

Visibility Algorithms

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Outline

- Visibility in graphics
- Depth Buffer
- Ray Casting
- Painter's algorithm
- BSP Trees
- Warnock's Algorithm
- Specialized Visibility Algorithms

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Visibility - Introduction

- Points A,B visible ⇔ line segment AB does not intersect opaque object
- Example: visibility from a view point



Visibility in Computer Graphics

- Hidden surface removal
- Shadows
- Radiosity
- Ray Tracing
- Visibility culling
- Games / Multi-User Environments
- Streaming

Hidden surface removal

- Creating "correct" 2D image of 3D scene
 - Finding visible objects and their visible parts
 - Eliminating invisible objects and invisible parts





Visibility algorithms

- Raster algorithms (image space)
 - Solve visibility for pixels
 - For each pixel
 - Find nearest object projected to pixel
 - Shade the pixel using object color
 - Algorithms: z-buffer, ray casting, painters alg.
- Vector algorithms (object space)
 - Vector based description of visibility
 - For each object
 - Find object parts not hidden by others
 - Draw visible/invisible parts
 - Algorithms: Naylor, Weiler-Atherton, Roberts
 - CAD systems, technical drawings, special applications

Complexity: O(P.N)

P .. #pixels N .. #objects

Complexity: O(N²)

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Depth buffer (Z-buffer)

- Ed Catmull 1975
 - Co-founder and president of Pixar
- Wolfgand Strasser 1975
- For each pixel depth of the nearest object
- Process objects in arbitrary order
- 1. Rasterize to fragments
- 2. Compare depth of each fragment with z-bufer content
- 3. If closer overwrite z-buffer and pixel color





Depth buffer – pseudocode

Two arrays: z_buffer, color_buffer

```
Clear color_buffer;
Set z-buffer to "infinity";
for (each object) {
  for (each object pixel P[x,y]) {
   if (z-buffer[x,y] > P[x,y].depth) {
      z_buffer[x,y] = P[x,y]. depth;
      color_buffer[x,y] = P[x,y].color;
```

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Depth buffer - details

- Computing pixel depth interpolation
- Linear interpolation of z" ~ 1/z (z" device coordinates)
- For perspective projection depth resolution is non-uniform
 - Nearer objects have higher depth resolution



z-fighting when rendering farther objects

Perspective projection - OpenGL





Depth distributions in z-buffer

- Careful setting of near-far planes
 - near = 1 / far = 10 : 50% between 1.0 a 1.8
 - near = 0.01 / far = 10 : 90% between 0.01 0.1
 - Median = 2*near*far/(near + far)



Depth Precision Issues - Example



Depth Precision Issues - Example



Resolving Z-fighting

- Careful settings of near(!) and far planes
- Rendering close and far objects
 - Several passes, updating near/far
 - combine using stencil
- W-buffer
 - stores eye space z, linear depth distribution
 - reciprocal of z_i' for each pixel
- Reverse z
 - Lapidous and Jiao. Optimal depth buffer for low-cost graphics hardware. HWWS '99.
 - https://developer.nvidia.com/content/depth-precision-visualized

Reverse Z



Perspectively correct interpolation

- LERP in screen space
 - non linear in object space (hyperbola) !
- Solution for color
 - Compute c'=c/z and z' = 1/z
 - LERP of c' and z'
 - For each pixel $c_i = c_i'/z_i'$
- The same for texture coordinates u, v (!)
- Note: OpenGL stores 1/z in w' component after persp. divide
 - Compute w' = 1/z and c'=c*w'
 - LERP of c' and w'
 - For each pixel $c_i = c_i'/w_i'$



Depth buffer - properties

- Benefits
 - Simplicity
 - No preprocessing or sorting
 - Easy parallelization and HW implementation
- Issues
 - Pixel overdraw
 - Mapping depth to z-buffer bit range
 - Transparent objects
 - Alias

Quiz – number of overdraws

- 10 polygons project to pixel in random order
- What is the average number of overdraws?



Intuitive answer

- Front-to-back 1x, back-to-front 10x
- So the average is 5.5 overdraws



Correct answer

- The first polygon must cause overdraw: 1
- The second is either back or front
 - Chance of overdraw: 1/2
- Third polygon
 - 1/3 chance that it is the closest and causes overdraw
- Harmonic series: 1 + 1/2 + 1/3 + ... + 1/10 = 2.9289

1 poly	1x	
4 polys	2.08x	
11 polys	3.02x	
31 polys	4.03x	
83 polys	5.00x	
12,367 polys	10.00x	

Aproximation for big N overdraw(N) = ln(N) + 0.57721



Depth buffer in OpenGL

- glutInitDisplayMode (... | GLUT_DEPTH | ...);
- glEnable(GL_DEPTH_TEST);
- glDepthFunc(GL_LESS);
- glClear(GL_DEPTH_BUFFER_BIT);
- glDepthMask(mask);
 - GL_TRUE read/write
 - GL_FALSE read only

Depth buffer and transparent objects

- Draw all non-transparent objects using z-buffer
- Sort all transparent objects back-to-front
- Render transparent objects with alfa-blending
 - OpenGL:
 - glDepthMask(GL_FALSE);
 - glBlendFunc(gl.ONE, gl.ONE_MINUS_SRC_ALPHA);
 - glEnable(GL_BLEND);
- Depth peeling
 - Iterative rendering layer by layer
 - Additional depth check: if z(current_layer) >= z(prev_layer) -> cull
 - Use "shadow test + alpha test" (Everitt 2001)

Alpha blending – Over & Under operator

- C=(r, g, b, α)
- α opacity
 - $\alpha = 0$ transparent
 - $\alpha = 1$ opaque



$$C = \alpha_s C_s + (1 - \alpha_s) C_d$$
 s over d

$$C = \alpha_s (1 - \alpha_d) C_s + \alpha_d C_d \qquad \text{s under d} \alpha = \alpha_s (1 - \alpha_d) + \alpha_d$$

- Should we draw back to front or front to back? And should we care?
- How to increase depth resolution?
- When to perform the depth test?
- How to handle transparent objects?

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Ray casting

- Cast ray for each image pixel [Appel68]
- Find the nearest intersection with scene object



- Complexity
 - Naive: *O*(*R*.*N*)
 - With spatial data structure: $O(R \cdot \log N)$

Accelerated ray casting

- Step 1: construct spatial DS
 - Preprocessing
 - BVH, kD-tree, octree, 3D grid
- Step 2: find the nearest intersection
 - Walk through cells intersected by the ray
 - Intersection found: terminate



Ray Casting – Generating (Primary) Rays

- Implicit camera parameters
 - MVP matrix inversion
- Explicit knowledge of camera parameters
 - position (o), view direction (v), up vector (u), view angle (0)

 Compute view coordinate system: a, s, t
 Ray through pixel x, y (image size width x height): ray_origin = o; ray_dir = Normalize(a + x/width*s + y/height*t - o);



Ray casting - properties

- Benefits
 - Flexibility (adaptive raster, ray tracing)
 - Efficient culling of occluded objects
- Drawbacks
 - Lower use of coherence
 - Requires spatial DS
 - Issue for dynamic scenes and HW implementation

Z-buffer vs. Ray Casting

	Scan-line coherence	Requires preprocessing	Efficient handling of occluded objects
Z-buffer	yes +	no +	no -
Ray casting	no -	yes -	yes +

Z-buffer better for dynamic scenes with low occlusion

Ray casting better for complex highly occluded scenes

Z-buffer GPU optimizations

- Z-cull
 - z_{min} , z_{max} for 8x8 pixel blocks
 - If $tri_{zmin} > tile_{zmax}$ discard
- Early-z test (for each pixel)
 - Apply z-test before shader execution
 - On newer GPUs used by default
 - Switched off when modifying "z" in shader
- HW occlusion queries, conditional rendering

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Painter's algorithm

- Rendering back to front
- Farther patches overwritten by closer ones
- Used in 2D drawing tools (layers)
- In 3D without explicit ordering more complicated
- Depth sort algorithm [Newell72]

Depth Sort Painter's algorithm

- Sort patches using zmax of each patch
- Farthest patch = candidate for rendering (P1)
- Series of tests to confirm the candidate using remaining patches

Depth Sort Painter's algorithm – cont.



Tests failed: swap (P2 = new candidate)

Cycle of candidates

- Can be detected using counter for candidate
- Solved by cutting the patch



Painter's algorithm - properties

Benefits

- No depth buffer needed
- Simplified version: easy implementation
- Issues
 - Overdraw
 - Correct depth order
 - Self intersections of patches not allowed

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Binary Space Partitioning (BSP)

- View independent sorting of the scene [Fuchs80]
- Two phases
 - BSP tree construction (1x)
 - Tree traversal and rendering (as painter's alg.)

BSP Tree Construction

- Recursive splitting by planes
- Planes typically defined using scene polygons



```
void RenderBSP (Node S)
if (camera in front of S.plane) {
      RenderBSP (S.back);
      Render(S.polygons);
      RenderBSP (S.front);
else {
      RenderBSP (S.front);
      Render(S.polygons);
      RenderBSP (S.back);
```

BSP tree and Z-buffer

- Reduce number of overdraws
- Traverse front-to-back (reverse order compared to painter's alg.)
- Alternatives to BSP tree
 - kD tree, octree, BVH

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Image Subdivision – Warnock's alg.

- Recursive fast rectangle clipping tests
- Recursion terminates in pixel /subpixel



Divide and Conquer [Warnock69]

- 1. No object: *background color*
- 2. One object: render
- 3. More objects, one closest: render closest
- 4. Recursively subdivide

Scan-line Algorithms

- Sort primitives by scan lines (Y)
- Compute spans: intersections of primitives and scan lines
- Elementary spans: intersection of spans
- Sort elementary spans (X)
- Find the closest object for each elementary span (Z)
- [Watkins70]
 - Bubble sort for X and Y
 - O(log n) search for Z

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Back-face Culling

- Eliminates ~ 50% polygons
- If d*n > 0 : cull
- In NDC: just check for sign of n'z
 - Computed from transformed vertices (not shading normal)

OpenGL:
 glFrontFace(GL_CCW);
 glCullFace(GL_FRONT);
 glEnable(GL_CULL_FACE);



Direct rendering of CSG models

- Specialized ray casting
- Intervals of ray/object intersections
- Solving set operations = set operations on intervals



Floating horizon algorithm

- Graphs of functions z = (x,y)
- Terrains (height field)
- Algorithm outline
 - Render front-to-back
 - Keep bottom and top horizon



A-Buffer

- Antialiasing, correct transparency
 - [Carpenter84], Lucasfilm: "The Road To Point Reyes"
 - Later used in RenderMan (Pixar)
- Ordered list of primitives for each pixel
- Storing not just depth
 - transparency, coverage, object ID, normal,...
- Polygon rasterization
 - Non-transparent polygon covers the whole pixel add to list and **remove** farther ones
 - Transparent polygon or partial pixel coverage insert to list, **do not remove** farther ones



- Rendering pass
 - For each pixel process the list front-to-back
 - Composition (subpixel rasterization, coverage mask 4x4)
 - Similar to MSAA



- Benefits
 - More general than z-buffer
 - Used in production rendering
 - Handles transparency

Loren Carpenter. 1984. The A -buffer, an antialiased hidden surface method. SIGGRAPH '84.

Other buffers...

A-buffer - Carpenter, 1984 G-buffer - Saito & Takahashi, 1991 M-buffer - Schneider & Rossignac, 1995 P-buffer - Yuan & Sun, 1997 T-buffer - Hsiung, Thibadeau & Wu, 1990 W-buffer - 3dfx, 1996? Z-buffer - Catmull, 1973 (?) ZZ-buffer - Salesin & Stolfi, 1989

Accumulation Buffer - Haeberli & Akeley, 1990 Area Sampling Buffer - Sung, 1992 Back Buffer - Baum, Cohen, Wallace & Greenberg, 1986 Close Objects Buffer - Telea & van Overveld, 1997 Color Buffer Compositing Buffer - Lau & Wiseman, 1994 Cross Scan Buffer - Lau & Wiseman, 1994 Delta Z Buffer - Yamamoto, 1991 Depth Buffer - 1984 Depth-Interval Buffer - Rossignac & Wu, 1989 Double Buffer - 1993

Escape Buffer - Hepting & Hart, 1995 Frame Buffer - Kajiya, Sutherland & Cheadle, 1975 Hierarchical Z-Buffer - Greene, 1993 Item Buffer - Weghorst, Hooper & Greenberg, 1984 Light Buffer - Haines & Greenberg, 1986 Mesh Buffer - Deering, 1995 Normal Buffer - Curington, 1985 Picture Buffer - Ollis & Borgwardt, 1988 Pixel Buffer - Peachey, 1987 Ray Distribution Buffer - Shinya, 1994 Ray-Z-Buffer - Lamparter, Muller & Winckler, 1990 Refreshing Buffer - Basil, 1977 Sample Buffer - Ke & Change, 1993 Shadow Buffer - GIMP, 1999 Sheet Buffer - Mueller & Crawfis, 1998 Stencil Buffer - 1997? Super Buffer - Gharachorloo & Pottle, 1985 Super-Plane Buffer - Zhou & Peng, 1992 **Triple Buffer** Video Buffer - Scherson & Punte, 1987 Volume Buffer - Sramek & Kaufman, 1999

Source: Eric Haines - Is the Hardware Z-Buffer Doomed?

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Questions?

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