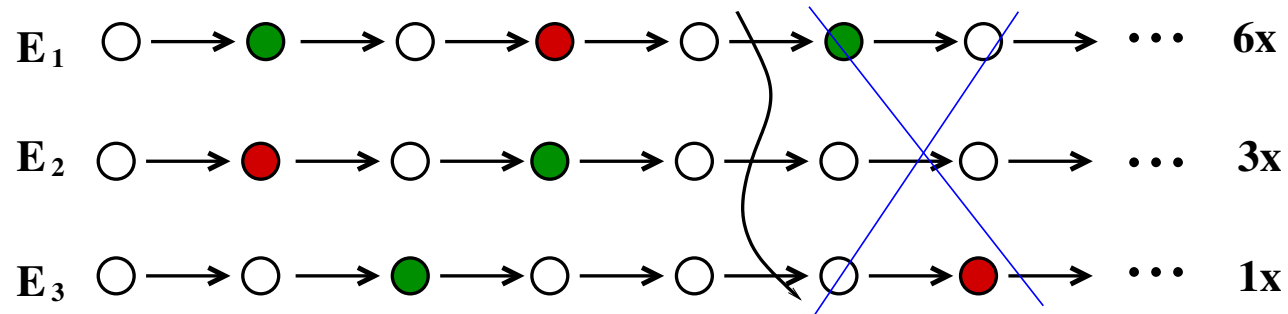
A: Infinite

B: Finite

C: $T = 1000$

D: $T = 4$

Policy Evaluation: How good is the strategy?

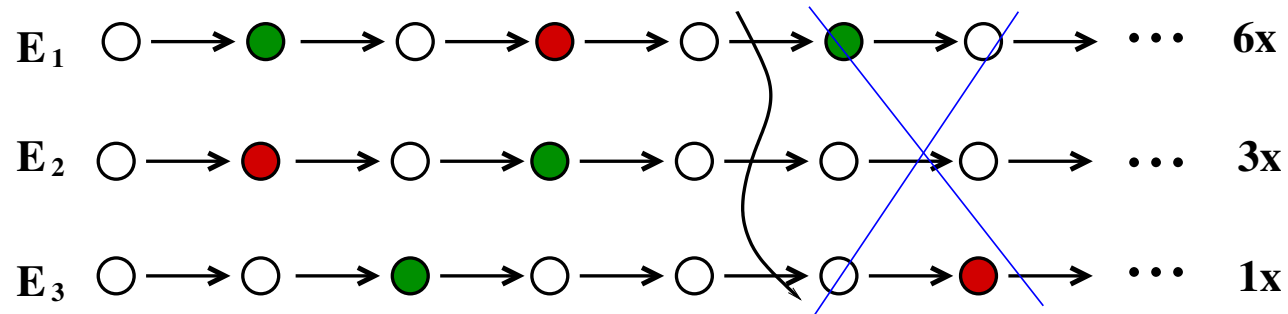


What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$

○ 0 ● 1 ● -0.3
2. Episode length: We'll chose $T = 4$
 - A: Infinite ⇐
 - B: Finite ⇐
 - C: $T = 1000$ ⇐
 - D: $T = 4$ ⇐

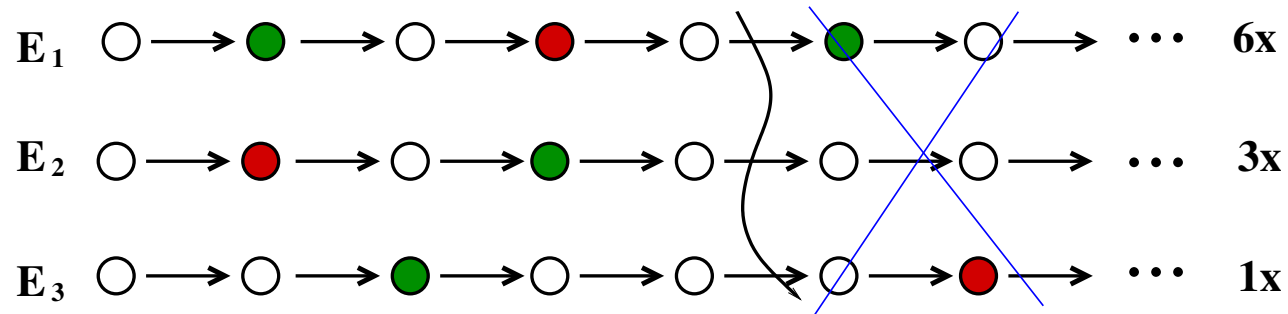
Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$ ○ 0 ● 1 ● -0.3
2. Episode length: We chose $T = 4$
3. Discount factor: γ
 - A: 1
 - B: 5
 - C: 0.8
 - D: 0.1

Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$

○ 0 ● 1 ● -0.3

2. Episode length: We chose $T = 4$

3. Discount factor: $0 \leq \gamma \leq 1$, we'll chose $\gamma = 0.8$

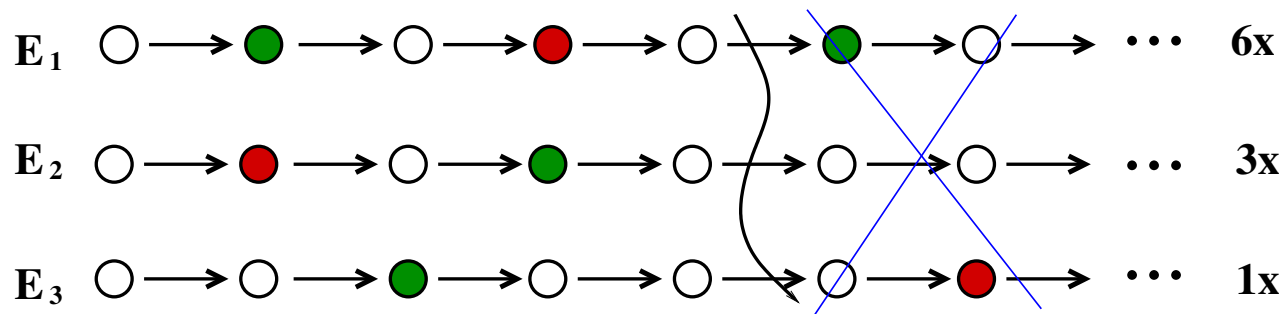
A: 1 ←

B: 5

C: 0.8 ←

D: 0.1 ←

Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$

○ 0 ● 1 ● -0.3

2. Episode length: We chose $T = 4$

3. Discount factor: $0 \leq \gamma \leq 1$, we'll chose $\gamma = 0.8$

4. Episode value calculation: return/utility G_t

A: $\sum_{n=1}^T \gamma^n$

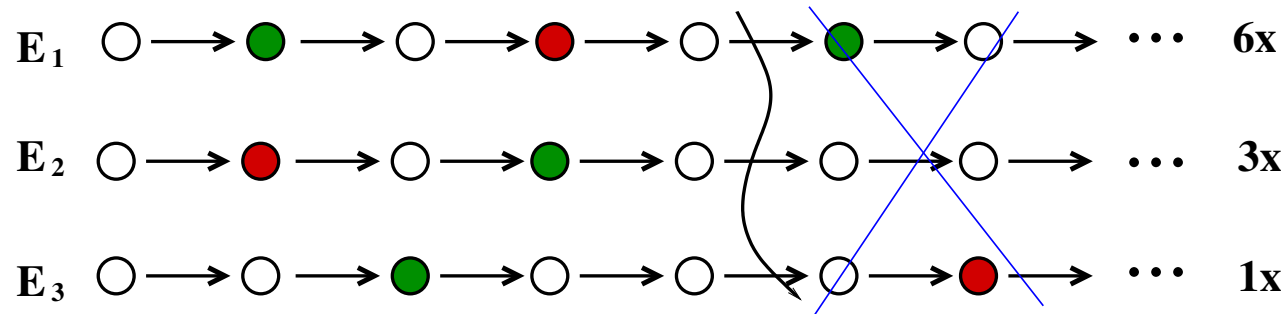
B: $\prod_{n=1}^T \gamma^n$

C: γr

D: $\prod_{n=1}^T \gamma^n r_n$

E: $\sum_{n=0}^T \gamma^n r_n$

Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$

○ 0 ● 1 ● -0.3

2. Episode length: We chose $T = 4$

3. Discount factor: $0 \leq \gamma \leq 1$, we'll chose $\gamma = 0.8$

4. Episode value calculation: return/utility $G_t = \sum_{n=0}^T \gamma^n r_n$

A: $\sum_{n=1}^T \gamma^n$

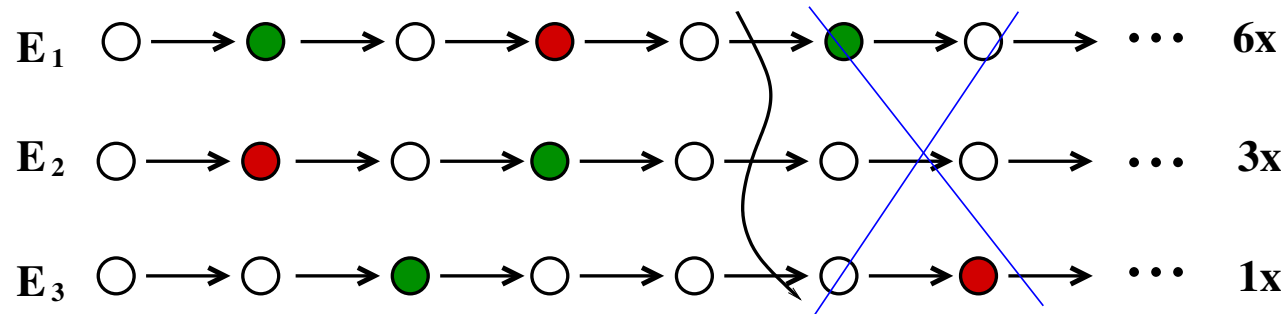
B: $\prod_{n=1}^T \gamma^n$

C: γr

D: $\prod_{n=1}^T \gamma^n r_n$

E: $\sum_{n=0}^T \gamma^n r_n \quad \Leftarrow$

Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$

\circ $\mathbf{0}$ \bullet $\mathbf{1}$ \bullet $\mathbf{-0.3}$

2. Episode length: We chose $T = 4$

3. Discount factor: $0 \leq \gamma \leq 1$, we'll chose $\gamma = 0.8$

4. Episode value calculation: return/utility $G_t = \sum_{n=0}^T \gamma^n r_n$

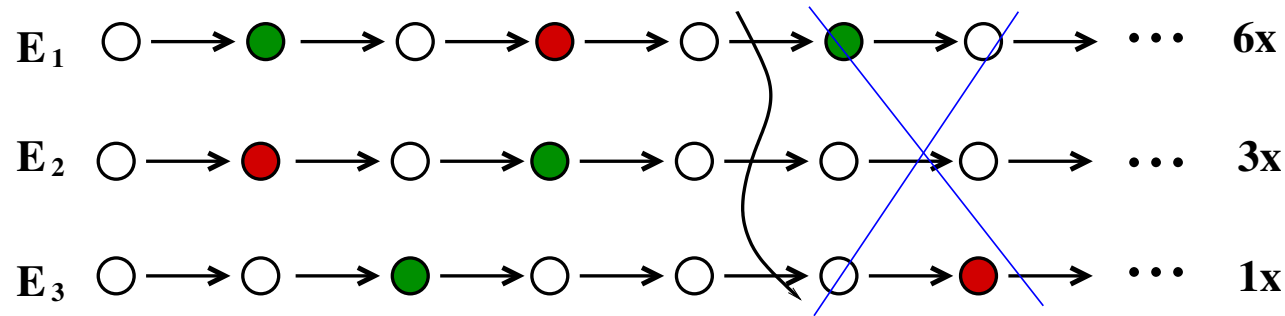
A: $G(E_1) = 0.7$

B: $G(E_1) = 0.65$

C: $G(E_1) = 0.95$

D: $G(E_1) = 0.8$

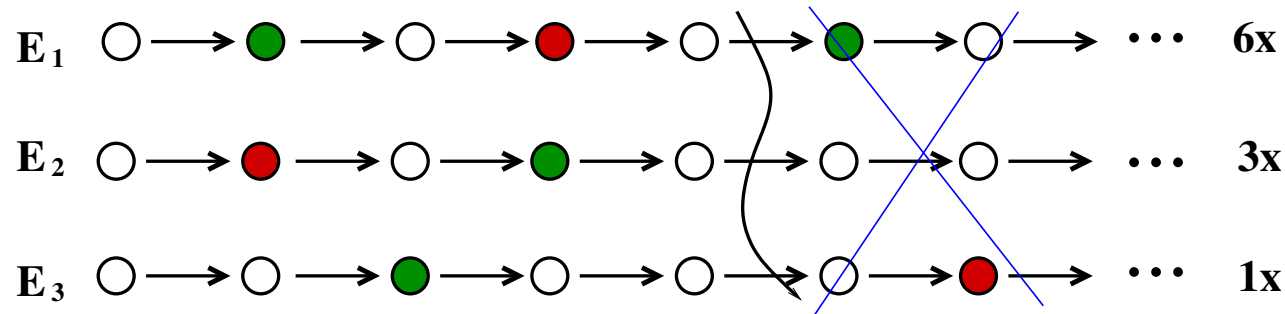
Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$ ○ 0 ● 1 ● -0.3
2. Episode length: We chose $T = 4$
3. Discount factor: $0 \leq \gamma \leq 1$, we'll chose $\gamma = 0.8$
4. Episode value calculation: return/utility $G_t = \sum_{n=0}^T \gamma^n r_n$
 - $G(E_1) = 0.65$
 - A: $G(E_1) = 0.7$
 - B: $G(E_1) = 0.65 = 0.8^0 \cdot 0 + 0.8^1 \cdot 1 + 0.8^2 \cdot 0 + 0.8^3 \cdot (-0.3) + 0.8^4 \cdot 0 \quad \Leftarrow$
 - C: $G(E_1) = 0.95$
 - D: $G(E_1) = 0.8$

Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$

○ 0 ● 1 ● -0.3

2. Episode length: We chose $T = 4$

3. Discount factor: $0 \leq \gamma \leq 1$, we'll chose $\gamma = 0.8$

4. Episode value calculation: return/utility $G_t = \sum_{n=0}^T \gamma^n r_n$

- $G(E_1) = 0.65$

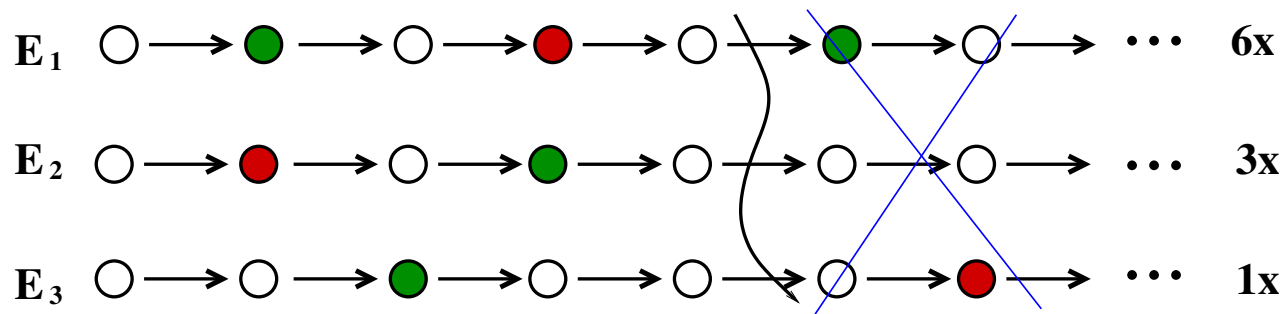
A: $G(E_2) = 0.272$

B: $G(E_2) = 0.4$

C: $G(E_2) = 0.7$

D: $G(E_2) = 0.99$

Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$

○ 0 ● 1 ● -0.3

2. Episode length: We chose $T = 4$

3. Discount factor: $0 \leq \gamma \leq 1$, we'll chose $\gamma = 0.8$

4. Episode value calculation: return/utility $G_t = \sum_{n=0}^T \gamma^n r_n$

• $G(E_1) = 0.65$, $G(E_2) = 0.272$

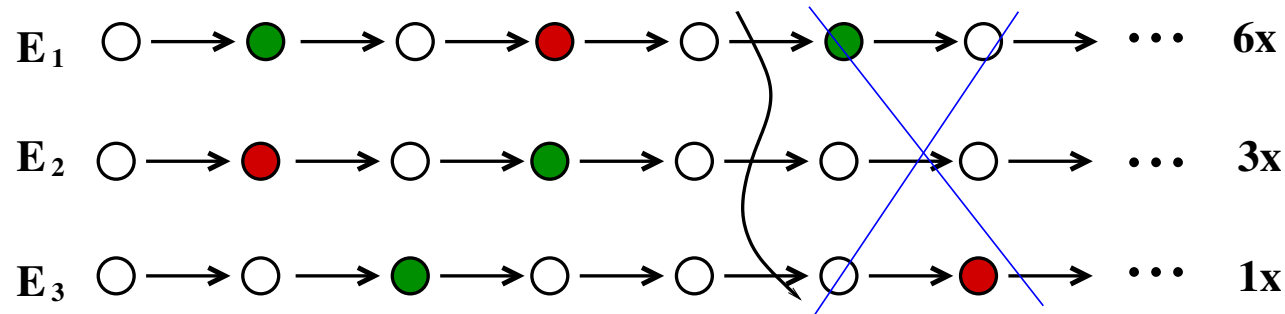
A: $G(E_2) = 0.272 = 0.8^1 \cdot (-0.3) + 0.8^3 \cdot 1 \quad \Leftarrow$

B: $G(E_2) = 0.4$

C: $G(E_2) = 0.7$

D: $G(E_2) = 0.99$

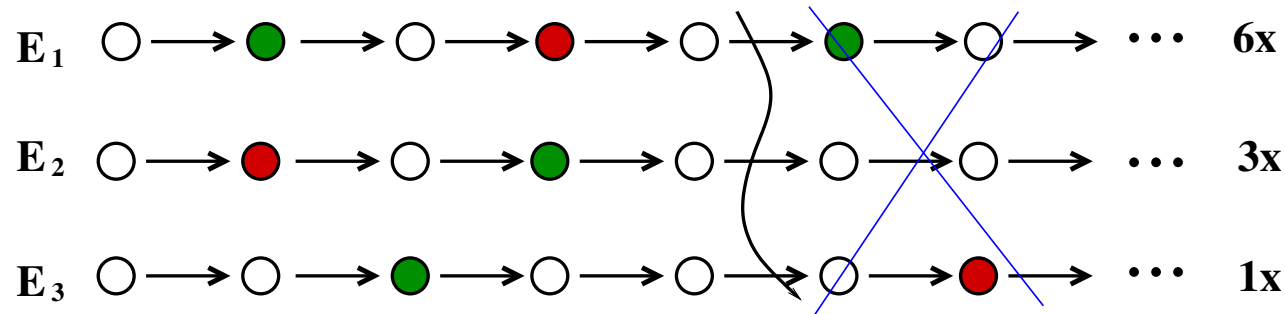
Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$ ○ 0 ● 1 ● -0.3
2. Episode length: We chose $T = 4$
3. Discount factor: $0 \leq \gamma \leq 1$, we'll chose $\gamma = 0.8$
4. Episode value calculation: return/utility $G_t = \sum_{n=0}^T \gamma^n r_n$
 - $G(E_1) = 0.65$, $G(E_2) = 0.272$
 - A: $G(E_3) = -0.3$
 - B: $G(E_3) = 0.7$
 - C: $G(E_3) = 0.64$
 - D: $G(E_3) = 0.8$

Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$

○ 0 ● 1 ● -0.3

2. Episode length: We chose $T = 4$

3. Discount factor: $0 \leq \gamma \leq 1$, we'll chose $\gamma = 0.8$

4. Episode value calculation: return/utility $G_t = \sum_{n=0}^T \gamma^n r_n$

• $G(E_1) = 0.65$, $G(E_2) = 0.272$, $G(E_3) = 0.64$

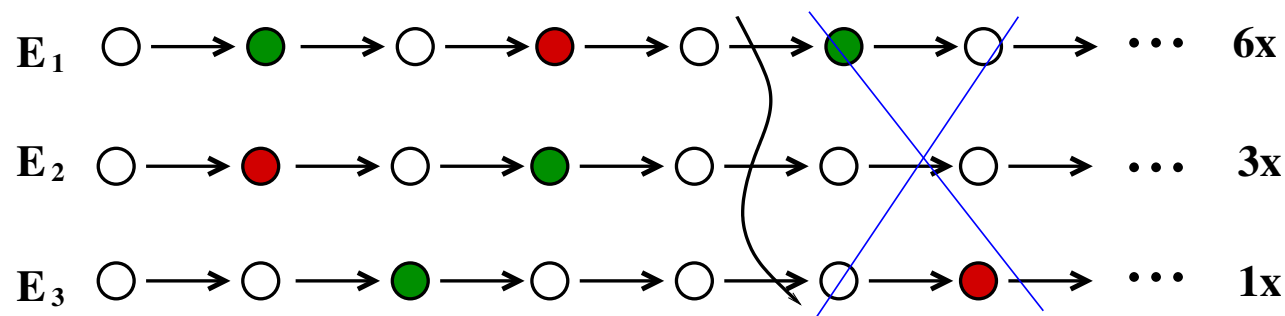
A: $G(E_3) = -0.3$

B: $G(E_3) = 0.7$

C: $G(E_3) = 0.64 = 0.8^2 \cdot 1$ ←

D: $G(E_3) = 0.8$

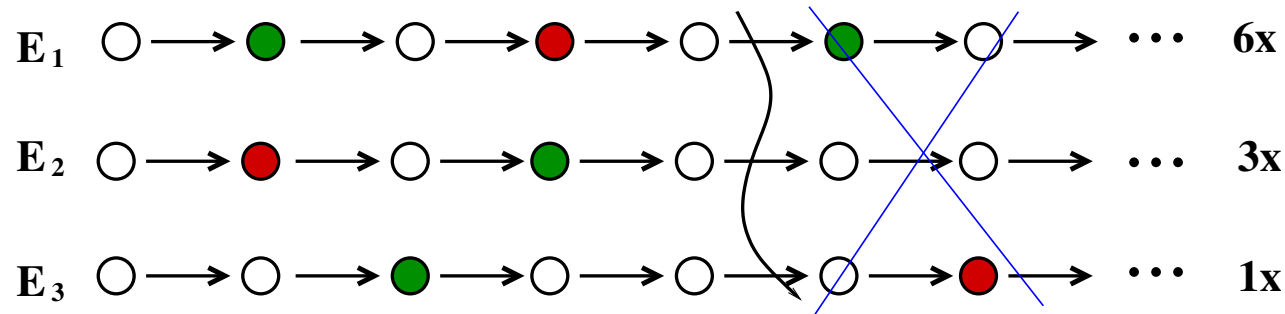
Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$ ○ 0 ● 1 ● -0.3
2. Episode length: We chose $T = 4$
3. Discount factor: $0 \leq \gamma \leq 1$, we'll chose $\gamma = 0.8$
4. Episode value calculation: return/utility $G_t = \sum_{n=0}^T \gamma^n r_n$
 - $G(E_1) = 0.65$, $G(E_2) = 0.272$, $G(E_3) = 0.64$
5. Calculation for the whole policy:
 - A: $\sum_{e=1}^E \sum_{n=0}^T \gamma^n r_n$
 - B: $\prod_{e=1}^E \sum_{n=0}^T \gamma^n r_n$
 - C: $\sum_{e=1}^E p_e \sum_{n=0}^T \gamma^n r_n$
 - D: $\max p_e \sum_{n=0}^T \gamma^n r_n$

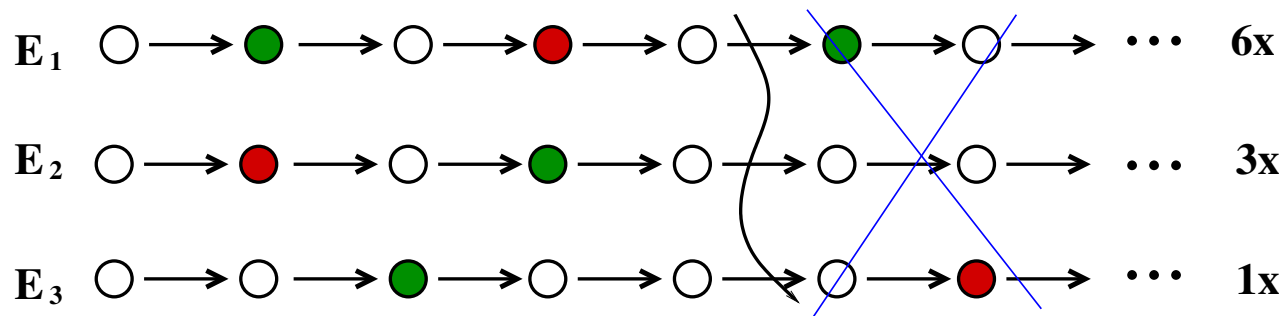
Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$ ○ 0 ● 1 ● -0.3
2. Episode length: We chose $T = 4$
3. Discount factor: $0 \leq \gamma \leq 1$, we'll chose $\gamma = 0.8$
4. Episode value calculation: return/utility $G_t = \sum_{n=0}^T \gamma^n r_n$
 - $G(E_1) = 0.65$, $G(E_2) = 0.272$, $G(E_3) = 0.64$
5. Calculation for the whole policy: $\sum_{e=1}^E p_e \sum_{n=0}^T \gamma^n r_n$
 - A: $\sum_{e=1}^E \sum_{n=0}^T \gamma^n r_n$
 - B: $\prod_{e=1}^E \sum_{n=0}^T \gamma^n r_n$
 - C: $\sum_{e=1}^E p_e \sum_{n=0}^T \gamma^n r_n$ \Leftarrow
 - D: $\max p_e \sum_{n=0}^T \gamma^n r_n$

Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$

\circ 0 \bullet 1 \bullet -0.3

2. Episode length: We chose $T = 4$

3. Discount factor: $0 \leq \gamma \leq 1$, we'll chose $\gamma = 0.8$

4. Episode value calculation: return/utility $G_t = \sum_{n=0}^T \gamma^n r_n$

• $G(E_1) = 0.65$, $G(E_2) = 0.272$, $G(E_3) = 0.64$

5. Calculation for the whole policy: $\sum_{e=1}^E p_e \sum_{n=0}^T \gamma^n r_n$

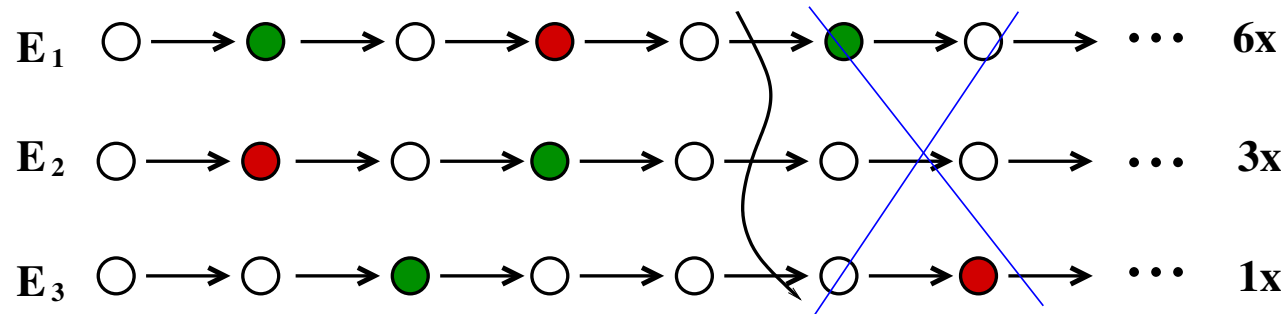
A: 0.535

B: 1.562

C: 1

D: 0.86

Policy Evaluation: How good is the strategy?



What do we need?

1. Evaluation of the state in the sequence: Immediate reward, reward function $r(s)$ ○ 0 ● 1 ● -0.3
2. Episode length: We chose $T = 4$
3. Discount factor: $0 \leq \gamma \leq 1$, we'll chose $\gamma = 0.8$
4. Episode value calculation: return/utility $G_t = \sum_{n=0}^T \gamma^n r_n$
 - $G(E_1) = 0.65$, $G(E_2) = 0.272$, $G(E_3) = 0.64$
5. Calculation for the whole policy: $\sum_{e=1}^E p_e \sum_{n=0}^T \gamma^n r_n = \mathbf{0.535}$
 - A: $0.535 = 0.6 \cdot 0.65 + 0.3 \cdot 0.272 + 0.1 \cdot 0.64$ ⇐
 - B: 1.562
 - C: 1
 - D: 0.86