Bayesian decision making

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Today two examples:

- 1. Bayesian decision making basics
- 2. Power outage
- 3. Prior probabilities in practise

A:
$$P(X = x_i) = \sum_j \frac{P(X = x_i, Y = y_j)}{P(Y = y_j)}$$

B: $P(X = x_i) = \sum_j P(X = x_i, Y = y_j)$
C: $P(X = x_i) = \sum_i P(X = x_i, Y = y_j)$
D: $P(Y = y_i) = \sum_j P(X = x_i, Y = y_j)$

What is correct?:

A: $P(X = x_i) = \sum_j \frac{P(X = x_i, Y = y_j)}{P(Y = y_j)}$ B: $P(X = x_i) = \sum_j P(X = x_i, Y = y_j)$ C: $P(X = x_i) = \sum_j P(X = x_i, Y = y_j)$ D: $P(Y = y_i) = \sum_j P(X = x_i, Y = y_j)$

• Sum rule of probability:
$$P(X = x_i) = \sum_j P(X = x_i, Y = y_j)$$

A:
$$P(X = x_i | Y = y_j) = P(Y = y_j, X = x_i)P(X = x_i)$$

B: $P(X = x_i, Y = y_j) = \frac{P(Y = y_j | X = x_i)}{P(X = x_i)}$
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What is correct?:

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Bayes' theorem:
$$P(Y = y_i | X = x_j) = \frac{P(X = x_i | Y = y_j)P(Y = y_j)}{P(X = x_j)}$$

What is correct?:

A: $\delta^* = \arg \max_{\delta} \sum_{x} \sum_{s} l(s, \delta(x)) P(x, s)$ B: $\delta^* = \arg \min_{\delta} \sum_{x} \sum_{s} l(s, \delta(x)) P(x|s)$ C: $\delta^* = \arg \min_{\delta} \sum_{x} \sum_{s} l(s, \delta(x)) P(x, s)$ D: $\delta^* = \arg \min_{\delta} \sum_{x} \sum_{s} l(s, x) P(x, s)$

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- C: $\delta^* = \arg \min_{\delta} \sum_{x} \sum_{s} I(s, \delta(x)) P(x, s)$
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• Sum rule of probability: $P(X = x_i) = \sum_j P(X = x_i, Y = y_j)$

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Bayes' theorem:
$$P(Y = y_i | X = x_j) = \frac{P(X = x_i | Y = y_j)P(Y = y_j)}{P(X = x_j)}$$

▶ Bayes optimal strategy: $\delta^* = \arg \min_{\delta} \sum_{x} \sum_{s} I(s, \delta(x)) P(x, s)$

A:
$$\delta^*(x) = \arg \min_d \sum_s l(s, d) P(s|x)$$

B: $\delta^*(x) = \arg \min_d \sum_s l(s, d) P(s, x)$
C: $\delta^*(x) = \arg \min_\delta \sum_x \sum_s l(s, \delta(x)) P(x, s)$
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► Bayes' theorem: $P(Y = y_i | X = x_j) = \frac{P(X = x_i | Y = y_j)P(Y = y_j)}{P(X = x_j)}$

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• BOS solution:
$$\delta^*(x) = \arg \min_d \sum_s l(s, d) P(s|x)$$

Assume l(s, d) = 1, if $d \neq s$, l(s, d) = 0 otherwise. What is correct?:

A:
$$\delta^*(x) = \arg\min_d P(d|x)$$

- B: $\delta^*(x) = \arg \max_d P(d|x)$
- C: $\delta^*(x) = \arg \max_d P(d|x)P(x)$
- D: $\delta^*(x) = \arg \max_d P(d|x)P(s)$

• Sum rule of probability: $P(X = x_i) = \sum_j P(X = x_i, Y = y_j)$

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• Sum rule of probability: $P(X = x_i) = \sum_j P(X = x_i, Y = y_j)$

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$$P(Y = y_i | X = x_j) = \frac{P(X = x_i | Y = y_j)P(Y = y_j)}{P(X = x_j)}$$

- ▶ Bayes optimal strategy: $\delta^* = \arg \min_{\delta} \sum_{x} \sum_{s} I(s, \delta(x)) P(x, s)$
- BOS solution: $\delta^*(x) = \arg \min_d \sum_s l(s, d) P(s|x)$
- $L_{0,1}$ classification: $\delta^*(x) = \arg \max_d P(d|x)$

Imagine you're spending your evening in a café and going around people with a scale and convincing them to weigh themselves. You noted the results into the following frequency table.

	40–55 kg	55–65 kg	65–75 kg	75- ∞ kg
male	4	6	9	15
female	6	8	7	3

Task 1: One person is randomly selected and has to leave the café. Estimate the probability that this person is a woman that weighs less than 65kg.

Formalize:

A: p(x = female | y < 65)

- B: p(x = female, y < 65)
- C: p(y < 65|x = female)
- D: p(x = male, y < 65)

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•
$$p(x = female, y < 65)$$

Calculate:

A: $\frac{14}{24}$ B: $\frac{8}{58}$ C: $\frac{14}{58}$ D: $\frac{24}{58}$

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Task 2: Let's assume the person in the first question didn't leave the café yet. Suddenly, the lights go out and the café is in complete darkness. You notice by sound that someone sat next to you.

Estimate the probability of that person being a ma
 Calculate p(x = male):
 A: ³⁴/₅₈
 B: ²⁴/₅₈
 C: ¹⁸/₂₄
 D: ²⁹/₅₈

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Estimate the probability of that person being a man.

Calculate p(x = male):

A: $\frac{34}{58}$ B: $\frac{24}{58}$ C: $\frac{18}{24}$ D: $\frac{29}{58}$

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You weigh this person and estimate that he/she weighs no more than 65kg. Estimate the probability of this person to be a woman.

Formalize:

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A: p(x = female|y < 65)
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B: p(x = female, y < 65)
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C: p(y < 65|x = female)
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D: p(x = male, y < 65)
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•
$$p(x = female|y < 65)$$

Calculate:

A: $\frac{8}{14}$ B: $\frac{9}{12}$ C: $\frac{7}{12}$ D: $\frac{7}{14}$

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•
$$p(x = female|y < 65)$$

Calculate:

A:
$$\frac{14}{14}$$

B: $\frac{9}{12}$
C: $P(x = female| < 65) = \frac{P(x = female|)}{P(x = female|)}$

C:
$$P(x = female| < 65) = \frac{P(x = female, y < 65)}{P(y < 65)} = \frac{P(y < 65|x = female) \cdot P(x = female)}{P(y < 65)} = \frac{\frac{12}{24} \cdot \frac{2}{56}}{\frac{24}{58}} = \frac{14}{24} = \frac{7}{12}$$

D: $\frac{7}{12}$

The probability distribution of height of men and women is known (see table).

x cm	XS (0–100)	S (100–125)	M (125–150)	L (150–175)	XL (175–200)	XXL (200-∞)	\sum
P(x male)	0.05	0.15	0.2	0.25	0.3	0.05	1
P(x female)	0.05	0.1	0.3	0.3	0.25	0.0	1

Task 1: Estimate whether a 168cm tall (i.e. L) person is male or female.

A: Male

B: Female

The probability distribution of height of men and women is known (see table).

x cm	XS (0–100)	S (100–125)	M (125–150)	L (150–175)	XL (175–200)	XXL (200-∞)	\sum
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Task 1: Estimate whether a 168cm tall (i.e. L) person is male or female.

A: Male

B: Female (if we assume that there are same the number of men and women.)

The probability distribution of height of men and women is known (see table).

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Task 1: Estimate whether a 168cm tall (i.e. L) person is male or female. **Female** Task 2: What would be the minimum ratio of men to change the previous answer into the opposite one.

Right step?

A: P(X = male, Y = L) = P(X = female, Y = L)B: P(X = male|Y = L) = P(X = female|Y = L)C: P(X = male|Y > L) = P(X = female|Y < L)D: P(X = male|Y > L) = P(X = female|Y < L)

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$$P(X = male, Y = L) = P(X = female, Y = L)$$

B: $P(X = male|Y = L) = P(X = female|Y = L)$
C: $P(X = male|Y > L) = P(X = female|Y < L)$
D: $P(X = male|Y > L) = P(X = female|Y < L)$

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Task 2: What would be the minimum ratio of men to change the previous answer into the opposite one.

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$$P(X = male|Y = L) = P(X = female|Y = L)$$

C: P(X = male | Y > L) = P(X = female | Y < L)

D: P(X = male | Y > L) = P(X = female | Y < L)

The probability distribution of height of men and women is known (see table).

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P(x male)	0.05	0.15	0.2	0.25	0.3	0.05	1
P(x female)	0.05	0.1	0.3	0.3	0.25	0.0	1

Task 1: Estimate whether a 168cm tall (i.e. L) person is male or female. **Female** Task 2: What would be the minimum ratio of men to change the previous answer into the opposite one. P(X = male|Y = L) = P(X = female|Y = L)

From the equation get value of?:

- A: P(X = male)
- B: P(X = male | Y = L)
- C: P(X = female | Y < L)
- D: P(X = male | Y > L)

The probability distribution of height of men and women is known (see table).

cm	XS (0–100)	S (100–125)	M (125–150)	L (150–175)	XL (175–200)	XXL (200-∞)	\sum
P(x male)	0.05	0.15	0.2	0.25	0.3	0.05	1
P(x female)	0.05	0.1	0.3	0.3	0.25	0.0	1

Task 1: Estimate whether a 168cm tall (i.e. L) person is male or female. **Female** Task 2: What would be the minimum ratio of men to change the previous answer into the opposite one. P(X = male|Y = L) = P(X = female|Y = L)

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Task 1: Estimate whether a 168cm tall (i.e. L) person is male or female. Female

Task 2: What would be the minimum ratio of men to change the previous answer into the opposite one. P(X = male|Y = L) = P(X = female|Y = L)

From the equation get value of? P(X = male)Calculate P(X = male):

A: $\frac{5}{11}$ B: $\frac{6}{11}$ C: $\frac{6}{10}$ D: $\frac{7}{12}$

The probability distribution of height of men and women is known (see table).

cm	XS (0–100)	S (100–125)	M (125–150)	L (150–175)	XL (175–200)	XXL (200-∞)	\sum
P(x male)	0.05	0.15	0.2	0.25	0.3	0.05	1
P(x female)	0.05	0.1	0.3	0.3	0.25	0.0	1

Task 1: Estimate whether a 168cm tall (i.e. L) person is male or female. **Female** Task 2: What would be the minimum ratio of men to change the previous answer into the opposite one. P(X = male|Y = L) = P(X = female|Y = L)

From the equation get value of? P(X = male)Calculate P(X = male):

B: $\frac{6}{11}$

$$\begin{array}{l} P(X = male|Y = L) = P(X = female|Y = L) \\ \frac{P(L|male) \cdot P(male)}{P(L)} = \frac{P(L|female) \cdot P(female)}{P(L)}, P(female) = 1 - P(male) \\ P(L|male) \cdot P(male) = P(L|female) \cdot (1 - P(male)) \\ 0.25 \cdot P(male) = 0.3 - 0.3 \cdot P(male) \Rightarrow P(male) = \frac{6}{11} \end{array}$$

The probability distribution of height of men and women is known (see table).

cm	XS (0–100)	S (100–125)	M (125–150)	L (150–175)	XL (175–200)	XXL (200-∞)	\sum
P(x male)	0.05	0.15	0.2	0.25	0.3	0.05	1
P(x female)	0.05	0.1	0.3	0.3	0.25	0.0	1

Task 3: Assuming there are 70% men and 30% women, consider the loss function I (s - state, d - decision): I(s = female, d = male) = 2, I(s = male, d = female) = 1, I(s = male, d = male) = I(s = female, d = female) = 0. How do you classify a person under consideration of L? How?:

A:
$$\delta^*(X = L) = \operatorname{argmin}_s \sum_s l(s, d) \cdot P(s|X = L)$$

B: $\delta^*(X = L) = \operatorname{argmin}_d l(s, d) \cdot P(s|X = L)$
C: $\delta^*(X = L) = \operatorname{argmin}_s \sum_d l(s, d) \cdot P(s|X = L)$
D: $\delta^*(X = L) = \operatorname{argmin}_d \sum_s l(s, d) \cdot P(s|X = L)$

The probability distribution of height of men and women is known (see table).

x cm	XS (0–100)	S (100–125)	M (125–150)	L (150–175)	XL (175–200)	XXL (200-∞)	\sum
P(x male)			0.2	0.25	0.3	0.05	1
P(x female)	0.05	0.1	0.3	0.3	0.25	0.0	1

Task 3: Assuming there are 70% men and 30% women, consider the loss function L (s = state, d = decision): l(s = female, d = male) = 2, l(s = male, d = female) = 1, l(s = male, d = male) = l(s = female, d = female) = 0. How do you classify a person under consideration of L? How?:

D: $\delta^*(X = L) = \operatorname{argmin}_d \sum_s I(s, d) \cdot P(s|X = L)$

The probability distribution of height of men and women is known (see table).

x cm	XS (0–100)	S (100–125)	M (125–150)	L (150–175)	XL (175–200)	XXL (200-∞)	\sum
P(x male)	0.05	0.15	0.2	0.25	0.3	0.05	1
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- A: female
- B: male

The probability distribution of height of men and women is known (see table).

x cm	XS (0–100)	S (100–125)	M (125–150)	L (150–175)	XL (175–200)	XXL (200-∞)	\sum
P(x male)			0.2	0.25	0.3	0.05	1
P(x female)	0.05	0.1	0.3	0.3	0.25	0.0	1

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The probability distribution of height of men and women is known (see table).

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Task 3: Assuming there are 70% men and 30% women, consider the loss function L (s = state, d = decision): l(s = female, d = male) = 2, l(s = male, d = female) = 1, l(s = male, d = male) = l(s = female, d = female) = 0. How do you classify a person under consideration of L? $P(male|L) = \frac{P(L|male) \cdot P(male)}{P(L)} = \frac{P(L|male) \cdot P(male)}{P(L|male) \cdot P(male) + P(L|female) \cdot P(female)} = \frac{0.25 \cdot 0.7}{0.25 \cdot 0.7 + 0.3 \cdot 0.3} = 0.66$ P(female|L) = 1 - 0.66 = 0.34 $\delta^*(X) = \operatorname{argmin}_d(l(female, d) \cdot P(female|L) + l(male, d) \cdot P(male|L))$

$$\delta^*(X) = \operatorname{argmin}_d \left\{ \begin{array}{l} d = \textit{female} : 0 \cdot 0.34 + 1 \cdot 0.66 = 0.66 \\ d = \textit{male} : 2 \cdot 0.34 + 0 \cdot 0.66 = 0.68 \end{array} \right\} \Rightarrow d = \textit{female}$$