

# 1 Introduction

## 1.1 RDF(S)

```
@prefix qb:      <http://purl.org/linked-data/cube#> .
@prefix cssz-measure: <https://data.cssz.cz/ontology/measure/> .
@prefix rdf:     <http://www.w3.org/1999/02/22-rdf-syntax-ns#> .
@prefix y-onto:  <https://data.cssz.cz/ontology/years/> .
@prefix xsd:     <http://www.w3.org/2001/XMLSchema#> .
@prefix skos:    <http://www.w3.org/2004/02/skos/core#> .
@prefix cssz:    <https://data.cssz.cz/ontology/> .
@prefix rdfs:    <http://www.w3.org/2000/01/rdf-schema#> .
@prefix cssz-dimension: <https://data.cssz.cz/ontology/dimension/> .

<https://data.cssz.cz/resource/observation/invalidita/2011/pk_id/t/60-64>
  rdf:type qb:Observation ;
  qb:dataSet <https://data.cssz.cz/resource/dataset/invalidita> ;
  cssz-dimension:druh-duchodu
    <https://data.cssz.cz/resource/pension-kind/PK_ID_2010> ;
  cssz-dimension:pohlavi
    <https://data.cssz.cz/ontology/sdmx/code/sex-T> ;
  cssz-dimension:refPeriod
    <https://data.cssz.cz/resource/reference.data.gov.uk/id/gregorian-year/2011> ;
  cssz-dimension:skupina-diagnoz-dle-who
    <https://data.cssz.cz/resource/icd-10/chapter/C_T> ;
  cssz-dimension:vekova-kategorie
    <https://data.cssz.cz/generated/resource/age/Y60T64> ;
  cssz-measure:pocet-nove-priznanych-duchodu 234.0 .
```

### 1.1.1 Core RDF

#### RDF

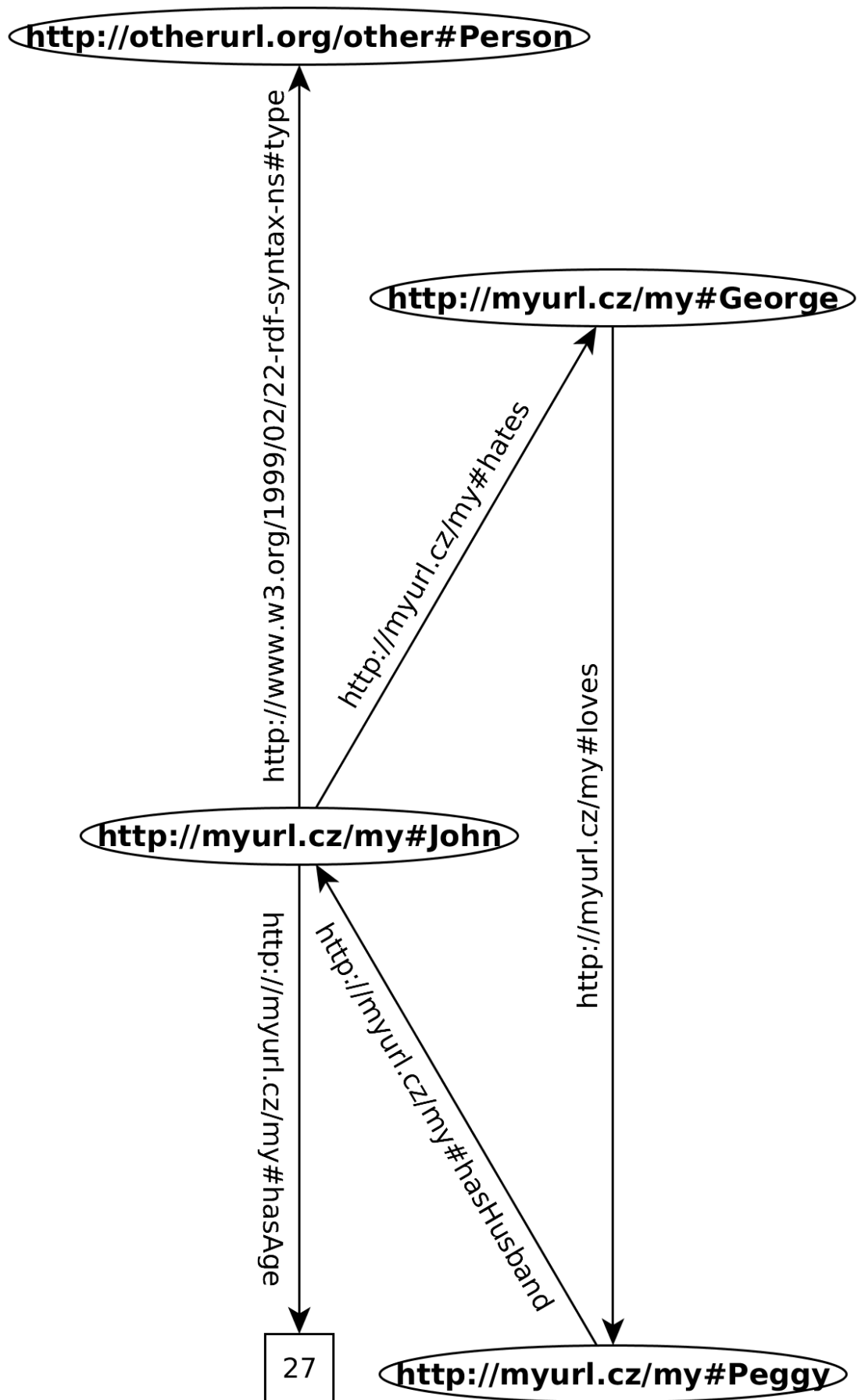
- RDF = **R**esource **D**escription **F**ramework
- RDF 1.0 – W3C Recommendation in 2004,

#### RDF Document

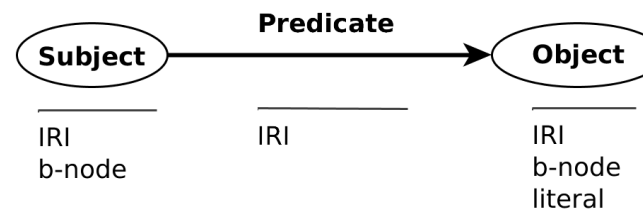
is a graph, where each

**node** is either an IRI (ellipse), a literal (rectangle), or a blank node (blank ellipse)

**edge** is labeled with IRI



## RDF Triple



is an ordered triple of the form (*Subject*, *Predicate*, *Object*):

### Definitions

**RDF Graph** is a set of RDF triples

**RDF Term** is either an *IRI*, a *blank node*, or a *literal*

### IRIs

- IRI = International Resource Identifier
- denotes a *document*, or a real *thing*
  - `<http://myurl.cz/my#Peggy>`
  - `<http://myurl.cz/my/document-about-peggy>`
- using hash (#) or slash (/) for delimiting particular entities in a namespace
- mapped to URIs = backward-compatibility

#### Note

- Two IRIs are equal iff their string representations are equal.
- No IRI is equal to any blank node, or literal.

### Namespaces

can be abbreviated using prefixes to improve readability

`rdf:type` (can be also abbreviated as `a`) instead of `http://www.w3.org/1999/02/22-rdf-syntax-ns#type`

`rdf:` `http://www.w3.org/1999/02/22-rdf-syntax-ns#`. This namespace defines basic resources, like `rdf:type`, `rdf:Property`.

`rdfs:` `http://www.w3.org/2000/01/rdf-schema#`. This namespace is used for metamodeling, like `rdfs:Class`, or `rdfs:subPropertyOf`.

`xsd:` `http://www.w3.org/2001/XMLSchema#`, for referencing XML Schema datatypes reused by RDF, like `xsd:integer`, or `xsd:string`.

#### Note

Often, a shortened IRI with empty prefix (e.g. `:x`) is used in examples. In such cases, the namespace is fixed, but unimportant for the example, if not stated otherwise.



**Blank Nodes (b-nodes)**

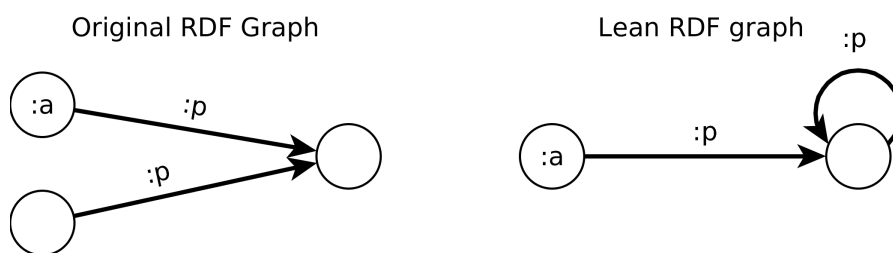
- denote existential variables,
- are local to the RDF document (cannot be reused outside),
- in Turtle/N-TRIPLES/SPARQL have `_:` prefix, e.g. `_:x`,

**Definition**

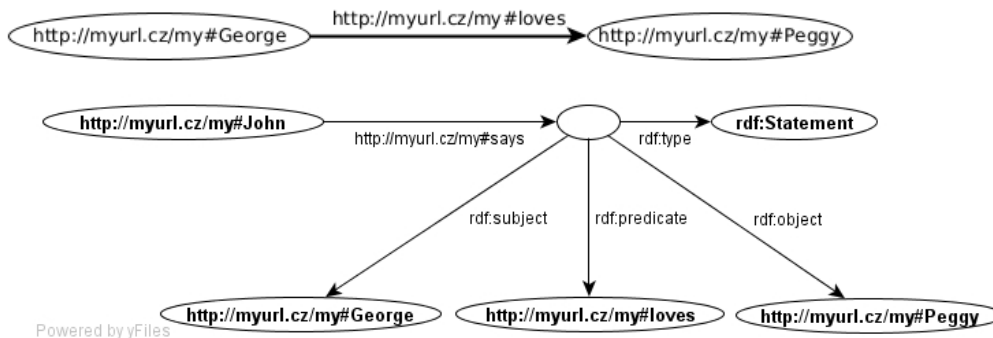
**Ground RDF Graph** is an RDF Graph containing no b-nodes.

**Instance** of RDF Graph  $G_1$  is an RDF Graph in which some b-nodes are replaced by an arbitrary RDF Term.

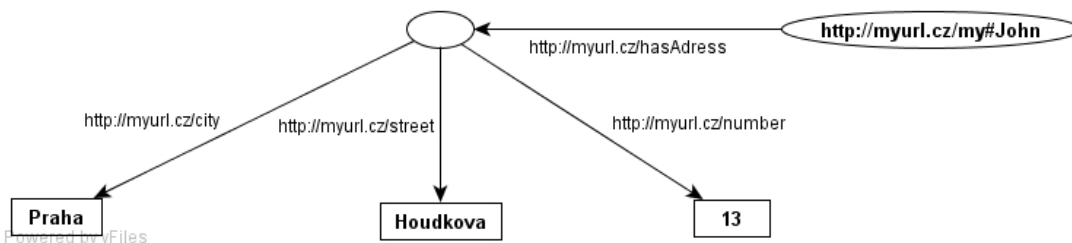
**Lean RDF Graph**  $G_1$  has no instance  $G_2$  which is a proper subgraph of  $G_1$ .



**Blank Nodes for statement reification**



**Blank Nodes for expressing complex values**



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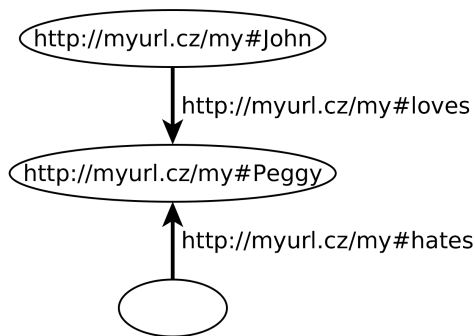
### Blank Nodes for other use-cases

- container description – multisets, sequences, alternatives
- modeling n-ary relations (e.g. birth)

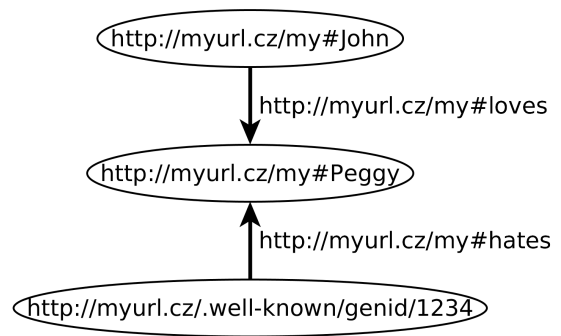
### Blank Node Skolemization

- replacing the blank nodes with fresh IRIs (*Skolem IRI*) to allow stronger identification of those resources
- the meaning of the RDF graph remains the same as before skolemization
- skolemized IRIs `http://.../.well-known/genid/xxx`, where xxx is a placeholder for a generated identifier.

Original RDF Graph



Skolemized RDF Graph



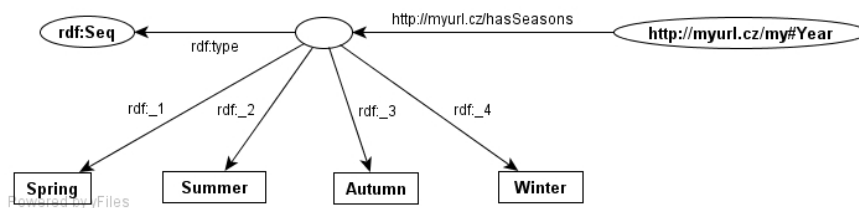
### Vocabularies

Various predefined vocabularies can be reused in your data, e.g.:

- schema.org – <http://schema.org/docs/schemas.html>
- Dublin Core – <http://dublincore.org/documents/dc-rdf/>. <https://www.dublincore.org/specifications/dublin-core/dcmi-terms/>
- FOAF – <http://www.foaf-project.org/>
- VOID – <http://www.w3.org/TR/void/>
- ...and many others

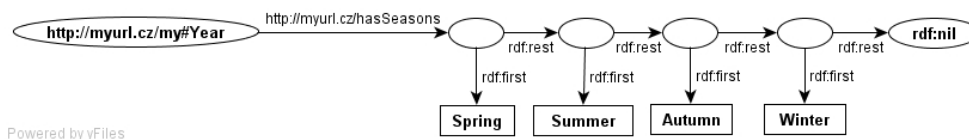
## 1.1.2 RDF features

### RDF containers



- `rdf:Bag` denotes an unordered sets of possibly repeating elements (multiset),
- `rdf:Seq` denotes an ordered seequence,
- `rdf:Alt` denotes an alternative choice from given resources/literals
- Container elements can be addressed by means of the `rdf : _x` property, where 'x' is a positive number,
- Containers are **not closed** – someone else can assert statements adding elements to our container,
- Containers can be modeled by means of blank nodes.

### RDF collections



- represent **closable** containers, similarly as LISP/Prolog lists
- `rdf:List` represents a list; the list head is available through `rdf:first` and the property is available through `rdf:rest`. The list can be closed by means of an empty list `rdf:nil`.

## RDF Model – Axiomatic Triples

### RDF 1.1

- RDF 1.1 Primer – W3C Working Group Note [Schreiber:13:RP]
- a set of W3C Recommendations in February 2014
- main differences to RDF 1.0:

## 1 Introduction

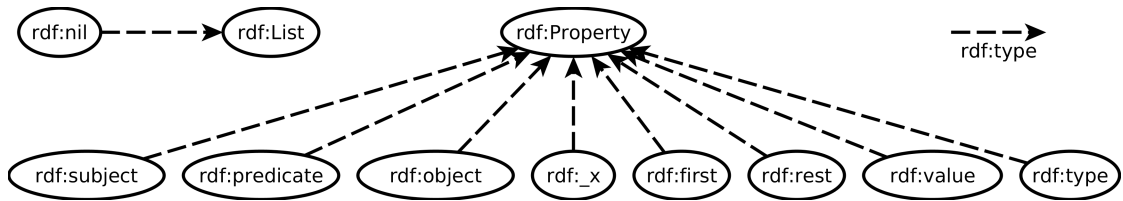


Figure 1.1: Visualization of axiomatic triples of RDF. Precise definition can be found in [Patel-Schneider:14:RS]

- identification of resources by IRIs
- all literals are *typed*, new datatypes introduced:

```
rdf:langString
rdf:HTML
rdf:XMLLiteral
```

The last two are non-normative in RDF 1.1

- additional XSD datatypes

```
xsd:duration,
xsd:dayTimeDuration,
xsd:yearMonthDuration,
xsd:dateTimeStamp
```

- additional serialization – JSON-LD, Turtle, TriG, N-Quads

### RDF\*

- extending RDF 1.1 to support more efficient reification
- <https://arxiv.org/pdf/1406.3399.pdf>
- statement `:man :hasSpouse :woman.`
- reified statement `<<:man :hasSpouse :woman>> :startDate "2020-02-11"`
- 

### 1.1.3 Metamodeling in RDFS

#### RDFS Basics

- RDFS = RDF Schema
- simple metamodeling language
- `rdfs` being shortcut for `http://www.w3.org/2000/01/rdf-schema#`
- `rdf` being shortcut for `http://www.w3.org/1999/02/22-rdf-syntax-ns#`



- RDF Schema 1.0 – W3C Recommendation in 2004 [Brickley:04:RVD]
- basic metamodeling vocabulary:

```

rdf:type,
rdfs:Class,
rdfs:subClassOf,
rdf:Property,
rdfs:subPropertyOf,
rdfs:domain,
rdfs:range

```

## Classes

- define instances :

```

ex:John rdf:type ex:Person .

```

- define classes (class rdfs:Class) :

```

ex:Person rdf:type rdfs:Class .

```

- create class hierarchies (property rdfs:subClassOf) :

```

ex:Woman rdfs:subClassOf ex:Person .

```

- multiple inheritance :

```

ex:Woman rdfs:subClassOf ex:Person .
ex:Woman rdfs:subClassOf ex:Female .

```

## Properties

- property definitions (resource rdf:Property) :

```

ex:hasParent rdf:type rdf:Property .

```

- creation of property hierarchies (property rdfs:subPropertyOf) :

```

ex:hasMother rdfs:subPropertyOf ex:hasParent .

```

- multiple inheritance

- domain and range definition :

```

ex:hasMother rdfs:domain ex:Person .
ex:hasMother rdfs:range ex:Woman .

```

- domains/ranges considered as conjunction :

```

ex:hasMother rdfs:range ex:Person .
ex:hasMother rdfs:range ex:Female .

```

## RDFS Model – Axiomatic Triples

# 1 Introduction

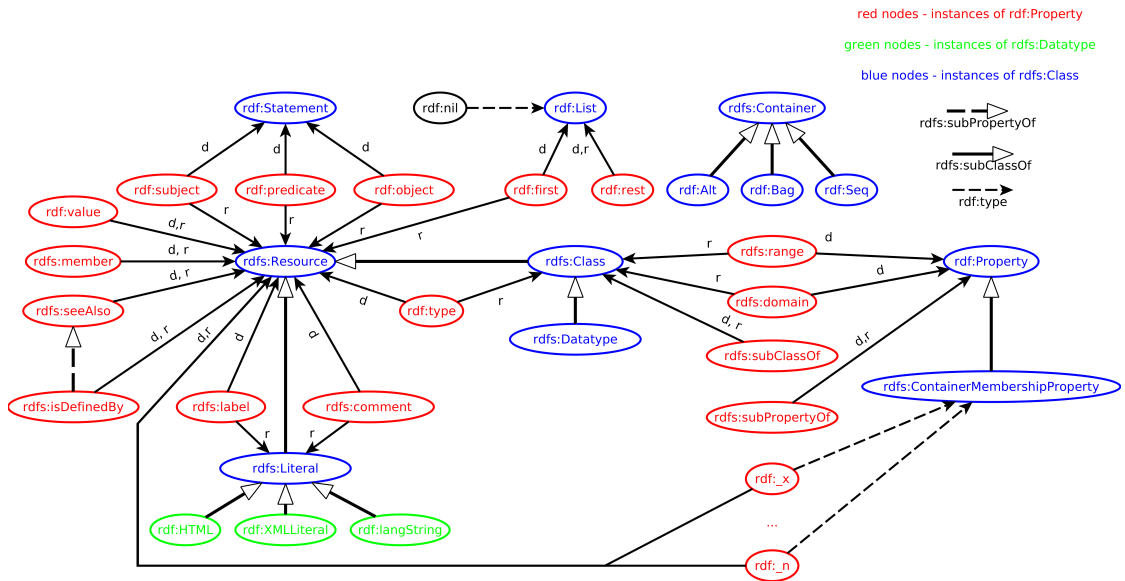


Figure 1.2: Visualization of axiomatic triples of RDFS. Precise definition can be found in [Patel-Schneider:14:RS]

## 1.1.4 RDF Syntaxes

### Syntaxes

Turtle family

**N-TRIPLES** , simple triples, for batch processing

**TURTLE** , well-readable, compact

**TriG** , extension of TURTLE for multiple graphs (RDF datasets)

**N-QUADS** , extension of N-TRIPLES for multiple graphs (RDF datasets)

**RDF/XML** , a frame-based syntax

**JSON-LD** , JSON syntax for RDF 1.1

**RDF-A** , syntax for embedding RDF 1.1 into HTML

### N-TRIPLES

*suitable for loading large data volumes*

```
<http://www.myurl.cz/my#George> <http://www.myurl.cz/my#loves> <http://www.myurl.cz/my#Peggy> .
<http://www.myurl.cz/my#Peggy> <http://www.myurl.cz/my#hasHusband> <http://www.myurl.cz/my#John> .
<http://www.myurl.cz/my#John> <http://www.myurl.cz/my#hates> <http://www.myurl.cz/my#George> .
<http://www.myurl.cz/my#John> <http://www.w3.org/1999/02/22-rdf-syntax-ns#type>
  <http://www.otherurl.org/other#Person> .
<http://www.myurl.cz/my#John> <http://www.myurl.cz#hasAge>
  "27"^^<http://www.w3.org/2001/XMLSchema#integer> .
```

**TURTLE***extension of N-TRIPLES, allowing shortcuts*

```

@prefix rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#> .
@prefix my: <http://www.myurl.cz/my#> .
@prefix xsd: <http://www.w3.org/2001/XMLSchema#> .
my:George my:loves my:Peggy .
my:Peggy my:hasHusband my:John .
my:John rdf:type <http://www.otherurl.org/other#Person> ;
        my:hates my:George ;
        my:hasAge "27"^^xsd:integer.

```

```

:a :p1 :o1 ;
   :p2 :o2 .

```

```

:a :p1 :o1 .
:a :p2 :o2 .

```

```

:a :p :o1, :o2 .

```

```

:a :p :o1 .
:a :p :o2 .

```

**TURTLE***extension of N-TRIPLES, allowing shortcuts*

```

:a :p1 [
  :p2 :o2 ;
  :p3 :o3 .
]

```

```

:a :p1 _:x .
_:x :p2 :o2 .
_:x :p3 :o3 .

```

```

:a :p (:o1 :o2 :o3) .

```

```

:a :p _:a .
_:a rdf:first :o1 .
_:a rdf:rest _:b .
_:b rdf:first :o2 .
_:b rdf:rest _:c .
_:c rdf:first :o3 .
_:c rdf:rest rdf:nil .

```

**RDF/XML***readable, expressive, plenty of syntactic sugar*

```

<rdf:RDF xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
  xmlns:base="http://myurl.cz/my#"
  xmlns:my="http://myurl.cz/my#"
  xmlns:other="http://otherurl.org/other#">
  <rdf:Description rdf:ID="George">
    <my:loves rdf:about="http://myurl.cz/my#Peggy"/>
  </rdf:Description>
  <rdf:Description rdf:ID="Peggy">
    <my:hasHusband rdf:about="http://myurl.cz/my#John"/>
  </rdf:Description>
  <other:Person rdf:ID="John">
    <my:hates rdf:about="http://myurl.cz/my#George"/>
    <my:hasAge rdf:datatype="http://www.w3.org/2001/XMLSchema#integer">
      27
    </my:hasAge>
  </other:Person>
</rdf:RDF>

```

**1.1.5 RDF Datasets****Definition**

**RDF dataset** is a collection of RDF graphs:

$$DS = \{DG, (i_1, G_1), \dots, (i_n, G_n)\}$$

consisting of a **default (unnamed) RDF graph**  $DG$  and zero or more **named RDF graphs**  $G_k$  identified by their IRI/blank node  $i_k$ .

- Default graphs might be independent on named graphs (in RDF4J they are not – default graph contains union of all named graphs).
- Blank nodes can be reused between different graphs in a single RDF dataset.
- For SPARQL 1.1, RDF dataset cannot use blank nodes as graph names.

**RDF Merge**

- **Merge** of RDF graphs  $G_1$  and  $G_2$  is an RDF graph created as follows:
  - rename b-nodes in  $G_1$ , so that no b-node label occur in both  $G_1$  and  $G_2$ .
  - union  $G_1$  and  $G_2$ .
- Example:
  - $G_1$  :

```

@prefix : <http://www.myurl.cz/my#> .
:a :p _:b .
:a :q _:c .

```

–  $G_2$  :

```
@prefix : <http://www.myurl.cz/my#> .
:a :s _:c .
:a :t _:d .
```

– merge of  $G_1$  and  $G_2$  :

```
@prefix : <http://www.myurl.cz/my#> .
:a :p _:b .
:a :q _:c .
:a :s _:e .
:a :t _:d .
```

### 1.1.6 Semantics of RDF(S)

#### Entailment Regimes and Semantic Extension

Precise definition of RDF semantics can be found in [Patel-Schneider:14:RS]

#### Definition

**Semantic Extension** is a set of semantic constraints on an RDF graph.

**Entailment Regime** is a set of entailments defined by the corresponding *semantic extension*.

- Four entailment regimes are predefined in RDF specs:

**Simple entailment** provides only structural matching of graphs with possible b-node renaming

**RDF entailment** interprets RDF vocabulary

**RDFS entailment** interprets RDF and RDFS vocabularies

**D entailment** additionally interprets datatypes

- All entailment regimes must be *monotonic* extensions of simple entailment

#### Simple Interpretation

#### Definition

A finite interpretation  $I = (IR, IP, IEXT, IS, IL)$  w.r.t. vocabulary  $N = (N_{IRI}, N_{lit})$  is defined as follows:

- $IR$  is a set of *resources*
- $IP$  is a set of *properties* (often  $IP \subseteq IR$ )
- $IEXT$  is a mapping  $IEXT : IP \rightarrow IR \times IR$
- $IS$  is a mapping  $IS : N_{IRI} \rightarrow IR \cup IP$
- $IL$  is a partial mapping  $IL : N_{lit} \rightarrow IR$

### Simple Interpretation Example

```
@prefix : <http://www.myurl.cz/my#> .
:John :loves :Mary .
:John :childcount 2 .
```

- $IR = \{John, Mary, 2\}$  (real resources)
- $IP = \{loves, childcount\}$  (real properties)
- $IEXT = \{(loves, \langle John, Mary \rangle), (childcount, \langle John, 2 \rangle)\}$
- $IS = \{\langle http://www.myurl.cz/my\#John, John \rangle, \langle http://www.myurl.cz/my\#Mary, Mary \rangle, \langle http://www.myurl.cz/my\#loves, loves \rangle, \langle http://www.myurl.cz/my\#childcount, childcount \rangle\}$
- $IL = \{\langle "2" \wedge http://www.w3.org/2001/XMLSchema\#integer, 2 \rangle\}$

### Simple Entailment

Simple entailment is just a “structural matching with b-node rewriting.”

#### Semantic Conditions on Simple Entailment

- if  $E$  is a literal, then  $I(E) = IL(E)$
- if  $E$  is an IRI, then  $I(E) = IS(E)$
- if  $E$  is a ground triple  $(s, p, o)$ , then  $I(E) = true$  iff  $I(p) \in IP$  and  $\langle I(s), I(o) \rangle \in IEXT(I(p))$
- if  $E$  is a ground RDF graph, then  $I(E) = true$  iff  $I(E') = true$  for each triple  $E' \in E$
- if  $E$  is an RDF graph, then  $I(E) = true$  iff there exists a mapping  $A : N_{bnode} \rightarrow IR$ , such that  $I(A(E)) = true$ , where  $A(E)$  is  $E$ , where each blank node  $B$  is replaced by  $A(B)$ .

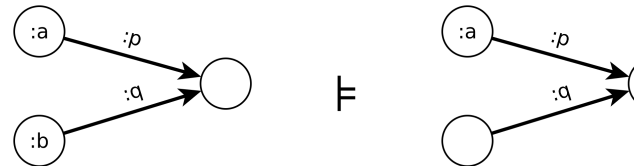
#### Simple Entailment

- graph  $G_1$  (simply) entails graph  $G_2$  (denoted  $G_1 \models G_2$ ) if  $I(G_2) = true$  whenever  $I(G_1) = true$ .
- if  $G_1 \models G_2$  and  $G_2 \models G_1$  then they are *logically equivalent*.

### How to Check Simple Entailment ?

#### Interpolation lemma

Graph  $G_1$  simply entails graph  $G_2$  iff a subgraph of  $G_1$  is an instance of  $G_2$ .



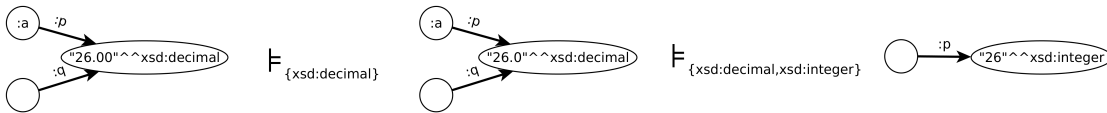
Simple entailment is NP in the size of  $G_1$  and  $G_2$ .

**D-Entailment**

In addition to blank nodes,  $D$ -entailment ( $\models_D$ ) interprets datatypes in the set  $D$  of recognized datatypes. Literals with non-recognized datatypes are treated as uninterpreted.

**Semantic Conditions on D-Entailment**

- if  $\text{rdf:langString} \in D$ , then for each literal  $\text{lex}@lang$ .,  $IL(\text{lex}@lang) = \langle \text{lex}, \text{lowercase}(lang) \rangle$
- if  $dIRI \in D$ , then for each literal  $\text{lex}^^dIRI$ :  $IL(\text{lex}^^dIRI) = L2V(I(dIRI))(\text{lex})$ , where
  - $I(dIRI)$  is a datatype identified by  $dIRI$
  - $L2V(d)$  transforms a lexical value to the value space of  $d$ .

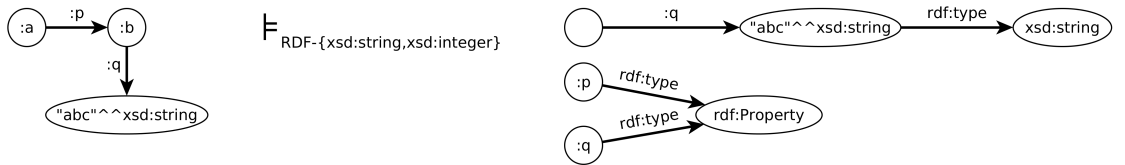


**RDF-Entailment**

In addition to  $D$ -entailment, RDF-entailment w.r.t  $D$  interprets properties in the RDF vocabulary.

**Entailment rules**

rule	$G$ contains	$t_i$ , s.t. $G \models_{RDF-D} t_i$
GrdfD1	$(s, p, \text{lex}^^d)$ $d \in D$	$(\text{lex}^^d, \text{rdf:type}, d)$
rdfD2	$(s, p, o)$	$(p, \text{rdf:type}, \text{rdf:Property})$



For example:

**RDFS-Entailment**

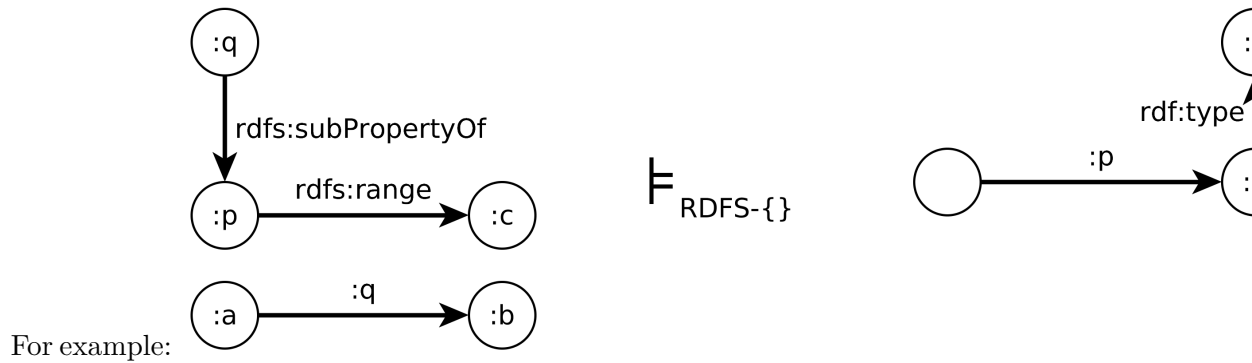
RDFS-entailment w.r.t  $D$  interprets most RDF and RDFS vocabulary.

**Entailment rules**

## 1 Introduction

rule	$G$ contains	$t_i$ , s.t. $G \models_{RDFS-D} t_i$
rdfs1	any IRI $dIRI \in D$ in $G$	$(dIRI, rdfs:type, rdfs:Datatype)$
rdfs2	$(s, p, o), (p, rdfs:domain, w)$	$(s, rdfs:type, w)$
rdfs3	$(s, p, o), (p, rdfs:range, w)$	$(o, rdfs:type, w)$
rdfs4	$(s, p, o)$	$(s, rdfs:type, rdfs:Resource)$ $(o, rdfs:type, rdfs:Resource)$
rdfs5	$(p_1, rdfs:subPropertyOf, p_2)$ $(p_2, rdfs:subPropertyOf, p_3)$	$(p_1, rdfs:subPropertyOf, p_3)$
rdfs6	$(p, rdfs:type, rdfs:Property)$	$(p, rdfs:subPropertyOf, p)$
rdfs7	$(p_1, rdfs:subPropertyOf, p_2)$ $(s, p_1, o)$	$(s, p_2, o)$
rdfs8	$(s, rdfs:type, rdfs:Class)$	$(s, rdfs:subClassOf, rdfs:Resource)$
rdfs9	$(c_1, rdfs:subClassOf, c_2)$ $(s, rdfs:type, c_1)$	$(s, rdfs:type, c_2)$
rdfs10	$(c, rdfs:type, rdfs:Class)$	$(c, rdfs:subClassOf, c)$
rdfs11	$(c_1, rdfs:subClassOf, c_2)$ $(c_2, rdfs:subClassOf, c_3)$	$(c_1, rdfs:subClassOf, c_3)$
rdfs12	$(p, rdfs:type, rdfs:ContainerMembershipProperty)$	$(p, rdfs:subPropertyOf, rdfs:member)$
rdfs13	$(d, rdfs:type, rdfs:Datatype)$	$(d, rdfs:subClassOf, rdfs:Literal)$

### RDFS-Entailment Example



### Entailment Checking

All discussed entailments can be checked by applying the entailment rules on *generalized RDF graphs*, i.e. **graphs that allow all RDF Terms in all positions – subject, predicate, object.**

#### Entailment checking procedure

$G_1 \models_X G_2$ , iff  $Clos_X(G_1)$  simply entails  $G_2$ , where  $Clos_X(G_1)$  is constructed as follows:

1. Add to  $G_1$  all axiomatic triples for  $X \in \{RDF-D, RDFS-D\}$  (visualized in Figure 1.1, resp. Figure 1.2)
2. For each container membership property IRI  $p$  occurring in  $G_1$ , add to  $G_1$  corresponding axiomatic triples for  $X$  containing  $p$ .
3. If no triples were added in the previous step, add axiomatic triples for  $X$  containing  $rdfs:_1$ .



4. Apply rules for  $X$  (i.e.  $\{Grdf\ D1, rdf\ D2\}$  for  $X = RDF$ , or  $\{Grdf\ 1, rdf\ D2, rdfs\ 1, \dots, rdfs\ 13\}$  for  $X = RDFS$ ) with  $D = \{rdf : langString, xsd : string\}$ , until exhaustion.

### **Entailment Checking Complexity**

- the previous procedure is finite and polynomial
- simple entailment checking itself is NP
- the less blank nodes, the more efficient