

Algorithm Configuration (Parameter Tuning) Problem

The objective of the parameter configuration (parameter tuning) problem is to find the parameter configuration $\theta \in \Theta$ resulting in the best performance of \mathcal{A} on distribution \mathcal{D} .

There are many ways of measuring the **cost**, $o(\mathcal{A}, \theta, I, s)$, of running algorithm \mathcal{A} with parameter configuration θ on an instance I , using seed s in case of randomized algorithm:

- the **computational resources** consumed by the given algorithm (such as runtime, memory or communication bandwidth),
- the **approximation error**,
- the **improvement** achieved over an instance-specific reference cost,
- the **quality** of the solution found.

Algorithm Configuration (Parameter Tuning) Problem

The behaviour of the algorithms can vary significantly between **multiple runs** on different instances or when randomized algorithms are run repeatedly with fixed parameters on a single problem instance.

Therefore, the **cost** of a candidate solution θ is defined as

$$c(\theta) = m(O_\theta)$$

the statistical population parameter m of the cost distribution $O_\theta(\mathcal{A}, \theta, \mathcal{D})$, over instances drawn from distribution of instances, \mathcal{D} , and multiple independent runs.

An optimal solution, θ^* , minimizes $c(\theta)$:

$$\theta^* \in \arg \min_{\theta \in \Theta} c(\theta).$$

For example, we might aim to minimize **mean runtime** or **median solution cost**.

The $O_\theta(\mathcal{A}, \theta, \mathcal{D})$ is typically unknown, so we can only acquire approximations of their statistics, $c(\theta)$, based on a limited number of samples (i.e. the cost of single executions of $\mathcal{A}(\theta)$) – let's denote an **approximation of $c(\theta)$ based on N samples** by $\hat{c}_N(\theta)$.

- For deterministic algorithms, the algorithm \mathcal{A} is run on $N \leq M$ instances (M is the size of the finite training set of instances).
- For randomized, algorithms, we can run multiple runs with different seeds if $M < N$.

ParamILS(N): Algorithm

```
Input : Initial configuration  $\theta_0 \in \Theta$ , algorithm parameters  $r, p_{restart}$ , and  $s$ .  
Output : Best parameter configuration  $\theta$  found.  
1 for  $i = 1, \dots, r$  do  
2    $\theta \leftarrow$  random  $\theta \in \Theta$ ;  
3   if  $\text{better}(\theta, \theta_0)$  then  $\theta_0 \leftarrow \theta$ ;  
4  $\theta_{ils} \leftarrow$  IterativeFirstImprovement ( $\theta_0$ ); First iteration of the ILS procedure  
5 while not TerminationCriterion() do  
6    $\theta \leftarrow \theta_{ils}$ ;  
   // ===== Perturbation  
7   for  $i = 1, \dots, s$  do  $\theta \leftarrow$  random  $\theta' \in \text{Nbh}(\theta)$ ;  
   // ===== Basic local search  
8    $\theta \leftarrow$  IterativeFirstImprovement ( $\theta$ );  
   // ===== AcceptanceCriterion  
9   if  $\text{better}(\theta, \theta_{ils})$  then  $\theta_{ils} \leftarrow \theta$ ;  
10  with probability  $p_{restart}$  do  $\theta_{ils} \leftarrow$  random  $\theta \in \Theta$ ;  
11 return overall best  $\theta_{inc}$  found;  
12 Procedure IterativeFirstImprovement ( $\theta$ )  
13 repeat  
14    $\theta' \leftarrow \theta$ ;  
15   foreach  $\theta'' \in \text{Nbh}(\theta')$  in randomized order do  
16     if  $\text{better}(\theta'', \theta')$  then  $\theta \leftarrow \theta''$ ; break;  
17 until  $\theta' = \theta$ ;  
18 return  $\theta$ ;
```

Initialization

Main body of the ILS procedure

How to define $\text{better}(\theta'', \theta')$?

FocusedILS

The question is how to choose the optimal number of training instances, N ?

- Using too small N leads to good training performance, but poor generalization to previously unseen test benchmarks.
- On the other hand, we cannot evaluate every parameter configuration on an enormous training set - if we did, search progress would be unreasonably slow.

FocusedILS is a variant of ParamILS that **adaptively varies the number of training samples** considered from one parameter configuration to another in order **to focus samples on promising configurations.**

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The question is how to compare two parameter configurations θ_1 and θ_2 for which $N(\theta_1) \leq N(\theta_2)$?

- *What if we computed the empirical statistics based on the available number of runs for each configuration?*

Can lead to systematic bias if, for example, the first instances are easier than the average ones.

FocusedILS: Procedure $better_{Foc}(\theta_1, \theta_2)$

Domination: Configuration θ_1 dominates θ_2 when at least as many runs have been conducted on θ_1 as on θ_2 , and the performance of $\mathcal{A}(\theta)$ on the first $N(\theta_2)$ runs is at least as good as that of $\mathcal{A}(\theta_2)$ on all of its runs.

θ_1 dominates θ_2 if and only if $N(\theta_1) \geq N(\theta_2)$ and $\widehat{c}_{N(\theta_2)}(\theta_1) \leq \widehat{c}_{N(\theta_2)}(\theta_2)$.

FocusedILS – procedure $better_{Foc}(\theta_1, \theta_2)$ implements a comparison strategy based on the domination

1. first it acquires one additional run for the configuration i having smaller $N(\theta_i)$, or one run for both configurations if $N(\theta_1) = N(\theta_2)$;
2. then, it continues performing runs in this way until one configuration dominates the other.
It returns true if θ_1 dominates θ_2 , and false otherwise.

It keeps track of the total number, B , of configurations evaluated since the last improving step.

- Whenever $better_{Foc}(\theta_1, \theta_2)$ returns true, B extra (bonus) runs are performed for θ_1 and B is reset to 0.
- This way it is ensured that many runs are performed with good configurations \implies the error made in every comparison of two configurations θ_1 and θ_2 decreases on expectation.

Recommended Material

Frank Hutter, Holger H. Hoos, Kevin Leyton-Brown, and Thomas Stützle: ParamILS: An Automatic Algorithm Configuration Framework. In *Journal of Artificial Intelligence Research (JAIR)*, volume 36, pp. 267-306, October 2009.

Other papers and SW available at <http://www.cs.ubc.ca/labs/beta/Projects/ParamILS/>

