## Multi-Robot Planning

Jan Faigl

Department of Computer Science
Faculty of Electrical Engineering
Czech Technical University in Prague

Lecture 12

B4M36UIR - Artificial Intelligence in Robotics



#### Overview of the Lecture

- Part 1 Multi-Robot Systems (MRS)
- Part 2 Multi-Robot Planning
- Part 3 MRS domains and tasks
- Part 4 Swarm and modular robots



#### Part I

Part 1 – Multi-Robot Systems (MRS)



## Multi-Robot Systems (MRS) - Intro

Formed by individual robots (agents) capable of perceiving the environment by their sensors, communicating with other agents, and changing the environment by their actions.

(A. Farinelli et al., Trans. on Syst. Man and Cyber., 2004)

- Challenges in MRS scenarios:
  - Path/Motion planning

How to find path for multiple robots?

- Collision avoidance
  - How to find obstacle-free path?
- Dynamic obstacles in the environment How to execute the plans deadlock-free?
- Limited communication radius
- Physical limitations of the robot
- Reliability of (centralized) MRS
- And others



Kiva Systems (Amazon warehouse)



A busy traffic intersection



## Multi-Robot vs. Single-Robot

- Pros.
  - Parallel task execution actions can be done in parallel
  - Improved robustness failure of an individual should not affect the whole team
  - Wider range of applications some tasks cannot be solved by a single robot or some specialization of the robot is needed (heterogeneous teams)
- Cons.
  - Interference the robots may interfere and disturb each other, there
    is an uncertainty about intentions of other robots
  - Communication there is a limited communication bandwidth between robots
  - Maintenance multiple robots are harder to maintain



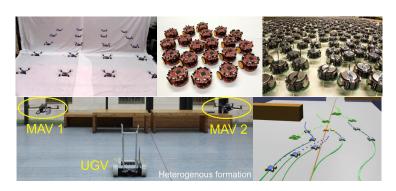
## Multi-Robot Systems - taxonomy (part 1)

- Cooperation
  - Cooperative robots cooperate to achieve joint goal
  - Competitive robots compete to best fulfill their own self-interest, i.e., robots can cooperate or form coalitions if that is in their own self-interest
- Communication
  - Implicit the information is transmitted through the environment
  - **Explicit** the information is transmitted directly between robots
- Organization
  - Centralized global coordination and planning
  - Hierarchical army model hierarchy of leaders
  - Decentralized local coordination, the global pattern of behavior is an emergent property



## Multi-Robot Systems - taxonomy (part 2)

- Team composition
  - homogeneous all robots have identical hardware and software
  - heterogeneous robots differ either in sensory-actuator capabilities or in the software control procedures
  - swarms large number of usually homogeneous robots, local control, little to no explicit communication





## Part II

## Part 2 - Multi-Robot Planning



## Multi-Robot Path Planning on Discrete Graphs (MPP)

#### MPP problem definition:

- G = (V, E) is a connected undirected simple graph where
  - $V = v_i$  is a the vertex set,
  - $E = \{(v_i, v_j)\}$  is the edge set.
- $\mathcal{R} = R_1, \cdots, R_m$  is a set of m robots.

Example of MPP - 15 puzzle

- Robots moves at discrete time steps.
- Each robot  $R_i$  is associated with an *start* and *goal* configuration  $(q_i^s, q_i^g)$
- MPP can be transformed to boolean satisfiability problem (3SAT).
- Finding optimal solution is NP-complete

(J. Yu, "Optimal Multi-Robot Path Planning on Graphs: Structure and Computational Complexity",

Robotics and Automation Letters, 2016)

Pebble motion problems - more "pebbles" can occupy one vertex



## Multi-Robot Path Planning on Discrete Graphs (MPP)

#### 9-puzzle example

(J. Yu, Robotics and Automation Letters, 2016)



Initial configurations



Desired goal configurations

Possible moves of two robots:



Impossible moves of two robots:







## Multi-Robot Path Planning on Discrete Graphs (MPP)

- Advantages of MPP on a discrete graph
  - Simple formulation
- Limitations of MPP on a discrete graph
  - A unit speed is assumed (one edge per time step)
  - A robot body is not considered
  - Some problems are hard to discretize
  - Even relatively small MPP instance can be computationally intractable



## Multi-Robot Motion Planning - part 1

#### ■ Fundamental problem in MRS

#### Formal notation:

- There is a set of m > 1 robots  $\mathcal{R} = R_1, \dots, R_m$
- each operating in a configuration space  $C_i$ , for  $1 \le i \le m$ ,
- let  $C_i^f \in C_i$  be each robot's free space,
- and  $C_i^o = C_i \setminus C_i^f$  be each robot's occupied space.
- The composite configuration space  $C = C_1 \times \cdots \times C_m$  is Cartesian product of each robot's configuration space.
- A composite configuration  $Q = (q_1, \dots, q_m) \in \mathcal{C}$  is *m*-tuple of robot configurations.
- For two robots R<sub>i</sub>, R<sub>j</sub>, i ≠ j, let I<sup>j</sup><sub>i</sub>(q<sub>j</sub>) ∈ C<sub>i</sub> be the set of configurations of robot R<sub>i</sub> that lead into collision with robot R<sub>j</sub> at configuration q<sub>j</sub>.
- Then the **composite free space** is defined as  $C^f \in C$  consists of configurations  $Q = (q_1, \dots, q_m)$  subject to:
  - $q_i \in \mathcal{C}_i^f$  for every  $1 \leq i \leq m$ ,
  - $q_i \notin I_i^j(q_i), q_i \notin I_i^i(q_i)$  for every  $1 \le i \le j \le m$ .
- The composite obstacle space is then defined as  $C^o = C \setminus C^f$ .



## Multi-Robot Motion Planning - part 2

#### ■ The problem:

- Set of Start configurations  $S = (q_1^s, \dots, q_m^s) \in \mathcal{C}^f$
- Set of Goal configurations  $G = (q_1^g, \dots, q_m^g) \in \mathcal{C}^f$
- Find a continuous trajectory  $\tau_i$ : [0,1] for each robot  $R_i$ , for  $1 \le i \le m$ , without collisions with obstacles and other robots, minimizing a cost function c, such that:  $\tau_i(0) = q_i^s$  and  $\tau_i(1) = q_i^g$
- The selection of a **cost function** c is subject to optimization criteria, e.g.:
  - 1. Min Total Time

minimize 
$$\sum_{i=1}^{m} t_i$$

2. Min Makespan

minimize 
$$\max_{1 \le i \le m} t_i$$

3. Min Total Distance

minimize 
$$\sum_{i=1}^{m} I_i$$

4. Min Max Distance

minimize 
$$\max_{1 \le i \le m} l_i$$

where  $t_i$  and  $l_i$  are the trajectory  $\tau_i$  duration and length, respectively



## Multi-Robot Motion Planning - Approaches

- Centralized planning planning directly in the composite configuration space.
  - Coupled planning direct planning in the composite configuration space
  - Assembly planning determining a sequence of motions that assembles the parts
  - Decoupled planning planning of each trajectory separately (Prioritized planning, Pairwise cooperation)
- Decentralized planning each robot plans its own trajectories and solves collision situations as they appear



## Centralized Planning - Coupled Planning

## Planning directly in the composite configuration space

$$C = C_1 \times \cdots \times C_m$$

- Utilizes standard path planning methods, such as random-sampling based approaches or grid-based planners
- m robots with d DOFs are assumed as a single robot with  $m \cdot d$  DOFs
- **Complete**, i.e., it always find a solution (if exists)
- Complexity  $\approx \exp(m \cdot d)$
- Becomes computationally intractable even for small number of robots.
- Finding optimal solution is NP-complete

(J. Yu, "Optimal Multi-Robot Path Planning on Graphs: Structure and Computational Complexity",

Robotics and Automation Letters, 2016)

■ Note, for **unlabeled case**, when there is no explicit mapping  $S \to G$ , i.e., you do not care which robot is on particular goal, the complexity is polynomial

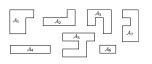
 $(\mathsf{M}.\mathsf{Turpin}\ \mathsf{et}\ \mathsf{al.},\ ^{\mathsf{u}}\mathsf{Goal}\ \mathsf{assignment}\ \mathsf{and}\ \mathsf{trajectory}\ \mathsf{planning}\ \mathsf{for}\ \mathsf{large}\ \mathsf{teams}\ \mathsf{of}\ \mathsf{interchangeable}\ \mathsf{robots}^{\mathsf{u}},$ 

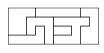


## Centralized Planning - Assembly Planning

- The task is to assembly final product from multiple parts.
- A single part is moved at a time.
- Result of the planning is a sequence of paths for individual parts.
- Planning is started from the final configurations backwards.







Courtesy of (S. M. LaValle, 2006)



## Centralized Planning - Decoupled Planning

- Planning for each robot  $R_i$ ,  $1 \le i \le m$  with d DOFs separately
- Coordination of particular plans is done later
- Not complete, not optimal
- Complexity  $\approx m \exp(d)$

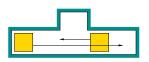
Methods of plan coordination:

#### Prioritized planning

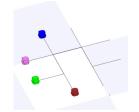
- Each robot is assigned with a priority
- Plans are constructed according to priorities
- Cannot prevent deadlocks
- (https://www.youtube.com/watch?v=dFm-JJhyuv0)

#### Pairwise cooperation

- Planning in coordination space Robot configuration is considered one-dimensional (position on a trajectory in time)
- Coordinations are incrementally solved for all the robots



Courtesy of (S. M. LaValle, 2006)





## Decentralized planning

- Each robot plans its own trajectory and resolves possible collision with other vehicles
- Both implicit and explicit communication types can be considered
- Collision situations are resolved as they appear

#### Collision resolution methods

- Based on the priority earliest collision is solved first
- Based on the shortest trajectory prolongation



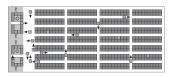
#### Kiva robots in Amazon warehouses

- Amazon acquired Kiva Systems for \$775 million in 2012
- Grid-based planning problem
- Restricted areas for human operators
- Classical A\* planning
- Task allocation problem
- About 30,000 robots in 2016
- Open-source example

(https://github.com/oliehoek/kiva)



Kiva Systems (Amazon warehouse)



An example of Amazon warehouse layout

((P. R. Wurman et al., "Coordinating Hundreds of Cooperative, Autonomous Vehicles in Warehouses",

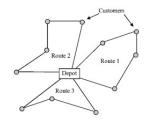
Al Magazine, 2008)



## Vehicle routing problem (VRP)

# Special case of a graph-based Multi-Robot planning with multiple goals.

- First introduced by Dantzig and Ramser in 1959.
- Generalization of the classical TSP with multiple vehicles.



(Souce: K. Ghoseiri et al., 2009)

- Problem definition
  - n customers.
  - m vehicles with maximal capacities  $a_k$ .
  - A single depot (both initial and final positions of vehicles).
  - Costs  $d_{i,j}$  between the given cities.
  - Find a set of routes with a minimal total cost.



## Vehicle routing problem

#### Possible formulations

- Vehicle Routing Problems with Pickup and Delivery (VRPPD) pickup and delivery locations are defined
- Vehicle routing problem with LIFO similar to VRPPD but with stack loading
- Vehicle Routing Problem with Time Windows (VRPTW) times windows of visits are limited
- Capacitated Vehicle Routing Problem (CVRP) each vehicle has its capacity (Uncapacitated VRP is also called mTSP)
- Open Vehicle Routing Problem (OVRP) return to depot is not required



#### Plan execution

#### Reactive control

- Agent follows the shortest path to the target
- Collision situations are resolved as they appear
- Cannot prevent deadlocks or infinite loops

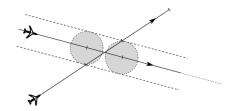
#### Deliberative control

- Planning of coordinated trajectories for all the robots
- Agents execute the path in an incremental way
- Guarantees deadlock free execution (if plans are executed precisely)



#### Reactive control

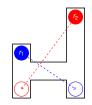
- Each agent plans its own path
- Each agent detects possible collisions
- Resolution of the conflicts:
  - set of evasion maneuvers,
  - adapting speed and heading,
  - complete re-planning





#### Plan execution environments with external disturbances

- Plan generated for each of m robot (agents) with d-DOF globally by existing approaches
- External disturbance such as
  - human operator
  - hardware failure
  - or any other unknown obstacle
- Resolution of the conflicts:
  - ALLSTOP stop all robots, deadlock-free but ineffective
  - reactive solve collision situations reactively, cannot avoid dead-locks
  - RMTRACK execute plans according to coordination diagram, i.e., do not change order at crossings





M.Čáp, IROS, 2016

(https://www.youtube.com/watch?v=29YRLJpB90Q)

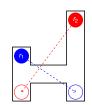


#### Plan execution environments with external disturbances

- Plan generated for each of m robot (agents) with d-DOF globally by existing approaches
- External disturbance such as
  - human operator
  - hardware failure
  - or any other unknown obstacle
- Resolution of the conflicts:
  - ALLSTOP stop all robots, deadlock-free but ineffective
  - reactive solve collision situations reactively, cannot avoid dead-locks
  - RMTRACK execute plans according to coordination diagram, i.e., do not change order at crossings

(M.Čáp, IROS, 2016)

(https://www.voutube.com/watch?v=29YRLJpB900)



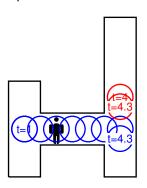


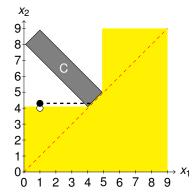


## RMTRACK - Plan execution in coordination space

(M.Čáp, IROS, 2016)

Coordination space shows mutual collisions of trajectories  $\tau_i$  and  $\tau_j$  with respect to the time scale







## Part III

Part 3 – MRS domains and tasks



#### MRS domains and tasks

- Data collection planning (https://www.youtube.com/watch?v=5MPSAReNzJU)
- Exploration (https://www.youtube.com/watch?v=tqMcK5YzwZc)
- Inspection
- Coverage
- Monitoring
- Pickup and delivery
- Pursuit evasion
- Cooperative transportation
- Multi-robot sensor fusion



## Part IV

Part 4 – Swarm and modular robots



#### Swarm robotics

An approach to **coordination** of (usually a large number of) robots in a **distributed** and **decentralized** way. A plain set of rules at individual level can produce a large set of complex behaviors at the swarm level that emerges from interactions between the robots and interactions of robots with the environment.

(Y. Tan, Z. Zheng, Defense Technology, 2013)

- Nature inspired, e.g., social insects, fish, birds, herding mammals
- Properties
  - Homogenity agents in a swarm are homogeneous robots, as such, they are assumed to be interchangeable
  - Locality agents can observe only part of the system within a certain range.
     Decisions depend on current neighborhood.
  - Little to no explicit communication swarms in nature are decentralized

(S. Iha et al. Anim. Behav. 2006)









#### Swarm robotics

An approach to **coordination** of (usually a large number of) robots in a **distributed** and **decentralized** way. A plain set of rules at individual level can produce a large set of complex behaviors at the swarm level that emerges from interactions between the robots and interactions of robots with the environment.

(Y. Tan, Z. Zheng, Defense Technology, 2013)

- Nature inspired, e.g., social insects, fish, birds, herding mammals
- Properties
  - Homogenity agents in a swarm are homogeneous robots, as such, they are assumed to be interchangeable
  - Locality agents can observe only part of the system within a certain range.
     Decisions depend on current neighborhood.
  - Little to no explicit communication swarms in nature are decentralized

(S. Jha et al., Anim. Behav., 2006)









#### Swarm robotics - behavior model

#### How to describe the control policies in swarms?

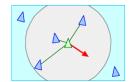
A distributed behavioral model - boids

(C.Reynolds, SIGGRAPH, 1987)

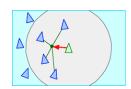
 Introduces three basic steering maneuvers based on local neighbors (flockmates)

**Separation** - steer to avoid local flockmates

Alignment - steer towards an average heading of local flockmates **Cohesion** - steer to the average position of the flockmates







Further complex behaviors can be developed, e.g., avoidance, following, aggregation, dispersion, homing



## Swarm robotics - applications

 Collective Movement - how can an uncoordinated group of robots move from one place to another

```
(M.Saska et al., ICRA, 2014)
```

 Distributed sensing - swarms are very effective in Source search missions

```
(J. E. Hurtado et al., JIRS, 2004)
```

Cooperative transportation

```
(C. R. Kube et al., RAS, 2000)
```

■ Collective mapping - e.g. area coverage, shoveling

```
(M.Saska et al., JIRS, 2014)
```



#### Modular robots

- Composed of elementary mechatronic modules that can assemble to form body of various shapes
- Pros.
  - Adaptability to various operation conditions
  - Failure recovery by ejecting or replacing broken modules
- Cons.
  - Complicated mechatronic design
  - Complicated development of locomotion strategies
- Locomotion control principles
  - Self-reconfiguration repeatedly disconnecting and reconnecting modules
  - Joint-controlled locomotion controlling individual limbs of the robot





#### Modular robots - Joint-controlled locomotion

# How to develop new locomotion rules for a robot with variable morphology?

- 1. Each module is an individual entity MPP
- 2. The whole robot is an individual entity Planning with motion primitives require synthesis of new gaits for each topology

solve the problem which leads to a blind random search

- Often used CPG controllers developed by genetic algorithms (GA)
- Leads to high-dimensional parameter optimization crucial role of cost function
  - Greedy optimization early iterations of GA does not provide ability to

```
(H.Lipson et al., Nature, 2000)
```

 Ranking quality and novelty of found solutions - low-performing solutions may help in solving other task (crippling walking robot)

```
(A.Cully et al., Evolutionary Computation, 2016)
```

(https://www.youtube.com/watch?v=2aTIL\_c-qwA)

 Random sampling with CPGs as motion primitives - combination of motion primitives may lead to feasible solutions

```
(V.Vonásek et al., SSCI, 2016)
```

(https://www.youtube.com/watch?v=4KNDk2jjUGs)



# Summary of the Lecture



## Topics Discussed

- MRS systems and their taxonomy
- Multi-robot path planning
- Multi-robot motion planning
  - Centralized approaches (Coupled, Assembly, Decoupled)
  - Decentralized approaches
- Vehicle routing problem
- Swarm robotics
- Modular robots
- Next: Game Theory in Robotics



## Topics Discussed

- MRS systems and their taxonomy
- Multi-robot path planning
- Multi-robot motion planning
  - Centralized approaches (Coupled, Assembly, Decoupled)
  - Decentralized approaches
- Vehicle routing problem
- Swarm robotics
- Modular robots
- Next: Game Theory in Robotics



Topics Discussed

Thank you for your attention!

