

Monocular Visual Odometry and Structure from Motion

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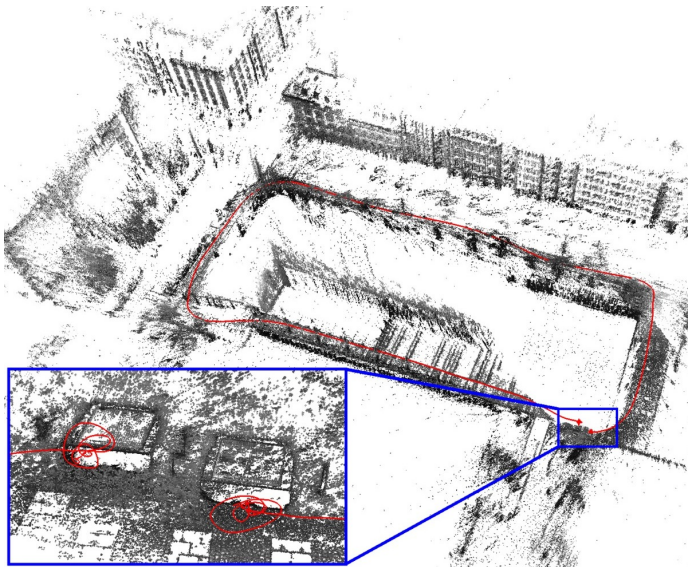
5. 11. 2021

Outline of the presentation

- Problem introduction
- Applications [22, 11, 28]
- Taxonomy of MVO
 - ▶ Direct vs Indirect
 - ▶ Sparse vs Dense
- Direct Sparse Odometry [8]
- CNN for pose and depth estimation [33]
- D3VO [31]
- Demo

Visual odometry and Structure from Motion

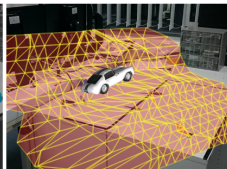
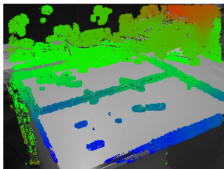
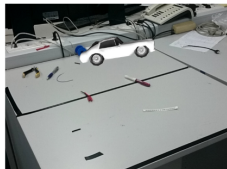
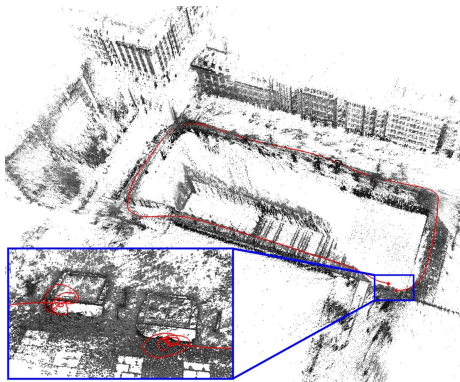
Problem introduction



Applications

Visual odometry

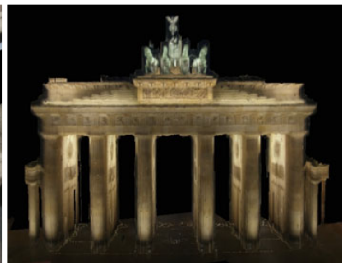
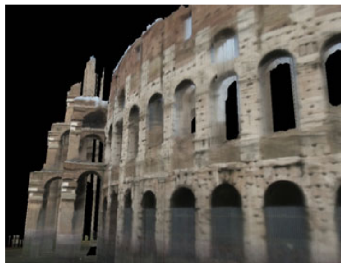
- Navigation [18, 8]
 - ▶ Mars exploration [16, 5]
 - ▶ Aerial vehicles [14, 29]
 - ▶ Underwater vehicles [7, 9]
 - ▶ Automotive [33, 12, 31]
- Augmented reality [25, 4]
- Calibration [27, 13]



Applications

Structure from Motion

- Image-based 3D modeling [20, 23, 26, 10]
- Hand-eye calibration [1, 24]
- Augmented reality [17, 30]
- Video enhancement and stabilization [15, 32]
- Segmentation and recognition [3, 2]

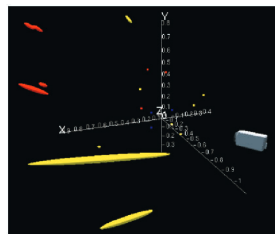


Taxonomy

Direct vs Indirect

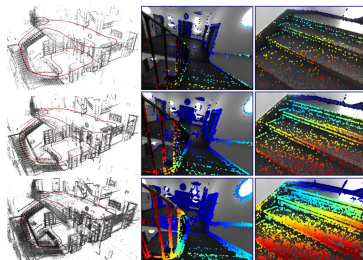
Indirect

- Generate an intermediate representation of raw measurements
- Using these intermediate values, calculate geometry and camera motion
- [21, 6]



Direct

- Use the raw measurements directly to calculate geometry and camera motion
- [8, 31, 12, 33]

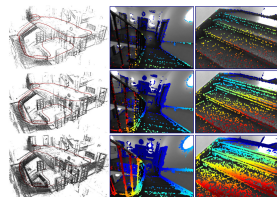


Taxonomy

Dense vs Sparse

Sparse

- Use and reconstruct only a selected set of independent points (keypoints, e.g., corners)
- [21, 6, 8]



Dense

- Use and reconstruct all the points in the 2D image domain
- [12, 33, 19]



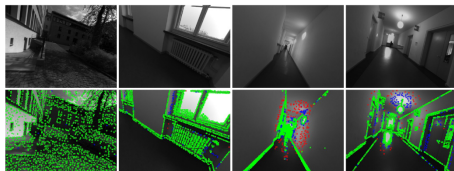
Direct Sparse Odometry (DSO)

Points selection

- Sparse \Rightarrow use and reconstruct only small set of points
 \rightarrow work with intensities
- Aim to keep a fixed number $N_p = 2000$ active points

1) Candidate point selection

- Choose points that are **well-distributed** in the image and have **high image gradient magnitude** w.r.t. their immediate surroundings
 - 1 Split the image to 32×32 regions
 - 2 Calculate an adaptive threshold gradient for that region $\bar{g} + g_{th}$
 - 3 Split the image to $d \times d$ blocks \rightarrow select pixel with highest gradient magnitude if it surpasses region threshold



Direct Sparse Odometry (DSO)

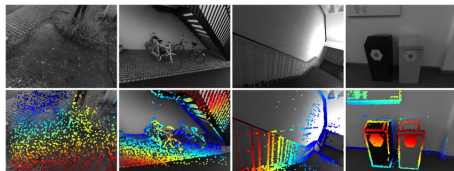
Points selection

2) Candidate point tracking

- Selected candidate points are tracked in subsequent images
→ discrete search along the epipolar line
- Best match is used to compute the depth of the candidate point

3) Candidate point activation

- Select new active points after maginalization of the old ones
- Candidate points are activated based on their distance from other active points



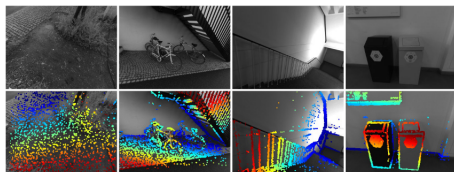
Direct Sparse Odometry (DSO)

Frames selection

- Direct \Rightarrow use raw measurements
 \rightarrow work with images
- Keep a window of $N_f = 7$ reference images (keyframes)

1) Initial frame tracking

- Tracking new frame w.r.t. latest KF:
 - 1 two-frame direct image alignment
 - 2 multi-scale image pyramid
 - 3 constant motion mode
- If the RMSE is still high, try RANSACing rotation



Direct Sparse Odometry (DSO)

Frames selection

2) Keyframe creation

- New KF is created based on three criterion:

- 1 Field of view should change \rightarrow mean square optical flow:

$$f = \sqrt{\frac{1}{n} \sum_{i=1}^n \|p - p'\|^2}$$

- 2 Translation causes occlusions and disocclusions \rightarrow mean OF without rotation:

$$f_t = \sqrt{\frac{1}{n} \sum_{i=1}^n \|p - p'_t\|^2}$$

- 3 Camera exposure time changed significantly:

$$a = |\log(e^{a_j - a_i} t_j t_i^{-1})|$$

- A new KF is taken if:

$$w_f \cdot f + w_{f_t} \cdot f_t + w_a \cdot a > T_{kf}$$

Direct Sparse Odometry (DSO)

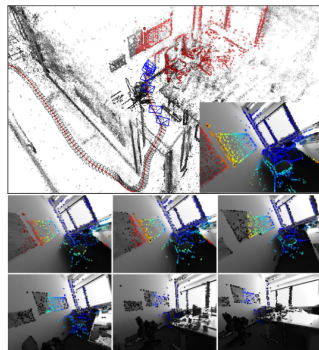
Frames selection

3) Keyframe marginalization

- Given active KFs l_1, \dots, l_n :
 - We keep two latest KFs l_1, l_2
 - If only 5 % of KF points is visible in l_1 , it is marginalized
 - If more than 7 KFs are active, we marginalize frames that are distant from others:

$$s(l_i) = \sqrt{d(i,1)} \sum_{j \in \{3, \dots, n\} \setminus i} \frac{1}{d(i,j) + \varepsilon}$$

- We first marginalize points in the KF and then the KF itself



Direct Sparse Odometry (DSO)

Photometric error and optimization

- Given a reference image I_i and a target image I_j , the photometric error of a point $\mathbf{p} \in I_i$ is defined as:

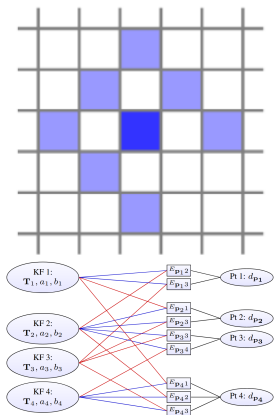
$$E_{\mathbf{p}}^j = \sum_{\mathbf{p} \in \mathcal{N}_{\mathbf{p}}} w_{\mathbf{p}} \left\| (I_j[\mathbf{p}'] - b_j) - \frac{t_j e^{a_j}}{t_i e^{a_i}} (I_i[\mathbf{p}] - b_i) \right\|_{\gamma},$$

$$\mathbf{p}' = P_c(\mathbf{R}P_c^{-1}(\mathbf{p}, d_p) + \mathbf{t}), \begin{bmatrix} \mathbf{R} & \mathbf{t} \\ \mathbf{0} & 1 \end{bmatrix} = \mathbf{T}_j \mathbf{T}_i^{-1}$$

- The total error is:

$$E_{\text{photo}} = \sum_{i \in \mathcal{F}} \sum_{\mathbf{p} \in \mathcal{P}_i} \sum_{j \in \text{obs}(\mathbf{p})} E_{\mathbf{p}}^j$$

- Optimizing $(\mathbf{T}_i, \mathbf{T}_j, d, \mathbf{c}, a_i, a_j, b_i, b_j)$ with sliding window using Gauss-Newton algorithm



Direct Sparse Odometry (**DSO**)

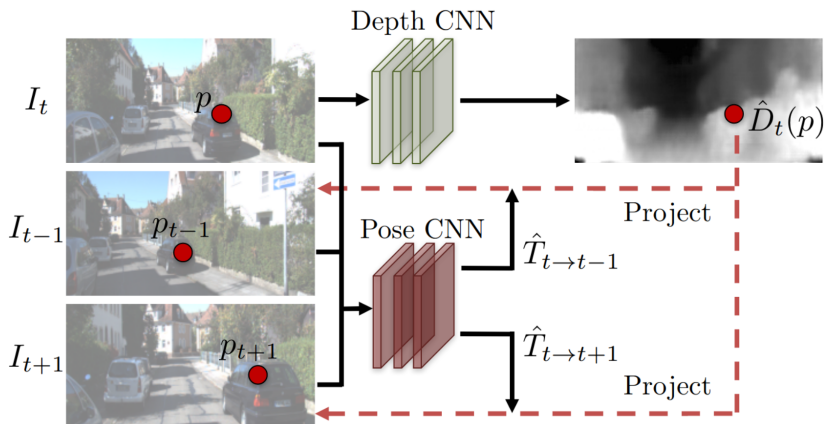
Experiments

SfMLearner

Overview

[33]

- Jointly train two different CNNs to predict depth and pose



SfMLearner

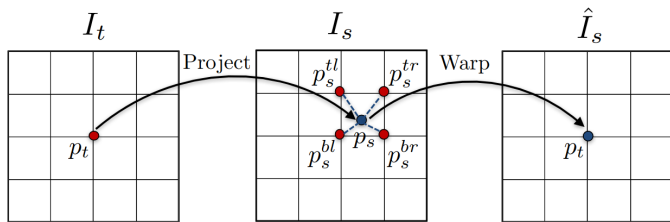
Loss function

- Given some target image I_t and source image I_s , the objective is formulated using view synthesis:

$$\mathcal{L}_{vs} = \sum_s \sum_{p \in I_t} |I_t(p) - \hat{I}_s(p)|$$

- i.e.,

$$p_s \sim P_c(\hat{T}_{t \rightarrow s} P_c^{-1}(\mathbf{p}_t, \hat{D}_t(\mathbf{p}_t)))$$



SfMLearner

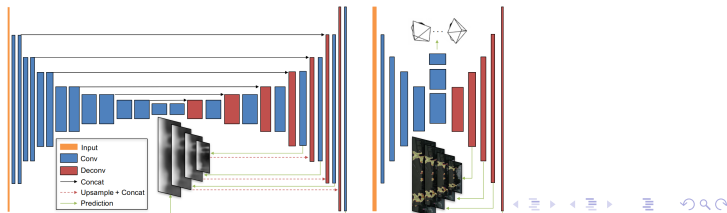
Explainability and network architectures

- There are many assumption on monocular view synthesis
→ To make the process more robust, they also use the explainability network that predicts, where the view synthesis will be successful
- The loss function for view synthesis is then:

$$\mathcal{L}_{vs} = \sum_s \sum_{p \in I_t} \hat{E}_s(p) |I_t(p) - \hat{I}_s(p)|$$

- The total loss is defined as:

$$\mathcal{L}_{\text{total}} = \mathcal{L}'_{vs} + \lambda_s \mathcal{L}'_{\text{smooth}} + \lambda_e \sum_s \mathcal{L}_{\text{reg}}(\hat{E}'_s)$$

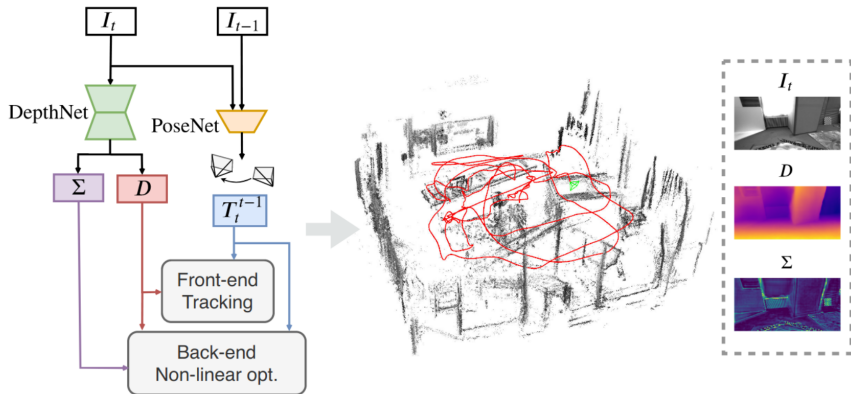


SfMLearner

Experiments

[31]

- Combines the previous two methods:
 - Self-supervised networks for depth, pose and uncertainty
 - Windowed sparse photometric bundle adjustment



- Minimize the photometric reprojection error:

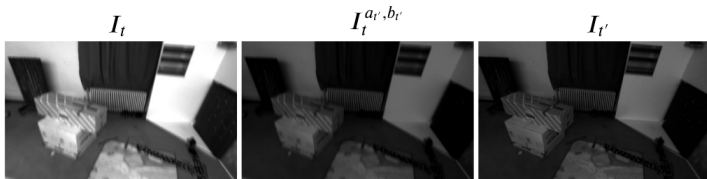
$$\mathcal{L}_{\text{self}} = \frac{1}{n} \sum_{p \in I_t} \min_{t'} r(I_t, \hat{I}_{t'}), \text{ where}$$

$$r(I_a, I_b) = \frac{\alpha}{2} (-\text{SSIM}(I_a, I_b)) + (1 - \alpha) \|I_a - I_b\|_1$$

- Modeling the change of camera exposure:

$$I^{a,b} = aI + b$$

$$\implies \mathcal{L}_{\text{self}} = \frac{1}{n} \sum_{p \in I_t} \min_{t'} r(I_t^{a_{t'}, b_{t'}}, \hat{I}_{t'})$$



- Uncertainty Σ_t works similarly to the explainability in SfMLearner:

$$\mathcal{L}_{\text{self}} = \frac{1}{n} \sum_{p \in I_t} \frac{\min_{t'} r(I_t^{a_{t'}, b_{t'}}, \hat{I}_{t'})}{\Sigma_t} + \log \Sigma_t$$

- The total loss is the combination of these self-supervised losses and the regularization losses on multiscale images:

$$\mathcal{L}_{\text{total}} = \frac{1}{s} \sum_s (\mathcal{L}_{\text{self}}^s + \lambda \mathcal{L}_{\text{reg}}^s), \text{ where}$$

$$\mathcal{L}_{\text{reg}} = \mathcal{L}_{\text{smooth}} + \beta \left[\sum_{t'} (a_{t'} - 1)^2 + b_{t'}^2 \right]$$

- **DepthNet** Input: I_t , Output: D_t, D_t^s, Σ_t
- **PoseNet** Input: $(I_t, I_{t'})$, Output: $\mathbf{T}_t^{t'}, a_{t'}, b_{t'}$

- Using predictions from self-supervised network $\hat{D}, \hat{\Sigma}, \hat{\mathbf{T}}_t^{t'}$
- Incorporating predictions to boost DSO [8]

1) Photometric energy

- Virtual stereo term E_p^+ :

$$E_{\text{photo}} \sum_{i \in \mathcal{F}} \sum_{\mathbf{p} \in \mathcal{P}_i} \left(\lambda E_p^+ + \sum_{j \in \text{obs}(\mathbf{p})} E_p^j \right), \text{ where}$$

$$E_p^+ = w_p \|l_i^+[\mathbf{p}^+] - l_i[\mathbf{p}]\|_\gamma$$

2) Pose energy

$$E_{\text{pose}} \sum_{i \in \mathcal{F} \setminus 0} \log \left[\hat{\mathbf{T}}_{i-1}^i \mathbf{T}_i^{i-1} \right] \Sigma_{\hat{\zeta}_{i-1}}^{-1} \log \left[\hat{\mathbf{T}}_{i-1}^i \mathbf{T}_i^{i-1} \right]$$

\implies Optimize $E_{\text{total}} = E_{\text{photo}} + E_{\text{pose}}$ using the Gauss-Newton method

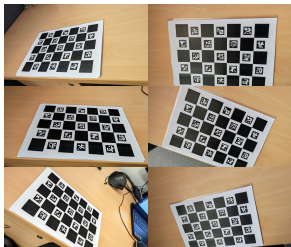
D3VO

Experiments

Demo

Calibration

- Obtain several pictures of some calibration target
- Detect markers positions from several locations and optimize camera parameters \rightarrow OpenCV



\implies Intrinsic parameters of my phone camera:

$$\mathbf{K} = \begin{pmatrix} 1440.62 & 0 & 953.99 \\ 0 & 1443.11 & 551.98 \\ 0 & 0 & 1 \end{pmatrix}$$

Demo

Pose, depth and reconstruction

- 1080p, 30 fps video around school premises



- DSO [8]: Trajectory & Sparse reconstruction
- SfMLearner [33]: Trajectory & Dense reconstruction
- (MonoDepth [12]: Trajectory & Dense reconstruction)

Comparison with other odometries

- LiDAR vs Stereo vs Mono

Visual Odometry / SLAM Evaluation 2012



40	RotRocc			0.88 %	0.0025 [deg/m]	0.3 s	2 cores @ 2.0 Ghz (C/C++)	<input type="checkbox"/>
M. Buczko and V. Willert: Flow-Decoupled Normalized Reprojection Error for Visual Odometry . 19th IEEE Intelligent Transportation Systems Conference (ITSC) 2016.								
41	D3VO			0.88 %	0.0021 [deg/m]	0.1 s	1 core @ 2.5 Ghz (C/C++)	<input type="checkbox"/>
N. Yang, L. Stumberg, R. Wang and D. Cremers: D3VO: Deep Depth, Deep Pose and Deep Uncertainty for Monocular Visual Odometry . The IEEE Conference on Computer Vision and Pattern Recognition (CVPR) 2020.								
42	SD-DEVO			0.88 %	0.0028 [deg/m]	0.06 s	1 cores @ 3.6 Ghz (C/C++)	<input type="checkbox"/>
129	VIS02-M		code	11.94 %	0.0234 [deg/m]	0.1 s	1 core @ 2.5 Ghz (C/C++)	<input type="checkbox"/>
A. Geiger, J. Ziegler and C. Stiller: StereoScan: Dense 3d Reconstruction in Real-time . IV 2011.								
130	MonoDepth2		code	12.59 %	0.0312 [deg/m]	1 s	1 core @ 2.5 Ghz (C/C++)	<input type="checkbox"/>
C. Godard, O. Mac Aodha, M. Firman and G. Brostow: Diving into self-supervised monocular depth estimation . ICCV 2019.								
131	MEGO			12.89 %	0.0451 [deg/m]	0.75 s	1 core @ 2.5 Ghz (C/C++)	<input type="checkbox"/>

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