#### Lecture slides for Automated Planning: Theory and Practice

#### Chapter 5 Plan-Space Planning

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#### **Motivation**

- Problem with state-space search
  - In some cases we may try many different orderings of the same actions before realizing there is no solution



 Least-commitment strategy: don't commit to orderings, instantiations, etc., until necessary

#### Outline

- Basic idea
- Open goals
- Threats
- The PSP algorithm
- Long example
- Comments

### **Plan-Space Planning - Basic Idea**

- Backward search from the goal
- Each node of the search space is a *partial plan* 
  - » A set of partially-instantiated actions
  - » A set of constraints
  - Make more and more refinements, until we have a solution
- Types of constraints:
  - precedence constraint: a must precede b
  - *binding constraints*:
    - » inequality constraints, e.g.,  $v_1 \neq v_2$  or  $v \neq c$
    - » equality constraints (e.g.,  $v_1 = v_2$  or v = c) and/or substitutions
  - causal link:
    - » use action a to establish the precondition p needed by action b
- How to tell we have a solution: no more *flaws* in the plan
  - Will discuss flaws and how to resolve them



## Flaws: 1. Open Goals

#### • Open goal:

 An action a has a precondition p that we haven't decided how to establish

- Resolving the flaw:
  - Find an action b

foo(*x*) Precond: ... Effects: p(*x*)

- (either already in the plan, or insert it)
- that can be used to establish p
  - can precede a and produce p
- Instantiate variables and/or constrain variable bindings
- Create a causal link



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#### Flaws: 2. Threats

Threat: a deleted-condition interaction

- Action *a* establishes a precondition (e.g., pq(x)) of action *b*
- Another action *c* is capable of deleting *p*
- Resolving the flaw:
  - impose a constraint to prevent *c* from deleting *p*
- Three possibilities:
  - Make *b* precede *c*
  - Make *c* precede *a*
  - Constrain variable(s)
     to prevent *c* from
     deleting *p*



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# **The PSP Procedure**

```
PSP(\pi)
    flaws \leftarrow \mathsf{OpenGoals}(\pi) \cup \mathsf{Threats}(\pi)
    if flaws = \emptyset then return(\pi)
    select any flaw \phi \in flaws
    resolvers \leftarrow \mathsf{Resolve}(\phi, \pi)
    if resolvers = \emptyset then return(failure)
    nondeterministically choose a resolver \rho \in resolvers
   \pi' \leftarrow \mathsf{Refine}(\rho, \pi)
    return(PSP(\pi'))
end
```

- PSP is both sound and complete
- It returns a partially ordered solution plan
  - Any total ordering of this plan will achieve the goals
  - Or could execute actions in parallel if the environment permits it

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## Example

- Similar (but not identical) to an example in Russell and Norvig's Artificial *Intelligence: A Modern Approach* (1st edition)
- Operators:
  - Start
     Precond: none
     Start and Finish are dummy actions that we'll use instead of the initial state and goal
     Effected At(Users) cells(UNC Drill) Cells(CM Decemb)

Effects: At(Home), sells(HWS,Drill), Sells(SM,Milk), Sells(SM,Banana)

Finish

Precond: Have(Drill), Have(Milk), Have(Banana), At(Home)

- Go(*l*,*m*) Precond: At(*l*) Effects: At(*m*), ¬At(*l*)
- Buy(p,s)
   Precond: At(s), Sells(s,p)
   Effects: Have(p)

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- Need to give PSP a plan  $\pi$  as its argument
  - Initial plan: Start, Finish, and an ordering constraint



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- The first three refinement steps
  - These are the only possible ways to establish the Have preconditions



Three more refinement steps

The only possible ways to establish the Sells preconditions



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• Two more refinements: the only ways to establish At(HWS) and At(SM)

This time, several threats occur



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- Nondeterministic choice: how to resolve the threat to  $At(s_1)$ ?
  - Our choice: make Buy(Drill) precede Go(l<sub>2</sub>, SM)
  - This also resolves the other two threats (why?)



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- Nondeterministic choice: how to establish  $At(l_1)$ ?
  - We'll do it from Start, with  $l_1$ =Home
  - How else could we have done it?



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Nondeterministic choice: how to establish  $At(l_2)$ ?

• We'll do it from Go(Home,HWS), with  $l_2$ = HWS



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- The only feasible way to establish At(Home) for Finish
  - This creates a bunch of threats



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• To remove the threats to At(SM) and At(HWS), make them precede  $Go(l_3, Home)$ 

This also removes the other threats



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#### **Final Plan**

- Establish  $At(l_3)$  with  $l_3$ =SM
- We're done!



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# Discussion

- How to choose which flaw to resolve first and how to resolve it?
  - We'll return to these questions in Chapter 10
- PSP doesn't commit to orderings and instantiations until necessary
  - Avoids generating search trees like this one:
- Problem: how to prune infinitely long paths?
  - Loop detection is based on recognizing states we've seen before
  - In a partially ordered plan, we don't know the states
- Can we prune if we see the same *action* more than once?

 $\rightarrow$  act1  $\rightarrow$  act2  $\rightarrow$  act1  $\rightarrow$  ...

 No. Sometimes we might need the same action several times in different states of the world

» Example on next slide

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Backward statespace search: ...  $\rightarrow$  act1  $\rightarrow$  act2 ...  $\rightarrow$  act2  $\rightarrow$  act1

# Example

3-digit binary counter starts at 000, want to get to 111	• Plan:
$s_0 = \{d_3=0, d_2=0, d_1=0\}, \text{ i.e., } 000$	
$g = \{d_3=1, d_2=1, d_1=1\}, \text{ i.e., } 111$	incr-
Operators to increment the counter by 1:	incr-
incr-xx0-to-xx1	incr-
Precond: <i>d</i> <sup>1</sup> =0	incr-
Effects: $d_1=1$	incr-
	incr-
incr-x01-to-x10	incr-
Precond: $d_2=0$ , $d_1=1$	
Effects: $d_2=1, d_1=0$	

incr-011-to-100 Precond:  $d_3=0$ ,  $d_2=1$ ,  $d_1=1$ Effects:  $d_3=1$ ,  $d_2=0$ ,  $d_1=0$ 

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initial states 0 0 0

initial state.		U	U	U	
incr-xx0-to-z	xx1	$\rightarrow$	0	0	1
incr-x01-to-	x10	$\rightarrow$	0	1	0
incr-xx0-to-z	xx1	$\rightarrow$	0	1	1
incr-011-to-	100	$\rightarrow$	1	0	0
incr-xx0-to-z	xx1	$\rightarrow$	1	0	1
incr-x01-to-	x10	$\rightarrow$	1	1	0
incr-xx0-to-z	xx1	$\rightarrow$	1	1	1

## **A Weak Pruning Technique**

- Can prune all partial plans of *n* or more actions, where *n* = |{all possible states}|
   This doesn't help very much
- I'm not sure whether there's a good pruning technique for plan-space planning