

# Funkční zobrazování a mapování mozku fMRI

J. Kybic, J. Hirsch<sup>1</sup>, J. Hornak<sup>2</sup>, M. Bock, J. Hozman, a další<sup>3</sup>

2008–2020

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<sup>1</sup><http://www.fmri.org>

<sup>2</sup><http://www.cis.rit.edu/htbooks/mri/>

<sup>3</sup><http://www.biac.duke.edu/education/courses/fall04/fmri/>

# Úvod

## Motivace a historie

- Anatomie

- Modality pro funkční zobrazování

## Aplikace

- Normální mozková aktivita

- Plánování operací

## fMRI

- Principy

- Příklad experimentu

## Vyhodnocování fMRI dat

- Signál a šum

- Lineární model

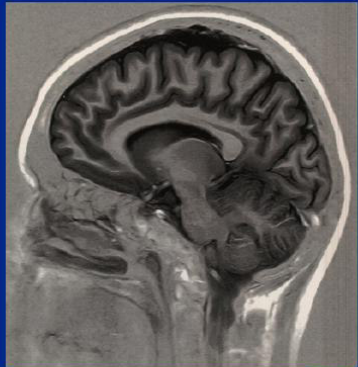
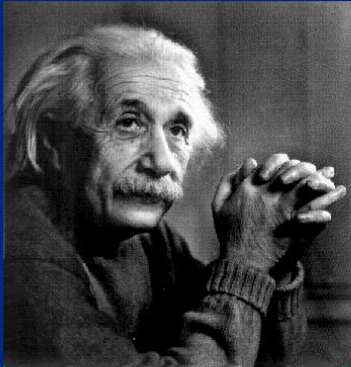
- Statistické testování

- Výběr regresorů

- Návrh experimentu

## (f)MRI — závěr

# A New View of Brain and Mind: Functional Neuroimaging



Columbia fMRI

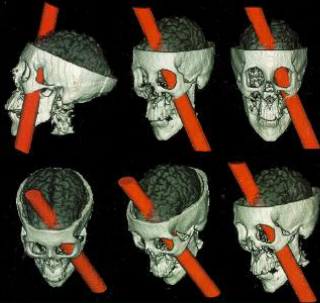


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SCIENCE

# SCIENCE

20 MAY 1994  
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\$6.00



**Paul Broca (1861)**  
Observed language-related  
deficits following left frontal  
damage to the brain.

**Karl Wernicke (1874)**  
Reported language-related  
deficits and motor deficits  
following left temporal  
damage to the brain.

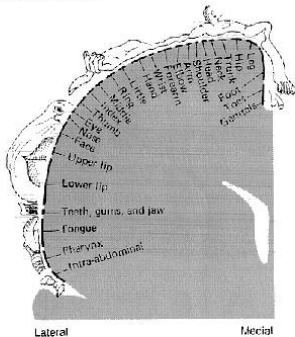
Columbia fMRI



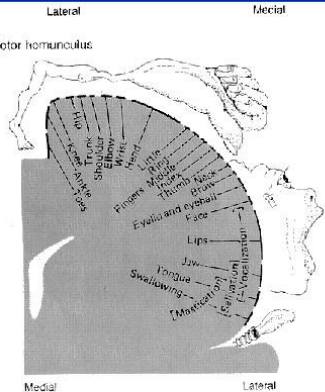
Wilder Penfield  
(1937-1954)

# Direct Cortical Stimulation

A Sensory homunculus



B Motor homunculus



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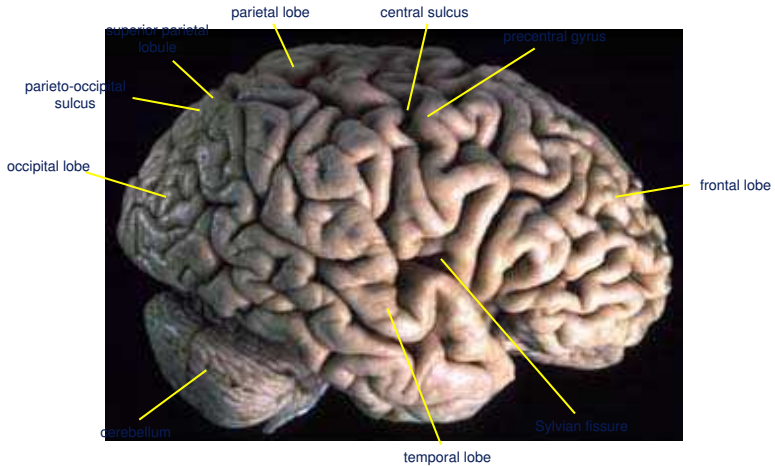
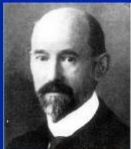


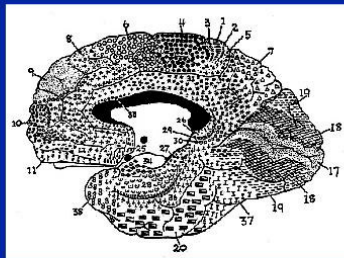
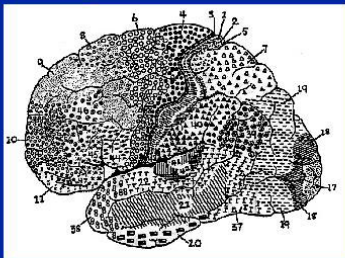
Fig 2.13



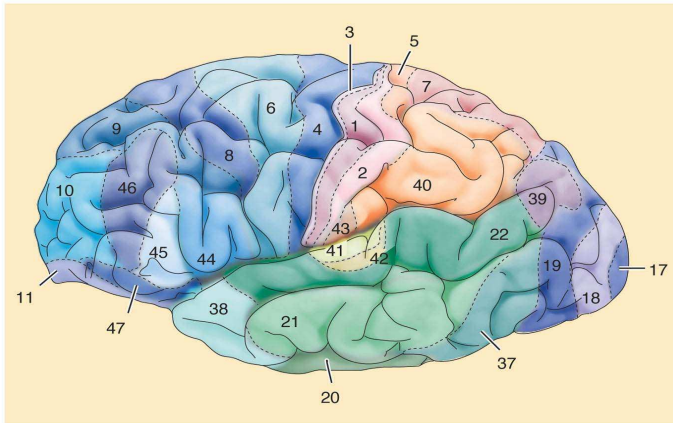
Korbinian  
Brodmann 1909



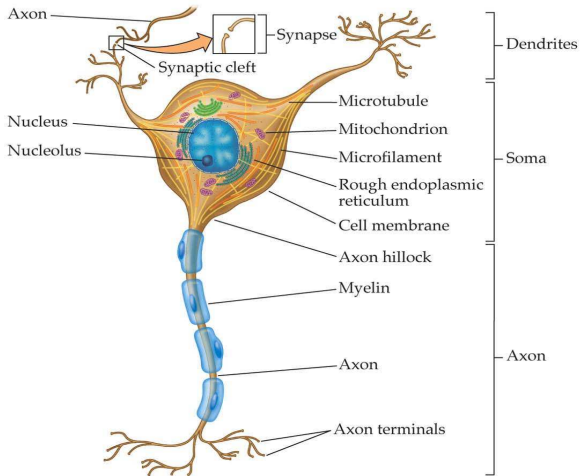
# Cortical Cytoarchitecture



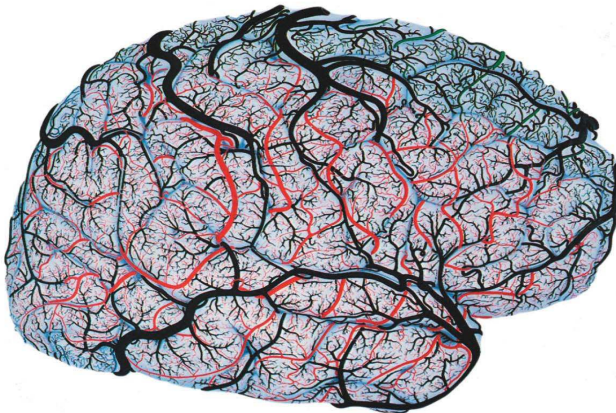
# Cytoarchitectonic map, Brodman



Mikrostruktura



Zásobování mozku krví



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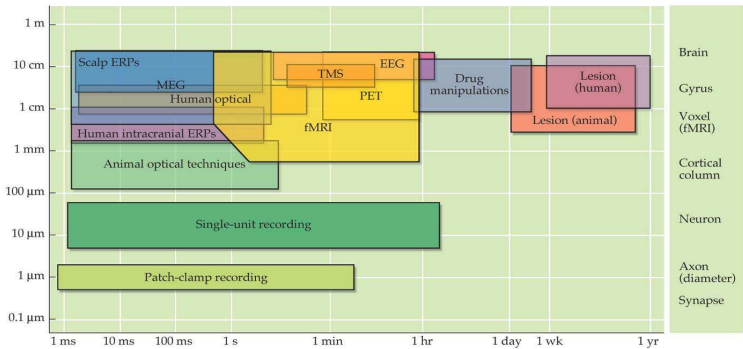
### (f)MRI — závěr

# Jak lokalizovat funkci mozku

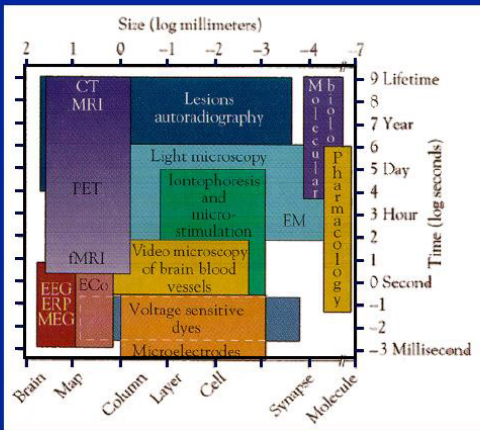
(Shrnutí a připomenutí)

- Invazivní
  - Následky zranění
  - Následky operací
  - Přímá stimulace (dnes jen na zvířatech)
  - Snímací elektrody
  - Optické snímání (při otevřené lebce svítíme laserem, optické vlastnosti se mění s průtokem krve a s elektrickým polem)
- Neinvazivní
  - MEG, EEG
  - fMRI
  - PET





FUNCTIONAL MAGNETIC RESONANCE IMAGING, Figure 1.7 © 2004 Sinauer Associates, Inc.



From: *Images of Mind* by Posner, M. and Raichle, M.  
 Scientific American Library, 1994, p. 24



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### (f)MRI — závěr

# Aplikace funkčního mapování mozku

- Porozumění struktuře mozku
- Porozumění procesům vnímání a myšlení
- Nové terapie
  - Porozumění fyziologickým příčinám duševních chorob
  - Porozumění fyziologickým příčinám bolesti a reakci na bolest
  - Porozumění účinkům drog
- Plánování operací
  - Identifikace nefunkčního centra
  - Omezení poškození důležitých center při chirurgické léčbě (epilepsie)

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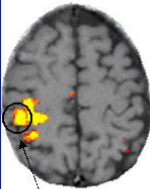
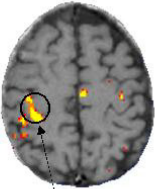
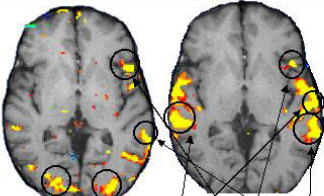
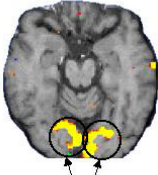
Statistické testování

Výběr regresorů

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## (f)MRI — závěr

# Standard Brain Mapping Tasks

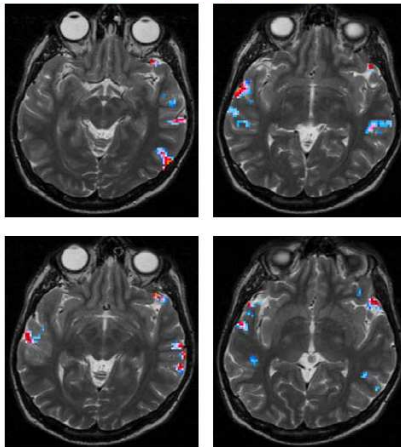
<b>SENSORY</b>	<b>MOTOR</b>	<b>LANGUAGE</b>		<b>VISION</b>
<b>Touch</b>	<b>Finger Thumb Tapping</b>	<b>Picture Naming</b>	<b>Listening to Words</b>	<b>Reversing Checkerboard</b>
(passive)	(active)	(active)	(passive)	(passive)
				
<b>GPoC</b>	<b>GPrC</b>	<b>GOi</b>	<b>GTT</b> <b>GFi</b> <b>GTs</b>	<b>CaS</b>

From Hirsch, J., et al; Neurosurgery 47: 711-722, 2000



## Funkční zobrazování (fMRI)

- Jsou vidět části mozku, které se používají při určité činnosti.
- Na obrázcích je činnost mozku při překladu slov.



# Sensory Motor Mapping

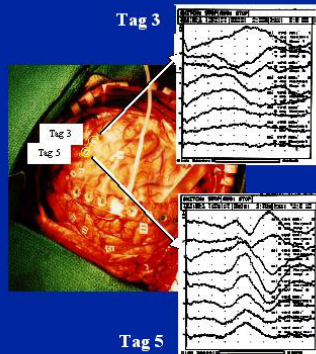
Craniotomy

SSEP

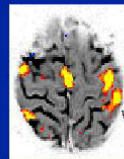
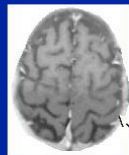
Direct Cortical  
Stimulation

Reference  
Image

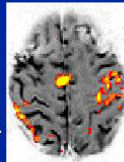
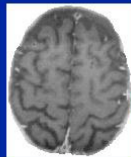
fMRI  
Localization



“Twitching of  
hand,  
focal seizure  
involving arm ”



“Twitching in  
1st three  
digits”



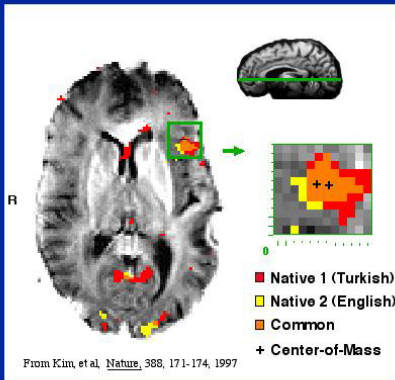
Columbia fMRI

From Hirsch, J., et al; Neurosurgery 47: 711-722, 2000





## “EARLY” BILINGUAL (Subject G) ANTERIOR Language Area



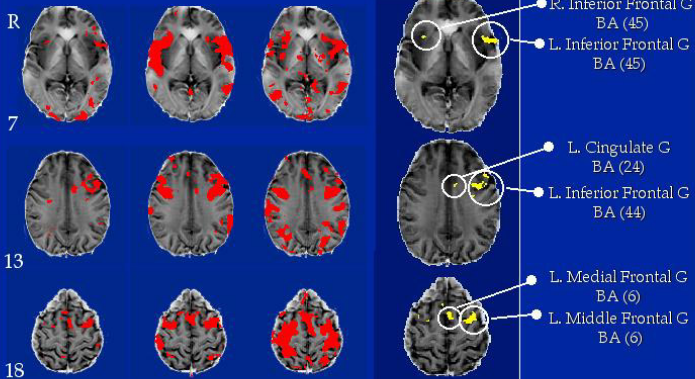
# OBJECT NAMING

VISUAL    AUDITORY    TACTILE =

**COMMON  
AREAS**

## OBJECT NAMING NETWORK

Subject HB

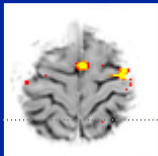


Hirsch, Moreno & Kim, *J. Cognitive Neuroscience*, 13, 1-16, 2001.



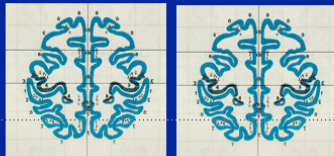
# Labeling of Active Brain Areas

Functional Brain



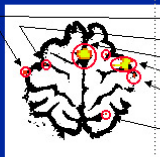
activity

Atlas Brain



labels

transfer



<u>Name</u>	<u>BA</u>	<u>Sector</u>
GPrC	4	c,E
GFs	6	b,E
GFd	6	a,E,60,-a
GFs	6	b,E,60
GRC	4	c,E,60
LPs	7	b,G,60

Columbia fMRI



# Co-Planar Stereotaxic Atlas of the Human Brain

3-Dimensional Proportional System: An Approach to Cerebral Imaging

Jean Talairach  
Pierre Tournoux  
Translated by  
Mark Royport

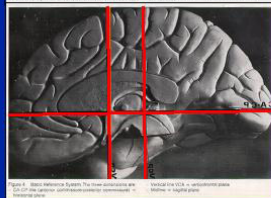
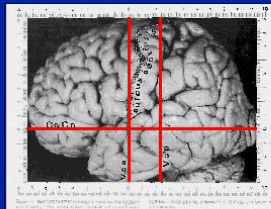
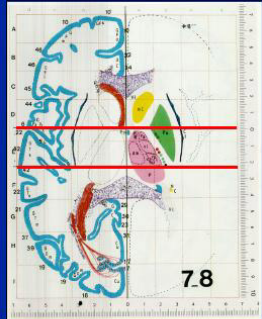
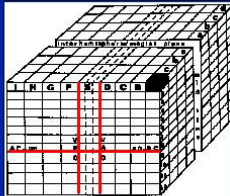
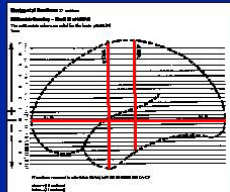
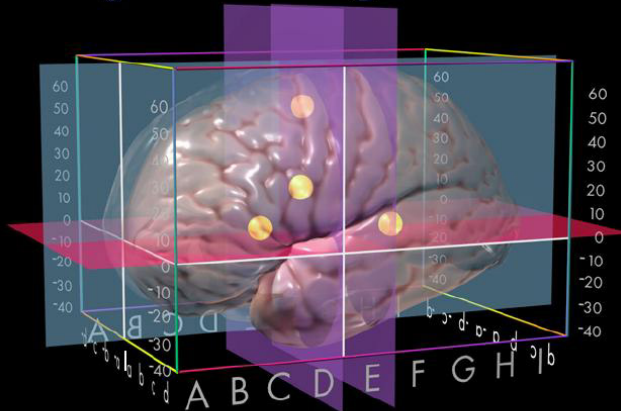


Figure 1. Lateral view of the human brain. The three axes are defined by the VSP, VAP, and VCP. The VSP is vertical, the VAP is horizontal, and the VCP is depth. The VSP is vertical, the VAP is horizontal, and the VCP is depth.



# Object Naming Network



Hirsch, Moreno & Kim, *J. Cognitive Neuroscience*, 13, 1-16, 2001.

**Columbia fMRI**



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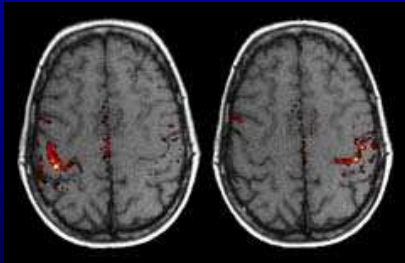
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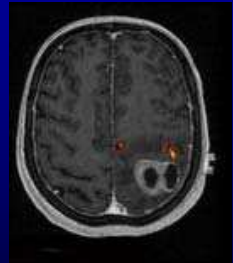
Návrh experimentu

### (f)MRI — závěr

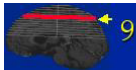
# Application: (Neuro)functional MRI



Volunteer



Patient w/ Glioblastoma

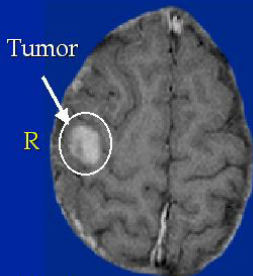


# IMAGING

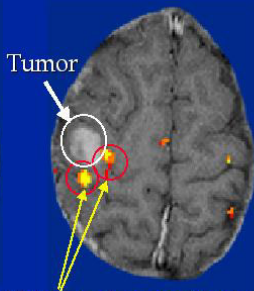
CONVENTIONAL

FUNCTIONAL

AFTER SURGERY



slice 9



Left Hand: Sensory/Motor



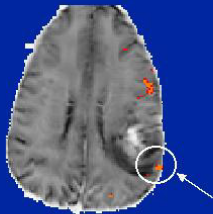
Left Hand Movement



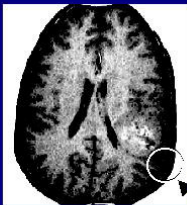


# Intra-Operative Language Mapping

## fMRI Map



## Cortical Stimulation



Word finding  
difficulty during  
picture naming



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## Essential Discoveries that enable PET and fMRI

Angelo Mosso



1881 Observed that blood flow changes were associated with mental activity

1890 Roy and Sherrington described an “intrinsic mechanism by which the vascular supply of the brain can be varied locally in correspondence with local variations in functional activity.”

Linus Pauling



1936 Discovered the Magnetic Properties of Hgb

Siege Ogawa



1991 Discovered the Blood Oxygen Level Dependent (BOLD) Signal



## PHYSIOLOGY

NEURAL ACTIVATION  
IS ASSOCIATED WITH AN  
INCREASE IN BLOOD FLOW

O<sub>2</sub> EXTRACTION IS  
RELATIVELY UNCHANGED

RESULT:  
REDUCTION IN THE  
PROPORTION OF DEOXY HGB  
IN THE LOCAL VASCULATURE

## PHYSICS

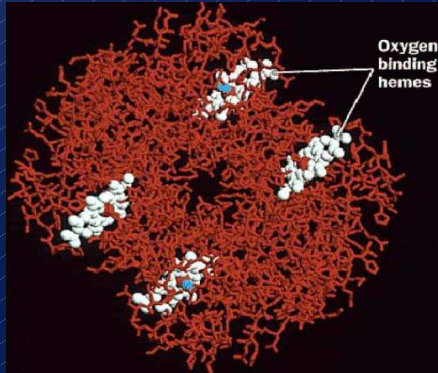
DEOXY HGB  
IS PARAMAGNETIC

AND DISTORTS THE LOCAL  
MAGNETIC FIELD CAUSING  
SIGNAL LOSS

RESULT:  
LESS DISTORTION OF THE  
MAGNETIC FIELD RESULTS IN  
LOCAL SIGNAL INCREASE



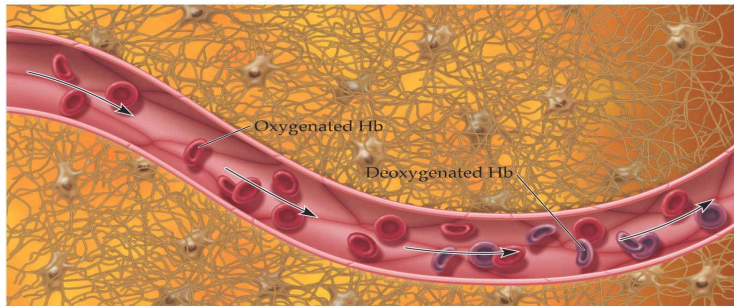
# Hemoglobin Molecule

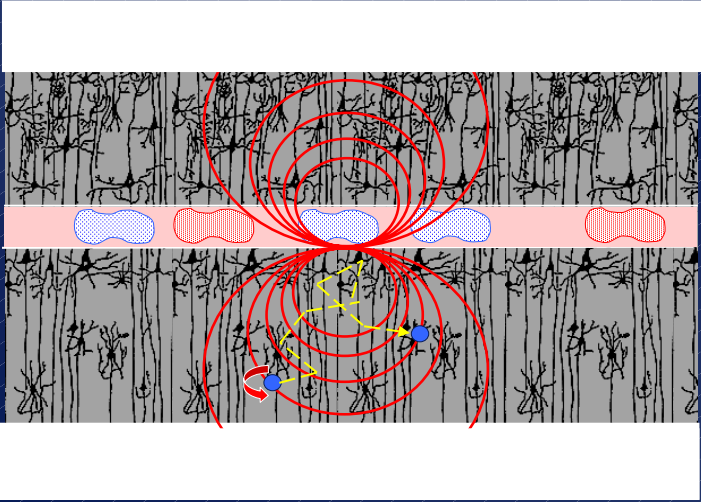


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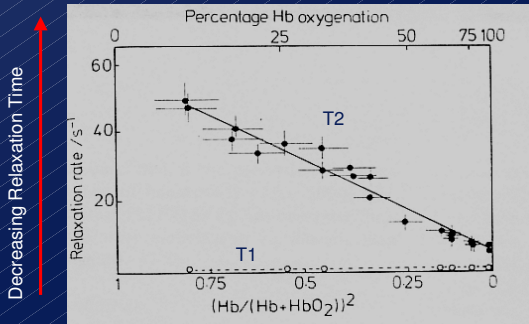
# BOLD Signal Generation

(B)





## Blood Deoxygenation affects T<sub>2</sub> Recovery



Increasing Blood Oxygenation

Thulborn et al., 1982

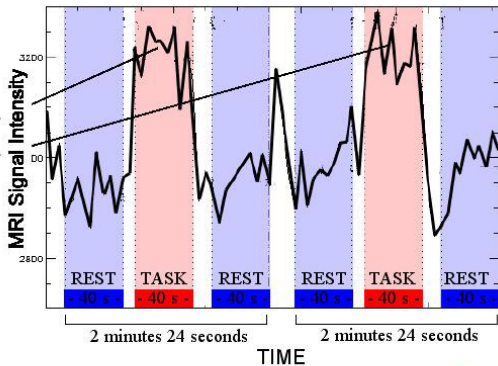
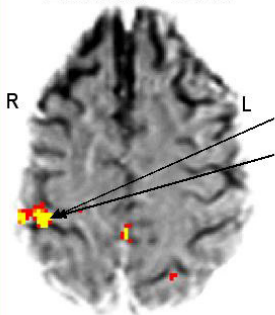


# BOLD

- **B**lood **O**xxygen **L**evel **D**ependent
- Gradient echo, EPI (kvůli rychlosti)
- Paramagnetické vlastnosti deoxyhemoglobinu → nehomogenita pole →  $T_2^*$  efekt
- Velmi slabý signál (SNR  $\approx 0.1$ )
- Průměrování:
  - Opakujeme např. 10 bloků (snímání) bez aktivity
  - ... 10 bloků (snímání) s aktivitou

# Magnetic Resonance Signals to Location of Function

Left Hand - Touch

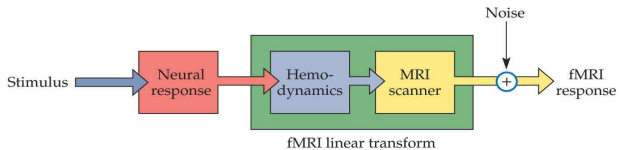


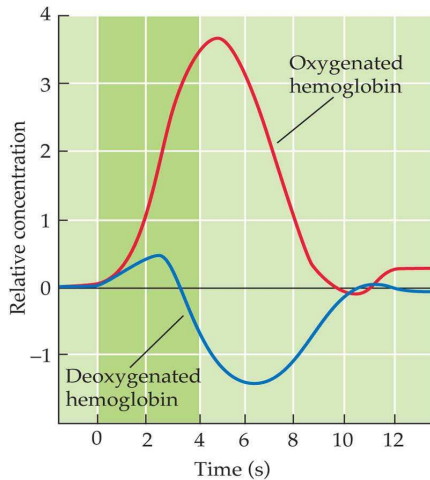
# Hemodynamická odezva

## Hemodynamic response

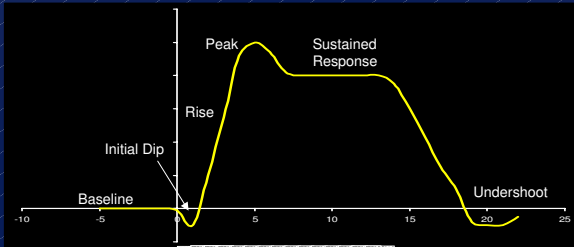
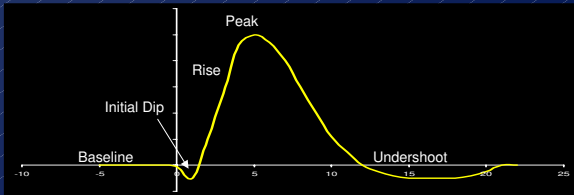
- Nervová aktivita → zásobování krví → BOLD signál
- Reakce není okamžitá, impulzní charakteristika se nazývá **hemodynamická odezva**
- Odezva se liší mezi subjekty i v rámci jednoho subjektu

# Hemodynamic response





## Basic Form of Hemodynamic Response



# fMRI IMAGING PARAMETERS

**SCANNER:**

GE Signa 1.5 T  
EPI Capability

**IN-PLANE RESOLUTION:** 1.5 mm x 1.5 mm

**SLICE THICKNESS:** 4.5 mm

**SLICE SEPARATION:** 0 mm

**NUMBER OF SLICES:** 21

**SLICE ORIENTATION:** Axial on AC/PC Line

**RESONATOR:** GE “bird cage”

**SEQUENCE:** GRADIENT ECHO

TR = 4000 msec TE = 60 msec

Flip Angle = 60 deg



## Position of Headcoil and Mirror





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Signál a šum

Lineární model

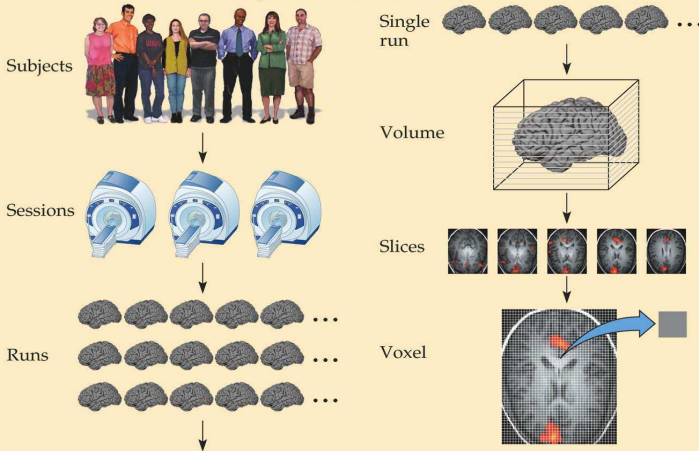
Statistické testování

Výběr regresorů

Návrh experimentu

### (f)MRI — závěr

# fMRI experimental data hierarchy



# The Experiment:

## fMRI adaptation of classic PET experiment

- Three Conditions in 21 second epochs
- 1st Condition: Word Generation



# The Experiment:

## fMRI adaptation of classic PET experiment

- Three Conditions in 21 second epochs
- 1st Condition: Word Generation

Noun is presented

Jellyfish

Screen

Healthy  
Volunteer



Bed

Scanner

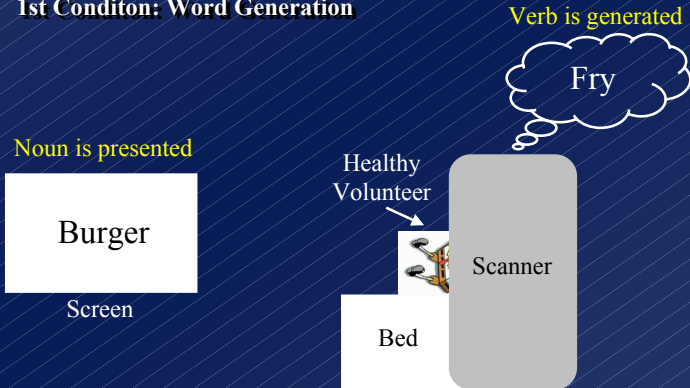
Verb is generated

Catch

# The Experiment:

## fMRI adaptation of classic PET experiment

- Three Conditions in 21 second epochs
- 1st Condition: Word Generation



# The Experiment:

## fMRI adaptation of classic PET experiment

- Three Conditions in 21 second epochs
- 1st Condition: Word Generation
- 2nd Condition: Word Shadowing

Verb is presented

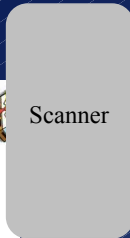


Screen

Healthy  
Volunteer



Bed



Verb is repeated



# The Experiment:

## fMRI adaptation of classic PET experiment

- Three Conditions in 21 second epochs
- 1st Condition: Word Generation
- 2nd Condition: Word Shadowing

Verb is presented

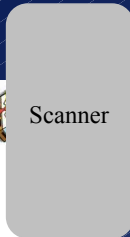


Screen

Healthy  
Volunteer



Bed



Verb is repeated



# The Experiment:

## fMRI adaptation of classic PET experiment

- Three Conditions in 21 second epochs
- 1st Condition: Word Generation
- 2nd Condition: Word Shadowing
- 3rd Condition: Baseline

Hair-cross is shown



Screen

Healthy  
Volunteer



Scanner

Bed



# The Experiment:

## fMRI adaptation of classic PET experiment

- Three Conditions in 21 second epochs
- 1st Condition: Word Generation
- 2nd Condition: Word Shadowing
- 3rd Condition: Baseline

Hair-cross is shown



Screen

Healthy  
Volunteer



Bed

Scanner

Z  
Z  
Z  
Z  
Z  
Z  
Z  
Z  
Z  
Z  
Z

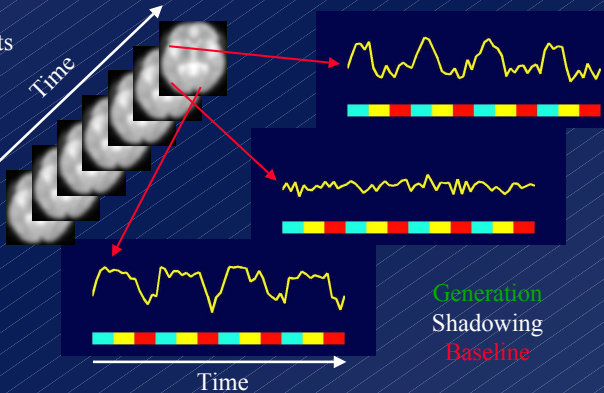
# The Data: Set of Volumes or Set of Time-series

Serial Snapshots  
of Volunteers  
brain

Time



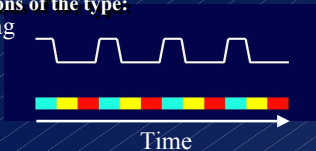
Volunteer



Generation  
Shadowing  
Baseline

## The Model: A Set of Hypothetical Time-series

- A **model** consists of a set of assumptions of the type:  
"I think a voxel that is into generating words might have a time-series looking like this"
- and



"A voxel that is into repeating, like this"



and

"A voxel that just doesn't care, like this"



Generation Shadowing Baseline

## Úvod

### Motivace a historie

Anatomie

Modality pro funkční zobrazování

### Aplikace

Normální mozková aktivita

Plánování operací

### fMRI

Principy

Příklad experimentu

### Vyhodnocování fMRI dat

Signál a šum

Lineární model

Statistické testování

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Návrh experimentu

### (f)MRI — závěr

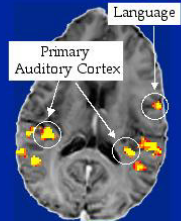
# COMPUTATIONS FOR FUNCTIONAL IMAGE PROCESSING

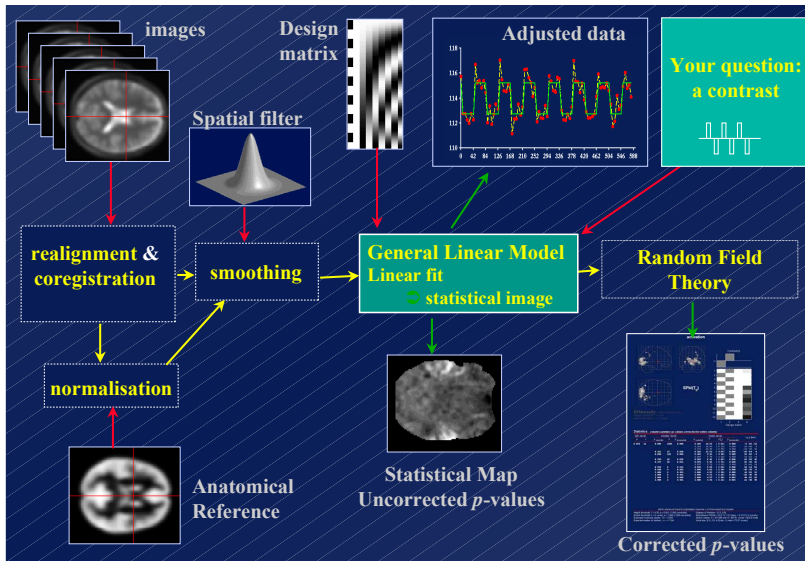
**Scanner**



RECONSTRUCTION  
ALIGNMENT  
VOXEL BY VOXEL  
ANALYSIS  
GRAPHICAL  
REPRESENTATION

**Functional  
Brain Map**





## Úvod

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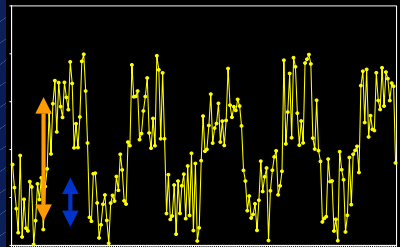
### (f)MRI — závěr

# Signal-Noise-Ratio (SNR)

**Task-Related  
Variability**

---

**Non-task-related  
Variability**





## What are typical SNRs for fMRI data?

- **Signal amplitude**
  - MR units: 5-10 units (baseline: ~700)
  - Percent signal change: 0.5-2%
- **Noise amplitude**
  - MR units: 10-50
  - Percent signal change: 0.5-5%
- **SNR range**
  - Total range: 0.1 to 4.0
  - Typical: 0.2 – 0.5

# Types of Noise

- **Thermal noise**
  - Responsible for variation in background
  - Eddy currents, scanner heating
- **Power fluctuations**
  - Typically caused by scanner problems
- **Variation in subject cognition**
  - Timing of processes
- **Head motion effects**
- **Physiological changes**
- **Differences across brain regions**
  - Functional differences
  - Large vessel effects
- **Artifact-induced problems**

## **Variability in Subject Behavior: Issues**

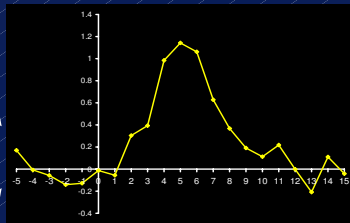
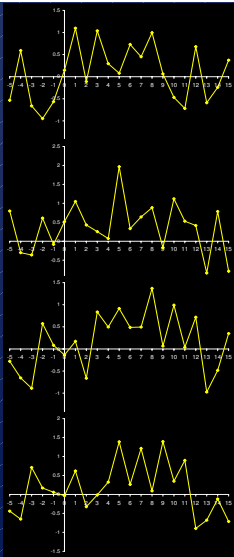
- **Cognitive processes are not static**
  - May take time to engage
  - Often variable across trials
  - Subjects' attention/arousal wax and wane
- **Subjects adopt different strategies**
  - Feedback- or sequence-based
  - Problem-solving methods
- **Subjects engage in non-task cognition**
  - Non-task periods do not have the absence of thinking

What can we do about these problems?

## Trial Averaging

- **Static signal, variable noise**
  - Assumes that the MR data recorded on each trial are composed of a signal + (random) noise
- **Effects of averaging**
  - Signal is present on every trial, so it remains constant through averaging
  - Noise randomly varies across trials, so it decreases with averaging
  - Thus, SNR increases with averaging

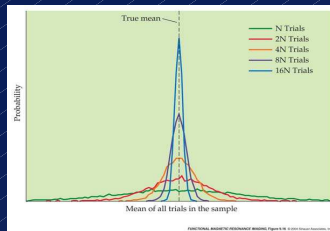
# Trial averaging



Average of 16 trials  
with SNR = 0.6

# Fundamental Rule of SNR

For Gaussian noise, experimental power increases with the square root of the number of observations



## **Caveats**

- **Signal averaging is based on assumptions**
  - **Data = signal + temporally invariant noise**
  - **Noise is uncorrelated over time**
- **If assumptions are violated, then averaging ignores potentially valuable information**
  - **Amount of noise varies over time**
  - **Some noise is temporally correlated (physiology)**
- **Nevertheless, averaging provides robust, reliable method for determining brain activity**

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### (f)MRI — závěr



## Signal, noise, and the General Linear Model

$$Y = \alpha M + \varepsilon$$

Measured Data

Amplitude (solve for)

Design Model

Noise

Cf. Boynton et al., 1996

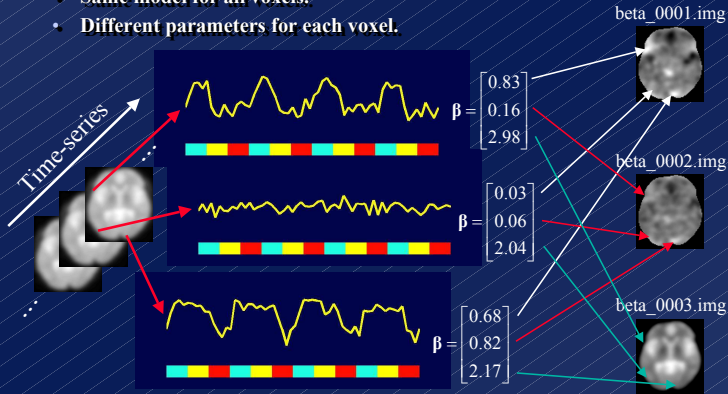




# The Estimation:

## The format of data, model and parameters

- Same model for all voxels.
- Different parameters for each voxel.

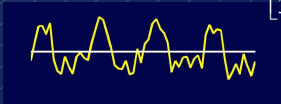


# The estimation revisited

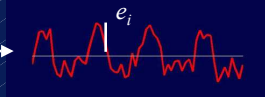
## What do I mean by "best" fit

- Data
- Some fit

$$\beta = \begin{bmatrix} 0 \\ 0 \\ 3.31 \end{bmatrix}$$



- Error

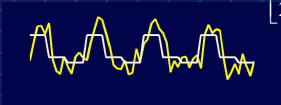


$$\sum_{i=1}^n e_i^2 = 17.16$$

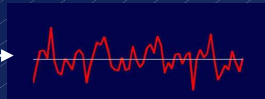
$$\sum_{i=1}^n e_i = 0$$

- Data
- Best fit

$$\beta = \begin{bmatrix} 0.83 \\ 0.16 \\ 2.98 \end{bmatrix}$$



- Error

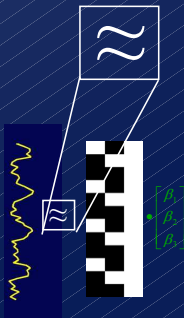


$$\sum_{i=1}^n e_i^2 = 9.47$$

$$\sum_{i=1}^n e_i = 0$$

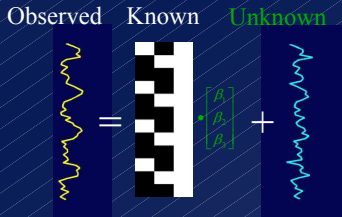
## Model revisited – again

Now, what's that  
all about?



Remember?

We need a model for the error!



$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{e}$$

$$\mathbf{e} \sim N(\mathbf{0}, \sigma^2 \mathbf{I})$$



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**Statistické testování**

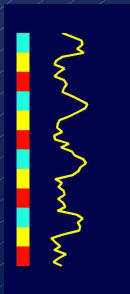
Výběr regresorů

Návrh experimentu

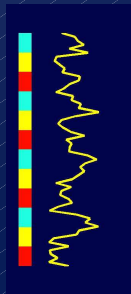
### (f)MRI — závěr



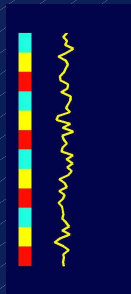
But why do we need the error?  
Would you trust these?



$\beta_1=1$   
 $\sigma=0.2$   
 $n=60$



$\beta_1=1$   
 $\sigma=0.5$   
 $n=60$



$\beta_1=0.3$   
 $\sigma=0.2$   
 $n=60$



$\beta_1=1$   
 $\sigma=0.2$   
 $n=15$

## But why do we need the error?

In conclusion:

- We trust long series with **large effects** and **small error**.

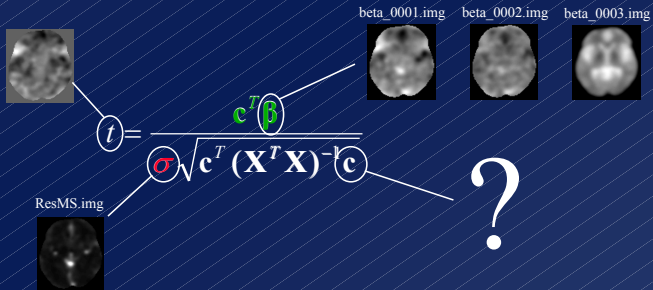
$$t = \frac{c^T \beta}{\sigma \sqrt{c^T (\mathbf{X}^T \mathbf{X})^{-1} c}}$$

Effect size

Uncertainty of effect size

## t-test

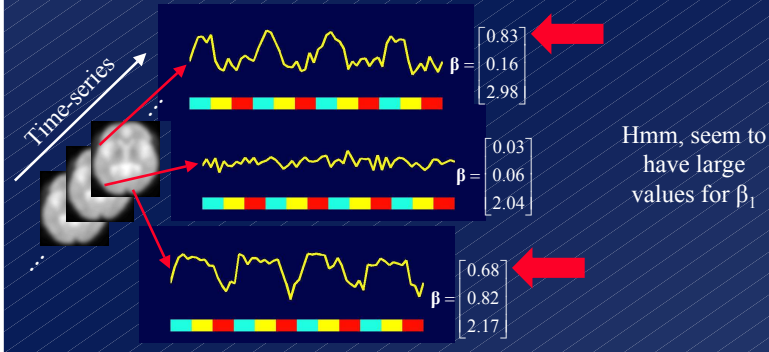
- We trust: Long series with **large effects** and **small error**.





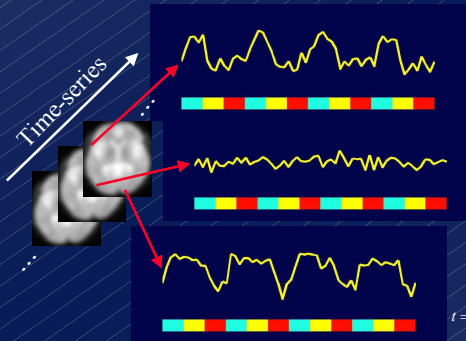
## Asking questions of your data *t*-contrasts

- Can we find voxels that are active in word-generation tasks?



## Asking questions of your data *t*-contrasts

- Can we find voxels that are active in word-generation tasks?



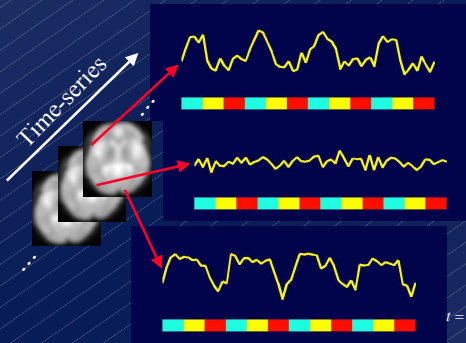
$$t = \frac{[1 \ 0 \ 0] \begin{bmatrix} 0.83 \\ 0.16 \\ 2.98 \end{bmatrix}}{0.41 * 0.32} = \frac{0.83}{0.41 * 0.32} = 6.42^{**}$$

$$t = \frac{[1 \ 0 \ 0] \begin{bmatrix} 0.03 \\ 0.06 \\ 2.04 \end{bmatrix}}{0.19 * 0.32} = \frac{0.03}{0.19 * 0.32} = 0.44$$

$$t = \frac{[1 \ 0 \ 0] \begin{bmatrix} 0.68 \\ 0.82 \\ 2.17 \end{bmatrix}}{0.40 * 0.32} = \frac{0.68}{0.40 * 0.32} = 5.41^{**}$$

## Asking questions of your data *t*-contrasts

- Voxels that are more active in generation than shadowing?



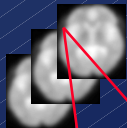
$$t = \frac{\begin{bmatrix} 1 & -1 & 0 \end{bmatrix} \begin{bmatrix} 0.83 \\ 0.16 \\ 2.98 \end{bmatrix}}{0.41 * 0.32} = \frac{0.67}{0.41 * 0.32} = 5.16^{**}$$

$$t = \frac{\begin{bmatrix} 1 & -1 & 0 \end{bmatrix} \begin{bmatrix} 0.03 \\ 0.06 \\ 2.04 \end{bmatrix}}{0.19 * 0.32} = \frac{-0.03}{0.19 * 0.32} = -0.58$$

$$t = \frac{\begin{bmatrix} 1 & -1 & 0 \end{bmatrix} \begin{bmatrix} 0.68 \\ 0.82 \\ 2.17 \end{bmatrix}}{0.40 * 0.32} = \frac{-0.14}{0.40 * 0.32} = -1.12$$

I'm sorry, can you pose that question differently?

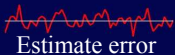
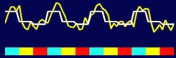
## *F*-contrasts



$$\beta = \begin{bmatrix} 0.83 \\ 0.16 \\ 2.98 \end{bmatrix}$$

Fit model

Get data

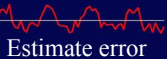
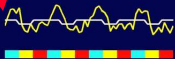


$$t^2 =$$



$$\beta = \begin{bmatrix} -0.25 \\ 3.40 \end{bmatrix}$$

Fit reduced model



$$t^2 =$$

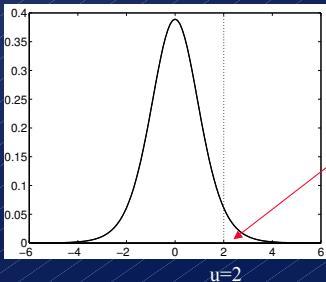
$$F \sim \frac{\text{green bar}}{\text{red bar}} = 41.21$$

(sort of)

cf.



## Inference at a single voxel



t-distribution

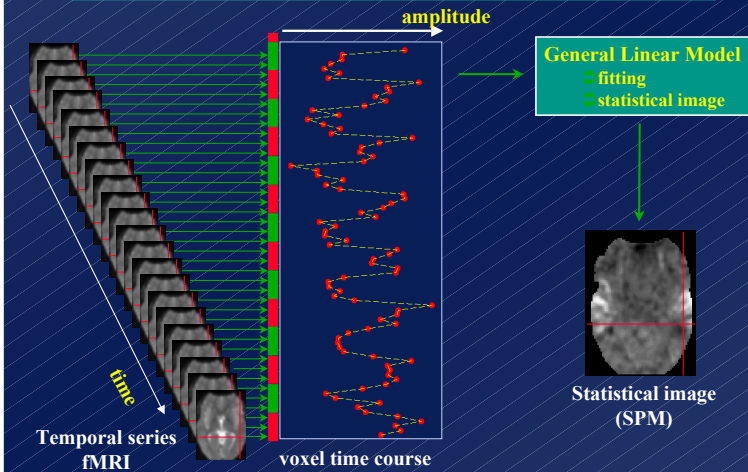
NULL hypothesis,  $H_0$ : activation is zero

$$\alpha = p(t > u | H_0)$$

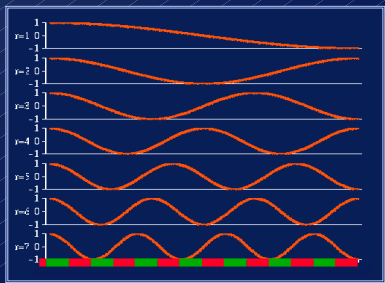
p-value: probability of getting a value of  $t$  at least as extreme as  $u$ . If  $\alpha$  is small we reject the null hypothesis.

$$u = (\text{effect size}) / \text{std}(\text{effect size})$$

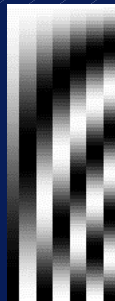
# One voxel = One test (t, F, ...)



**Add more reference functions ...**



**Discrete cosine transform basis functions**



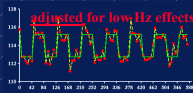
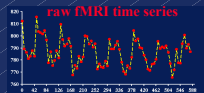
## ...design matrix

The diagram illustrates the linear regression equation  $Y = X\beta + \epsilon$  using matrix and vector notation. On the left, a vertical vector  $Y$  is labeled "Data vector". This is followed by an equals sign, then a matrix  $X$  labeled "design matrix", which is multiplied by a vector  $\beta$  labeled "parameters". The vector  $\beta$  contains the parameters  $\alpha$ ,  $\mu$ ,  $\beta_3$ ,  $\beta_4$ ,  $\beta_5$ ,  $\beta_6$ ,  $\beta_7$ ,  $\beta_8$ , and  $\beta_9$ . A plus sign follows, then a vertical vector  $\epsilon$  labeled "error vector". A large diagonal label " $=$  the betas (here: 1 to 9)" points to the  $\beta$  vector.

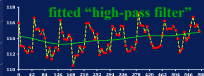
$$Y = X\beta + \epsilon$$

Labels: Data vector, design matrix, parameters, error vector, the betas (here: 1 to 9)

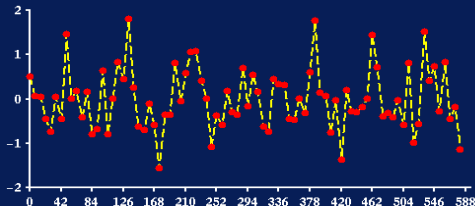
**Fitting the model = finding some estimate of the betas  
= minimising the sum of square of the residuals  $S^2$**



fitted box-car



residuals



$$\frac{\sum \text{the squared values of the residuals}}{\text{number of time points minus the number of estimated betas}} = S^2$$

## Summary ...

- ◆ *We put in our model regressors (or covariates) that represent how we think the signal is varying (of interest and of no interest alike)*
- ◆ *Coefficients (= parameters) are estimated using the Ordinary Least Squares (OLS) or Maximum Likelihood (ML) estimator.*
- ◆ *These estimated parameters (the “betas”) **depend** on the scaling of the regressors.*
- ◆ *The residuals, their sum of squares and the resulting tests (t,F), **do not** depend on the scaling of the regressors.*

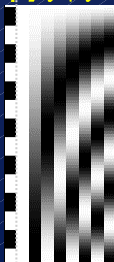


# T test - one dimensional contrasts - SPM{t}

A *contrast* = a linear combination of parameters:  $c' \times \beta$

$$c' = 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0$$

$b_1 \ b_2 \ b_3 \ b_4 \ b_5 \dots$



box-car amplitude  $> 0$  ?

=

$\beta_1 > 0$  ?

=>

Compute  $1 \times b_1 + 0 \times b_2 + 0 \times b_3 + 0 \times b_4 + 0 \times b_5 + \dots$

and

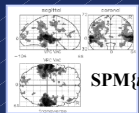
divide by estimated standard deviation

*contrast of  
estimated  
parameters*

$$T = \frac{\text{contrast of estimated parameters}}{\sqrt{\text{variance estimate}}}$$

$c' b$

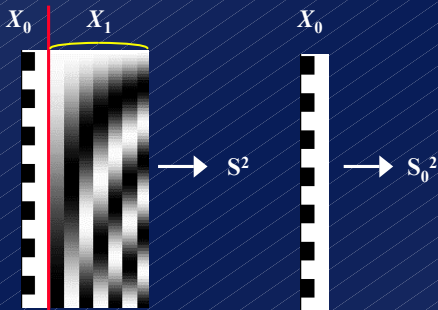
$$T = \frac{c' b}{\sqrt{s^2 c' (X' X)^{-1} c}}$$



## F-test (SPM{F}) : a reduced model or ...

*Tests multiple linear hypotheses : Does  $X_1$  model anything ?*

**$H_0$** : True (reduced) model is  $X_0$



This (full) model ?

Or this one?

**additional  
variance  
accounted for  
by tested effects**

$$F = \frac{\text{additional variance accounted for by tested effects}}{\text{error variance estimate}}$$

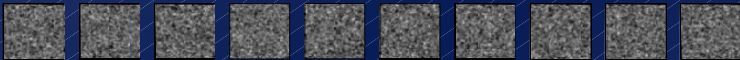
$$F \sim (S_0^2 - S^2) / S^2$$



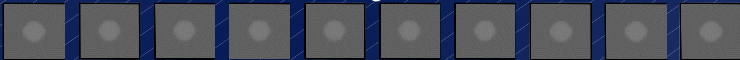
Bonferroni correction

# Inference for Images

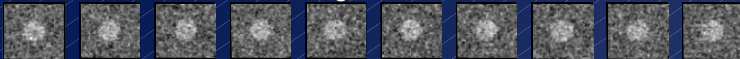
Noise



Signal



Signal+Noise



## Use of 'uncorrected' p-value, $\alpha=0.1$



Using an 'uncorrected' p-value of 0.1 will lead us to conclude on average that 10% of voxels are active when they are not.

This is clearly undesirable. To correct for this we can define a null hypothesis for images of statistics.

# Family-wise Null Hypothesis

*FAMILY-WISE NULL HYPOTHESIS:*

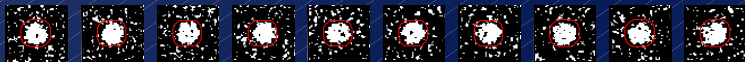
*Activation is zero everywhere*

If we reject a voxel null hypothesis  
at *any* voxel, we reject the family-wise  
Null hypothesis

A FP **anywhere** in the image  
gives a Family Wise Error (FWE)

Family-Wise Error (FWE) rate = 'corrected' p-value

Use of 'uncorrected' p-value,  $\alpha=0.1$



Use of 'corrected' p-value,  $\alpha=0.1$



FWE

## The Bonferroni correction

The Family-Wise Error rate (FWE),  $\alpha$ , for a family of  $N$  **independent** voxels is

$$\alpha = Nv$$

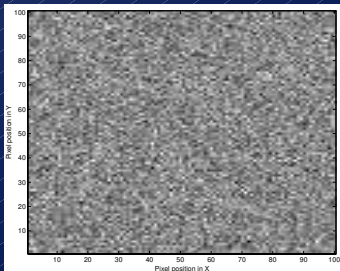
where  $v$  is the voxel-wise error rate. Therefore, to ensure a particular FWE set

$$v = \alpha / N$$

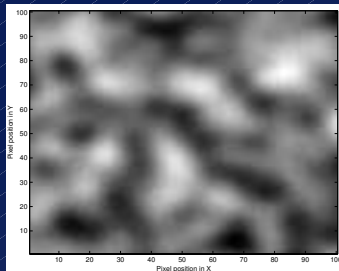
BUT ...

# The Bonferroni correction

Independent Voxels



Spatially Correlated Voxels



Bonferroni is too conservative for brain images

# Applied Smoothing

## Smoothness

smoothness » voxel size

practically

$$FWHM \geq 3 \times \text{VoxDim}$$

Typical applied smoothing:

Single Subj fMRI: 6mm

PET: 12mm

Multi Subj fMRI: 8-12mm

PET: 16mm



## Úvod

### Motivace a historie

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### Aplikace

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### fMRI

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Příklad experimentu

### Vyhodnocování fMRI dat

Signál a šum

Lineární model

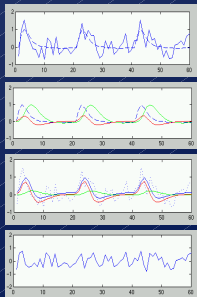
Statistické testování

**Výběr regresorů**

Návrh experimentu

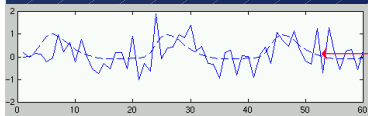
### (f)MRI — závěr

## Summary ... (2)

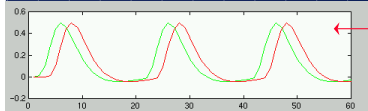


- ◆ *The residuals should be looked at ... (non random structure ?)*
- ◆ *We rather test flexible models if there is little a priori information, and precise ones with a lot a priori information*
- ◆ *In general, use the F-tests to look for an overall effect, then look at the betas or the adjusted data to characterise the response shape*
- ◆ *Interpreting the test on a single parameter (one regressor) can be difficult: cf the delay or magnitude situation*

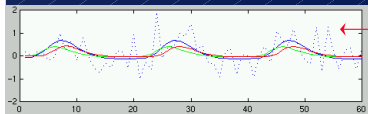
## Correlation between regressors



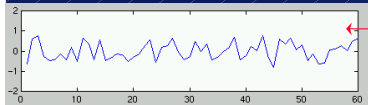
True signal



Model (green and red)



Fit (blue : global fit)



Residual

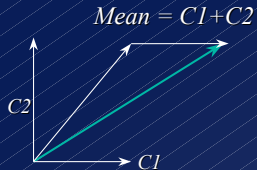
$\hat{\beta}?$ 

## “completely” correlated ...

$$Y = Xb + e$$

$$X = \begin{matrix} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \\ 0 & 1 & 1 \end{matrix}$$

$\swarrow$     $\uparrow$     $\swarrow$   
Cond 1   Cond 2   Mean



Parameters are **not unique** in general! Some contrasts have no meaning: **NON ESTIMABLE**

## Summary ... (3)

- ◆ *We implicitly test for an additional effect only, so we may miss the signal if there is some correlation in the model*
- ◆ *Orthogonalisation is not generally needed - parameters and test on the changed regressor don't change*
- ◆ *It is always simpler (if possible!) to have orthogonal regressors*
- ◆ *In case of correlation, use F-tests to see the overall significance. There is generally no way to decide to which regressor the « common » part should be attributed to*
- ◆ *In case of correlation and if you need to orthogonalise a part of the design matrix, there is no need to re-fit a new model: change the contrast*

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### (f)MRI — závěr

## **What is fMRI Experimental Design?**

- **Controlling the timing and quality of cognitive operations (IVs) to influence resulting brain processes (DVs)**
- **What can we control?**
  - **Experimental comparisons (what is to be measured?)**
  - **Stimulus properties (what is presented?)**
  - **Stimulus timing (when is it presented?)**
  - **Subject instructions (what do subjects do with it?)**

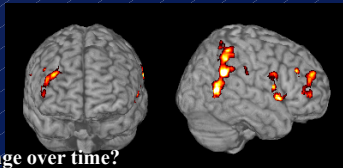
## **Refractory Periods**

- **Definition: a change in the responsiveness to an event based upon the presence or absence of a similar preceding event**
  - **Neuronal refractory period**
  - **Vascular refractory period**

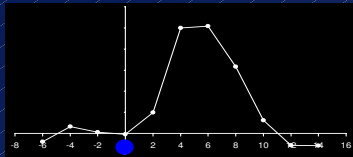


## Detection vs. Estimation

- **Detection:** What is active?



- **Estimation:** How does activity change over time?



# **fMRI Design Types**

- 1) Blocked Designs**
- 2) Event-Related Designs**
  - a) Periodic Single Trial**
  - b) Jittered Single Trial**
  - c) Staggered or Interleaved Single Trial**
- 3) Mixed Designs**
  - a) Combination blocked/event-related**
  - b) Variable stimulus probability**

# **fMRI Design Types**

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## What are Blocked Designs?

- **Blocked designs segregate different cognitive processes into distinct time periods**

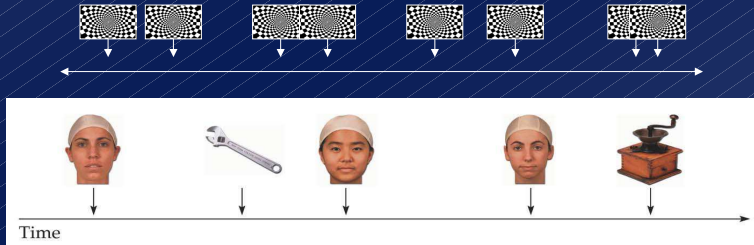


## **Limitations of Blocked Designs**

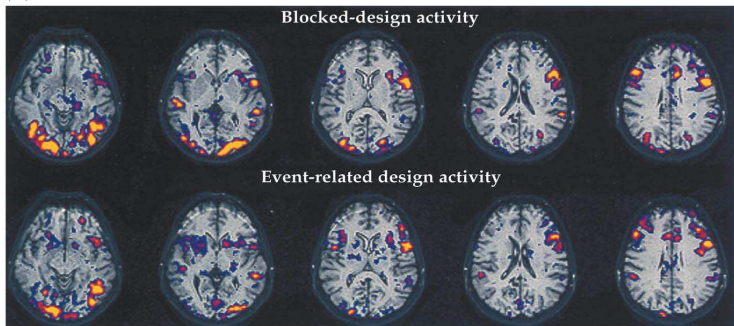
- **Very sensitive to signal drift**
  - Sensitive to head motion, especially when only a few blocks are used.
- **Poor choice of baseline may preclude meaningful conclusions**
- **Many tasks cannot be conducted repeatedly**
- **Difficult to estimate the HDR**

## What are Event-Related Designs?

- **Event-related designs associate brain processes with discrete events, which may occur at any point in the scanning session.**



(A)



Word-stem completion task. Blocked design: 30s on/off. Event-related design: 15s ISI.

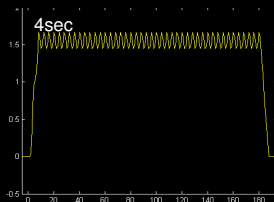
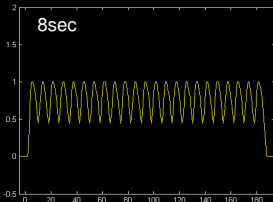
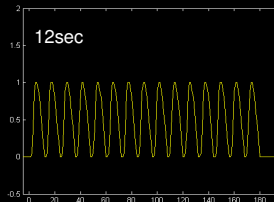
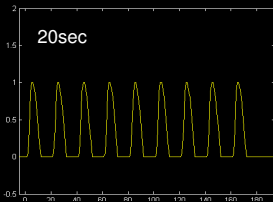
## 2a. Periodic Single Trial Designs

- Stimulus events presented infrequently with long interstimulus intervals





## Trial Spacing Effects: Periodic Designs

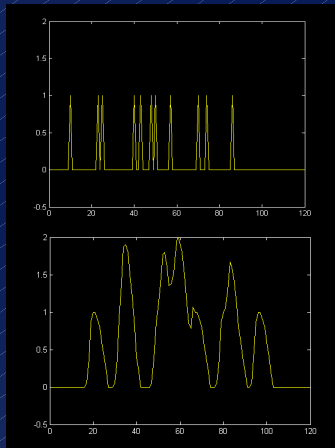
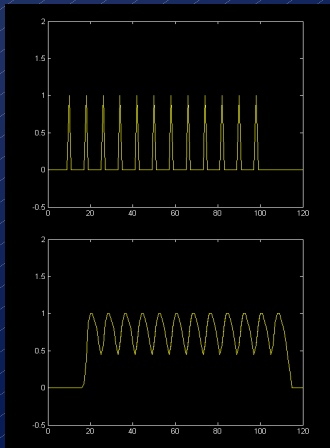


## 2b. Jittered Single Trial Designs

- Varying the timing of trials within a run
- Varying the timing of events within a trial



## Effects of Jittering on Stimulus Variance

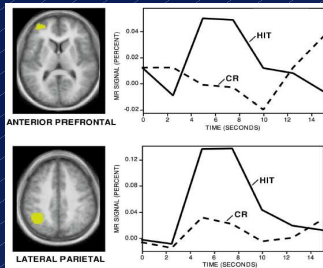
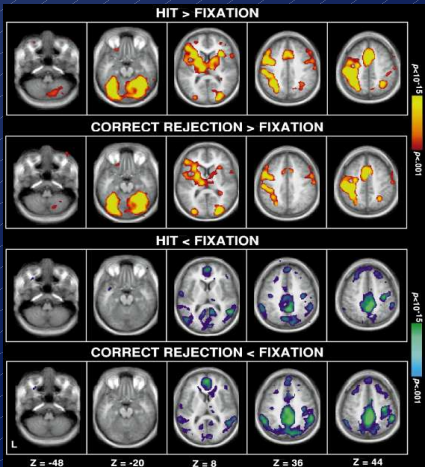


# Post-hoc sorting

## Dodatečné třídění

- Rozhodneme se až dodatečně (podle výsledku experimentu), do které kategorie pokus zařadíme.
- **Typický příklad:** Subjekt odpověděl správně/špatně.

# Post-Hoc Sorting of Trials



Data from old/new episodic memory test.

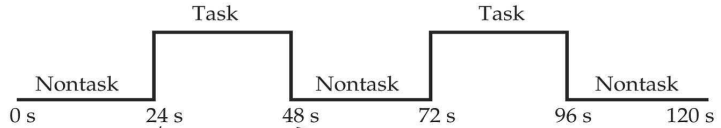
From Konishi, et al., 2000

## **Limitations of Event-Related Designs**

- **Differential effects of interstimulus interval**
  - Long intervals do not optimally increase stimulus variance
  - Short intervals may result in refractory effects
- **Detection ability dependent on form of HDR**
- **Length of “event” may not be known**

### **3a. Combination Blocked/Event**

- **Both blocked and event-related design aspects are used (for different purposes)**
  - Blocked design is used to evaluate *state-dependent* effects
  - Event-related design is used to evaluate *item-related* effects
- **Analyses are conducted largely independently between the two measures**
  - Cognitive processes are assumed to be independent

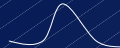
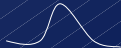




# Mixed Blocked/Event-related Design



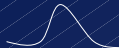
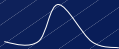
Target-related Activity (Phasic)



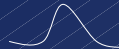
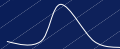
Blocked-related Activity (Tonic)

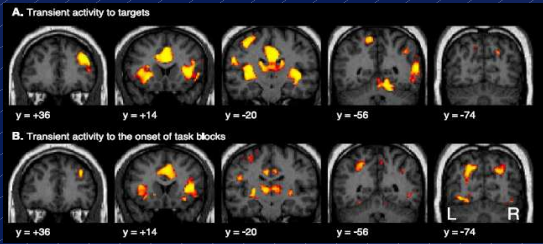
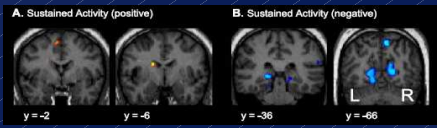
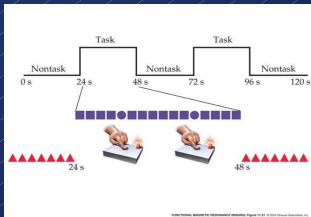


Task-Initiation Activity (Tonic)



Task-Offset Activity (Tonic)

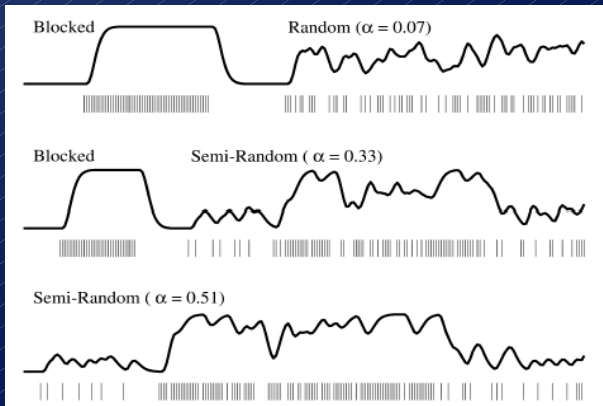




## **3b. Variable Stimulus Probability**

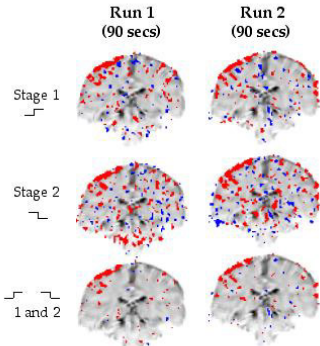
- **Stimulus probability is varied in a blocked fashion**
  - Appears similar to the combination design
- **Mixed design used to maximize experimental power for single design**
- **Assumes that processes of interest do not vary as a function of stimulus timing**
  - Cognitive processing
  - Refractory effects

## Random and Semi-Random Designs

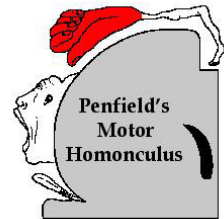
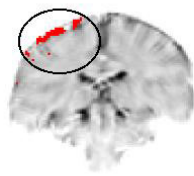


From Liu et al., 2001

# MULTI-STAGE ANALYSIS WITH COINCIDENCE



COINCIDENCE  
Run 1 AND Run 2



**Left Hand: Finger Thumb Tapping**



# Summary of Experiment Design

- **Main Issues to Consider**
  - What design constraints are induced by my task?
  - What am I trying to measure?
  - What sorts of non-task-related variability do I want to avoid?
- **Rules of thumb**
  - **Blocked Designs:**
    - Powerful for detecting activation
    - Useful for examining state changes
  - **Event-Related Designs:**
    - Powerful for estimating time course of activity
    - Allows determination of baseline activity
    - Best for post hoc trial sorting
  - **Mixed Designs**
    - Best combination of detection and estimation
    - Much more complicated analyses

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### (f)MRI — závěr

## MRI — závěr

- ⊕ 3D zobrazování
- ⊕ Výborné prostorové rozlišení
- ⊕ Neinvazivní
- ⊕ Obrovská variabilita — nejuniverzálnější ze zobrazovacích technik



## MRI — závěr

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- ⊕ Neinvazivní
- ⊕ Obrovská variabilita — nejuniverzálnější ze zobrazovacích technik
- ⊖ Cena
- ⊖ Silná (elektro)magnetická pole — opatrnost nutná
- ⊖ Nepohodlí — hluk, stísněný prostor

## fMRI — závěr

- ⊕ Lze zjistit, kde mozek pracuje
- ⊕ In-vivo
- ⊕ Neinvazivní
- ⊕ Relativně dobré prostorové rozlišení
- ⊖ Špatné časové rozlišení
- ⊖ Nutnost průměrování (nelze snímat ojedinělé jevy)