

Lecture 1: MATLAB Environment, Basic Math Operators

B0B17MTB, BE0B17MTB – MATLAB

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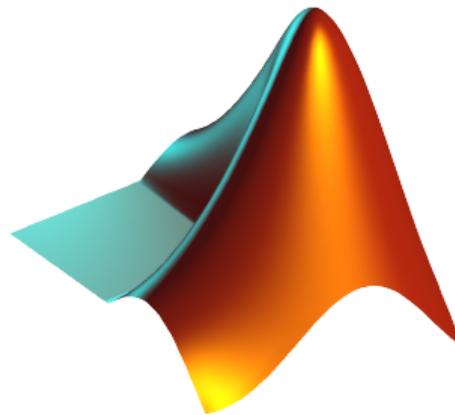
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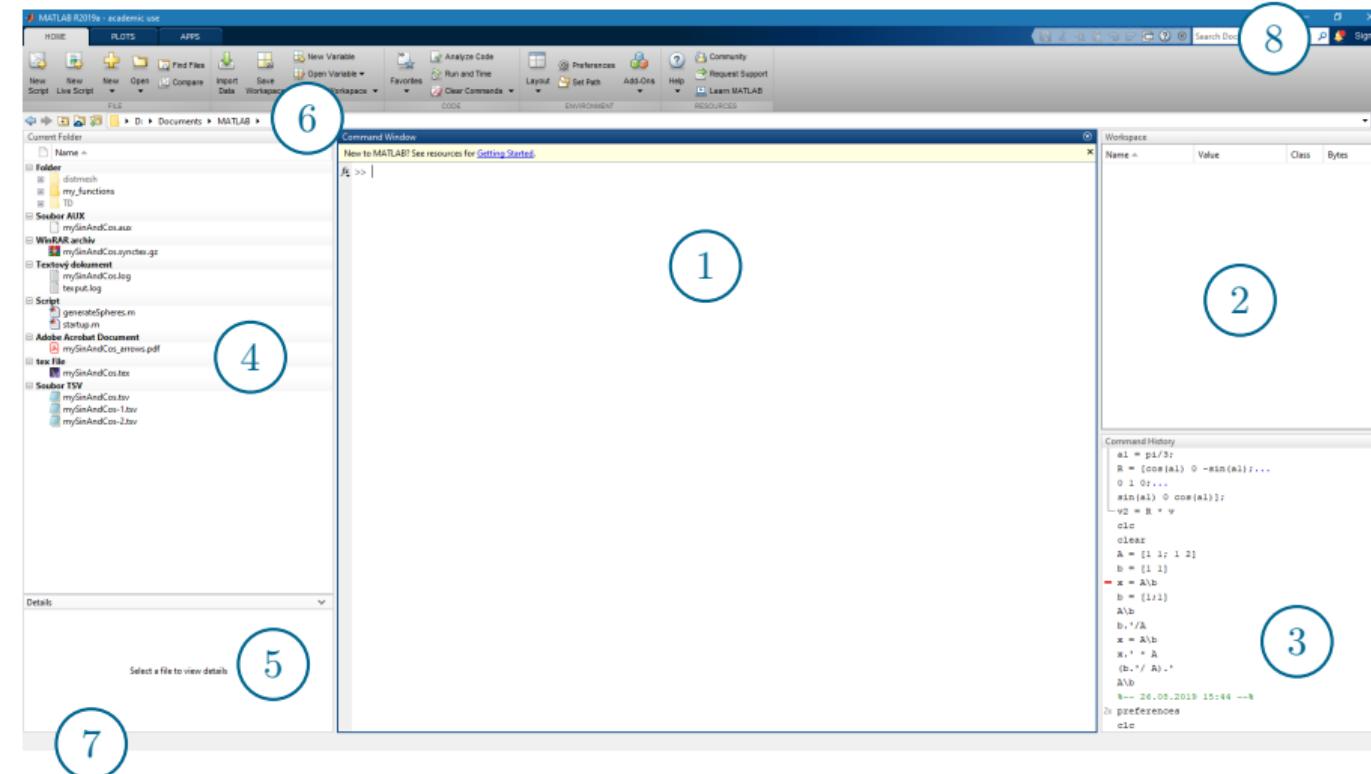
Outline

1. MATLAB Environment
2. Scalars, Vectors, Matrices
3. Basic Math Operations
4. Exercises





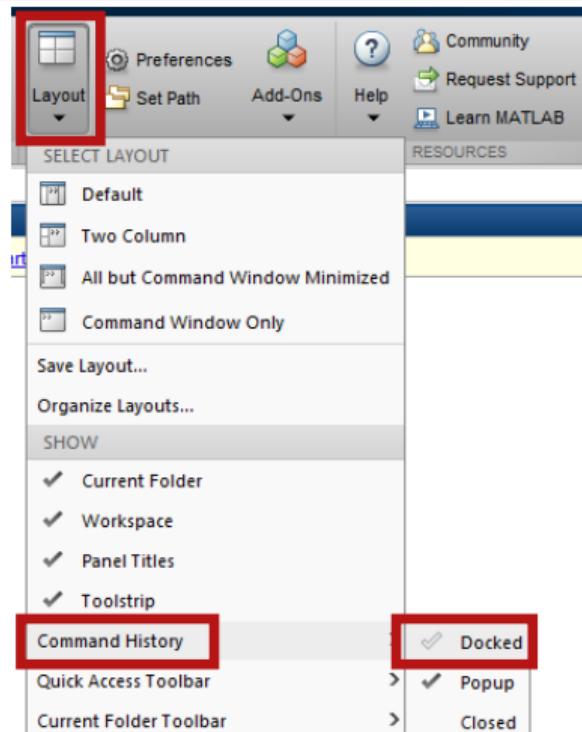
The MATLAB Environment





The MATLAB Environment – Panels

1. Command Window
2. Workspace
3. Command History – *not activated, to activate →*
4. Current Folder
5. Current Folder – Details
6. Current Working Directory
7. Status (“Busy” when MATLAB is executing your code)
8. Search in documentation





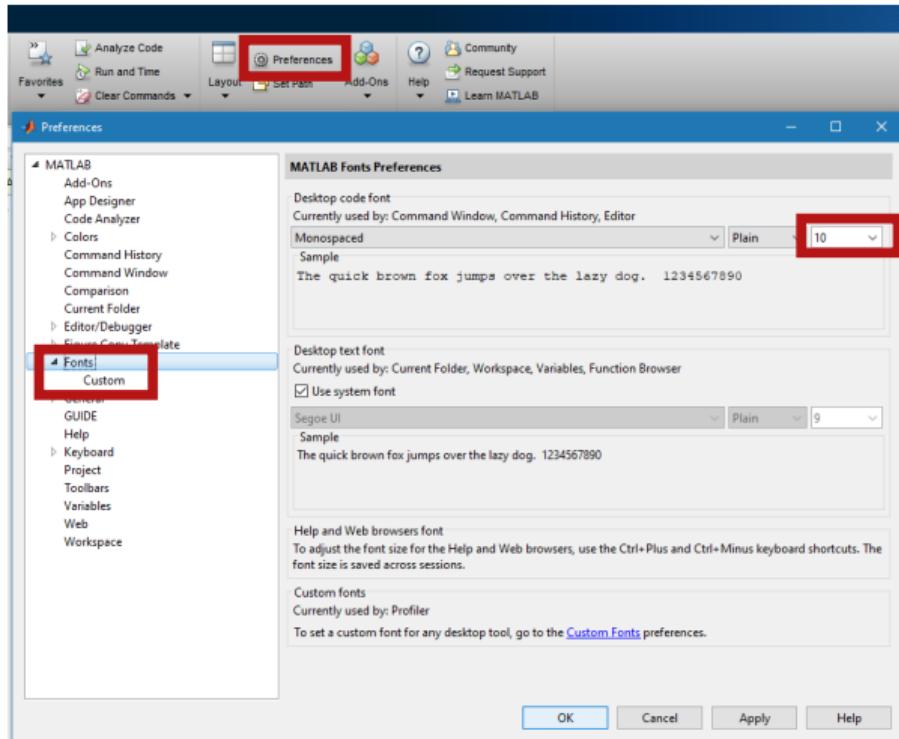
Preferences

- ▶ Command:

```
>> preferences
```

- ▶ Ribbon menu:

- ▶ Change font size.





Documentation

```
>> doc % opens documentation window
```

```
>> help % MATLAB help
```

```
>> demo % tutorials
```



The Help Structure

- ▶ Command:

```
>> help sin
```

- ▶ Output:

```
sin    Sine of argument in radians.  
sin(X) is the sine of the elements of X.
```

See also asin, sind, sinpi.

Reference page for sin



The Documentation Structure I.

► Command:

```
>> doc sin
```

1. Documentation page
2. Search field
3. Documentation contents
4. Bookmarks of this page

The screenshot shows the MATLAB Documentation interface. At the top, there's a toolbar with various icons. Below it is a navigation bar with tabs: Documentation (which is selected), All, Examples, and Functions. A search bar labeled 'Search Help' is located on the right of the navigation bar. The main content area has a title 'sin' with a subtitle 'Sine of argument in radians'. There are sections for 'Syntax' (containing the command `y = sin(X)`), 'Description' (explaining it returns the sine of the elements of `X`), 'Examples' (one example shown), and 'Extended Capabilities' (mentioning GPU support). On the left, there's a sidebar with a tree view of documentation categories like 'MATLAB', 'Mathematics', and 'Elementary Math', and a section for the 'sin' function itself with links to 'Syntax', 'Description', 'Examples', etc. Numbered circles (1 through 4) are overlaid on the interface to point to specific features: circle 1 points to the search bar, circle 2 points to the 'All' tab in the navigation bar, circle 3 points to the 'CONTENTS' sidebar, and circle 4 points to the 'See Also' link in the sidebar.



The Documentation Structure II.

- ▶ Check the origin of the function.
 - ▶ Several functions with the same name may exist.
- ▶ Functions types by origin:
 - ▶ MATLAB core functions – most of them build-in, some are available for editing (not recommended!).
 - ▶ Functions from installed toolboxes.
 - ▶ User-created functions.
- ▶ Calling priority for functions will be discussed later.
- ▶ During this course, **always open a function from core installation.**

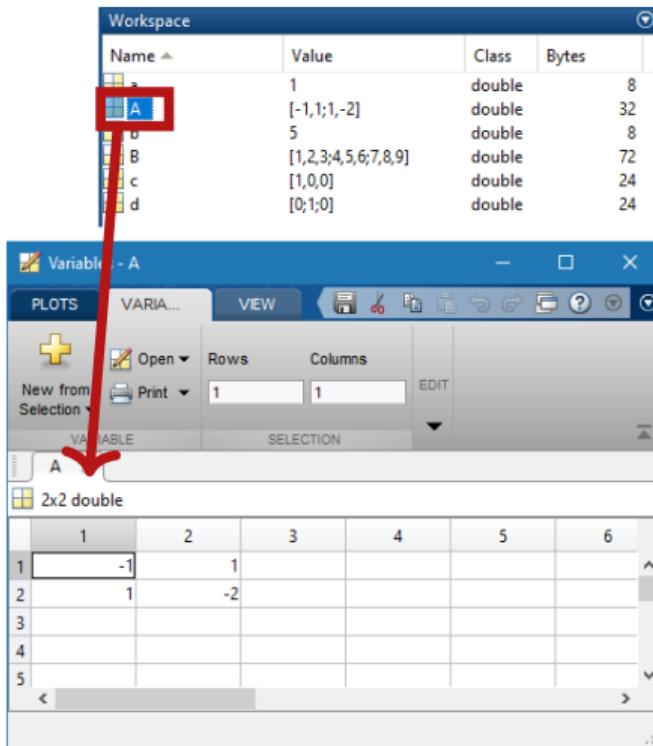
A screenshot of a MATLAB documentation search interface. The search bar at the top contains the text "sin". Below it, a list of search results is displayed under the heading "Functions". The results are:

Result	Description	Origin
<code>fx sin</code> - Sine of argument in radians		MATLAB
<code>fx sin</code> - Symbolic sine function		Symbolic Math Toolbox
<code>fx sin</code> - Sine of fixed-point values		Fixed-Point Designer
<code>fx sind</code> - Sine of argument in degrees		MATLAB
<code>fx sinh</code> - Hyperbolic sine of argument in radians		MATLAB
» 136 more		



Workspace Browser

- ▶ List of variables.
- ▶ Deleting/modification of existing variables.
- ▶ Saving/loading.
- ▶ Values, Class and Memory information.
 - ▶ Other information can be added: size, min, max, ...
 - ▶ All information can be obtained using MATLAB functions that we learn later, *e.g.*, min, max, max, length.
- ▶ Fast data plotting option (in ribbon).





MATLAB Commands

► Matlab is cAsE sEnSiTiVe!

- ▶ Almost entirely, with certain exceptions (properties of graphics objects, ...).
- ▶ Pay attention to typos and variable names (see later).
 - ▶ New versions of MATLAB offer certain options.

```
>> AA = [1 1 1]
>> Aa
```

▶ Beware of different syntax in Mathematica.

- ▶ Following syntax is incorrect both in MATLAB and Mathematica:

```
>> Sin(pi/2) % function names start with lower case
>> cos[pi/2] % function input is in parentheses ()
```

- ▶ Will be discussed in the next lectures.



Naming Conventions

- ▶ Names of variables can have max. 63 characters starting with letter
(» `namelengthmax`)
 - ▶ Letters and numbers are allowed, other symbols (colon “：“, hyphen “-” and others) are not.
 - ▶ Underscore is allowed in the variable name “_” (not at the beginning, though!).
- ▶ Lowercase letters in the names of scalars and variables (`a = 17.59;`).
- ▶ Matrix names usually start with a capital letter (`A = [..];`).
- ▶ Iteration variables, variables used in `for` cycles usually named `m`, `n`, `k`, etc.
 - ▶ It is advisable to avoid `i` and `j` (complex unit).
- ▶ Avoid, if possible, standalone letter “1” (to be confused with one “1”) and predefined variables in MATLAB environment (see later).
- ▶ Choose names corresponding to the meaning of each particular variable.
- ▶ Avoid using names of existing functions or scripts (overloading can occur).
- ▶ The same conventions are valid for names of functions and scripts.



Variable Names

- ▶ Examples of valid variable names:

```
a, A, b, c, x1, x2, M_12, test1, matrix_A, fx, fX
```

- ▶ Examples of invalid variable names:

```
lvar      % starts with a number (not possible in MATLAB)
matrix A % contains space
coef.a    % possible only if coef is of type 'struct'
Test-1    % algebraic expressing: ans = Test - 1
f(y)      % makes sense when using symbolic expressions
```

- ▶ Examples of valid numbers in MATLAB,

```
3, -66, +0.0015, .015, 1e2, 1.6025e-10, 05.1
```



Functions who, whos

- ▶ Function `who` lists all variables in MATLAB Workspace.
 - ▶ Wide variety of options.
- ▶ Functions `whos` lists the variable names + dimension, size and data type of the variables or displays content of a file.
 - ▶ Wide variety of options.

```
>> whos ('-file', 'matlab.mat');
```

```
>> a = 15; b = true; c = 'test'; d = 1 + 5j;  
>> who  
>> whos  
>> Ws = whos;
```



Workspace – Output Deletion

- ▶ To clean (erase) command window:

```
>> clc
```

- ▶ To clean one (or more) variable(s):

```
>> clear      % whole Workspace is deleted  
>> clear XX    % variable XX is deleted  
>> clear XX YY % variables XX and YY are deleted  
>> clear z*     % everything starting with 'z' is deleted
```

- ▶ `clear` has a number of other options (graphics, I/O)



Command History Window

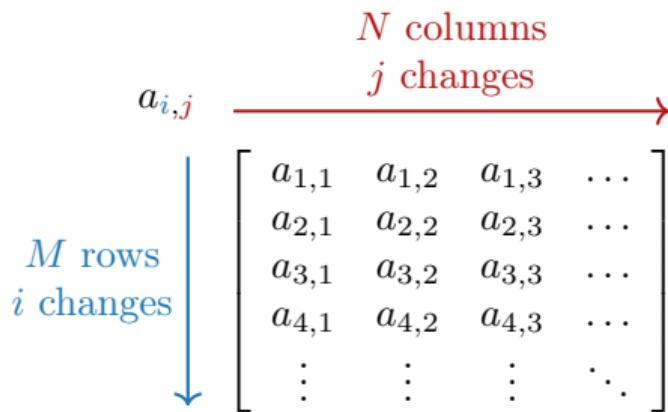
- ▶ Command History window stores all commands from the Command Window.
- ▶ Command History is accessible through ↑ or ↓.
- ▶ it is possible to filter out past commands by, e.g.:
» A = [+ ↑.
- ▶ It is possible to copy-and-paste entire Command History:
SHIFT / CTRL / CTRL + A → CTRL + C.



Matrices in MATLAB

- ▶ Matrix is a basic data structure in MATLAB.
- ▶ There are following variables types depending on size:
 - ▶ scalar: 1×1
 - ▶ vector: $M \times 1$ or $1 \times N$
 - ▶ matrix: $M \times N$
 - ▶ array (multidimensional matrices):
 $M \times N \times P \times Q \times R \times \dots$
- ▶ Matrices can be complex.
- ▶ It can contain text as well (beware the length).

- ▶ M -by- N matrix:





Matrix Creation

- ▶ Following techniques are available:
 - ▶ element-by-element entering (suitable for small matrices only),
 - ▶ colon notation “:” to define elements of series,
 - ▶ generation by built-in functions,
 - ▶ generation of matrices in m-files,
 - ▶ import and export from/to external files(.mat, .txt, .xls, ...).



Matrix Construction Element-by-element I.

- ▶ Test following commands to construct matrices by element enumeration.
 - ▶ Suitable for small matrices only.

```
>> a1 = -1
```

```
>> v1 = [-1 0 1]
```

```
>> v2 = [-1; 0; 1]
```

```
>> M1 = [-1 0 1; -2 0 2]
```

```
>> M2 = [-1 -2; 0 0 ; 1 2]
```

```
>> M3 = [[-1 -2]; [0 0]] % inner brackets are redundant
```

$$a_1 = a_2 = -1$$

$$\mathbf{v}_1 = \begin{bmatrix} -1 & 0 & 1 \end{bmatrix}$$

$$\mathbf{v}_2 = \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix}$$

$$\mathbf{M}_1 = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \end{bmatrix}$$

$$\mathbf{M}_2 = \begin{bmatrix} -1 & -2 \\ 0 & 0 \\ 1 & 2 \end{bmatrix}$$

$$\mathbf{M}_3 = \begin{bmatrix} -1 & -2 \\ 0 & 0 \end{bmatrix}$$



Matrix Construction Element-by-element II.

- ▶ Construct following matrices:
 - ▶ Matrix values are defined inside square brackets [],
 - ▶ semicolon “;” separates individual rows of a matrix.

$$\mathbf{A} = \begin{bmatrix} -1 & -1 \\ 1 & -1 \end{bmatrix} \quad \mathbf{B} = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$



Matrix Construction

- ▶ Semicolon placed at the end of a command suppresses display of the output in Command Window.

```
>> a = 1  
>> b = 5;
```

- ▶ When there is more than one command on the same line, comma is used to separate each of the commands.

```
>> a = 1, b = 5  
>> a = 1; b = 5;
```

- ▶ Note: it is possible to copy and paste code including “»”
- ▶ Row vs column vector:

```
>> c = [1 0 0]  
>> d = [0; 0; 1]
```



Basic Math Operators I.

- ▶ Operator types:
 - ▶ arithmetics:
 - ▶ matrix,
 - ▶ vector,
 - ▶ relational,
 - ▶ logical and other (to be mentioned later ...).
- ▶ Other operations using MATLAB functions:
 - ▶ complex conjugate,
 - ▶ sum, determinant, square root,
 - ▶ and hundreds of other functions ...

+	addition
-	subtraction
*	multiplication
^	power
.'	transpose
\	left matrix division
/	right matrix division
.	dot notation



Operator Precedence in MATLAB

- ▶ According to the following table:
 - ▶ see MATLAB → Language Fundamentals → Operators and Elementary Operations → Arithmetic

1	parentheses	()
2	transpose, power	' . ' ^ . ^
3	unary plus, unary minus, logical negation	+ - ~
4	multiplication, division	* . * / \ . / . \
5	addition, subtraction	+ -
6	colon operator	:
7	relation operators	< > <= >= == ~=
8	logical AND (element-wise)	&
9	logical OR (element wise)	
10	logical AND (short-circuit)	&&
11	logical OR (short-circuit)	



Basic Math Operators II.

- ▶ Type in following commands:
 - ▶ Zero can be omitted with a decimal number beginning with zero (not recommended).

```
>> a3 = -2/4  
>> a4 = -0.5  
>> a5 = -.5
```

- ▶ What is the difference between a_3 , a_4 and a_5 ?
- ▶ Beware the precedence of operators (we see in the next slides):

```
>> 3*5*6  
>> a1 = 15  
>> a2 = 10;  
>> a2/a3  
>> a2/a3*a4  
>> a2/ (a3*a4)
```

- ▶ Explain the difference between $a2/a3*a4$ and $a2/ (a3/a4)$.
- ▶ Verify the rules of operator precedence from the previous slide.



Lengthy commands in MATLAB

- ▶ It is suitable to structure command blocks for clarity:

- ▶ next line: SHIFT + ENTER

```
>> A = [1 1 1]; B = [2 2 2]; % SHIFT + ENTER  
C = [2 3 2];
```

- ▶ Three dots notation:

- ▶ For continuation of the same command on the next line.
 - ▶ Compare results:

```
>> A1 = [ 1 1 ...  
2 3]
```

```
>> A2 = [ 1 1  
2 3]
```



Basic Math Functions I.

- ▶ Math functions in MATLAB are generally divided in three groups:

- ▶ **Scalar:**

- ▶ Function operates over individual elements of a matrix,
 - ▶ *e.g.: sin, sqrt, log, factorial.*

- ▶ **Vector:**

- ▶ Function operates over individual rows/columns of a matrix,
 - ▶ *e.g.: sum, max.*

- ▶ **Matrix:**

- ▶ Function operates over a whole matrix,
 - ▶ *e.g.: det, trace.*



Basic Math Functions II.

- ▶ Using MATLAB help, calculate the following expression: $a \sin^2(\alpha) + a \cos^2(\alpha) - a$
 - ▶ Use numerical values your own choice.
- ▶ Verify following logarithmic identity: $\log_{10}(a) + \log_{10}(b) - \log_{10}(ab) = 0$
- ▶ Find sum of all elements in individual rows of the following matrix:

$$T = \begin{bmatrix} \frac{1}{2} & \frac{1}{3} & \frac{1}{4} & \frac{1}{5} \\ 6 & 7 & 7 & 9 \\ 0.2 & 0.3 & 0.4 & 0.5 \end{bmatrix}$$



Basic Math Functions III.

- ▶ Assume following vectors $\mathbf{u} = (1, 2, 3)$ and $\mathbf{v} = (3, 2, 1)$.

- ▶ Calculate:

$$\mathbf{u}\mathbf{v}^T \quad \mathbf{v}\mathbf{u}^T$$

$$\mathbf{v}^T\mathbf{u} \quad \mathbf{u}^T\mathbf{v}$$

$$\mathbf{u} \cdot \mathbf{v} \quad \mathbf{u} \times \mathbf{v}$$

$$\mathbf{A} = \begin{bmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{bmatrix}$$

$$\mathbf{A}^T = \begin{bmatrix} 1 & 3 & 5 \\ 2 & 4 & 6 \end{bmatrix}$$

- ▶ Following functions are needed:

- ▶ transpose ('.') of a matrix,
 - ▶ dot scalar product,
 - ▶ cross product.

- ▶ What is the result of the above mentioned operations?



Matrix Division in MATLAB

- ▶ Two cases are distinguished:
 - ▶ **left** division (`\` – `mldivide`),
 - ▶ **right** division (`/` – `mrdivide`).
- ▶ Solution of a linear system of equations:
 - ▶ **A** is an invertible (regular) matrix,
 - ▶ **b** is a column (row) vector.

$$\begin{matrix} \textcolor{blue}{A} \\ \textcolor{green}{x} \end{matrix} = \textcolor{red}{b}$$

$$\mathbf{Ax} = \mathbf{b}$$

$$\mathbf{x} = \mathbf{A}^{-1}\mathbf{b}$$

$$\begin{matrix} \textcolor{green}{x} \\ \textcolor{blue}{A} \end{matrix} = \textcolor{red}{b}$$

$$\mathbf{x}\mathbf{A} = \mathbf{b}$$

$$\mathbf{x} = \mathbf{b}\mathbf{A}^{-1}$$

```
>> x = A \ b
```

```
>> x = b / A
```



Basic Math Functions IV.

- ▶ Find the sum of diagonal elements (trace of a matrix) of the matrix **T** with elements coming from normal distribution with mean equal to 10 and standard deviation equal to 4.
- ▶ Find determinant of matrix **U**.

$$\mathbf{U} = \begin{bmatrix} 1 & 2 & 3 \\ 0 & 2 & 0 \\ 0 & -2 & -1 \end{bmatrix}$$

```
>> T = 10 + 4*randn(7, 7);
```

```
>> U = [1 2 3; 0 2 0; ...
0 -2 -1];
```

- ▶ Solve the linear system of equations:

$$x_1 + 2x_2 + 3x_3 = 6$$

$$\mathbf{Ax} = \mathbf{b}$$

$$4x_1 + 5x_2 + 6x_3 = 15$$

$$\mathbf{x} = \mathbf{A}^{-1}\mathbf{b}$$

$$7x_1 + 8x_2 + x_3 = 16$$



Predefined Values in MATLAB

- ▶ MATLAB contains several predefined values:
 - ▶ `eps` – precision of single/double numbers (Determines the shortest distance between two single/double numbers).
 - ▶ `ans` – *answer* – most recent answer.
 - ▶ `NaN` – *not a number* (every expression containing `NaN` is `NaN`)
 - ▶ `NaN` can be used advantageously in some cases.
 - ▶ `Inf` – *infinite number* (variable `Inf` can be used in calculation:)
 - ▶ Pay attention to `Inf` propagation throughout your code (use allowed operations only).
 - ▶ `i`, `j` – complex unit.
 - ▶ They are all basically functions (without input parameter).
- ▶ Check results of the following expressions:

```
>> t1 = 10/0    % t1 = Inf
>> t2 = 0/0    % t2 = NaN
>> t3 = t1*5    % t3 = Inf
>> t4 = t1 + t2 % t4 = NaN
```

- ▶ `pi`, `intmin`, `intmax`, `realmin`, `realmax`, ... (functions)



Format of Command Line Output

- ▶ Up to now we have been using basic setup.
- ▶ MATLAB offers number of other formatting options
 - ▶ Use `format style`.
 - ▶ Output format does not change neither the computation accuracy nor the accuracy of stored results (`eps`, `realmax`, `realmin`, ... still apply).

<code>style</code>	format description
<code>short</code>	fixed 4 decimal points are displayed
<code>long</code>	15 decimal points for double precision, 7 decimal points for single precision
<code>shortE</code>	floating-point format (scientific notation)
<code>longE</code>	-//-
<code>bank</code>	two decimal points only (eur – cents)
<code>rat</code>	MATLAB attempts to display the results as a fraction
<code>compact</code>	suppressed the display of blank lines
and others...	note: omitting <code>style</code> parameter restores default setup



Format of Command Line Output

- ▶ Try following output format settings:
 - ▶ Each format is suitable for different type of problems.

```
>> s = [-5 1/2 1/3 10*pi sqrt(2)];  
>> format long; s  
>> format rat; s  
>> format bank; s  
>> format hex; s  
>> format +; s  
>> format; s
```

- ▶ There exist other formats with slight differences.
 - ▶ Check doc `format`
- ▶ Later, we will learn how to use formatted conversion into strings (commands `sprintf` and `fprintf`).



Complex Numbers I.

- ▶ More entry options in MATLAB.

```
>> C1 = 1 + 1j % prefered
>> C2 = 1 + 5i % prefered
>> C3 = 1 + 5*i % NO!
>> C4 = sqrt(-1)
>> C5 = complex(1, 2)
>> C6 = 1e1i
>> C7 = exp(1j*pi/4)
```

- ▶ Frequently used functions:

real, imag	real and imaginary part of a complex number
conj	complex conjugate
abs	absolute value of a complex number
angle	angle in complex plane [rad]
complex	constructs complex number from real and imaginary components
isreal	checks if the input is a complex number (more on that later)
i, j	complex unit
cplxpair	sort complex numbers into complex conjugate pairs



Complex Numbers II.

- ▶ Create complex number $z = 1 + 1j$ and its complex conjugate $s = z^*$.
- ▶ Switch between Cartesian and polar form (find $|z|$ and φ).

$$z = \operatorname{Re}\{z\} + \operatorname{Im}\{z\} = a + jb$$

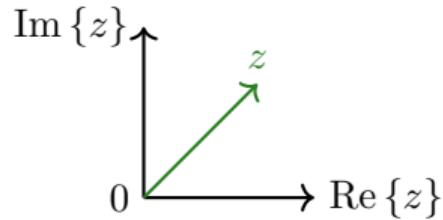
$$z = |z| e^{j\varphi}, |z| = \sqrt{a^2 + b^2}$$

$$z = |z| (\cos \varphi + j \sin \varphi)$$

- ▶ Verify Moivre's theorem:

$$z^n = (|z| e^{j\varphi})^n$$

$$z^n = |z|^n (\cos(n\varphi) + j \sin(n\varphi))$$



Exercises



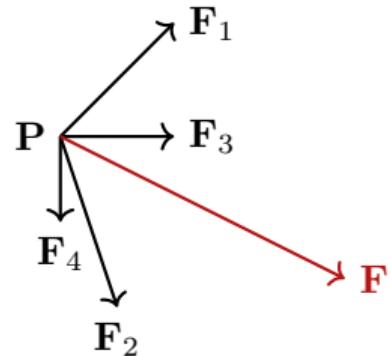
Exercise I.

- ▶ Following forces were localized at point **P** in *xy* plane:

$$\begin{array}{ll} \mathbf{F}_1 = [2, 2] & \mathbf{F}_3 = [2, 0] \\ \mathbf{F}_2 = [1, -3] & \mathbf{F}_4 = [2, -1.5] \end{array}$$

- ▶ What is the direction of the resultant force **F**?
- ▶ Normalize the resulting vector.

$$\mathbf{n}_F = \frac{\mathbf{F}}{|\mathbf{F}|} = \frac{\mathbf{F}}{\sqrt{F_x^2 + F_y^2 + F_z^2}}$$





Exercise II.

- ▶ Type-in following commands:

```
>> clear, clc;  
>> w1 = [1 2 3 4]  
>> w2 = [-2 -3 -4]  
>> w3 = [-2; -3; -4]  
>> w4 = w1^2, w5 = w2 - w1
```

- ▶ Compare differences.
- ▶ What is the cause of error in calculation of w4 and w5?
- ▶ Try also:

```
>> w3*3, w1 - 3  
>> w1 + [5 5 5 5]  
>> w6 = 5*w1 - [3 5 6] - w2
```

- ▶ Calculate the norm (magnitude) of vector w1.

- ▶ Try more options.

- ▶ How to modify the calculation in the case of a complex vector?



Exercise III.

- ▶ Calculate roots of the quadratic function:

$$-2x^2 - 5x = 3.$$

- ▶ First, rearrange the terms of the function.

$$2x^2 + 5x + 3 = 0 \Rightarrow a = 2, b = 5, c = 3$$

$$x_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-5 \pm \sqrt{25 - 24}}{4}$$
$$x_1 = -1, \quad x_2 = -\frac{3}{2}$$

- ▶ MATLAB provides particular function for calculation of roots a function, try to search it out.



Exercise IV.

- ▶ Think over how many ways there are to calculate the length of hypotenuse when two legs of a triangle are given.
 - ▶ Make use of various MATLAB operators and functions.
 - ▶ Consider also the case where the legs are complex numbers.



Exercise V.

- ▶ Create an arbitrary vector \mathbf{v} and rotate it around arbitrary angle α in xz plane using rotation matrix \mathbf{R} .

$$\mathbf{v}' = \mathbf{R}\mathbf{v}$$

$$\mathbf{R} = \begin{bmatrix} \cos \alpha & 0 & -\sin \alpha \\ 0 & 1 & 0 \\ \sin \alpha & 0 & \cos \alpha \end{bmatrix}$$



Exercise VI.

- ▶ Use the following code and round the resulting number to:

```
>> r = 1 + 10*rand(1)
```

- ▶ nearest integer,
- ▶ nearest integer greater than r ,
- ▶ nearest integer lower than r ,
- ▶ zero,
- ▶ zero with precision of 2 decimal digits.
- ▶ Find remainder after r is divided by 0.1.
 - ▶ *modulus vs. remainder after division*



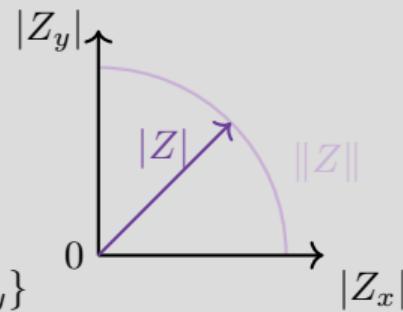
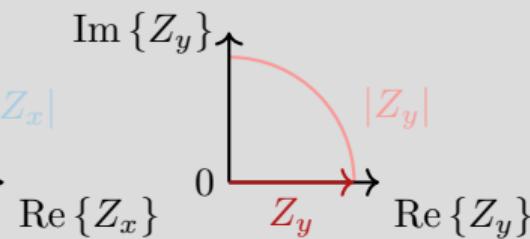
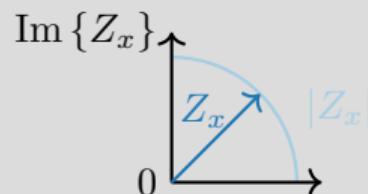
Exercise VII.

- ▶ Find out the magnitude of a complex vector (avoid indexing).
 - ▶ Use `abs` and `sqrt`.

$$\mathbf{Z} = \begin{bmatrix} 1 + 1j & \sqrt{2} \end{bmatrix}$$

$$\|\mathbf{Z}\| = ?, \quad \mathbf{Z} \in \mathbb{C}^2$$

- ▶ Alternatively, use following functions:
 - ▶ `norm`
 - ▶ `dot` (*dot product*)
 - ▶ `hypot` (*hypotenuse*)



Questions?

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