

Network Inference & Link Prediction

Network Application Diagnostics

B2M32DSA

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October 31, 2019



- 1 Preliminary Tools
 - Classification Evaluation
 - Network Terminology
- 2 Network Inference
 - Introduction
 - Network Inference Example - Viber
- 3 Link Prediction
 - Introduction
 - Scoring Functions

Outline

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Classification Predictions ^[?]

- **The expectation:** the terms *positive* and *negative* refer to the classifier's prediction.
- **The observation:** the terms *true* and *false* refer to whether that prediction corresponds to the external judgment.
- The confusion matrix (CZ kontingenční tabulka)

		Predicted / Classified	
		Negative	Positive
Actual	Negative	True Negative	False Positive
	Positive	False Negative	True Positive

- **TN / True Negative**

- the real case is negative
- and predicted negative

- **FP / False Positive**

- the real case is negative
- but predicted positive
- Type I error

- **TP / True Positive**

- the real case is positive
- and predicted as positive

- **FN / False Negative**

- the real case is positive
- but predicted negative
- Type II error



Precision and Recall ^[?, ?]

• Precision

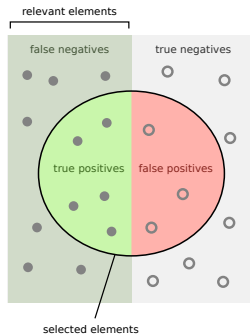
- the probability that a (randomly selected) retrieved document is relevant.
- the probability that a (randomly selected) object is correctly classified.

$$\text{Precision} = \frac{TP}{TP + FP}$$

• Recall

- the probability that a (randomly selected) relevant document is retrieved in a search.
- the probability that a (randomly selected) class object is correctly classified.

$$\text{Recall} = \frac{TP}{TP + FN}$$



How many selected items are relevant?

$$\text{Precision} = \frac{\text{Green}}{\text{Green} + \text{Red}}$$

How many relevant items are selected?

$$\text{Recall} = \frac{\text{Green}}{\text{Green} + \text{Light Green}}$$

Accuracy and F1-Measure ^[?, ?]

• Accuracy

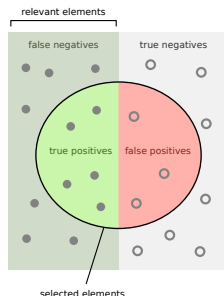
- the proportion of true results (both true positives and true negatives) among the total number of cases examined.

$$\text{Accuracy} = \frac{TP + TN}{TP + TN + FP + FN}$$

• F1-Measure

- the harmonic mean of precision and recall.
- an *F1* score reaches its best value at 1 (perfect precision and recall) and worst at 0.

$$F1 = \left(\frac{\text{Precision}^{-1} + \text{Recall}^{-1}}{2} \right)^{-1} = \frac{2 \times \text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}$$



How many selected items are relevant?

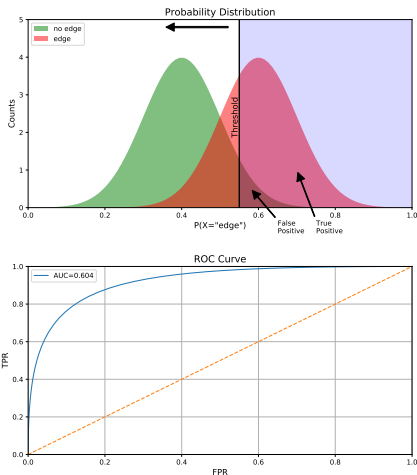


How many relevant items are selected?



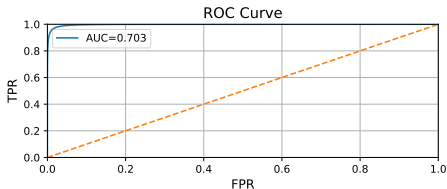
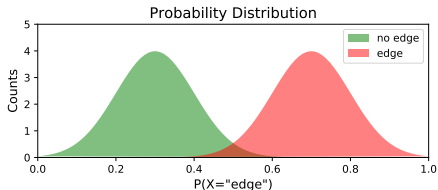
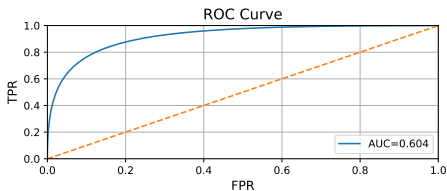
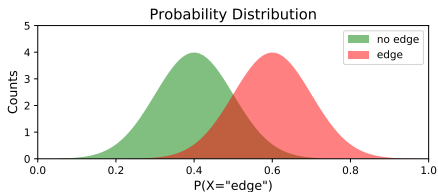
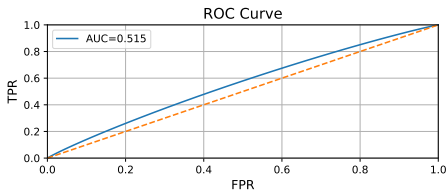
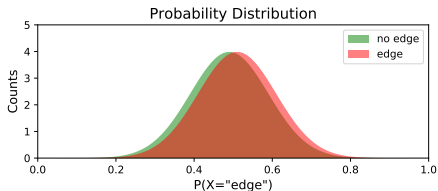
ROC Curves ^[?]

- Plotting the true positive rate (TPR) against the false positive rate (FPR).
- Dealing with heavy class imbalance.
- The model performance is measured by the area under the ROC curve (AUC).
- The best possible AUC is 1.
- The worst AUC is 0.5 (the 45 degrees random line).
- If the AUC is below 0.5, do the exact opposite of what the model recommends.



$$TPR = \frac{TP}{TP + FN}, \quad FPR = \frac{FP}{FP + TN}$$

ROC Performance Assessment ^[?]



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Graph Notation ^[?]

- Let $G(V, E)$ be an undirected random network graph.
- $V^{(2)}$ is the set of distinct unordered pairs of vertices.
- E is the set of edges in G .
- $N_v = |V|$ is the number of vertices.
- $N_e = |E|$ is the number of edges.
- $V^{(2)} \setminus E$ is the set of non-edges in G .
- $V_{obs}^{(2)}$ is the observed presence or absence of edges.
- $V_{miss}^{(2)} = V^{(2)} \setminus V_{obs}^{(2)}$ is the set of edges for which observations are missing.
- Sparse graph: $|E| \ll |V|^2$
- The set $\mathcal{N}(u)$ of neighbors of $u \in V$ in $G(V, E)$:

$$\mathcal{N}(u) = \{v | v \in V, e = uv \in E\}$$



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Network Topology Inference ^[?]

- What should constitute a vertex and an edge is determined by user-specified decisions and rules.
- Such a network graph construction lacks an element of validation.
 - if the network representation is “accurate”,
 - i.e. capturing some well-defined but unobservable relational structure.
 - What accuracy can be expected given the available measurements?
 - Are there other similar representations with about the same accuracy?
 - How is the representation robust to changes in the measurements?
 - How is the representation useful for other purposes?

Network Topology Inference Problem

- Given a set of measurements from a system of interest, e.g.
 - vertex attributes $\mathbf{x} = (x_1, \dots, x_{N_V})$
 - binary indicators $\mathbf{y} = [y_{ij}]$ of certain edges.
- and given a collection \mathcal{G} of potential graphs G ,
- select an appropriate member of \mathcal{G} that best captures the underlying state of the system.

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Network Inference Problems ^[?]

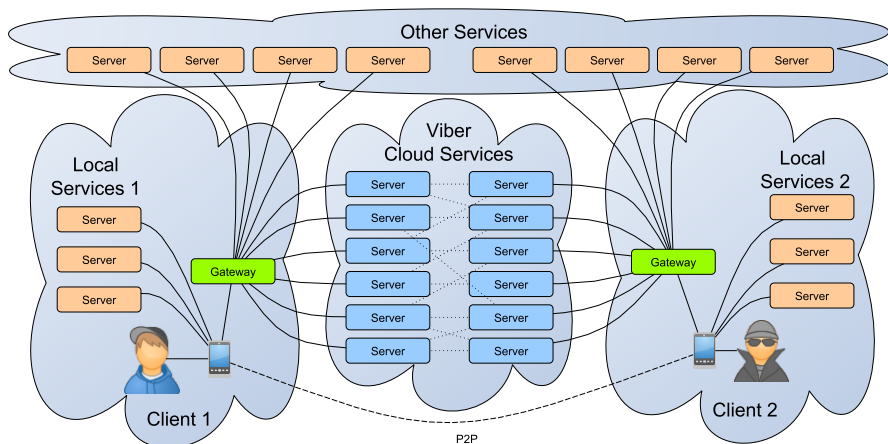
- **Link Prediction** . . . inferring whether or not a pair of vertices does or does not have an edge between them
 - using measurements that include a subset of vertex pairs whose edge/non-edge status is already observed.
 - knowledge of all of the vertices.
 - the status of some of the edges/non-edges
- **Association Graph Inference** . . . the relation defining edges is itself unobserved and must be inferred from measurements reflecting these characteristics.
 - no knowledge of edge status anywhere in the network graph,
 - relevant measurements at all of the vertices are assumed.
- **Tomographic Network Inference** . . . the measurements are available only at vertices that are somehow at the perimeter of the network.
 - measurements at only a particular subset of vertices are known.



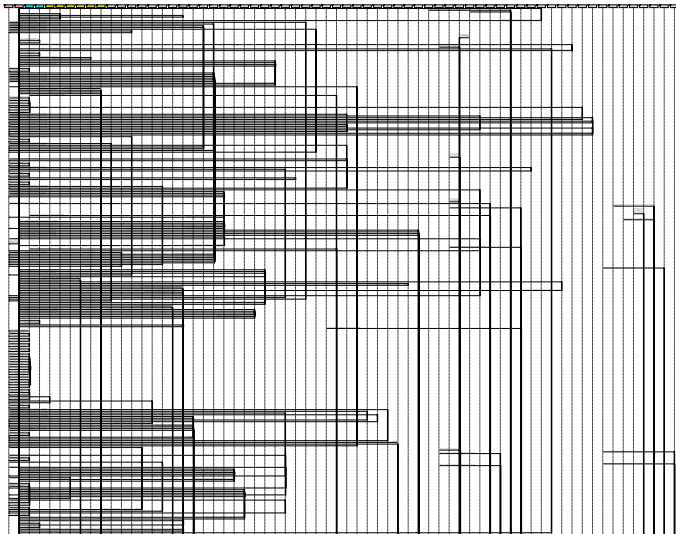
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Exemplar (Viber) Environment ^[?]



Example Capture Characteristics ^[?]



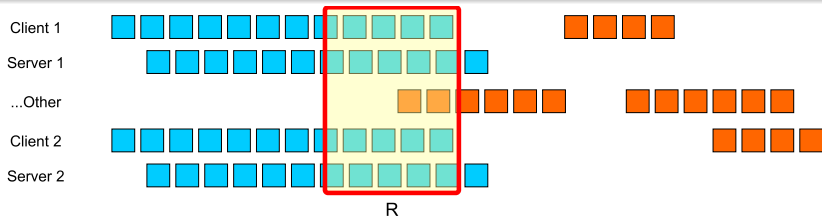
- 138882 PCAP blocks
- 1788 transport sessions
- 2 clients
- 22 viber.com servers
- 150 peers of 2 clients
- 5660 possible concurrent sessions
- **How to analyze?**



Concurrent Communication Detection ^[?]

Selection of IP nodes

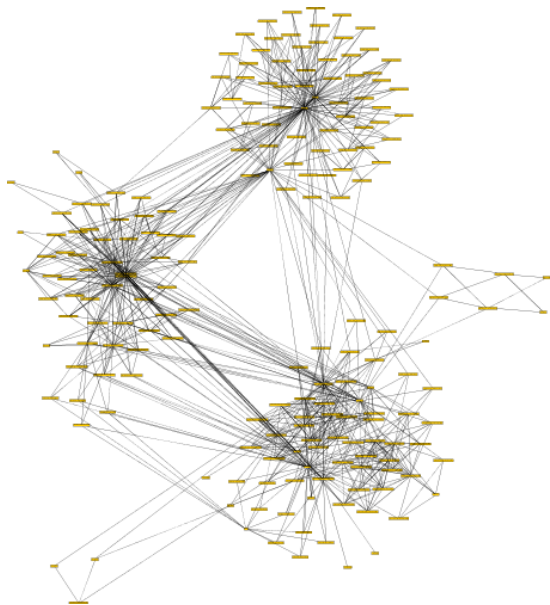
- *viber.com* servers → viber clients → other Viber servers
- classified based on entropy based characteristics of TCP/IP distributions



$$s(a, b) = \frac{\sum_{\forall i, j: t_a[i] - t_b[j] < R} R / (t_a[i] - t_b[j])}{\sum_{\forall i, j: t_a[i] - t_b[j] < R} 1}$$

In our experiments: $R = 50ms$, $s(a, b) > 0.001$

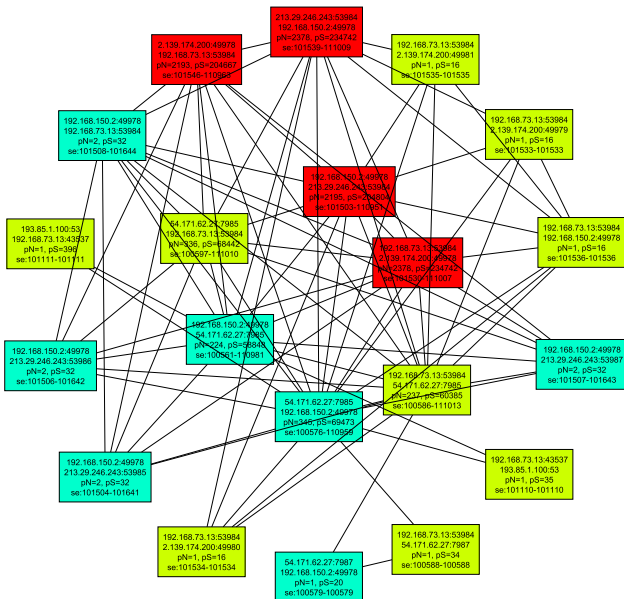
UDP packet sequence concurrency as a complex network ^[?]



- captures with two clients
- "*communities*" of concurrent sessions
- some clusters related to only one client
- interesting clusters consist of nodes of both clients



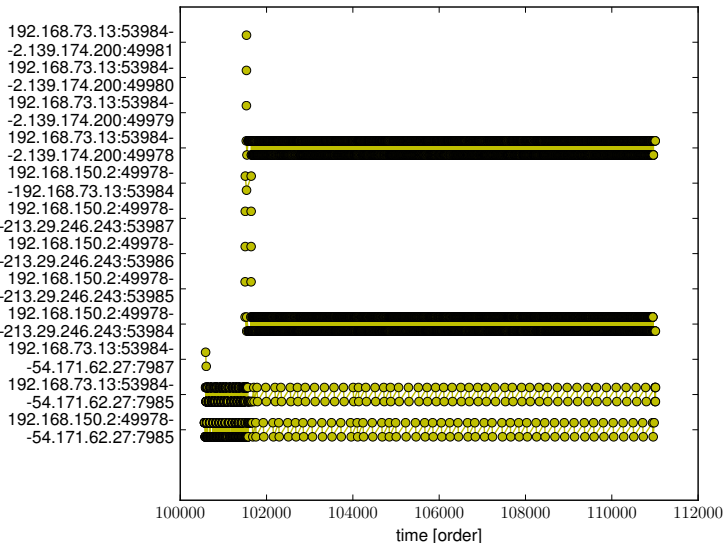
UDP packet sequence concurrency network component [?]



- restricted on one of the components
- two *Viber* clients
- 192.168.73.13
- 192.168.150.2



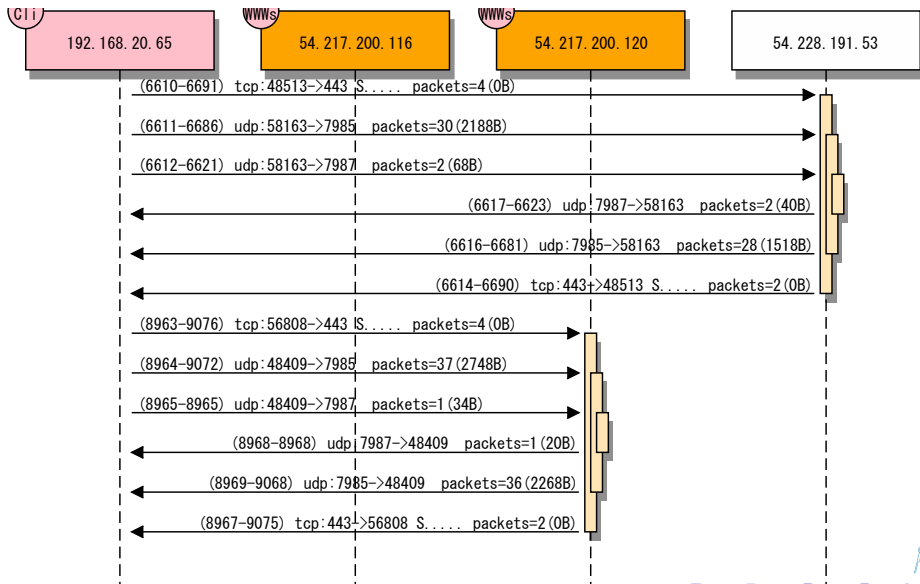
UDP packet sequence concurrency - packet timing ^[?]

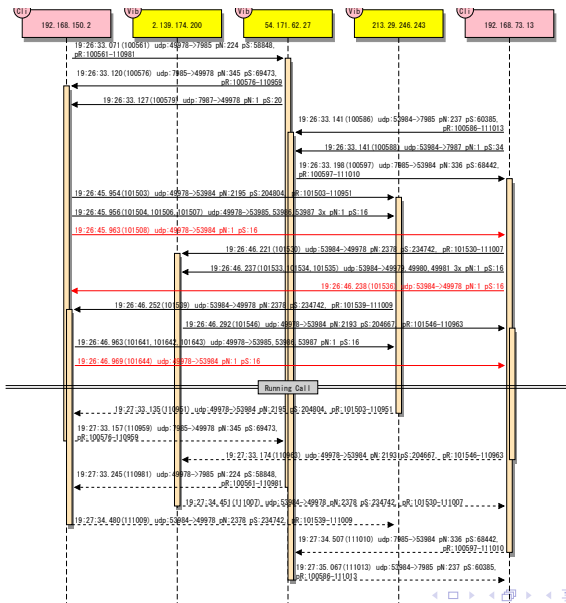


- signals
- calls
- keep-alive packets
- direct client to client packets

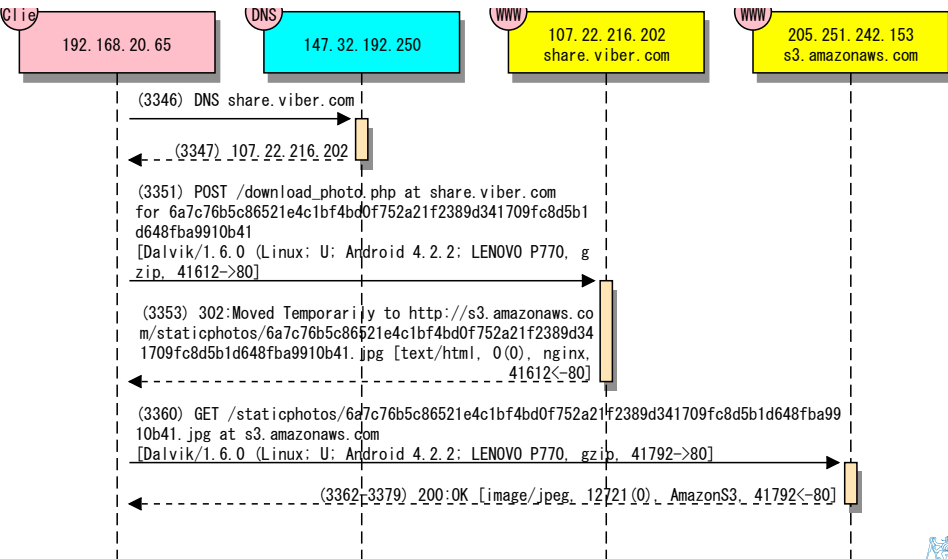


Message Sending [?]



Voice Call ^[?]

Security/Privacy Assessment - Contact Picture Transfer



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Link Prediction Motivation ^[?]

- Networks are highly dynamic objects
 - they grow and change . . . e.g. by adding new edges
- Network evolution models
 - To what extent can the evolution of a network be modeled using features *intrinsic to the network itself*?
 - A number of proximity measures lead to predictions that outperform a random prediction by factors 40 to 50.
 - The network topology might contain latent information from which one can infer future edges (interactions).
- Recovery of a hidden/latent informal network by observing the official observable network part.



Link Prediction Definition ^[?, ?]

● Link Prediction

- A network is changing over time.
- Given a snapshot of a network at time t ,
- predict edges added in the interval (t, t')

● Link Completion (missing links identification).

- Given a network,
- infer links that are consistent with the structure, but missing.
- *Find unobserved edges*

● Link Reliability

- Estimate the reliability of given links in the graph.

What can be predicted?

- Link existence,
- Link weight,
- Link type,
- Link cardinality.

Link Prediction ^[?, ?]

- Given a graph $G(V, E)$
- The number of *missing edges*: $|V|(|V| - 1)/2 - |E|$
- Probability of a correct random guess $O(\frac{1}{|v|^2})$
 - in sparse graphs ($|E| \ll |V|^2$)
- Each edge $e \in E$ represents an interaction between its endpoints at a particular time $t(e)$.
- Multiple interactions are represented by parallel edges with different time-stamps.
- $G[t, t']$ is the subgraph of G restricted to edges with time-stamps between t and t' , $t < t'$.

Link prediction phases

- 1 **Learning:** *training* interval $[t_0, t'_0] \dots G[t_0, t'_0]$
- 2 **Prediction:** *testing* interval $[t_1, t'_1] \dots G[t_1, t'_1]$

Link Prediction ^[?, ?]

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Link prediction phases

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Scoring Algorithm ^[?, ?]

- Proximity/Similarity score $c(v_1, v_2)$... it is assumed that the higher the score the higher the probability that the vertexes v_1 and v_2 interact and they are linked by the edge.

Link prediction by proximity scoring

- 1 Compute proximity/similarity score $c(v_1, v_2)$ for each pair of nodes.
- 2 Sort all pairs by the decreasing score.
- 3 Select top pairs as new links
 - n pairs
 - pairs above a treshold.

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Scoring Functions - Neighborhood Based ^[?, ?]

Local neighborhoods of v_i and v_j

- Number of **common neighbors**:

- based on the idea that links are formed between nodes who share many common neighbors

$$c^{CN}(v_i, v_j) = |\mathcal{N}(v_i) \cap \mathcal{N}(v_j)|$$

- **Jaccard's coefficient**:

- a measure of the likelihood that a neighbor of v_i is a neighbor of v_j and vice versa.

$$c^{JA}(v_i, v_j) = \frac{|\mathcal{N}(v_i) \cap \mathcal{N}(v_j)|}{|\mathcal{N}(v_i) \cup \mathcal{N}(v_j)|}$$

- **Adamic/Adar**:

- The larger weight is assigned to common neighbors v of v_i and v_j which themselves have few neighbors $\log |\mathcal{N}(v)|$,
- i.e. v_i and v_j are “related” because of the rarer neighbor v .

$$c^{AA}(v_i, v_j) = \sum_{v \in \mathcal{N}(v_i) \cap \mathcal{N}(v_j)} \frac{1}{\log |\mathcal{N}(v)|}$$



Scoring Functions - Neighborhood Based ^[?]

Preferential attachment:

- A new node is attached to a network node u that has a higher probability of fitness expressed as the size of its neighborhood $|\mathcal{N}(u)$.

$$c(v_i, v_j) = |\mathcal{N}(v_i)| |\mathcal{N}(v_j)|$$



Scoring Functions - Path Based ^[?]

Paths and ensembles of paths between v_i and v_j

- Shortest path:

$$- \min_s \{path_{ij}^s > 0\}$$

- Katz score:

$$\sum_{\ell=1}^{\infty} \beta^{\ell} |paths^{(\ell)}(v_i, v_j)| = \sum_{\ell=1}^{\infty} (\beta \mathbf{A})_{ij}^{\ell} = (\mathbf{I} - \beta \mathbf{A})^{-1} - \mathbf{I}$$

- Personalized (rooted) PageRank:

$$PR = \alpha(\mathbf{D}^{-1} \mathbf{A})^T PR + (1 - \alpha)$$



Scoring Functions - Path Based ^[?]

Local neighborhoods of v_i and v_j

- Number of common neighbors

$$|\mathcal{N}(v_i) \cap \mathcal{N}(v_j)|$$

- Jaccard's coefficient

$$\frac{|\mathcal{N}(v_i) \cap \mathcal{N}(v_j)|}{|\mathcal{N}(v_i) \cup \mathcal{N}(v_j)|}$$

- Adamic/Adar:

$$\sum_{v \in \mathcal{N}(v_i) \cap \mathcal{N}(v_j)} \frac{1}{\log |\mathcal{N}(v)|}$$



Summary

- Network inference problem
- Network inference case study
- Link prediction problem
- Link prediction scoring functions

Competencies

- Define precision, recall, accuracy, and $F1$ -measure used in classification evaluation.
- How ROC curves are used in classification problems?
- Define the network inference problem and its subproblems.
- How is it possible to detect packet sequence concurrency?
- Define the link prediction problem and its subproblems.
- Define typical scoring functions used in the link prediction problem.

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