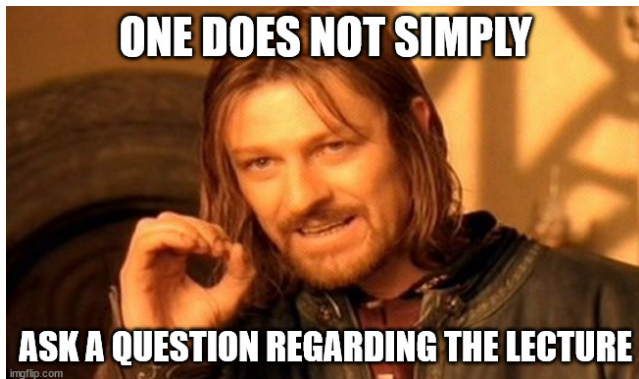


Landmark heuristics

Michaela Urbanovská

PUI Tutorial
Week 4

- Any questions regarding the lecture?



- 4 answers (yaaay!)
- Tempo of lectures + tutorials OK

LM-Cut Heuristic

- Relaxation heuristic
- Uses disjunctive operator landmarks
- Admissible (and actually very successful) heuristic

Disjunctive operator landmark

Disjunctive operator landmark $L \subseteq O$ is set of operators such that every plan π contains at least one operator $o \in L$.

Previously...

$$F = \{a, b, c, d, e, f, g\} \quad S_I = \{a, b\}$$

$$S_G = \{f, g\}$$

	pre	add	del	c
$O = O_1$	a	c, d	a	1
O_2	a, b	e	b	
O_3	b, e	d, f	a, e	
O_4	b	a	b	
O_5	d, e	g	e	

	a	b	c	d	e	f	g
Δ_1	0	0	1	1	1	1	1
			1	1	2	2	

	O_1	O_2	O_3	O_4	O_5
U	1	2	1	1	2
	0	1	1	0	1
		0	0		0

$$C = \{a, b, c, d, e, \underline{f}, \underline{g}\}$$

$$\begin{array}{l}
 k = a \quad O_1 \quad O_2 \\
 k = b \quad O_1 \quad O_3 \quad O_4 \\
 k = c \\
 k = d \quad O_5 \\
 k = e \quad O_3 \quad O_5
 \end{array}
 \begin{array}{l}
 \vdots \\
 \vdots \\
 \vdots \\
 \vdots \\
 \vdots
 \end{array}
 \begin{array}{l}
 k = f \\
 k = g
 \end{array}$$

$$h^{\max}(S_I) = 2$$

$$h^{\text{add}}(S_I) = 9$$

Delta function

- Function Δ_1 from previous tutorial:

- $\Delta_1(s, f) =$

$$\begin{cases} 0 & \text{if } f \in s, \\ \inf & \text{if } \forall o \in O : f \notin \text{add}(o), \\ \min\{c(o) + \Delta_1(s, o) \mid o \in O, f \in \text{add}(o)\} & \text{otherwise.} \end{cases}$$

Supporter of an operator

Supporter is a **fact**.

Function $supp(o) = \operatorname{argmax}_{f \in pre(o)} \Delta_1(s, f)$ maps each operator $o \in O$ to its **supporter**.

(s denotes the state where we compute the heuristic estimate)

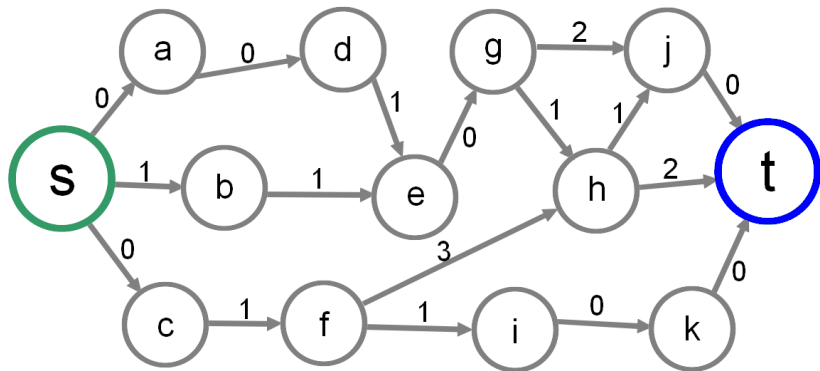
Justification graph

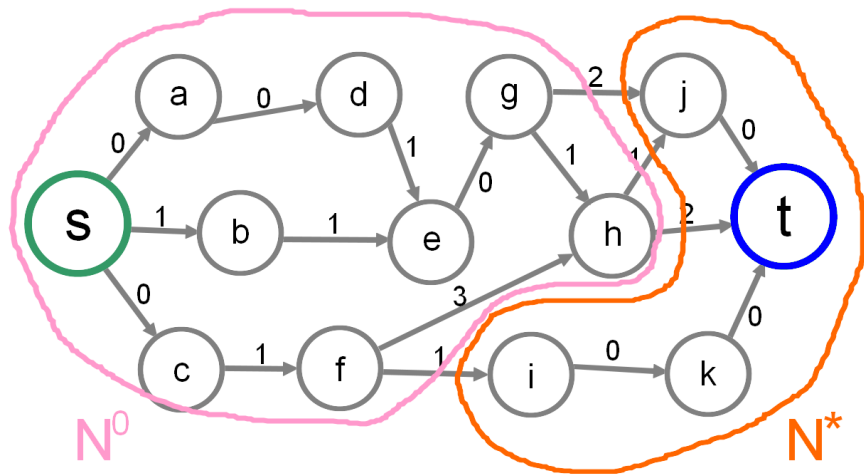
$G = (N, E)$ is a **directed labeled** multigraph.

- $N = \{n_f | f \in F\}$ (set of nodes)
- $E = \{(n_s, n_t, o) | o \in O, s = \text{supp}(o), t \in \text{add}(o)\}$ (set of edges)
- Edge $e = (a, b, l)$ denotes edge from a to b with label l

s-t cut

- **s-t cut** $C(G, s, t) = (N^0, N^* \cup N^b)$
- partitioning of nodes from the **justification graph** $G = (N, E)$
- N^* contains nodes from which t can be reached with zero-cost path
- N^0 contains nodes which can be reached from s without passing any node from N^*
- $N^b = N \setminus (N^0 \cup N^*)$ (*all the other nodes*)





Algorithm 2: Algorithm for computing $h^{\text{lm-cut}}(s)$.

Input: $\Pi = \langle \mathcal{F}, \mathcal{O}, s_{\text{init}}, s_{\text{goal}}, c \rangle$, state s

Output: $h^{\text{lm-cut}}(s)$

```

1 if  $h^{\text{max}}(\Pi, s_{\text{init}}) = \infty$  then
2   |  $h^{\text{lm-cut}}(s) \leftarrow \infty$  and terminate;
3 end
4  $h^{\text{lm-cut}}(s) \leftarrow 0$ ;
5  $\Pi_1 = \langle \mathcal{F}' = \mathcal{F} \cup \{I, G\}, \mathcal{O}' = \mathcal{O} \cup \{o_{\text{init}}, o_{\text{goal}}\}, s'_{\text{init}} = \{I\}, s'_{\text{goal}} = \{G\}, c_1 \rangle$ , where
   pre( $o_{\text{init}}$ ) =  $\{I\}$ , add( $o_{\text{init}}$ ) =  $s$ , del( $o_{\text{init}}$ ) =  $\emptyset$ , pre( $o_{\text{goal}}$ ) =  $s_{\text{goal}}$ , add( $o_{\text{goal}}$ ) =  $\{G\}$ ,
   del( $o_{\text{goal}}$ ) =  $\emptyset$ ,  $c_1(o_{\text{init}}) = 0$ ,  $c_1(o_{\text{goal}}) = 0$ , and  $c_1(o) = c(o)$  for all  $o \in \mathcal{O}$ ;
6  $i \leftarrow 1$ ;
7 while  $h^{\text{max}}(\Pi_i, s'_{\text{init}}) \neq 0$  do
8   | Construct a justification graph  $G_i$  from  $\Pi_i$ ;
9   | Construct an s-t-cut  $\mathcal{C}_i(G_i, n_I, n_G) = (N_i^0, N_i^* \cup N_i^b)$ ;
10  | Create a landmark  $L_i$  as a set of labels of edges that cross the cut  $\mathcal{C}_i$ , i.e., they
    |   lead from  $N_i^0$  to  $N_i^*$ ;
11  |  $m_i \leftarrow \min_{o \in L_i} c_i(o)$ ;
12  |  $h^{\text{lm-cut}}(s) \leftarrow h^{\text{lm-cut}}(s) + m_i$ ;
13  | Set  $\Pi_{i+1} = \langle \mathcal{F}', \mathcal{O}', s'_{\text{init}}, s'_{\text{goal}}, c_{i+1} \rangle$ , where  $c_{i+1}(o) = c_i(o) - m_i$  if  $o \in L_i$ , and
    |    $c_{i+1}(o) = c_i(o)$  otherwise;
14  |  $i \leftarrow i + 1$ ;
15 end

```

- Sustainability of class materials is also important! So we're reusing!
- Last year's materials: [here](#)

- LM-Cut implementation
- Everything you need to do the assignment 1!



Feedback form link

