Lecture 11: Set Operations, Data Treatment (I/O)

B0B17MTB, BE0B17MTB – MATLAB

Miloslav Čapek, Viktor Adler, Michal Mašek, and Vít Losenický

Department of Electromagnetic Field
Czech Technical University in Prague
Czech Republic
matlab@fel.cvut.cz

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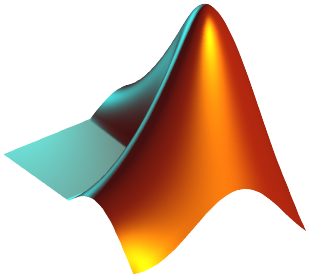
Outline



Set Operations

- There exist following operations (operators) in MATLAB applicable to arrays or individual elements:
  - arithmetic (part #1),
  - relational (part #3),
  - logical (part #3),
  - set (part #11),
  - bit-wise (`>> doc bit-wise`).
- Set operations are applicable to vectors, matrices, arrays, cells, strings, tables,...
- Mutual sizes of these structures are usually not important.

Function	Description
`intersect`	intersection of two sets
`union`	union of two sets
`setdiff`	difference of two sets
`setxor`	exclusive OR of two sets
`unique`	unique values in a set
`sort`	sorting
`sortrows`	row sorting
`ismember`	is an element member of a set?
`issorted`	is a set sorted?

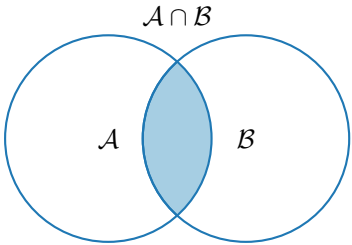
Set Operations: intersect and union

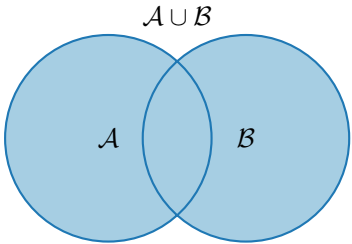
- Intersection of sets: `intersect`.
  - Example: intersection of a matrix and a vector:

```
>> A = [1 -1; 3 4; 0 2];
>> b = [0 3 -1 5 7];
>> c = intersect(A, b)
% c = [-1; 0; 3]
```

- Union of sets: `union`.
  - Example: All set operations can be carried out row-wise (in that case the number of columns has to be observed):

```
>> A = [1 2 3; 4 5 1; 1 7 1];
>> b = [4 5 1];
>> C = union(A, b, 'rows')
% C = [1 2 3; 1 7 1; 4 5 1]
```





Set Operations: `setdiff` and `setxor`

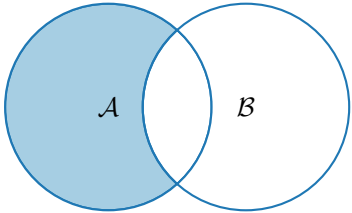
- Intersection of a set and complement of another set: `setdiff`.
  - Example: All set operations return more than one output – we get the elements as well as the indexes:

```
>> A = [1 1; 3 NaN];
>> B = [2 3; 0 1];
>> [C, ai] = setdiff(A,B)
% C = NaN, ai = 4, i.e.: C = A(ai)
```

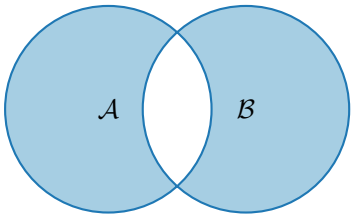
- Exclusive intersection (XOR): `setxor`.
  - Example: All set operations can be carried out either as `'stable'` (not changing the order of elements) or as `'sorted'`:

```
>> A = [5 1 0 4];
>> B = [1 3 5];
>> [C, ia, ib] = setxor(A, B, 'stable')
% C = [0 4 3], ia = [3; 4], ib = [2]
```

$\mathcal{A} \setminus \mathcal{B} = \mathcal{A} \cap \mathcal{B}^c$



$\mathcal{A} \oplus \mathcal{B} = \overline{\mathcal{A} \cap \mathcal{B}}$



Set Operations: unique

- Selection of unique elements of an array: `unique`.
  - Example: Set operations are also applicable to arrays not (exclusively) containing numbers:

$$\begin{bmatrix} c & b & a & d \\ a & c & b & a \\ c & c & d & b \end{bmatrix} \subseteq \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix}$$

```
>> A = {'Joe', 'Tom', 'Sam'};
>> B = {'Tom', 'John', 'Karl', 'Joe'};
>> C = unique([A B])
% C = {'John', 'Karl', 'Joe', 'Sam', 'Tom'}
```

- It is possible to combine all above mentioned techniques.
  - Example: Row-wise listing of unique elements of a matrix including indexes:

```
>> A = round(rand(10, 3)).*mod(10:-1:1, 3)'
>> [C, ai, ci] = unique(sum(A, 2), 'rows', 'stable')
```

  - Interpret the meaning of the above code? Is the `rows` parameter necessary?

Set Operations I.

- Consider three vectors **a**, **b**, **c** containing natural numbers $x \in \mathbb{N}$ so that:
  - vector **a** contains all primes up to (and including) 1000,
  - vector **b** contains all even numbers up to (and including) 1000,
  - vector **c** is complement of **b** in the same interval.
- Find vector **v** so that $\mathbf{v} = \mathbf{a} \cap (\mathbf{b} + \mathbf{c})$, and
- $\mathbf{b} + \mathbf{c} \equiv [b_i + c_i]$, $b_{i-1} < b_i < b_{i+1}$, $c_{i-1} < c_i < c_{i+1}$, $\forall i \in \{1, \ldots, 500\}$.
  - What elements does **v** contain?
  - How many elements are there in **v**?

```
v =
  Columns 1 through 18
     3     7    11    19    23    31    43    47    59    67    71    79    83   103   107   127   131   139
  Columns 19 through 36
   151   163   167   179   191   199   211   223   227   239   251   263   271   283   307   311   331   347
  Columns 37 through 54
   359   367   379   383   419   431   439   443   463   467   479   487   491   499   503   523   547   563
  Columns 55 through 72
   571   587   599   607   619   631   643   647   659   683   691   719   727   739   743   751   787   811
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   823   827   839   859   863   883   887   907   911   919   947   967   971   983   991
ans =
    87
```

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Set Operations II.a

- Estimate the result of the following operation (and verify using MATLAB):

$$\mathbf{w} = (\mathbf{b} \cup \mathbf{c}) \setminus \mathbf{a}.$$

  - What is specific about elements of the resulting vector $\mathbf{w}$?

- With the help of logical indexing and mathematical functions determine how many elements of $\mathbf{w}$ are divisible by 3.

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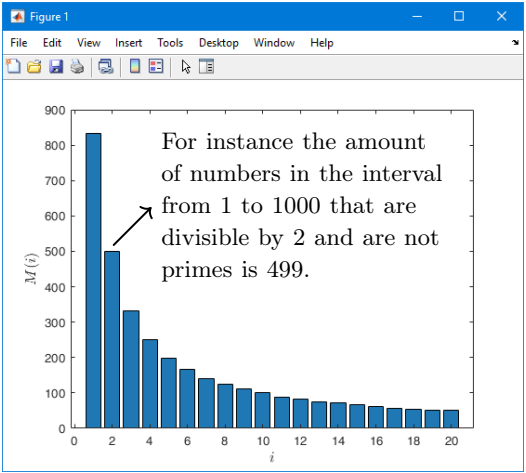
Set Operations II.b

- Write previous exercise as a script:

```
%% script depicts number of integers from 1 to 1000 in
% dependence on division remainders
clear; clc;
N = 1000;
a = primes(N);
b = 2:2:N;
c = setdiff(1:N, b);
w = setdiff(union(b, c), a);
% ...
   m = sum(not(mod(w, 3)));
% ...
```

- Modify the script in the way to calculate how many elements of **w** are divisible by numbers 1 to 20.
  - Use for instance `for` loop to get the result.
  - Plot the results using `bar` function.

Set Operations II.c



Set Operations III.a

- Radio relay link operates at frequency of 80 GHz at 20 km distance with 64-QAM modulation.
  - Phase stability of $\pm 0.5°$ is required for sufficiently low bit error rate without using synchronization and coding.
  - That corresponds to the change of distance between antennas equal to $\pm 5\,\mu$m.
  - The statistics of link distance with normal distribution containing 10^6 elements can be generated as:

```
L = 20e3; % length of path
deviation = 5e-6; % standard deviation
N = 1e6; % number of trials
distances = L + randn(1, N)*deviation; % random distances
```

- How many times is the distance `L` contained in the vector `distances`?
- How many unique elements are there in `distances`?
- Can the distribution be considered continuous?

Catching Errors I.

- Used particularly in the cases where unexpected event can occur:
  - in general operations with files (reading, saving),
  - evaluation of encapsulated code (function `eval`, `assignin`),
  - working with variables, properties of which (*e.g.*, size) is not yet known,
  - evaluation of code related to an object that may not exist anymore (GUI).

```
try
   % regular piece of code
catch
   % code that is evaluated if the regular code failed
end
```

- It is possible (and is recommended) to use an identifier of the error.

Catching Errors II.

- Error identifier can be used to decide what to do with the error.
  - Example: In the case of multiplication error caused by different size of vectors, it is possible to display a warning.
  - Also, the error can be later raised again either by evoking the last error occurred or as a new error with its own identifier.

```
try
    A = [1 1 1];
    B = [1 1];
    c = A.*B;
catch exc
    if strcmp(exc.identifier, 'MATLAB:dimagree')
        disp('Mind the vector size!');
    end
    % throw(exc); % local stack shown
    % rethrow(exc); % complete stack shown
end
```

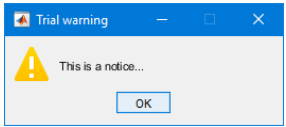
Warning Message in MATLAB

- Warning message in MATLAB is displayed using function `warning`.

```
a = 1e3;
if a > 1e2
   warning('Input coefficient has to be smaller than 10!');
end
```

  - The function is used by MATLAB, therefore, it is possible to temporarily deactivate selected internal warnings.
- Function `lastwarn` returns last warning activated.
- It is advantageous to use function `warndlg` with GUI (it just show a window, not throws the warning).

```
f = warndlg('This is a notice..', ...
   'Trial warning', 'modal');
```



Error Message in MATLAB

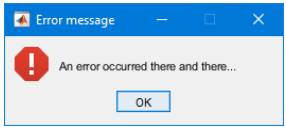
- Error message (in red color) is displayed using function `error`.

```
a = 100;
if a > 10
   error('Input has to be equal of smaller than 10!');
end
```

  - Terminates program execution.
  - Identifier can be attached.

- It is advantageous to use function `errordlg` with GUI (it just show a window, not throws the error).

```
f = errordlg('An error occurred there and there..',
...
   'Error message', 'modal');
```



Launching External Programs

- Rarely used.

- External programs are launched using the exclamation mark (`!`).
  - The whole line after the "!" is processed as operation system command:

```
>> !calc
```

  - If you don't want to interrupt execution of Matlab by the launch, add "&":

```
>> !calc &
>> !notepad notes.txt &
```

  - It is possible to run Matlab with several ways:

```
>> doc matlab Windows
>> doc matlab UNIX
```

Data Import and Export I.

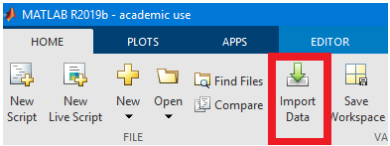
- Matlab supports wide range of file formats:
  - *e.g.*, `mat`, `txt`, `xls`, `jpeg`, `bmp`, `png`, `wav`, `avi`, and others,
  - for details see MATLAB → Data Import and Analysis → Data Import and Export → Supported File Formats for Import and Export.
  - Packages exist for work with, for instance, `dwg` and similar formats.
  - It is possible to read a general file containing ASCII characters as well.

- In this course we shall see how to:
  - read data from file, read image, read files line by line (see Lecture 6),
  - store in file, write in file,
  - import from Excel,
  - export to Excel.

Data Import and Export II.

- Following can be applied to whole group of formats:
  - `Home` → `Import Data`,
  - command `uiimport` and proceed with a following interface,
  - file drag and drop to MATLAB Workspace window.

- For storing in various formats see following functions.
  - `save`, `dlmwrite`, `xlswrite`, `imwrite`, `audiowrite`, ...



Functions cd, pwd, dir

- Function `cd` changes current folder:

```
cd FD % jumps into FD folder
cd   % lists current folder
cd .. % jumps up one directory
cd \  % jumps up to root
```

- Function `pwd` identifies current folder.
- Function `dir` lists current folder content.
- For other functions (`mkdir`, `rmdir`, ...) see MATLAB Documentation.

Completion/Parsing of File Paths: `fullfile`, `fileparts`

- Build full file name from parts with function `fullfile`,
  - *i.e.*, insert automatically correct separator (Windows: `\\`, Unix: `/`).
- Use whenever you work with paths.
- To get the correct separator for current platform use function `filesep`.

- Parse full path into file path, file name, and extension with function `fileparts`.

```
myPath = {'Data', 'Corrected'};
myFile = 'measuredData';
myExt  = '.mat';

f = fullfile(myPath{:}, [myFile myExt])

[myPath2, myFile2, myExt2] = fileparts(f)
```

```
f =
    'Data\Corrected\measuredData.mat'
myPath2 =
    'Data\Corrected'
myFile2 =
    'measuredData'
myExt2 =
    '.mat'
>>
```

Import from Excel

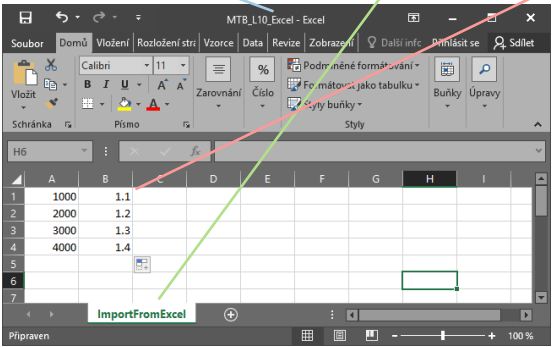
- Use function `xlsread` to import into Excel.
  - Alternatively, use aforementioned function `uiimport`.

```
Data = xlsread('MTB_L10_Excel.xlsx', 'ImportFromExcel', 'A1:B4')
```

file name

sheet

cells

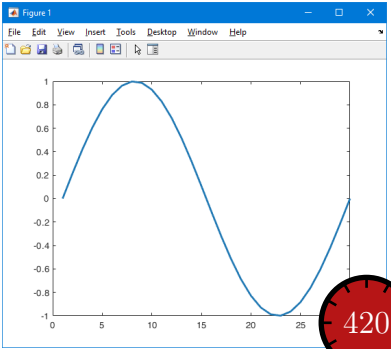



```
Data =
   1.0e+03 *
    1.0000    0.0011
    2.0000    0.0012
    3.0000    0.0013
    4.0000    0.0014
>>
```

Program Flow

Import from Excel

- Read all numerical data from Excel file `measurement1.xlsx` on course's webpage.
  - Thereafter, plot dependence of values in column `values` on values in column `experiment`.
  - Verify the size of data read.



Export to Excel

- Function `xlswrite` is used to export data from MATLAB to Excel.
  - Example: Write data `fx` in file `file.xlsx` in sheet `Sheet1` in line 1 starting with column `A`.

```
fx = 1:10;
xlswrite('file.xlsx', fx, 1, 'A1');
```

  - Example: Write data `fx` in file `file2.xlsx` in sheet `NewSheet` in column `B` starting with line 1.

```
fx = 1:10;
xlswrite('file2.xlsx', fx', 'NewSheet', 'B1');
```

Export to Excel

- Evaluate function

$$f(x) = \cos(x) + \frac{\cosh(x)}{10}$$

on the interval $x \in [-\pi, \pi]$ with step 0.01.

  - Resulting variables x and $f(x)$ write to file `Excel_file.xlsx` in the 1st sheet, variable x is in column `A`, variable $f(x)$ is in column `B`.
  - Verify whether data written in the sheet are correct.

Saving and Loading Binary Data (Reminder)

- Numerical data can be saved *en block*:
  - Notice the vector transposition.
  - `tsv` extension here because of Ti*k*Z.

```
x  = 0:0.01:2*pi;
fx = sin(x) .* cos(x).^2 + x.^(1/3);
Data = [x.' fx.'];
save('myData.tsv', 'Data', '-ascii');
```

- Load binary data from file line by line:

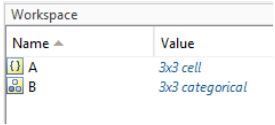
```
fid = fopen('myData.tsv');
while ~feof(fid)
  thisLine = fgetl(fid) % your data...
end
fclose(fid);
```

- Save binary data into file line by line:
- See also: Lecture 6.

```
fid = fopen('myData2.txt', 'w+');
Data = {'this if the first line', ...
   'this is the second line'};
for iLine = 1:length(Data)
   fprintf(fid, '%s\n', Data{iLine});
end
fclose(fid);
```

Data Type `categorical`

- Array of qualitative data with values from finite set of discrete non-numerical data.
  - Array of non-numerical values corresponding to a category (*e.g.*, to the category "mean of transport" correspond following values: `scooter`, `wheelbarrow`, ...).
  - Values can be specified by name (*e.g.*, values `'r'`, `'g'`, `'b'`, they can be an attribute for name `'red'`, `'green'`, `'blue'`).
  - `categorical` arrays has its own icon in MATLAB Workspace.



Creation of `categorical` Arrays

- Creation of `categorical` array from an arbitrary array of values (*e.g.*, cell array of strings):

```
A = {'r' 'b' 'g'; ...
    'g' 'r' 'b'; ...
    'b' 'r' 'g'} % cell array of strings
B = categorical(A) % categorical arrays
categories(B)     % listing of individual categories
```

- Wide range of tools for combining, adding, removing, renaming, arranging, ...
- For more see `>> doc categorical arrays`

```
A =

  3×3 cell array

    {'r'}    {'b'}    {'g'}
    {'g'}    {'r'}    {'b'}
    {'b'}    {'r'}    {'g'}

B =

  3×3 categorical array

     r        b        g
     g        r        b
     b        r        g

ans =

  3×1 cell array

    {'b'}
    {'g'}
    {'r'}
```

Advantages of `categorical` Arrays

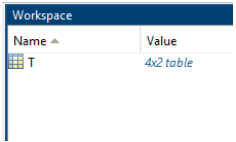
- More natural arranging of data by names.
  - Note: as in numerical arrays, logical operator `eq` (==) is used to compare strings in categorical arrays instead of function `strcmp()` used with strings.
- Mathematical arranging of strings.
  - Setting "size" in other than alphabetical manner (*e.g.*, `small < medium < large`):

```
allSizes = {'medium','large','small',...
        'small','medium','large',...
        'medium','small'};
valueset = {'small','medium','large'};
sizeOrd = categorical(allSizes, valueset, 'Ordinal', true);
comparison = sizeOrd > fliplr(sizeOrd)
```

- Memory is used efficiently to store data.
  - Data in memory is not stored as string.
  - Only categories are stored as string in memory.

Data Type `table`

- Array in form of a table that enables to have columns of various data types and sizes (similar to `cell` array).
  - Each column has to have the same number of lines (same as matrix).
  - Tables have its own icon in MATLAB Workspace.
- For more see `doc >> table`.



Creation of `table`

- Created by inserting individual vectors as columns of the table:

```
name = {'Miloslav'; 'Viktor'; 'Michal'; 'Vit'};
matlabSemester = [3; 3; 2; 1];
favoriteDrink = categorical({'b'; 'm'; 'w'; 'w'}, ...
    {'w'; 'm'; 'b'}, ...
    {'wine'; 'milk'; 'beer'});

T = table(matlabSemester, favoriteDrink, 'RowNames', name)
```

```
T =

  4×2 table

                matlabSemester    favoriteDrink
                ______________    _____________

    Miloslav          3             beer
    Viktor            3             milk
    Michal            2             wine
    Vit               1             wine

>>
```

Advantages of `table`

- Well-structured data,
- access to data via numerical and name indexing,
  - *e.g.*, listing all “Smiths” in the table and display their “age”,
- possibility to store metadata in table’s properties,
  - *e.g.*, for column “age” it is possible to set unit to “year”.

Questions?

B0B17MTB, BE0B17MTB – MATLAB

matlab@fel.cvut.cz

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