#### Lecture 1: MATLAB Environment, Basic Math Operators BE0B17MTB – Matlab

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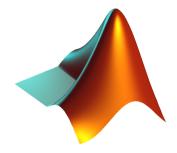
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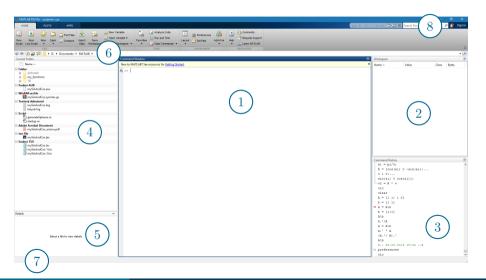
- 1. MATLAB Environment
- 2. Scalars, Vectors, Matrices
- 3. Basic Math Operations
- 4. Excercises



### The MATLAB Environment



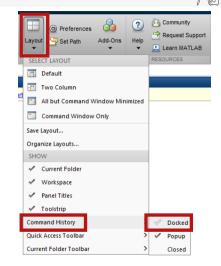




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#### The MATLAB Environment – Panels

- 1. Command Window
- 2. Workspace
- 3. Command History not activated, to activate  $\rightarrow$
- 4. Current Folder
- 5. Current Folder Details
- 6. Current Working Directory
- 7. Status ("Busy" when MATLAB is executing your code)
- 8. Search in documentation



#### Preferences

► Command:

#### >> preferences

- ▶ Ribbon menu:
  - ▶ Change font size.

Run and Time	Preferences     Community     Preferences     Community     Preferences     Community     Preferences     Community     Community     Community     Community     Community     Community     Community     Community
A Preferences	- 🗆 X
MATLAB     Add-Dons     Adg Deligier     Adg Deligier     Adg Deligier     Converter     Calors     Converter     Converter	MATLAB Fonts Preferences           Destops code font           Currently used by Command Window, Command History, Editor           Monospaced           Sample           The quick brown fox jumps over the lasy dog. 1234567880
	Desktop test fort Currently used by: Current Folder, Workspace, Variables, Function Browser [] Use system fort [Segue U] Sample The quick brown for jumps over the lazy dog. 123457890
	Help and Web browsers font To adjust the font ize for the Help and Web browsers, use the Ctrl+Plus and Ctrl+Minus keyboard shortcuts. The font ize is saved across sessions.
	Cutent fors Currently used by Profiler To set a custom form for any desktop tool, go to the <u>Custom Fonts</u> preferences.
	OK Cancel Apply Help



#### Documentation



>> doc % opens documentation window

>> help % MATLAB help

>> demo % tutorials

#### The Help Structure



#### ► Command:

>> help sin

#### ► Output:

sin Sine of argument in radians.
sin(X) is the sine of the elements of X.
See also asin, sind, sinpi.
Reference page for sin

## The Documentation Structure I.



#### ► Command:

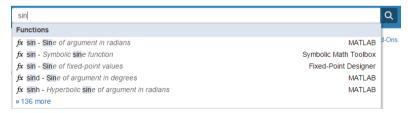
>> doc sin

- 1. Documentation page
- 2. Search field
- 3. Documentation contents
- 4. Bookmarks of this page

🚱 Help		
💠 🕸 🏠 🚖 - 🚳   🛛 sin 兴 🕂		
Documentation All	Examples Functions Search Help 2	
CONTENTS Close		
« Documentation Home	Sine of argument in radians	collapse all in page
« MATLAB « Mathematics		consport on in page
« Elementary Math « Trigerometry	Syntax (1)	
sin	$Y = \sin(X)$	
ON THIS PAGE	Description	
Syntax	Y = sin(X) returns the sine of the elements of X. The sin function operates element-wise on arrays. The function accepts t and complex inputs.	both real example
Description	<ul> <li>For real values of x, sin(x) returns real values in the interval [-1, 1].</li> </ul>	
Examples Input Arguments	<ul> <li>For complex values of X, sin(X) returns complex values.</li> </ul>	
Output Arguments	Examples	collapse all
More About Extended Capabilities	✓ Plot Sine Function	
See Also	Plot the sine function over the domain $-\pi \le x \le \pi$ . Open L	ive Script
4	x = -pi:0.01;pi;	
	<pre>plot(x,sin(x)), grid on</pre>	
	1	
	0.8	
	0.6	
	0.4	

### The Documentation Structure II.

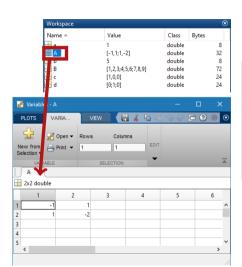
- ▶ Check the origin of the function.
  - ▶ Several functions with the same name may exist.
- ▶ Functions types by origin:
  - ▶ MATLAB core functions most of them build-in, some are available for editing (not recommended!).
  - ▶ Functions from installed toolboxes.
  - User-created functions.
- ▶ Calling priority for functions will be discussed later.
- ▶ During this course, always open a function from core installation.





#### Workspace Browser

- ▶ List of variables.
- ▶ Deleting/modification of existing variables.
- ► Saving/loading.
- ▶ Values, Class and Memory information.
  - ▶ Other information can be added: size, min, max, ...
  - All information can be obtained using MATLAB functions that we learn later, e.g., min, max, max, length.
- ▶ Fast data plotting option (in ribbon).





Introduction

### MATLAB Commands



#### ► Matlab is cAsE sEnSiTiVe!

- ▶ Almost entirely, with certain exceptions (properties of graphics objects, ...).
- ▶ Pay attention to typos and variable names (see later).
  - ▶ New versions of MATLAB offer certain options.

>> AA = [1 1 1] >> Aa

▶ Beware of different syntax in Mathematica.

▶ Following syntax is incorrect both in MATLAB and Mathematica:

```
>> Sin(pi/2) % function names start with lower case
>> cos[pi/2] % function input is in parentheses ()
```

▶ Will be discussed in the next lectures.

## Naming Conventions



- ▶ Names of variables can have max. 63 characters starting with letter (>> namelengthmax)
  - ▶ Letters and numbers are allowed, other symbols (colon ":", hyphen "-" and others) are not.
  - ▶ Underscore is allowed in the variable name "\_" (not at the beginning, though!).
- ▶ Lowercase letters in the names of scalars and variables (a = 17.59;).
- ▶ Matrix names usually start with a capital letter (A = [ ...];).
- ▶ Iteration variables, variables used in for cycles usually named m, n, k, etc.
  - ▶ It is advisable to avoid i and j (complex unit).
- ▶ Chose the names to correspond to the purpose of the variable.
- ▶ Avoid, if possible, standalone letter "1" (to be confused with one "1") and predefined variables in MATLAB environment (see later).
- ▶ Choose names corresponding to the meaning of each particular variable.
- ▶ Avoid using names of existing functions or scripts (overloading can occur).
- ▶ The same conventions are valid for names of functions and scripts.

#### Variable Names



▶ Examples of valid variable names:

a, A, b, c, x1, x2,  $M_12$ , test1, matrix\_A, fx, fX

▶ Examples of invalid variable names:

1var %	starts with a number (not possible in MATLAB)
matrix A %	contains space
coef.a %	possible only if coef is of type 'struct'
Test-1 %	algebraic expressing: ans = Test - 1
f(y) %	makes sense when using symbolic expressinos

▶ Examples of valid numbers in MATLAB,

▶ Pay attention to imaginary unit:

3, -66, +0.0015, .015, 1.6025e-10, 3i, 3.17e5i, -3.51j

#### Functions who, whos

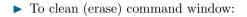


- ▶ Function who lists all variables in MATLAB Workspace.
  - ▶ Wide variety of options.
- ▶ Functions whos lists the variable names + dimension, size and data type of the variables or displays content of a file.
  - ▶ Wide variety of options.

```
>> whos('-file', 'matlab.mat');
```

```
>> a = 15; b = true; c = 'test'; d = 1 + 5j;
>> who
>> whos
>> Ws = whos:
```

#### Workspace – Output Deletion



>> clc

► To clean one (or more) variable(s):

>>	clear	%	whole Workspace is deleted
>>	clear XX	%	variable XX is deleted
>>	clear XX YY	%	variables XX and YY are deleted
>>	clear z*	%	everything starting with $'z'$ is deleted

▶ clear has a number of other options (graphics, I/O)



## Command History Window

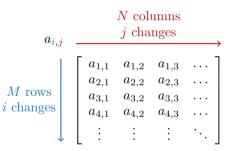
- ▶ Command History window stores all commands from the Command Window.
- ▶ Command History is accessible though  $\uparrow$  or  $\downarrow$ .
- ▶ it is possible to filter out past commands by, *e.g.*: >> A =  $[ + \uparrow$ .
- ▶ It is possible to copy-and-paste entire Command History: SHIFT / CTRL / CTRL + A  $\rightarrow$  CTRL + C.



#### Matrices in MATLAB

- Matrix is a basic data structure in MATLAB.
- ▶ There are following variables types depending on size:
  - $\blacktriangleright$  scalar:  $1 \times 1$
  - ▶ vector:  $M \times 1$  or  $1 \times N$
  - ▶ matrix:  $M \times N$
  - array (multidimensional matrices):  $M \times N \times P \times Q \times R \times \dots$
- ▶ Matrices can be complex.
- ▶ It can contains text as well (beware the length).

▶ M-by-N matrix:



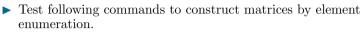


#### Matrix Creation

- ▶ Following techniques are available:
  - ▶ element-by-element entering (suitable for small matrices only),
  - ▶ colon notation":" to define elements of series,
  - ▶ generation by built-in functions,
  - ▶ generation of matrices in m-files,
  - ▶ import and export from/to external files(.mat, .txt, .xls, ...).



### Matrix Construction Element-by-element I.

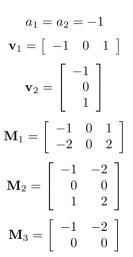


▶ Suitable for small matrices only.

>> a1 = -1>> a2 = [-1] % brackets are redundant

>> v1 = [-1 0 1] >> v2 = [-1; 0; 1]

>> M1 =  $\begin{bmatrix} -1 & 0 & 1; & -2 & 0 & 2 \end{bmatrix}$ >> M2 =  $\begin{bmatrix} -1 & -2; & 0 & 0; & 1 & 2 \end{bmatrix}$ >> M3 =  $\begin{bmatrix} \begin{bmatrix} -1 & -2 \end{bmatrix}; & \begin{bmatrix} 0 & 0 \end{bmatrix} \end{bmatrix}$  inner brackets are redundant





### Matrix Construction Element-by-element II.

- ► Construct following matrices:
  - ▶ Matrix values are defined inside square brackets [],
  - ▶ semicolon ";" separates individual rows of a matrix.

$$\mathbf{A} = \begin{bmatrix} -1 & -1 \\ 1 & -1 \end{bmatrix} \qquad \mathbf{B} = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$





### Matrix Construction



 Semicolon placed at the end of a command suppresses display of the output in Command Window.

>> a = 1 >> b = 5;

▶ When there is more than one command on the same line, comma is used to separate each of the commands.

>> a = 1, b = 5 >> a = 1; b = 5;

▶ Note: it is possible to copy and paste code including ">>"

▶ Row vs column vector:

>> c =  $[1 \ 0 \ 0]$ >> d =  $[0; \ 0; \ 1]$ 



## Basic Math Operators I.

▶ Operator types:

#### ▶ arithmetics:

- ▶ matrix,
- $\blacktriangleright$  vector,
- $\blacktriangleright$  relational,
- ▶ logical and other (to be mentioned later ...).
- ▶ Other operations using MATLAB functions:
  - ▶ complex conjugate,
  - ▶ sum, determinant, square root,
  - ▶ and hundreds of other functions . . .

- + addition
- subtraction
- \* multiplication
- **^** power
- ' transpose
- $\$  left matrix division
- / right matrix division

#### dot notation



## Operator Precedence in MATLAB

- ► According to the following table:
  - $\blacktriangleright$  see MATLAB  $\rightarrow$  Language Fundamentals  $\rightarrow$  Operators and Elementary Operations  $\rightarrow$  Arithmetic

1	parentheses	()					
2	transpose, power	1.1	. '	^	. ^		
3	unary plus, unary minus, logical negation	+	-	~			
4	multiplication, division	*	.*	/	\	./	.\
5	addition, subtraction	+	-				
6	colon operator	:					
$\overline{7}$	relation operators	<	>	<=	>=	==	~=
8	logical AND (element-wise)	&					
9	logical OR (element wise)						
10	logical AND (short-circuit)	&&					
11	logical OR (short-circuit)						



#### Basic Math Operators II.



- ▶ Type in following commands:
  - > Zero can be omitted with a decimal number beginning with zero (not recommended).

>> a3 = -2/4 >> a4 = -0.5 >> a5 = -.5

- What is the difference between  $a_3$ ,  $a_4$  and  $a_5$ ?
- ▶ Beware the precedence of operators (wee see in the next slides):

>> 3\*5\*6 >> a1 = 15 >> a2 = 10; >> a2/a3 >> a2/a3\*a4 >> a2/(a3\*a4)

- $\blacktriangleright$  Explain the difference between a2/a3\*a4 and a2/(a3/a4).
- ▶ Verify the rules of operator precedence from the previous slide.



## Lengthy commands in MATLAB



- ▶ It is suitable to structure command blocks for clarity:
  - $\blacktriangleright$  next line: SHIFT + ENTER

>> A = [1 1 1]; B = [2 2 2]; % SHIFT + ENTER C = [2 3 2];

▶ Three dots notation:

- ▶ For continuation of the same command on the next line.
- ▶ Compare results:

>> A1 = [ 1 1 ... 2 3]

>> A2 = [ 1 1 2 3]

#### Basic Math Functions I.

- ▶ Math functions in MATLAB are generally divided in three groups:
  - ► Scalar:
    - ▶ Function operates over individual elements of a matrix,
    - e.g.: sin, sqrt, log, factorial.
  - ► Vector:
    - ▶ Function operates over individual rows/columns of a matrix,
    - ▶ *e.g.*: sum, max.
  - ► Matrix:
    - ▶ Function operates over a whole matrix,
    - ▶ e.g.: det, trace.



#### Basic Math Functions II.



Using MATLAB help, calculate the following expression: a sin<sup>2</sup>(α) + a cos<sup>2</sup>(α) - a
 Use numerical values your own choice.

▶ Verify following logarithmic identity:  $\log_{10}(a) + \log_{10}(b) - \log_{10}(ab) = 0$ 

▶ Find sum of all elements in individual rows of the following matrix:

$$T = \begin{bmatrix} \frac{1}{2} & \frac{1}{3} & \frac{1}{4} & \frac{1}{5} \\ 6 & 7 & 7 & 9 \\ 0.2 & 0.3 & 0.4 & 0.5 \end{bmatrix}$$



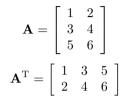
### Basic Math Functions III.

- ▶ Assume following vectors  $\mathbf{u} = (1, 2, 3)$  and  $\mathbf{v} = (3, 2, 1)$ .
  - ► Calculate:
- $\begin{array}{lll} \mathbf{u}\mathbf{v}^{\mathrm{T}} & \mathbf{v}\mathbf{u}^{\mathrm{T}} \\ \mathbf{v}^{\mathrm{T}}\mathbf{u} & \mathbf{u}^{\mathrm{T}}\mathbf{v} \end{array}$
- $\mathbf{u}\cdot\mathbf{v} \quad \mathbf{u}\times\mathbf{v}$
- ▶ Following functions are needed:
  - ▶ transpose (. ') of a matrix,
  - ▶ dot scalar product,
  - ▶ cross product.
- ▶ What is the result of the above mentioned operations?









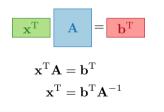
#### Matrix Division in MATLAB

- ▶ Two cases are distinguished:
  - ▶ left division  $(\backslash mldivide)$ ,
  - ▶ right division (/ mrdivide).
- ▶ Solution of a linear system of equations:
  - ▶ A is an invertible (regular) matrix,
  - **b** is a row (column) vector.



$$\mathbf{A}\mathbf{x} = \mathbf{b}$$
  
 $\mathbf{x} = \mathbf{A}^{-1}\mathbf{b}$ 

 $>> x = A \setminus b$ 



>> x = (b.' / A).'

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#### Basic Math Functions IV.

- ▶ Find the sum of diagonal elements (trace of a matrix) of the matrix T with elements coming from normal distribution with mean equal to 10 and standard deviation equal to 4.
- ▶ Find determinant of matrix **U**.

$$\mathbf{U} = \left[ \begin{array}{rrr} 1 & 2 & 3 \\ 0 & 2 & 0 \\ 0 & -2 & -1 \end{array} \right]$$

▶ Solve the linear system of equations:

$$x_1 + 2x_2 + 3x_3 = 6 Ax = b$$
  

$$4x_1 + 5x_2 + 6x_3 = 15 x = A^{-1}b$$
  

$$7x_1 + 8x_2 + x_3 = 16$$



>> T = 
$$10 + 4 + randn(7, 7);$$



### Predefined Values in MATLAB

- MATLAB contains several predefined values:
  - ▶ eps precision of single/double numbers (Determines the shortest distance between two single/double numbers).
  - ▶ ans answer most recent answer.
  - ▶ NaN not a number (every expressing containing NaN is NaN)
    - ▶ NaN can be used advantageously in some cases.
  - ▶ Inf *infinite number* (variable Inf can be used in calculation:))
    - ▶ Pay attention to **Inf** propagation throughout your code (use allowed operations only).
  - ▶ i, j complex unit.
    - ▶ They are all basically functions (without input parameter).
  - ▶ Check results of the following expressions:

>>	t1	=	10/0		%	t1	=	Inf
>>	t2	=	0/0		%	t2	=	NaN
>>	t3	=	t1*5		%	t3	=	Inf
>>	t4	=	t1 +	t2	%	t4	=	NaN

pi, intmin, intmax, realmin, realmax, ... (functions)







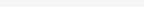
#### Format of Command Line Output

- ▶ Up to now we have been using basic setup.
- ▶ MATLAB offers number of other formatting options
  - ▶ Use format style.
  - ▶ Output format does not change neither the computation accuracy nor the accuracy of stored results (eps, realmax, realmin, ... still apply).

style	format description
short	fixed 4 decimal points are displayed
long	15 decimal points for double precision, 7 decimal points for single precision
shortE	floating-point format (scientific notation)
longE	-//-
bank	two decimal points only $(eur - cents)$
rat	MATLAB attempts to display the results as a fraction
compact	suppressed the display of blank lines
and others	note: omitting style parameter restores default setup



### Format of Command Line Output



- ► Try following output format settings:
  - ▶ Each format is suitable for different type of problems.

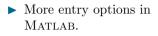
```
>> s = [-5 1/2 1/3 10*pi sqrt(2)];
>> format long; s
>> format rat; s
>> format bank; s
>> format bank; s
>> format hex; s
>> format +; s
>> format; s
```

- ▶ There exist other formats with slight differences.
  - Check doc format
- ▶ Later, we will learn how to use formatted conversion into strings (commands sprintf and fprintf).





## Complex Numbers I.



>>	C1	=	1	+	1 j	%	prefered
>>	C2	=	1	+	5i	%	prefered
>>	СЗ	=	1	+	i		
>>	C4	=	1	+	j5		
>>	C5	=	sc	1 r t	; ( - :	1)	
>>	C6	=	С	omp	lea	c (1	L, 2)

▶ Frequently used functions:

real,imag	real and imaginary part of a com-
	plex number
$\operatorname{conj}$	complex conjugate
abs	absolute value of a complex num-
	ber
angle	angle in complex plane [rad]
complex	constructs complex number from
	real and imaginary components
isreal	checks if the input is a complex
	number (more on that later)
i, j	complex unit
cplxpair	sort complex numbers into com-
	plex conjugate pairs



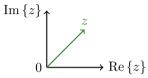
## Complex Numbers II.

- Create complex number z = 1 + 1j and its complex conjugate s = z\*.
- Switch between Cartesian and polar form (find |z| and  $\varphi$ ).

$$\begin{split} z &= \operatorname{Re} \left\{ z \right\} + \operatorname{Im} \left\{ z \right\} = a + \mathrm{j} b \\ z &= |z| \operatorname{e}^{\mathrm{j} \varphi}, |z| = \sqrt{a^2 + b^2} \\ z &= |z| \left( \cos \varphi + \mathrm{j} \sin \varphi \right) \end{split}$$

▶ Verify Moivre's theorem:

$$z^{n} = (|z| e^{j\varphi})^{n}$$
  
$$z^{n} = |z|^{n} (\cos (n\varphi) + j \sin (n\varphi))$$







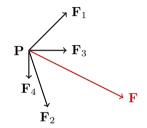
#### Exercise I.



 $\blacktriangleright$  Following forces were localized at point **P** in xy plane:

$$\begin{aligned} \mathbf{F}_1 &= [2,2] & \mathbf{F}_3 &= [2,0] \\ \mathbf{F}_2 &= [1,-3] & \mathbf{F}_4 &= [2,-1.5] \end{aligned}$$

 $\blacktriangleright$  What is the direction of the resultant force **F**?



▶ Normalize the resulting vector.

$$\mathbf{n}_{\mathrm{F}} = \frac{\mathbf{F}}{|\mathbf{F}|} = \frac{\mathbf{F}}{\sqrt{F_x^2 + F_y^2 + F_z^2}}$$



#### Exercise II.



▶ Type-in following commands:

```
>> clear, clc;
>> w1 = [1 2 3 4]
>> w2 = [-2 -3 -4]
>> w3 = [-2; -3; -4]
>> w4 = w1^2, w5 = w2 - w1
```

- ▶ Compare differences.
- ▶ What is the cause of error in calculation of w4 and w5?

► Try also:

>> w3\*3, w1 - 3 >> w1 + [5 5 5 5] >> w6 = 5\*w1 - [3 5 6] - w2

- ▶ Calculate the norm (magnitude) of vector w1.
  - ▶ Try more options.

▶ How to modify the calculation in the case of a complex vector?



#### Exercise III.

▶ Calculate roots of the quadratic function:

$$-2x^2 - 5x = 3.$$

▶ First, rearrange the terms of the function.

$$2x^{2} + 5x + 3 = 0 \implies a = 2, b = 5, c = 3$$
$$x_{1,2} = \frac{-b \pm \sqrt{b^{2} - 4ac}}{2a} = \frac{-5 \pm \sqrt{25 - 24}}{4}$$
$$x_{1} = -1, \ x_{2} = -\frac{3}{2}$$

► MATLAB provides particular function for calculation of roots a function, try to search it out.







#### Exercise IV.



- ▶ Think over how many ways there are to calculate the length of hypotenuse when two legs of a triangle are given.
  - ▶ Make use of various MATLAB operators and functions.
  - ▶ Consider also the case where the legs are complex numbers.

#### Exercise V.



• Create an arbitrary vector  $\mathbf{v}$  and rotate it around arbitrary angle  $\alpha$  in xz plane using rotation matrix  $\mathbf{R}$ .

$$\mathbf{v}' = \mathbf{R}\mathbf{v}$$
$$\mathbf{R} = \begin{bmatrix} \cos\alpha & 0 & -\sin\alpha \\ 0 & 1 & 0 \\ \sin\alpha & 0 & \cos\alpha \end{bmatrix}$$



#### Exercise V.



▶ Use the following code and round the resulting number to:

```
>> r = 1 + 10*rand(1)
```

- ▶ nearest integer,
- $\triangleright$  nearest integer greater than r,
- $\blacktriangleright$  nearest integer lower than r,
- ► zero,
- ▶ zero with precision of 2 decimal digits.
- Find remainder after r is divided by 0.1.
  - ▶ modulus vs. remainder after division



#### Exercise VI.

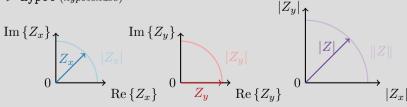


▶ Use abs and sqrt.

$$\mathbf{Z} = \begin{bmatrix} 1+1j & \sqrt{2} \end{bmatrix}$$

$$\|\mathbf{Z}\| = ?, \quad \mathbf{Z} \in \mathbb{C}^2$$

- ▶ Alternatively, use following functions:
  - ▶ norm
  - ▶ dot (dot product)
  - ▶ hypot (hypotenuse)







# Questions?

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